Alaska Tutorials are designed specifically for Alaska Standards and prepare students for the PEAKS exams in English and Mathematics.

Math Tutorials offer targeted instruction, practice and review designed to develop computational fluency, deepen conceptual understanding, and apply mathematical practices. They automatically identify and address learning gaps down to elementary-level content, using adaptive remediation to bring students to grade-level no matter where they start. Students engage with the content in an interactive, feedback-rich environment as they progress through standards-aligned modules. By constantly honing the ability to apply their knowledge in abstract and real world scenarios, students build the depth of knowledge and higher order skills required to demonstrate their mastery when put to the test.

In each module, the Learn It and Try It make complex ideas accessible to students through focused content, modeled logic and process, multi-modal representations, and personalized feedback as students reason through increasingly challenging problems. The Review It offers a high impact summary of key concepts and relates those concepts to students' lives. The Test It assesses students' mastery of the module's concepts, providing granular performance data to students and teachers after each attempt. To help students focus on the content most relevant to them, unit-level pretests and posttests can quickly identify where students are strong and where they're still learning.

Unit 1: Equations and Inequalities

- **FORMULATING AND SOLVING EQUATIONS FROM WORD PROBLEMS**
  - F-LE.2: Linear, Quadratic, and Exponential Models Construct and compare linear, quadratic, and exponential models and solve problems. Construct linear and exponential functions, including arithmetic and geometric sequences, given a graph, a description of a relationship, or inputoutput table of values.
  - F-LE.1.b: Linear, Quadratic, and Exponential Models Construct and compare linear, quadratic, and exponential models and solve problems. Distinguish between situations that can be modeled with linear functions and with exponential functions. Recognize situations in which one quantity changes at a constant rate per unit interval relative to another.
  - F-LE.2: Linear, Quadratic, and Exponential Models Construct and compare linear, quadratic, and exponential models and solve problems. Construct linear and exponential functions, including arithmetic and geometric sequences, given a graph, a description of a relationship, or inputoutput table of values.
  - A-CED.1: Creating Equations and Inequalities Create equations and inequalities that describe numbers or relationships. Create equations and inequalities in one variable and use them to solve problems.

- A-SSE.1.a: Seeing Structure in Expressions Interpret the structure of expressions. Interpret expressions that represent a quantity in terms of its context. Interpret parts of an expression, such as terms, factors, and coefficients.

- **FORMULATING AND SOLVING INEQUALITIES FROM WORD PROBLEMS**
  - A-SSE.1.a: Seeing Structure in Expressions Interpret the structure of expressions. Interpret expressions that represent a quantity in terms of its context. Interpret parts of an expression, such as terms, factors, and coefficients.
  - A-CED.1: Creating Equations and Inequalities Create equations and inequalities that describe numbers or relationships. Create equations and inequalities in one variable and use them to solve problems.
  - A-CED.3: Creating Equations and Inequalities Create equations and inequalities that describe numbers or relationships. Represent constraints by equations or inequalities, and by systems of equations and/or inequalities, and interpret solutions as viable or nonviable options in a modeling context.
  - A-REI.3: Reasoning with Equations and Inequalities Solve equations and inequalities in one variable. Solve linear equations and inequalities in one variable, including equations with coefficients represented by letters.

Unit 2: Literal Equations and Geometric Sequences

- **LITERAL EQUATIONS**
  - A-CED.1: Creating Equations and Inequalities Create equations and inequalities that describe numbers or relationships. Create equations and inequalities in one variable and use them to solve problems.
  - A-REI.3: Reasoning with Equations and Inequalities Solve equations and inequalities in one variable. Solve linear equations and inequalities in one variable, including equations with coefficients represented by letters.
  - A-CED.4: Creating Equations and Inequalities Create equations and inequalities that describe numbers or relationships. Rearrange formulas (literal equations) to highlight a quantity of interest, using the same reasoning as in solving equations.
- **SUMS OF GEOMETRIC SEQUENCES**
  - A-SSE.4: Seeing Structure in Expressions Write expressions in equivalent forms to solve problems. Derive the formula for the sum of a finite geometric series (when the common ratio is not 1), and use the formula to solve problems.

Unit 3: Functions

- **FUNCTIONS AND RELATIONS**
  - F-IF.2: Interpreting Functions Understand the concept of a function and use function notation. Use function notation, evaluate functions for inputs in their domains, and interpret statements that use function notation in terms of a context.
  - F-IF.1: Interpreting Functions Understand the concept of a function and use function notation. Understand that a function from one set (called the domain) to another set (called the range) assigns to each element of the domain exactly one element of the range. If is a function and is an element of

its domain, then () denotes the output of corresponding to the input . The graph of is the graph of the equation = ().

- F-IF.7.b: Interpreting Functions Analyze functions using different representations. Graph functions expressed symbolically and show key features of the graph, by hand in simple cases and using technology for more complicated cases. Graph square root, cube root, and piecewisedefined functions, including step functions and absolute value functions.

- **DOMAIN AND RANGE**
  - F-IF.5: Interpreting Functions Interpret functions that arise in applications in terms of the context. Relate the domain of a function to its graph and, where applicable, to the quantitative relationship it describes.
- **INVERSE FUNCTIONS**
  - F-BF.4.c: Building Functions Build new functions from existing functions. Find inverse functions. Read values of an inverse function from a graph or a table, given that the function has an inverse.
  - F-BF.4.a: Building Functions Build new functions from existing functions. Find inverse functions. Solve an equation of the form () = for a simple function that has an inverse and write an expression for the inverse.
  - F-BF.4.b: Building Functions Build new functions from existing functions. Find inverse functions. Verify by composition that one function is the inverse of another.
  - F-BF.4.d: Building Functions Build new functions from existing functions. Find inverse functions. Produce an invertible function from a noninvertible function by restricting the domain.

Unit 4: Linear Functions, Equations, and Inequalities

- **SLOPE**
  - F-IF.4.a: Interpreting Functions Interpret functions that arise in applications in terms of the context. For a function that models a relationship between two quantities, interpret key features of graphs and tables in terms of the quantities, and
  - F-IF.6: Interpreting Functions Interpret functions that arise in applications in terms of the context. Calculate and interpret the average rate of change of a function (presented symbolically or as a table) over a specified interval. Estimate the rate of change from a graph.
  - F-IF.1: Interpreting Functions Understand the concept of a function and use function notation. Understand that a function from one set (called the domain) to another set (called the range) assigns to each element of the domain exactly one element of the range. If is a function and is an element of its domain, then () denotes the output of corresponding to the input . The graph of is the graph of the equation = ().
  - G-GPE.5: Expressing Geometric Properties with Equations Use coordinates to prove simple geometric theorems algebraically. Prove the slope criteria for parallel and perpendicular lines and use them to solve geometric problems (e.g., find the equation of a line parallel or perpendicular to a given line that passes through a given point).
- **GRAPHING AND ANALYZING LINEAR FUNCTIONS**

- F-IF.1: Interpreting Functions Understand the concept of a function and use function notation. Understand that a function from one set (called the domain) to another set (called the range) assigns to each element of the domain exactly one element of the range. If is a function and is an element of its domain, then () denotes the output of corresponding to the input . The graph of is the graph of the equation = ().
- F-IF.4.b: Interpreting Functions Interpret functions that arise in applications in terms of the context. For a function that models a relationship between two quantities, sketch graphs showing key features given a verbal description of the relationship.
- F-LE.2: Linear, Quadratic, and Exponential Models Construct and compare linear, quadratic, and exponential models and solve problems. Construct linear and exponential functions, including arithmetic and geometric sequences, given a graph, a description of a relationship, or inputoutput table of values.
- F-IF.5: Interpreting Functions Interpret functions that arise in applications in terms of the context. Relate the domain of a function to its graph and, where applicable, to the quantitative relationship it describes.
- F-LE.2: Linear, Quadratic, and Exponential Models Construct and compare linear, quadratic, and exponential models and solve problems. Construct linear and exponential functions, including arithmetic and geometric sequences, given a graph, a description of a relationship, or inputoutput table of values.
- F-IF.1: Interpreting Functions Understand the concept of a function and use function notation. Understand that a function from one set (called the domain) to another set (called the range) assigns to each element of the domain exactly one element of the range. If is a function and is an element of its domain, then () denotes the output of corresponding to the input . The graph of is the graph of the equation = ().
- F-IF.4.a: Interpreting Functions Interpret functions that arise in applications in terms of the context. For a function that models a relationship between two quantities, interpret key features of graphs and tables in terms of the quantities, and
- F-IF.6: Interpreting Functions Interpret functions that arise in applications in terms of the context. Calculate and interpret the average rate of change of a function (presented symbolically or as a table) over a specified interval. Estimate the rate of change from a graph.
- F-LE.2: Linear, Quadratic, and Exponential Models Construct and compare linear, quadratic, and exponential models and solve problems. Construct linear and exponential functions, including arithmetic and geometric sequences, given a graph, a description of a relationship, or inputoutput table of values.

- **GRAPHING AND MANIPULATING Y = MX + B**
  - A-CED.2: Creating Equations and Inequalities Create equations and inequalities that describe numbers or relationships. Create equations in two or more variables to represent relationships between quantities; graph equations on coordinate axes with labels and scales.

