

Chapter 3.3 Notes Properties of Functions

- * Function is “even” if the graph is symmetric with respect to the y-axis.
- * Function is “odd” if the graph is symmetric with respect to the x-axis.
- * A function can increase, decrease, or stay the same.
- * Local maximum — the “x” value where the graph reaches a peak
- * Local minimum — the “x” value where the graph reaches a valley
- * Local maximum value — the value of “y” where the graph reaches a peak
- * Local minimum value — the value of “y” where the graph reaches a valley
- * Absolute maximum — the highest point on a graph
- * Absolute minimum — the lowest point on the graph

* average rate of change:
$$\frac{f(b) - f(a)}{b - a}$$

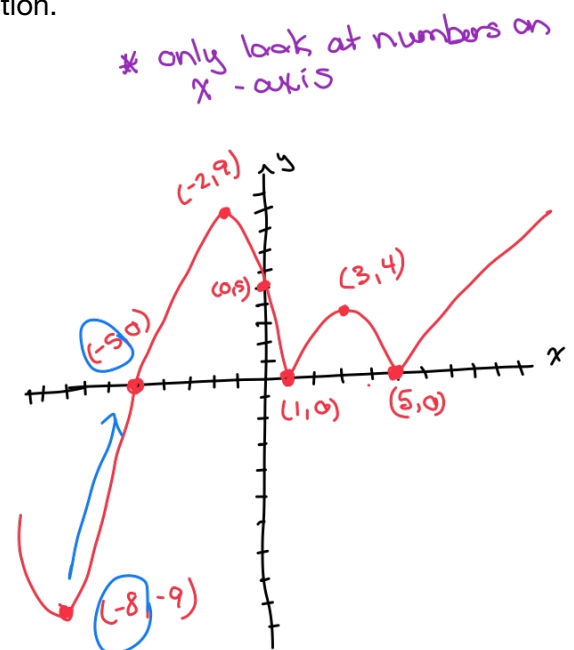
1. Use the graph of the function f given below to answer the question.
* is f increasing on the interval $[-8, -5]$?

$[-8, -5]$

yes, its increasing

* Look at the first number. Find the ordered pair with that number as the x in the ordered pair (the 1st number in the ordered pair.)

* Look at the second number. Find the ordered pair with that number as the x in the ordered pair (the 1st number in the ordered pair.)



- * Look at the line between the points. If the line slants up \nearrow , then it is increasing.
- * If the line slants down \searrow , then it's decreasing.

2. Use the graph of the function f given below to answer the question.
 *is f increasing on the interval $[-2, 3]$?

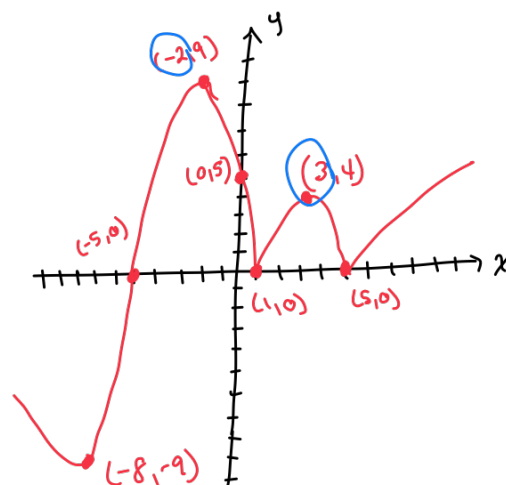
**only look at numbers on x-axis*

$[-2, 3]$

No, because it increases + decreases

* Look at the first number. Find the ordered pair with that number as the x in the ordered pair (the 1st number in the ordered pair.)

* Look at the second number. Find the ordered pair with that number as the x in the ordered pair (the 1st number in the ordered pair.)