- F-IF.1: Interpreting Functions Understand the concept of a function and use function notation. Understand that a function from one set (called the domain) to another set (called the range) assigns to each element of the domain exactly one element of the range. If is a function and is an element of its domain, then () denotes the output of corresponding to the input . The graph of is the graph of the equation = ().
- F-IF.4.b: Interpreting Functions Interpret functions that arise in applications in terms of the context. For a function that models a relationship between two quantities, sketch graphs showing key features given a verbal description of the relationship.
- F-LE.2: Linear, Quadratic, and Exponential Models Construct and compare linear, quadratic, and exponential models and solve problems. Construct linear and exponential functions, including arithmetic and geometric sequences, given a graph, a description of a relationship, or inputoutput table of values.
- F-IF.1: Interpreting Functions Understand the concept of a function and use function notation. Understand that a function from one set (called the domain) to another set (called the range) assigns to each element of the domain exactly one element of the range. If is a function and is an element of its domain, then () denotes the output of corresponding to the input . The graph of is the graph of the equation = ().
- S-ID.7: Interpreting Categorical and Quantitative Data Interpret linear models. Interpret the slope (rate of change) and the intercept (constant term) of a linear model in the context of the data.
- F-IF.4.a: Interpreting Functions Interpret functions that arise in applications in terms of the context. For a function that models a relationship between two quantities, interpret key features of graphs and tables in terms of the quantities, and
- F-IF.6: Interpreting Functions Interpret functions that arise in applications in terms of the context. Calculate and interpret the average rate of change of a function (presented symbolically or as a table) over a specified interval. Estimate the rate of change from a graph.
- F-LE.1.b: Linear, Quadratic, and Exponential Models Construct and compare linear, quadratic, and exponential models and solve problems. Distinguish between situations that can be modeled with linear functions and with exponential functions. Recognize situations in which one quantity changes at a constant rate per unit interval relative to another.
- F-LE.5: Linear, Quadratic, and Exponential Models Interpret expressions for functions in terms of the situation they model. Interpret the parameters in a linear or exponential function in terms of a context.
- F-IF.7.a: Interpreting Functions Analyze functions using different representations. Graph functions expressed symbolically and show key features of the graph, by hand in simple cases and using technology for more complicated cases. Graph linear and quadratic functions and show intercepts, maxima, and minima.

Unit 5: Exponential Functions

- **EXPONENTIAL FUNCTIONS**

- F-IF.4.a: Interpreting Functions Interpret functions that arise in applications in terms of the context. For a function that models a relationship between two quantities, interpret key features of graphs and tables in terms of the quantities, and
- F-IF.4.b: Interpreting Functions Interpret functions that arise in applications in terms of the context. For a function that models a relationship between two quantities, sketch graphs showing key features given a verbal description of the relationship.
- F-IF.8.b: Interpreting Functions Analyze functions using different representations. Write a function defined by an expression in different but equivalent forms to reveal and explain different properties of the function. Use the properties of exponents to interpret expressions for exponential functions.
- F-LE.1.c: Linear, Quadratic, and Exponential Models Construct and compare linear, quadratic, and exponential models and solve problems. Distinguish between situations that can be modeled with linear functions and with exponential functions. Recognize situations in which a quantity grows or decays by a constant percent rate per unit interval relative to another.
- F-IF.6: Interpreting Functions Interpret functions that arise in applications in terms of the context. Calculate and interpret the average rate of change of a function (presented symbolically or as a table) over a specified interval. Estimate the rate of change from a graph.
- F-IF.1: Interpreting Functions Understand the concept of a function and use function notation. Understand that a function from one set (called the domain) to another set (called the range) assigns to each element of the domain exactly one element of the range. If is a function and is an element of its domain, then () denotes the output of corresponding to the input . The graph of is the graph of the equation = ().
- F-IF.5: Interpreting Functions Interpret functions that arise in applications in terms of the context. Relate the domain of a function to its graph and, where applicable, to the quantitative relationship it describes.
- F-IF.7.e: Interpreting Functions Analyze functions using different representations. Graph functions expressed symbolically and show key features of the graph, by hand in simple cases and using technology for more complicated cases. Graph exponential and logarithmic functions, showing intercepts and end behavior, and trigonometric functions, showing period, midline, and amplitude.
- A-SSE.1.b: Seeing Structure in Expressions Interpret the structure of expressions. Interpret expressions that represent a quantity in terms of its context. Interpret complicated expressions by viewing one or more of their parts as a single entity.
- A-SSE.3.c: Seeing Structure in Expressions Write expressions in equivalent forms to solve problems. Choose and produce an equivalent form of an expression to reveal and explain properties of the quantity represented by the expression. Use the properties of exponents to transform expressions for exponential functions.
- A-CED.1: Creating Equations and Inequalities Create equations and inequalities that describe numbers or relationships. Create equations and inequalities in one variable and use them to solve problems.
- A-CED.2: Creating Equations and Inequalities Create equations and inequalities that describe numbers or relationships. Create equations in two or more variables to represent relationships between

quantities; graph equations on coordinate axes with labels and scales.

- F-LE.2: Linear, Quadratic, and Exponential Models Construct and compare linear, quadratic, and exponential models and solve problems. Construct linear and exponential functions, including arithmetic and geometric sequences, given a graph, a description of a relationship, or inputoutput table of values.
- F-LE.5: Linear, Quadratic, and Exponential Models Interpret expressions for functions in terms of the situation they model. Interpret the parameters in a linear or exponential function in terms of a context.

- **EXPONENTIAL GROWTH AND DECAY**
  - F-IF.8.b: Interpreting Functions Analyze functions using different representations. Write a function defined by an expression in different but equivalent forms to reveal and explain different properties of the function. Use the properties of exponents to interpret expressions for exponential functions.
  - F-LE.1.a: Linear, Quadratic, and Exponential Models Construct and compare linear, quadratic, and exponential models and solve problems. Distinguish between situations that can be modeled with linear functions and with exponential functions. Show that linear functions grow by equal differences over equal intervals, and that exponential functions grow by equal factors over equal intervals.
  - F-LE.5: Linear, Quadratic, and Exponential Models Interpret expressions for functions in terms of the situation they model. Interpret the parameters in a linear or exponential function in terms of a context.
  - A-SSE.1.b: Seeing Structure in Expressions Interpret the structure of expressions. Interpret expressions that represent a quantity in terms of its context. Interpret complicated expressions by viewing one or more of their parts as a single entity.
  - F-LE.1.c: Linear, Quadratic, and Exponential Models Construct and compare linear, quadratic, and exponential models and solve problems. Distinguish between situations that can be modeled with linear functions and with exponential functions. Recognize situations in which a quantity grows or decays by a constant percent rate per unit interval relative to another.
  - F-LE.2: Linear, Quadratic, and Exponential Models Construct and compare linear, quadratic, and exponential models and solve problems. Construct linear and exponential functions, including arithmetic and geometric sequences, given a graph, a description of a relationship, or inputoutput table of values.
  - S-ID.6.a: Interpreting Categorical and Quantitative Data Summarize, represent, and interpret data on two categorical and quantitative variables. Represent data on two quantitative variables on a scatter plot, and describe how the variables are related. Fit a function to the data; use functions fitted to data to solve problems in the context of the data. Use given functions or choose a function suggested by the context. Emphasize linear, quadratic, and exponential models.
  - F-LE.1.b: Linear, Quadratic, and Exponential Models Construct and compare linear, quadratic, and exponential models and solve problems. Distinguish between situations that can be modeled with linear functions and with exponential functions. Recognize situations in which one quantity changes at a constant rate per unit interval relative to another.

- F-LE.2: Linear, Quadratic, and Exponential Models Construct and compare linear, quadratic, and exponential models and solve problems. Construct linear and exponential functions, including arithmetic and geometric sequences, given a graph, a description of a relationship, or inputoutput table of values.
- F-LE.3: Linear, Quadratic, and Exponential Models Construct and compare linear, quadratic, and exponential models and solve problems. Observe using graphs and tables that a quantity increasing exponentially eventually exceeds a quantity increasing linearly, quadratically, or (more generally) as a polynomial function.
- A-CED.2: Creating Equations and Inequalities Create equations and inequalities that describe numbers or relationships. Create equations in two or more variables to represent relationships between quantities; graph equations on coordinate axes with labels and scales.
- F-LE.2: Linear, Quadratic, and Exponential Models Construct and compare linear, quadratic, and exponential models and solve problems. Construct linear and exponential functions, including arithmetic and geometric sequences, given a graph, a description of a relationship, or inputoutput table of values.

Unit 6: Logarithmic Expressions and Functions

- **EVALUATING LOGARITHMIC EXPRESSIONS**
  - A-SSE.1.b: Seeing Structure in Expressions Interpret the structure of expressions. Interpret expressions that represent a quantity in terms of its context. Interpret complicated expressions by viewing one or more of their parts as a single entity.
  - A-SSE.2: Seeing Structure in Expressions Interpret the structure of expressions. Use the structure of an expression to identify ways to rewrite it.
  - F-LE.4: Linear, Quadratic, and Exponential Models Construct and compare linear, quadratic, and exponential models and solve problems. For exponential models, express as a logarithm the solution to = where , , and are numbers and the base is 2, 10, or ; evaluate the logarithm using technology.
- **LOGARITHMIC FUNCTIONS**
  - F-IF.4.a: Interpreting Functions Interpret functions that arise in applications in terms of the context. For a function that models a relationship between two quantities, interpret key features of graphs and tables in terms of the quantities, and
  - F-BF.4.a: Building Functions Build new functions from existing functions. Find inverse functions. Solve an equation of the form () = for a simple function that has an inverse and write an expression for the inverse.
  - F-BF.4.c: Building Functions Build new functions from existing functions. Find inverse functions. Read values of an inverse function from a graph or a table, given that the function has an inverse.
  - F-BF.5: Building Functions Build new functions from existing functions. Understand the inverse relationship between exponents and logarithms and use this relationship to solve problems involving logarithms and exponents.

- F-LE.4: Linear, Quadratic, and Exponential Models Construct and compare linear, quadratic, and exponential models and solve problems. For exponential models, express as a logarithm the solution to = where , , and are numbers and the base is 2, 10, or ; evaluate the logarithm using technology.
- F-IF.5: Interpreting Functions Interpret functions that arise in applications in terms of the context. Relate the domain of a function to its graph and, where applicable, to the quantitative relationship it describes.
- F-LE.4: Linear, Quadratic, and Exponential Models Construct and compare linear, quadratic, and exponential models and solve problems. For exponential models, express as a logarithm the solution to = where , , and are numbers and the base is 2, 10, or ; evaluate the logarithm using technology.
- F-IF.7.e: Interpreting Functions Analyze functions using different representations. Graph functions expressed symbolically and show key features of the graph, by hand in simple cases and using technology for more complicated cases. Graph exponential and logarithmic functions, showing intercepts and end behavior, and trigonometric functions, showing period, midline, and amplitude.

Unit 7: Solving Exponential and Logarithmic Equations and Inequalities

- **SOLVING EXPONENTIAL EQUATIONS**
  - A-SSE.3.c: Seeing Structure in Expressions Write expressions in equivalent forms to solve problems. Choose and produce an equivalent form of an expression to reveal and explain properties of the quantity represented by the expression. Use the properties of exponents to transform expressions for exponential functions.
  - F-IF.8.b: Interpreting Functions Analyze functions using different representations. Write a function defined by an expression in different but equivalent forms to reveal and explain different properties of the function. Use the properties of exponents to interpret expressions for exponential functions.
  - F-BF.4.a: Building Functions Build new functions from existing functions. Find inverse functions. Solve an equation of the form () = for a simple function that has an inverse and write an expression for the inverse.
  - F-LE.4: Linear, Quadratic, and Exponential Models Construct and compare linear, quadratic, and exponential models and solve problems. For exponential models, express as a logarithm the solution to = where , , and are numbers and the base is 2, 10, or ; evaluate the logarithm using technology.
  - F-IF.4.a: Interpreting Functions Interpret functions that arise in applications in terms of the context. For a function that models a relationship between two quantities, interpret key features of graphs and tables in terms of the quantities, and
  - F-IF.4.b: Interpreting Functions Interpret functions that arise in applications in terms of the context. For a function that models a relationship between two quantities, sketch graphs showing key features given a verbal description of the relationship.
  - F-IF.7.e: Interpreting Functions Analyze functions using different representations. Graph functions expressed symbolically and show key features of the graph, by hand in simple cases and using technology for more complicated cases. Graph exponential and logarithmic functions, showing intercepts and end behavior, and trigonometric functions, showing period, midline, and amplitude.

- **SOLVING EXPONENTIAL INEQUALITIES**
  - A-CED.3: Creating Equations and Inequalities Create equations and inequalities that describe numbers or relationships. Represent constraints by equations or inequalities, and by systems of equations and/or inequalities, and interpret solutions as viable or nonviable options in a modeling context.
  - A-SSE.1.b: Seeing Structure in Expressions Interpret the structure of expressions. Interpret expressions that represent a quantity in terms of its context. Interpret complicated expressions by viewing one or more of their parts as a single entity.
  - A-CED.1: Creating Equations and Inequalities Create equations and inequalities that describe numbers or relationships. Create equations and inequalities in one variable and use them to solve problems.
  - A-CED.2: Creating Equations and Inequalities Create equations and inequalities that describe numbers or relationships. Create equations in two or more variables to represent relationships between quantities; graph equations on coordinate axes with labels and scales.
  - F-LE.1.c: Linear, Quadratic, and Exponential Models Construct and compare linear, quadratic, and exponential models and solve problems. Distinguish between situations that can be modeled with linear functions and with exponential functions. Recognize situations in which a quantity grows or decays by a constant percent rate per unit interval relative to another.
- **SOLVING LOGARITHMIC EQUATIONS**
  - F-IF.1: Interpreting Functions Understand the concept of a function and use function notation. Understand that a function from one set (called the domain) to another set (called the range) assigns to each element of the domain exactly one element of the range. If is a function and is an element of its domain, then () denotes the output of corresponding to the input . The graph of is the graph of the equation = ().
  - F-IF.4.a: Interpreting Functions Interpret functions that arise in applications in terms of the context. For a function that models a relationship between two quantities, interpret key features of graphs and tables in terms of the quantities, and
  - F-LE.4: Linear, Quadratic, and Exponential Models Construct and compare linear, quadratic, and exponential models and solve problems. For exponential models, express as a logarithm the solution to = where , , and are numbers and the base is 2, 10, or ; evaluate the logarithm using technology.

Unit 8: Arithmetic with Polynomials 1

- **POLYNOMIAL BASICS**
  - A-SSE.1.a: Seeing Structure in Expressions Interpret the structure of expressions. Interpret expressions that represent a quantity in terms of its context. Interpret parts of an expression, such as terms, factors, and coefficients.
  - A-SSE.2: Seeing Structure in Expressions Interpret the structure of expressions. Use the structure of an expression to identify ways to rewrite it.
  - A-APR.1: Arithmetic with Polynomials and Rational Expressions Perform arithmetic operations on polynomials. Add, subtract, and multiply polynomials. Understand that polynomials form a system

similar to the integers, namely, they are closed under the operations of addition, subtraction, and multiplication.

- **ADDITION AND SUBTRACTION OF POLYNOMIALS**
  - A-SSE.2: Seeing Structure in Expressions Interpret the structure of expressions. Use the structure of an expression to identify ways to rewrite it.
  - A-APR.1: Arithmetic with Polynomials and Rational Expressions Perform arithmetic operations on polynomials. Add, subtract, and multiply polynomials. Understand that polynomials form a system similar to the integers, namely, they are closed under the operations of addition, subtraction, and multiplication.

Unit 9: Arithmetic with Polynomials 2

- **MULTIPLICATION OF POLYNOMIALS**
  - A-APR.1: Arithmetic with Polynomials and Rational Expressions Perform arithmetic operations on polynomials. Add, subtract, and multiply polynomials. Understand that polynomials form a system similar to the integers, namely, they are closed under the operations of addition, subtraction, and multiplication.
  - A-SSE.2: Seeing Structure in Expressions Interpret the structure of expressions. Use the structure of an expression to identify ways to rewrite it.
- **DIVISION OF POLYNOMIALS**
  - A-APR.2: Arithmetic with Polynomials and Rational Expressions Understand the relationship between zeros and factors of polynomials. Know and apply the Remainder Theorem: For a polynomial () and a number , the remainder on division by is (), so () = 0 if and only if ( ) is a factor of ().
  - A-SSE.2: Seeing Structure in Expressions Interpret the structure of expressions. Use the structure of an expression to identify ways to rewrite it.
  - A-APR.2: Arithmetic with Polynomials and Rational Expressions Understand the relationship between zeros and factors of polynomials. Know and apply the Remainder Theorem: For a polynomial () and a number , the remainder on division by is (), so () = 0 if and only if ( ) is a factor of ().
  - A-APR.6: Arithmetic with Polynomials and Rational Expressions Rewrite rational expressions. Rewrite simple rational expressions in different forms; write ()/() in the form () + ()/(), where (), (), (), and () are polynomials with the degree of () less than the degree of (), using inspection, long division, or, for the more complicated examples, a computer algebra system.

Unit 10: Graphs and Representations of Quadratic Functions

- **ANALYZING GRAPHS OF QUADRATIC FUNCTIONS**
  - F-IF.5: Interpreting Functions Interpret functions that arise in applications in terms of the context. Relate the domain of a function to its graph and, where applicable, to the quantitative relationship it describes.
  - F-IF.1: Interpreting Functions Understand the concept of a function and use function notation. Understand that a function from one set (called the domain) to another set (called the range) assigns to each element of the domain exactly one element of the range. If is a function and is an element of

its domain, then () denotes the output of corresponding to the input . The graph of is the graph of the equation = ().

- F-IF.4.a: Interpreting Functions Interpret functions that arise in applications in terms of the context. For a function that models a relationship between two quantities, interpret key features of graphs and tables in terms of the quantities, and
- F-IF.4.b: Interpreting Functions Interpret functions that arise in applications in terms of the context. For a function that models a relationship between two quantities, sketch graphs showing key features given a verbal description of the relationship.
- F-IF.7.a: Interpreting Functions Analyze functions using different representations. Graph functions expressed symbolically and show key features of the graph, by hand in simple cases and using technology for more complicated cases. Graph linear and quadratic functions and show intercepts, maxima, and minima.
- F-IF.1: Interpreting Functions Understand the concept of a function and use function notation. Understand that a function from one set (called the domain) to another set (called the range) assigns to each element of the domain exactly one element of the range. If is a function and is an element of its domain, then () denotes the output of corresponding to the input . The graph of is the graph of the equation = ().
- F-BF.3: Building Functions Build new functions from existing functions. Identify the effect on the graph of replacing () by () + , (), (), and (+) for specific values of (both positive and negative); find the value of given the graphs.
- A-REI.4.b: Reasoning with Equations and Inequalities Solve equations and inequalities in one variable. Solve quadratic equations in one variable. Solve quadratic equations by inspection (e.g., for = 49), taking square roots, completing the square, the quadratic formula and factoring, as appropriate to the initial form of the equation. Recognize when the quadratic formula gives complex solutions and write them as for real numbers and .
- F-IF.9: Interpreting Functions Analyze functions using different representations. Compare properties of two functions each represented in a different way (algebraically, graphically, numerically, in tables, or by verbal descriptions).

- **REPRESENTATIONS OF QUADRATIC FUNCTIONS**
  - A-SSE.2: Seeing Structure in Expressions Interpret the structure of expressions. Use the structure of an expression to identify ways to rewrite it.
  - A-REI.4.a: Reasoning with Equations and Inequalities Solve equations and inequalities in one variable. Solve quadratic equations in one variable. Use the method of completing the square to transform any quadratic equation in x into an equation of the form ( ) = q that has the same solutions. Derive the quadratic formula from this form.
  - F-IF.8.a: Interpreting Functions Analyze functions using different representations. Write a function defined by an expression in different but equivalent forms to reveal and explain different properties of the function. Use the process of factoring and completing the square in a quadratic function to show zeros, extreme values, and symmetry of the graph, and interpret these in terms of a context.

- A-CED.2: Creating Equations and Inequalities Create equations and inequalities that describe numbers or relationships. Create equations in two or more variables to represent relationships between quantities; graph equations on coordinate axes with labels and scales.
- A-CED.3: Creating Equations and Inequalities Create equations and inequalities that describe numbers or relationships. Represent constraints by equations or inequalities, and by systems of equations and/or inequalities, and interpret solutions as viable or nonviable options in a modeling context.
- F-IF.1: Interpreting Functions Understand the concept of a function and use function notation. Understand that a function from one set (called the domain) to another set (called the range) assigns to each element of the domain exactly one element of the range. If is a function and is an element of its domain, then () denotes the output of corresponding to the input . The graph of is the graph of the equation = ().
- F-IF.4.b: Interpreting Functions Interpret functions that arise in applications in terms of the context. For a function that models a relationship between two quantities, sketch graphs showing key features given a verbal description of the relationship.
- A-SSE.3.a: Seeing Structure in Expressions Write expressions in equivalent forms to solve problems. Choose and produce an equivalent form of an expression to reveal and explain properties of the quantity represented by the expression. Factor a quadratic expression to reveal the zeros of the function it defines.
- A-APR.3: Arithmetic with Polynomials and Rational Expressions Understand the relationship between zeros and factors of polynomials. Identify zeros of polynomials when suitable factorizations are available, and use the zeros to construct a rough graph of the function defined by the polynomial.
- F-IF.7.c: Interpreting Functions Analyze functions using different representations. Graph functions expressed symbolically and show key features of the graph, by hand in simple cases and using technology for more complicated cases. Graph polynomial functions, identifying zeros (using technology) or algebraic methods when suitable factorizations are available, and showing end behavior.
- F-IF.4.a: Interpreting Functions Interpret functions that arise in applications in terms of the context. For a function that models a relationship between two quantities, interpret key features of graphs and tables in terms of the quantities, and

- **MULTIPLE REPRESENTATIONS OF FUNCTIONS**

  - A-CED.2: Creating Equations and Inequalities Create equations and inequalities that describe numbers or relationships. Create equations in two or more variables to represent relationships between quantities; graph equations on coordinate axes with labels and scales.
  - F-IF.9: Interpreting Functions Analyze functions using different representations. Compare properties of two functions each represented in a different way (algebraically, graphically, numerically, in tables, or by verbal descriptions).

Unit 11: Solving Quadratic Equations 1

- **SOLVING QUADRATIC EQUATIONS BY FACTORING**

- A-SSE.3.a: Seeing Structure in Expressions Write expressions in equivalent forms to solve problems. Choose and produce an equivalent form of an expression to reveal and explain properties of the quantity represented by the expression. Factor a quadratic expression to reveal the zeros of the function it defines.
- A-REI.4.b: Reasoning with Equations and Inequalities Solve equations and inequalities in one variable. Solve quadratic equations in one variable. Solve quadratic equations by inspection (e.g., for = 49), taking square roots, completing the square, the quadratic formula and factoring, as appropriate to the initial form of the equation. Recognize when the quadratic formula gives complex solutions and write them as for real numbers and .
- F-IF.8.a: Interpreting Functions Analyze functions using different representations. Write a function defined by an expression in different but equivalent forms to reveal and explain different properties of the function. Use the process of factoring and completing the square in a quadratic function to show zeros, extreme values, and symmetry of the graph, and interpret these in terms of a context.
- A-APR.4: Arithmetic with Polynomials and Rational Expressions Use polynomial identities to solve problems. Prove polynomial identities and use them to describe numerical relationships.
- A-REI.4.b: Reasoning with Equations and Inequalities Solve equations and inequalities in one variable. Solve quadratic equations in one variable. Solve quadratic equations by inspection (e.g., for = 49), taking square roots, completing the square, the quadratic formula and factoring, as appropriate to the initial form of the equation. Recognize when the quadratic formula gives complex solutions and write them as for real numbers and .
- F-IF.1: Interpreting Functions Understand the concept of a function and use function notation. Understand that a function from one set (called the domain) to another set (called the range) assigns to each element of the domain exactly one element of the range. If is a function and is an element of its domain, then () denotes the output of corresponding to the input . The graph of is the graph of the equation = ().
- F-IF.7.a: Interpreting Functions Analyze functions using different representations. Graph functions expressed symbolically and show key features of the graph, by hand in simple cases and using technology for more complicated cases. Graph linear and quadratic functions and show intercepts, maxima, and minima.
- A-CED.2: Creating Equations and Inequalities Create equations and inequalities that describe numbers or relationships. Create equations in two or more variables to represent relationships between quantities; graph equations on coordinate axes with labels and scales.

- **QUADRATIC FORMULA**
  - A-REI.4.b: Reasoning with Equations and Inequalities Solve equations and inequalities in one variable. Solve quadratic equations in one variable. Solve quadratic equations by inspection (e.g., for = 49), taking square roots, completing the square, the quadratic formula and factoring, as appropriate to the initial form of the equation. Recognize when the quadratic formula gives complex solutions and write them as for real numbers and .

- A-REI.4.b: Reasoning with Equations and Inequalities Solve equations and inequalities in one variable. Solve quadratic equations in one variable. Solve quadratic equations by inspection (e.g., for = 49), taking square roots, completing the square, the quadratic formula and factoring, as appropriate to the initial form of the equation. Recognize when the quadratic formula gives complex solutions and write them as for real numbers and .
- N-CN.7: The Complex Number System Use complex numbers in polynomial identities and equations. Solve quadratic equations with real coefficients that have complex solutions.
- F-IF.1: Interpreting Functions Understand the concept of a function and use function notation. Understand that a function from one set (called the domain) to another set (called the range) assigns to each element of the domain exactly one element of the range. If is a function and is an element of its domain, then () denotes the output of corresponding to the input . The graph of is the graph of the equation = ().
- F-IF.4.a: Interpreting Functions Interpret functions that arise in applications in terms of the context. For a function that models a relationship between two quantities, interpret key features of graphs and tables in terms of the quantities, and
- F-IF.7.a: Interpreting Functions Analyze functions using different representations. Graph functions expressed symbolically and show key features of the graph, by hand in simple cases and using technology for more complicated cases. Graph linear and quadratic functions and show intercepts, maxima, and minima.
- A-CED.3: Creating Equations and Inequalities Create equations and inequalities that describe numbers or relationships. Represent constraints by equations or inequalities, and by systems of equations and/or inequalities, and interpret solutions as viable or nonviable options in a modeling context.
- A-REI.4.b: Reasoning with Equations and Inequalities Solve equations and inequalities in one variable. Solve quadratic equations in one variable. Solve quadratic equations by inspection (e.g., for = 49), taking square roots, completing the square, the quadratic formula and factoring, as appropriate to the initial form of the equation. Recognize when the quadratic formula gives complex solutions and write them as for real numbers and .

Unit 12: Solving Quadratic Equations 2

- **COMPLETING THE SQUARE**
  - A-REI.4.a: Reasoning with Equations and Inequalities Solve equations and inequalities in one variable. Solve quadratic equations in one variable. Use the method of completing the square to transform any quadratic equation in x into an equation of the form ( ) = q that has the same solutions. Derive the quadratic formula from this form.
  - A-REI.4.b: Reasoning with Equations and Inequalities Solve equations and inequalities in one variable. Solve quadratic equations in one variable. Solve quadratic equations by inspection (e.g., for = 49), taking square roots, completing the square, the quadratic formula and factoring, as appropriate to the initial form of the equation. Recognize when the quadratic formula gives complex solutions and write them as for real numbers and .

- F-IF.8.a: Interpreting Functions Analyze functions using different representations. Write a function defined by an expression in different but equivalent forms to reveal and explain different properties of the function. Use the process of factoring and completing the square in a quadratic function to show zeros, extreme values, and symmetry of the graph, and interpret these in terms of a context.
- A-SSE.3.b: Seeing Structure in Expressions Write expressions in equivalent forms to solve problems. Choose and produce an equivalent form of an expression to reveal and explain properties of the quantity represented by the expression. Complete the square in a quadratic expression to reveal the maximum or minimum value of the function it defines.
- A-REI.4.a: Reasoning with Equations and Inequalities Solve equations and inequalities in one variable. Solve quadratic equations in one variable. Use the method of completing the square to transform any quadratic equation in x into an equation of the form ( ) = q that has the same solutions. Derive the quadratic formula from this form.
- A-REI.4.a: Reasoning with Equations and Inequalities Solve equations and inequalities in one variable. Solve quadratic equations in one variable. Use the method of completing the square to transform any quadratic equation in x into an equation of the form ( ) = q that has the same solutions. Derive the quadratic formula from this form.
- A-REI.4.b: Reasoning with Equations and Inequalities Solve equations and inequalities in one variable. Solve quadratic equations in one variable. Solve quadratic equations by inspection (e.g., for = 49), taking square roots, completing the square, the quadratic formula and factoring, as appropriate to the initial form of the equation. Recognize when the quadratic formula gives complex solutions and write them as for real numbers and .
- F-IF.7.a: Interpreting Functions Analyze functions using different representations. Graph functions expressed symbolically and show key features of the graph, by hand in simple cases and using technology for more complicated cases. Graph linear and quadratic functions and show intercepts, maxima, and minima.

- **COMPLEX NUMBERS AND QUADRATIC FUNCTIONS**
  - A-REI.4.b: Reasoning with Equations and Inequalities Solve equations and inequalities in one variable. Solve quadratic equations in one variable. Solve quadratic equations by inspection (e.g., for = 49), taking square roots, completing the square, the quadratic formula and factoring, as appropriate to the initial form of the equation. Recognize when the quadratic formula gives complex solutions and write them as for real numbers and .
  - A-REI.4.b: Reasoning with Equations and Inequalities Solve equations and inequalities in one variable. Solve quadratic equations in one variable. Solve quadratic equations by inspection (e.g., for = 49), taking square roots, completing the square, the quadratic formula and factoring, as appropriate to the initial form of the equation. Recognize when the quadratic formula gives complex solutions and write them as for real numbers and .
  - N-CN.7: The Complex Number System Use complex numbers in polynomial identities and equations. Solve quadratic equations with real coefficients that have complex solutions.
  - A-REI.4.b: Reasoning with Equations and Inequalities Solve equations and inequalities in one variable. Solve quadratic equations in one variable. Solve quadratic equations by inspection (e.g., for = 49),

taking square roots, completing the square, the quadratic formula and factoring, as appropriate to the initial form of the equation. Recognize when the quadratic formula gives complex solutions and write them as for real numbers and .

- N-CN.1: The Complex Number System Perform arithmetic operations with complex numbers. Know there is a complex number such that = 1, and every complex number has the form + with and real.
- N-CN.2: The Complex Number System Perform arithmetic operations with complex numbers. Use the relation = 1 and the commutative, associative, and distributive properties to add, subtract, and multiply complex numbers.

Unit 13: Factoring Polynomials

- **FACTORING SPECIAL CASES**
  - A-SSE.2: Seeing Structure in Expressions Interpret the structure of expressions. Use the structure of an expression to identify ways to rewrite it.
  - A-APR.4: Arithmetic with Polynomials and Rational Expressions Use polynomial identities to solve problems. Prove polynomial identities and use them to describe numerical relationships.
  - A-SSE.1.b: Seeing Structure in Expressions Interpret the structure of expressions. Interpret expressions that represent a quantity in terms of its context. Interpret complicated expressions by viewing one or more of their parts as a single entity.
  - A-APR.3: Arithmetic with Polynomials and Rational Expressions Understand the relationship between zeros and factors of polynomials. Identify zeros of polynomials when suitable factorizations are available, and use the zeros to construct a rough graph of the function defined by the polynomial.
- **FACTORING CUBIC POLYNOMIALS**
  - A-SSE.2: Seeing Structure in Expressions Interpret the structure of expressions. Use the structure of an expression to identify ways to rewrite it.
  - A-APR.4: Arithmetic with Polynomials and Rational Expressions Use polynomial identities to solve problems. Prove polynomial identities and use them to describe numerical relationships.
  - A-SSE.1.b: Seeing Structure in Expressions Interpret the structure of expressions. Interpret expressions that represent a quantity in terms of its context. Interpret complicated expressions by viewing one or more of their parts as a single entity.
  - A-APR.3: Arithmetic with Polynomials and Rational Expressions Understand the relationship between zeros and factors of polynomials. Identify zeros of polynomials when suitable factorizations are available, and use the zeros to construct a rough graph of the function defined by the polynomial.

Unit 14: Factoring Higher-Order Polynomials

- **FACTORING HIGHER-ORDER POLYNOMIALS**
  - A-SSE.1.a: Seeing Structure in Expressions Interpret the structure of expressions. Interpret expressions that represent a quantity in terms of its context. Interpret parts of an expression, such as terms, factors, and coefficients.

- A-SSE.1.b: Seeing Structure in Expressions Interpret the structure of expressions. Interpret expressions that represent a quantity in terms of its context. Interpret complicated expressions by viewing one or more of their parts as a single entity.
- A-APR.3: Arithmetic with Polynomials and Rational Expressions Understand the relationship between zeros and factors of polynomials. Identify zeros of polynomials when suitable factorizations are available, and use the zeros to construct a rough graph of the function defined by the polynomial.
- A-SSE.2: Seeing Structure in Expressions Interpret the structure of expressions. Use the structure of an expression to identify ways to rewrite it.
- A-APR.4: Arithmetic with Polynomials and Rational Expressions Use polynomial identities to solve problems. Prove polynomial identities and use them to describe numerical relationships.

- **FACTOR THEOREM AND REMAINDER THEOREM**
  - A-APR.6: Arithmetic with Polynomials and Rational Expressions Rewrite rational expressions. Rewrite simple rational expressions in different forms; write ()/() in the form () + ()/(), where (), (), (), and () are polynomials with the degree of () less than the degree of (), using inspection, long division, or, for the more complicated examples, a computer algebra system.
  - F-IF.2: Interpreting Functions Understand the concept of a function and use function notation. Use function notation, evaluate functions for inputs in their domains, and interpret statements that use function notation in terms of a context.
  - A-APR.2: Arithmetic with Polynomials and Rational Expressions Understand the relationship between zeros and factors of polynomials. Know and apply the Remainder Theorem: For a polynomial () and a number , the remainder on division by is (), so () = 0 if and only if ( ) is a factor of ().

Unit 15: Polynomial Functions and Complex Numbers

- **GRAPHS OF POLYNOMIAL FUNCTIONS**
  - A-APR.3: Arithmetic with Polynomials and Rational Expressions Understand the relationship between zeros and factors of polynomials. Identify zeros of polynomials when suitable factorizations are available, and use the zeros to construct a rough graph of the function defined by the polynomial.
  - F-IF.4.a: Interpreting Functions Interpret functions that arise in applications in terms of the context. For a function that models a relationship between two quantities, interpret key features of graphs and tables in terms of the quantities, and
  - F-IF.7.c: Interpreting Functions Analyze functions using different representations. Graph functions expressed symbolically and show key features of the graph, by hand in simple cases and using technology for more complicated cases. Graph polynomial functions, identifying zeros (using technology) or algebraic methods when suitable factorizations are available, and showing end behavior.
  - F-IF.4.b: Interpreting Functions Interpret functions that arise in applications in terms of the context. For a function that models a relationship between two quantities, sketch graphs showing key features given a verbal description of the relationship.

- F-BF.3: Building Functions Build new functions from existing functions. Identify the effect on the graph of replacing () by () + , (), (), and (+) for specific values of (both positive and negative); find the value of given the graphs.

- **COMPLEX NUMBERS**
  - N-CN.1: The Complex Number System Perform arithmetic operations with complex numbers. Know there is a complex number such that = 1, and every complex number has the form + with and real.
  - N-CN.2: The Complex Number System Perform arithmetic operations with complex numbers. Use the relation = 1 and the commutative, associative, and distributive properties to add, subtract, and multiply complex numbers.

Unit 16: Polynomial Identities and Complex Numbers

- **POLYNOMIAL IDENTITIES**
  - A-SSE.2: Seeing Structure in Expressions Interpret the structure of expressions. Use the structure of an expression to identify ways to rewrite it.
  - A-APR.4: Arithmetic with Polynomials and Rational Expressions Use polynomial identities to solve problems. Prove polynomial identities and use them to describe numerical relationships.
  - A-REI.4.a: Reasoning with Equations and Inequalities Solve equations and inequalities in one variable. Solve quadratic equations in one variable. Use the method of completing the square to transform any quadratic equation in x into an equation of the form ( ) = q that has the same solutions. Derive the quadratic formula from this form.
  - A-REI.4.b: Reasoning with Equations and Inequalities Solve equations and inequalities in one variable. Solve quadratic equations in one variable. Solve quadratic equations by inspection (e.g., for = 49), taking square roots, completing the square, the quadratic formula and factoring, as appropriate to the initial form of the equation. Recognize when the quadratic formula gives complex solutions and write them as for real numbers and .
  - A-APR.5: Arithmetic with Polynomials and Rational Expressions Use polynomial identities to solve problems. Know and apply the Binomial Theorem for the expansion of (+) in powers of and for a positive integer , where and are any numbers, with coefficients determined for example by Pascals Triangle.
- **POLYNOMIAL IDENTITIES AND COMPLEX NUMBERS**
  - A-SSE.2: Seeing Structure in Expressions Interpret the structure of expressions. Use the structure of an expression to identify ways to rewrite it.
  - A-APR.4: Arithmetic with Polynomials and Rational Expressions Use polynomial identities to solve problems. Prove polynomial identities and use them to describe numerical relationships.
  - N-CN.8: The Complex Number System Use complex numbers in polynomial identities and equations. Extend polynomial identities to the complex numbers. For example, rewrite + 4 as (+ 2)(2).
  - A-REI.4.b: Reasoning with Equations and Inequalities Solve equations and inequalities in one variable. Solve quadratic equations in one variable. Solve quadratic equations by inspection (e.g., for = 49), taking square roots, completing the square, the quadratic formula and factoring, as appropriate to

the initial form of the equation. Recognize when the quadratic formula gives complex solutions and write them as for real numbers and .

- N-CN.7: The Complex Number System Use complex numbers in polynomial identities and equations. Solve quadratic equations with real coefficients that have complex solutions.
- N-CN.8: The Complex Number System Use complex numbers in polynomial identities and equations. Extend polynomial identities to the complex numbers. For example, rewrite + 4 as (+ 2)(2).
- N-CN.9: The Complex Number System Use complex numbers in polynomial identities and equations. Know the Fundamental Theorem of Algebra; show that it is true for quadratic polynomials.

Unit 17: Radical Functions and Equations

- **ANALYZING GRAPHS OF SQUARE ROOT FUNCTIONS**
  - F-IF.4.b: Interpreting Functions Interpret functions that arise in applications in terms of the context. For a function that models a relationship between two quantities, sketch graphs showing key features given a verbal description of the relationship.
  - F-BF.3: Building Functions Build new functions from existing functions. Identify the effect on the graph of replacing () by () + , (), (), and (+) for specific values of (both positive and negative); find the value of given the graphs.
  - G-CO.6: Congruence Understand congruence in terms of rigid motions. Use geometric descriptions of rigid motions to transform figures and to predict the effect of a given rigid motion on a given figure; given two figures, use the definition of congruence in terms of rigid motions to decide if they are congruent.
  - F-IF.7.b: Interpreting Functions Analyze functions using different representations. Graph functions expressed symbolically and show key features of the graph, by hand in simple cases and using technology for more complicated cases. Graph square root, cube root, and piecewisedefined functions, including step functions and absolute value functions.
  - F-BF.4.a: Building Functions Build new functions from existing functions. Find inverse functions. Solve an equation of the form () = for a simple function that has an inverse and write an expression for the inverse.
  - F-BF.4.c: Building Functions Build new functions from existing functions. Find inverse functions. Read values of an inverse function from a graph or a table, given that the function has an inverse.
  - F-IF.4.a: Interpreting Functions Interpret functions that arise in applications in terms of the context. For a function that models a relationship between two quantities, interpret key features of graphs and tables in terms of the quantities, and
  - F-IF.5: Interpreting Functions Interpret functions that arise in applications in terms of the context. Relate the domain of a function to its graph and, where applicable, to the quantitative relationship it describes.
- **SOLVING SQUARE ROOT EQUATIONS**
  - A-REI.2: Reasoning with Equations and Inequalities Understand solving equations as a process of reasoning and explain the reasoning. Solve simple rational and radical equations in one variable, and

give examples showing how extraneous solutions may arise.

- F-IF.4.b: Interpreting Functions Interpret functions that arise in applications in terms of the context. For a function that models a relationship between two quantities, sketch graphs showing key features given a verbal description of the relationship.

Unit 18: Rational Expressions and Equations

- **OPERATIONS WITH RATIONAL EXPRESSIONS**
  - A-APR.7: Arithmetic with Polynomials and Rational Expressions Rewrite rational expressions. Add, subtract, multiply, and divide rational expressions. Understand that rational expressions form a system similar to the rational numbers, closed under addition, subtraction, multiplication, and division by a nonzero rational expression.
  - A-SSE.2: Seeing Structure in Expressions Interpret the structure of expressions. Use the structure of an expression to identify ways to rewrite it.
- **SOLVING RATIONAL EQUATIONS**
  - A-REI.2: Reasoning with Equations and Inequalities Understand solving equations as a process of reasoning and explain the reasoning. Solve simple rational and radical equations in one variable, and give examples showing how extraneous solutions may arise.
  - F-IF.7.d: Interpreting Functions Analyze functions using different representations. Graph functions expressed symbolically and show key features of the graph, by hand in simple cases and using technology for more complicated cases. Graph rational functions, identifying zeros and discontinuities (asymptotes/holes) using technology, and algebraic methods when suitable factorizations are available, and showing end behavior.
  - A-CED.3: Creating Equations and Inequalities Create equations and inequalities that describe numbers or relationships. Represent constraints by equations or inequalities, and by systems of equations and/or inequalities, and interpret solutions as viable or nonviable options in a modeling context.

Unit 19: Rational Functions

- **ANALYZING GRAPHS OF RATIONAL FUNCTIONS**
  - F-BF.3: Building Functions Build new functions from existing functions. Identify the effect on the graph of replacing () by () + , (), (), and (+) for specific values of (both positive and negative); find the value of given the graphs.
  - F-IF.7.d: Interpreting Functions Analyze functions using different representations. Graph functions expressed symbolically and show key features of the graph, by hand in simple cases and using technology for more complicated cases. Graph rational functions, identifying zeros and discontinuities (asymptotes/holes) using technology, and algebraic methods when suitable factorizations are available, and showing end behavior.
  - F-IF.4.a: Interpreting Functions Interpret functions that arise in applications in terms of the context. For a function that models a relationship between two quantities, interpret key features of graphs and tables in terms of the quantities, and

- F-IF.4.b: Interpreting Functions Interpret functions that arise in applications in terms of the context. For a function that models a relationship between two quantities, sketch graphs showing key features given a verbal description of the relationship.
- F-IF.5: Interpreting Functions Interpret functions that arise in applications in terms of the context. Relate the domain of a function to its graph and, where applicable, to the quantitative relationship it describes.

- **MODELING SITUATIONS WITH RATIONAL FUNCTIONS**
  - A-SSE.1.b: Seeing Structure in Expressions Interpret the structure of expressions. Interpret expressions that represent a quantity in terms of its context. Interpret complicated expressions by viewing one or more of their parts as a single entity.
  - A-CED.2: Creating Equations and Inequalities Create equations and inequalities that describe numbers or relationships. Create equations in two or more variables to represent relationships between quantities; graph equations on coordinate axes with labels and scales.
  - A-CED.3: Creating Equations and Inequalities Create equations and inequalities that describe numbers or relationships. Represent constraints by equations or inequalities, and by systems of equations and/or inequalities, and interpret solutions as viable or nonviable options in a modeling context.
  - F-BF.1.a: Building Functions Build a function that models a relationship between two quantities. Write a function that describes a relationship between two quantities. Determine an explicit expression, a recursive process, or steps for calculation from a context.
  - A-REI.2: Reasoning with Equations and Inequalities Understand solving equations as a process of reasoning and explain the reasoning. Solve simple rational and radical equations in one variable, and give examples showing how extraneous solutions may arise.

Unit 20: Nonlinear Functions

- **LINEAR VERSUS NONLINEAR FUNCTIONS**
  - F-LE.1.a: Linear, Quadratic, and Exponential Models Construct and compare linear, quadratic, and exponential models and solve problems. Distinguish between situations that can be modeled with linear functions and with exponential functions. Show that linear functions grow by equal differences over equal intervals, and that exponential functions grow by equal factors over equal intervals.
  - F-LE.1.b: Linear, Quadratic, and Exponential Models Construct and compare linear, quadratic, and exponential models and solve problems. Distinguish between situations that can be modeled with linear functions and with exponential functions. Recognize situations in which one quantity changes at a constant rate per unit interval relative to another.
  - F-LE.2: Linear, Quadratic, and Exponential Models Construct and compare linear, quadratic, and exponential models and solve problems. Construct linear and exponential functions, including arithmetic and geometric sequences, given a graph, a description of a relationship, or inputoutput table of values.
  - F-IF.6: Interpreting Functions Interpret functions that arise in applications in terms of the context. Calculate and interpret the average rate of change of a function (presented symbolically or as a table) over a specified interval. Estimate the rate of change from a graph.

- F-IF.4.a: Interpreting Functions Interpret functions that arise in applications in terms of the context. For a function that models a relationship between two quantities, interpret key features of graphs and tables in terms of the quantities, and
- F-LE.1.c: Linear, Quadratic, and Exponential Models Construct and compare linear, quadratic, and exponential models and solve problems. Distinguish between situations that can be modeled with linear functions and with exponential functions. Recognize situations in which a quantity grows or decays by a constant percent rate per unit interval relative to another.
- F-IF.4.b: Interpreting Functions Interpret functions that arise in applications in terms of the context. For a function that models a relationship between two quantities, sketch graphs showing key features given a verbal description of the relationship.
- F-IF.9: Interpreting Functions Analyze functions using different representations. Compare properties of two functions each represented in a different way (algebraically, graphically, numerically, in tables, or by verbal descriptions).

- **ABSOLUTE VALUE FUNCTIONS**
  - F-IF.5: Interpreting Functions Interpret functions that arise in applications in terms of the context. Relate the domain of a function to its graph and, where applicable, to the quantitative relationship it describes.
  - F-IF.1: Interpreting Functions Understand the concept of a function and use function notation. Understand that a function from one set (called the domain) to another set (called the range) assigns to each element of the domain exactly one element of the range. If is a function and is an element of its domain, then () denotes the output of corresponding to the input . The graph of is the graph of the equation = ().
  - F-IF.4.a: Interpreting Functions Interpret functions that arise in applications in terms of the context. For a function that models a relationship between two quantities, interpret key features of graphs and tables in terms of the quantities, and
  - F-IF.4.b: Interpreting Functions Interpret functions that arise in applications in terms of the context. For a function that models a relationship between two quantities, sketch graphs showing key features given a verbal description of the relationship.
  - F-IF.7.b: Interpreting Functions Analyze functions using different representations. Graph functions expressed symbolically and show key features of the graph, by hand in simple cases and using technology for more complicated cases. Graph square root, cube root, and piecewisedefined functions, including step functions and absolute value functions.
  - F-BF.3: Building Functions Build new functions from existing functions. Identify the effect on the graph of replacing () by () + , (), (), and (+) for specific values of (both positive and negative); find the value of given the graphs.
- **ARITHMETIC OPERATIONS ON FUNCTIONS**
  - F-BF.1.b: Building Functions Build a function that models a relationship between two quantities. Write a function that describes a relationship between two quantities. Combine standard function types using arithmetic operations.

Unit 21: Trigonometry and Trigonometric Functions

- **RADIANS AND THE UNIT CIRCLE**
  - F-TF.1: Trigonometric Functions Extend the domain of trigonometric functions using the unit circle. Understand radian measure of an angle as the length of the arc on the unit circle subtended by the angle.
  - F-TF.2: Trigonometric Functions Extend the domain of trigonometric functions using the unit circle. Explain how the unit circle in the coordinate plane enables the extension of trigonometric functions to all real numbers, interpreted as radian measures of angles traversed counterclockwise around the unit circle.
  - G-C.5: Circles Find arc lengths and areas of sectors of circles. Use and apply the concepts of arc length and areas of sectors of circles. Determine or derive using similarity the fact that the length of the arc intercepted by an angle is proportional to the radius, and define the radian measure of the angle as the constant of proportionality; derive the formula for the area of a sector.
  - F-TF.3: Trigonometric Functions Extend the domain of trigonometric functions using the unit circle. Use special triangles to determine geometrically the values of sine, cosine, tangent for /3, /4 and /6, and use the unit circle to express the values of sine, cosines, and tangent for , + , and 2 in terms of their values for , where is any real number.
  - F-TF.4: Trigonometric Functions Extend the domain of trigonometric functions using the unit circle. Use the unit circle to explain symmetry (odd and even) and periodicity of trigonometric functions.
  - G-CO.1: Congruence Experiment with transformations in the plane. Demonstrates understanding of key geometrical definitions, including angle, circle, perpendicular line, parallel line, line segment, and transformations in Euclidian geometry. Understand undefined notions of point, line, distance along a line, and distance around a circular arc.
  - G-SRT.8: Similarity, Right Triangles, and Trigonometry Define trigonometric ratios and solve problems involving right triangles. Use trigonometric ratios and the Pythagorean Theorem to solve right triangles in applied problems.
- **TRIGONOMETRIC FUNCTIONS**
  - F-IF.4.b: Interpreting Functions Interpret functions that arise in applications in terms of the context. For a function that models a relationship between two quantities, sketch graphs showing key features given a verbal description of the relationship.
  - F-IF.7.e: Interpreting Functions Analyze functions using different representations. Graph functions expressed symbolically and show key features of the graph, by hand in simple cases and using technology for more complicated cases. Graph exponential and logarithmic functions, showing intercepts and end behavior, and trigonometric functions, showing period, midline, and amplitude.
  - F-TF.2: Trigonometric Functions Extend the domain of trigonometric functions using the unit circle. Explain how the unit circle in the coordinate plane enables the extension of trigonometric functions to all real numbers, interpreted as radian measures of angles traversed counterclockwise around the unit circle.

- F-TF.5: Trigonometric Functions Model periodic phenomena with trigonometric functions. Choose trigonometric functions to model periodic phenomena with specified amplitude, frequency, and midline.
- F-TF.8: Trigonometric Functions Prove and apply trigonometric identities. Prove the Pythagorean identity sin() + cos() = 1 and use it to calculate trigonometric ratios.

Unit 22: Parent Functions and Transformations

- **PARENT FUNCTIONS**
  - F-IF.7.c: Interpreting Functions Analyze functions using different representations. Graph functions expressed symbolically and show key features of the graph, by hand in simple cases and using technology for more complicated cases. Graph polynomial functions, identifying zeros (using technology) or algebraic methods when suitable factorizations are available, and showing end behavior.
  - F-IF.4.a: Interpreting Functions Interpret functions that arise in applications in terms of the context. For a function that models a relationship between two quantities, interpret key features of graphs and tables in terms of the quantities, and
  - F-IF.5: Interpreting Functions Interpret functions that arise in applications in terms of the context. Relate the domain of a function to its graph and, where applicable, to the quantitative relationship it describes.
  - F-BF.3: Building Functions Build new functions from existing functions. Identify the effect on the graph of replacing () by () + , (), (), and (+) for specific values of (both positive and negative); find the value of given the graphs.
  - F-IF.4.b: Interpreting Functions Interpret functions that arise in applications in terms of the context. For a function that models a relationship between two quantities, sketch graphs showing key features given a verbal description of the relationship.
  - F-IF.7.b: Interpreting Functions Analyze functions using different representations. Graph functions expressed symbolically and show key features of the graph, by hand in simple cases and using technology for more complicated cases. Graph square root, cube root, and piecewisedefined functions, including step functions and absolute value functions.
  - F-IF.7.e: Interpreting Functions Analyze functions using different representations. Graph functions expressed symbolically and show key features of the graph, by hand in simple cases and using technology for more complicated cases. Graph exponential and logarithmic functions, showing intercepts and end behavior, and trigonometric functions, showing period, midline, and amplitude.
- **TRANSFORMATIONS OF PARENT FUNCTIONS**
  - F-IF.4.b: Interpreting Functions Interpret functions that arise in applications in terms of the context. For a function that models a relationship between two quantities, sketch graphs showing key features given a verbal description of the relationship.
  - F-IF.7.b: Interpreting Functions Analyze functions using different representations. Graph functions expressed symbolically and show key features of the graph, by hand in simple cases and using

technology for more complicated cases. Graph square root, cube root, and piecewisedefined functions, including step functions and absolute value functions.

- F-IF.7.c: Interpreting Functions Analyze functions using different representations. Graph functions expressed symbolically and show key features of the graph, by hand in simple cases and using technology for more complicated cases. Graph polynomial functions, identifying zeros (using technology) or algebraic methods when suitable factorizations are available, and showing end behavior.
- F-IF.7.e: Interpreting Functions Analyze functions using different representations. Graph functions expressed symbolically and show key features of the graph, by hand in simple cases and using technology for more complicated cases. Graph exponential and logarithmic functions, showing intercepts and end behavior, and trigonometric functions, showing period, midline, and amplitude.
- F-BF.3: Building Functions Build new functions from existing functions. Identify the effect on the graph of replacing () by () + , (), (), and (+) for specific values of (both positive and negative); find the value of given the graphs.
- F-IF.4.a: Interpreting Functions Interpret functions that arise in applications in terms of the context. For a function that models a relationship between two quantities, interpret key features of graphs and tables in terms of the quantities, and
- F-BF.3: Building Functions Build new functions from existing functions. Identify the effect on the graph of replacing () by () + , (), (), and (+) for specific values of (both positive and negative); find the value of given the graphs.
- G-CO.6: Congruence Understand congruence in terms of rigid motions. Use geometric descriptions of rigid motions to transform figures and to predict the effect of a given rigid motion on a given figure; given two figures, use the definition of congruence in terms of rigid motions to decide if they are congruent.
- F-IF.5: Interpreting Functions Interpret functions that arise in applications in terms of the context. Relate the domain of a function to its graph and, where applicable, to the quantitative relationship it describes.
- F-BF.3: Building Functions Build new functions from existing functions. Identify the effect on the graph of replacing () by () + , (), (), and (+) for specific values of (both positive and negative); find the value of given the graphs.

- **MULTIPLE TRANSFORMATIONS OF PARENT FUNCTIONS**
  - F-IF.4.a: Interpreting Functions Interpret functions that arise in applications in terms of the context. For a function that models a relationship between two quantities, interpret key features of graphs and tables in terms of the quantities, and
  - F-IF.4.b: Interpreting Functions Interpret functions that arise in applications in terms of the context. For a function that models a relationship between two quantities, sketch graphs showing key features given a verbal description of the relationship.
  - F-BF.3: Building Functions Build new functions from existing functions. Identify the effect on the graph of replacing () by () + , (), (), and (+) for specific values of (both positive and negative); find the value of

given the graphs.

- G-CO.6: Congruence Understand congruence in terms of rigid motions. Use geometric descriptions of rigid motions to transform figures and to predict the effect of a given rigid motion on a given figure; given two figures, use the definition of congruence in terms of rigid motions to decide if they are congruent.
- F-IF.5: Interpreting Functions Interpret functions that arise in applications in terms of the context. Relate the domain of a function to its graph and, where applicable, to the quantitative relationship it describes.
- F-BF.3: Building Functions Build new functions from existing functions. Identify the effect on the graph of replacing () by () + , (), (), and (+) for specific values of (both positive and negative); find the value of given the graphs.
- F-IF.7.c: Interpreting Functions Analyze functions using different representations. Graph functions expressed symbolically and show key features of the graph, by hand in simple cases and using technology for more complicated cases. Graph polynomial functions, identifying zeros (using technology) or algebraic methods when suitable factorizations are available, and showing end behavior.
- F-BF.3: Building Functions Build new functions from existing functions. Identify the effect on the graph of replacing () by () + , (), (), and (+) for specific values of (both positive and negative); find the value of given the graphs.
- G-CO.2: Congruence Experiment with transformations in the plane. Represent transformations in the plane using, e.g., transparencies and geometry software; describe transformations as functions that take points in the plane as inputs and give other points as outputs. Compare transformations that preserve distance and angle to those that do not (e.g., translation versus horizontal stretch).
- F-IF.7.b: Interpreting Functions Analyze functions using different representations. Graph functions expressed symbolically and show key features of the graph, by hand in simple cases and using technology for more complicated cases. Graph square root, cube root, and piecewisedefined functions, including step functions and absolute value functions.
- F-BF.3: Building Functions Build new functions from existing functions. Identify the effect on the graph of replacing () by () + , (), (), and (+) for specific values of (both positive and negative); find the value of given the graphs.
- F-IF.7.e: Interpreting Functions Analyze functions using different representations. Graph functions expressed symbolically and show key features of the graph, by hand in simple cases and using technology for more complicated cases. Graph exponential and logarithmic functions, showing intercepts and end behavior, and trigonometric functions, showing period, midline, and amplitude.
- F-BF.3: Building Functions Build new functions from existing functions. Identify the effect on the graph of replacing () by () + , (), (), and (+) for specific values of (both positive and negative); find the value of given the graphs.

Unit 23: Systems of Equations

- **SOLVING THREE-VARIABLE SYSTEMS OF LINEAR EQUATIONS**

- A-CED.3: Creating Equations and Inequalities Create equations and inequalities that describe numbers or relationships. Represent constraints by equations or inequalities, and by systems of equations and/or inequalities, and interpret solutions as viable or nonviable options in a modeling context.
- A-REI.5: Reasoning with Equations and Inequalities Solve systems of equations. Show that, given a system of two equations in two variables, replacing one equation by the sum of that equation and a multiple of the other produces a system with the same solutions.

- **SYSTEMS OF NONLINEAR EQUATIONS**
  - A-REI.7: Reasoning with Equations and Inequalities Solve systems of equations. Solve a simple system consisting of a linear equation and a quadratic equation in two variables algebraically and graphically.
  - A-REI.11: Reasoning with Equations and Inequalities Represent and solve equations and inequalities graphically. Explain why the coordinates of the points where the graphs of the equations = () and = () intersect are the solutions of the equation () = (); find the solutions approximately, e.g., using technology to graph the functions, make tables of values, or find successive approximations. Include cases where () and/or () are linear, polynomial, rational, absolute value, exponential, and logarithmic functions.
  - A-REI.5: Reasoning with Equations and Inequalities Solve systems of equations. Show that, given a system of two equations in two variables, replacing one equation by the sum of that equation and a multiple of the other produces a system with the same solutions.
  - A-REI.11: Reasoning with Equations and Inequalities Represent and solve equations and inequalities graphically. Explain why the coordinates of the points where the graphs of the equations = () and = () intersect are the solutions of the equation () = (); find the solutions approximately, e.g., using technology to graph the functions, make tables of values, or find successive approximations. Include cases where () and/or () are linear, polynomial, rational, absolute value, exponential, and logarithmic functions.
  - A-CED.3: Creating Equations and Inequalities Create equations and inequalities that describe numbers or relationships. Represent constraints by equations or inequalities, and by systems of equations and/or inequalities, and interpret solutions as viable or nonviable options in a modeling context.
  - A-REI.6: Reasoning with Equations and Inequalities Solve systems of equations. Solve systems of linear equations exactly and approximately, e.g., with graphs or algebraically, focusing on pairs of linear equations in two variables.
  - A-REI.11: Reasoning with Equations and Inequalities Represent and solve equations and inequalities graphically. Explain why the coordinates of the points where the graphs of the equations = () and = () intersect are the solutions of the equation () = (); find the solutions approximately, e.g., using technology to graph the functions, make tables of values, or find successive approximations. Include cases where () and/or () are linear, polynomial, rational, absolute value, exponential, and logarithmic functions.
  - A-REI.11: Reasoning with Equations and Inequalities Represent and solve equations and inequalities graphically. Explain why the coordinates of the points where the graphs of the equations = () and = () intersect are the solutions of the equation () = (); find the solutions approximately, e.g., using

technology to graph the functions, make tables of values, or find successive approximations. Include cases where () and/or () are linear, polynomial, rational, absolute value, exponential, and logarithmic functions.

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- A-REI.11: Reasoning with Equations and Inequalities Represent and solve equations and inequalities graphically. Explain why the coordinates of the points where the graphs of the equations = () and = () intersect are the solutions of the equation () = (); find the solutions approximately, e.g., using technology to graph the functions, make tables of values, or find successive approximations. Include cases where () and/or () are linear, polynomial, rational, absolute value, exponential, and logarithmic functions.
- A-REI.11: Reasoning with Equations and Inequalities Represent and solve equations and inequalities graphically. Explain why the coordinates of the points where the graphs of the equations = () and = () intersect are the solutions of the equation () = (); find the solutions approximately, e.g., using technology to graph the functions, make tables of values, or find successive approximations. Include cases where () and/or () are linear, polynomial, rational, absolute value, exponential, and logarithmic functions.

Unit 24: Statistical Design and Analysis

- **ANALYZING STATISTICAL SAMPLES**
  - S-IC.1: Making Inferences and Justifying Conclusions Understand and evaluate random processes underlying statistical experiments. Understand statistics as a process for making inferences about population parameters based on a random sample from that population.
  - S-IC.4: Making Inferences and Justifying Conclusions Make inferences and justify conclusions from sample surveys, experiments, and observational studies. Use data from a sample survey to estimate a population mean or proportion; develop a margin of error through the use of simulation models for random sampling.
  - S-IC.2: Making Inferences and Justifying Conclusions Understand and evaluate random processes underlying statistical experiments. Decide if a specified model is consistent with results from a given datagenerating process, e.g., using simulation.
- **EXPERIMENTAL AND OBSERVATIONAL DESIGN**
  - S-IC.3: Making Inferences and Justifying Conclusions Make inferences and justify conclusions from sample surveys, experiments, and observational studies. Recognize the purposes of and differences among sample surveys, experiments, and observational studies; explain how randomization relates to each.
- **CONCLUSIONS IN DATA**

- S-IC.5: Making Inferences and Justifying Conclusions Make inferences and justify conclusions from sample surveys, experiments, and observational studies. Use data from a randomized experiment to compare two treatments; use simulations to decide if differences between parameters are significant.
- S-IC.6: Making Inferences and Justifying Conclusions Make inferences and justify conclusions from sample surveys, experiments, and observational studies. Evaluate reports based on data.

Unit 25: Statistics and Probability

- **NORMAL DISTRIBUTION**
  - S-ID.3: Interpreting Categorical and Quantitative Data Summarize, represent, and interpret data on a single count or measurement variable. Interpret differences in shape, center, and spread in the context of the data sets, accounting for possible effects of extreme data points (outliers).
  - S-ID.4: Interpreting Categorical and Quantitative Data Summarize, represent, and interpret data on a single count or measurement variable. Use the mean and standard deviation of a data set to fit it to a normal distribution and to estimate population percentages. Recognize that there are data sets for which such a procedure is not appropriate. Use calculators, spreadsheets, and tables to estimate areas under the normal curve.
  - S-IC.4: Making Inferences and Justifying Conclusions Make inferences and justify conclusions from sample surveys, experiments, and observational studies. Use data from a sample survey to estimate a population mean or proportion; develop a margin of error through the use of simulation models for random sampling.
- **ANALYZING DECISIONS IN PROBABILITY**
  - S-MD.6: Using Probability to Make Decisions Use probability to evaluate outcomes of decisions. Use probabilities to make fair decisions (e.g., drawing by lots, using a random number generator).
  - S-MD.7: Using Probability to Make Decisions Use probability to evaluate outcomes of decisions. Analyze decisions and strategies using probability concepts (e.g., product testing, medical testing, pulling a hockey goalie at the end of a game).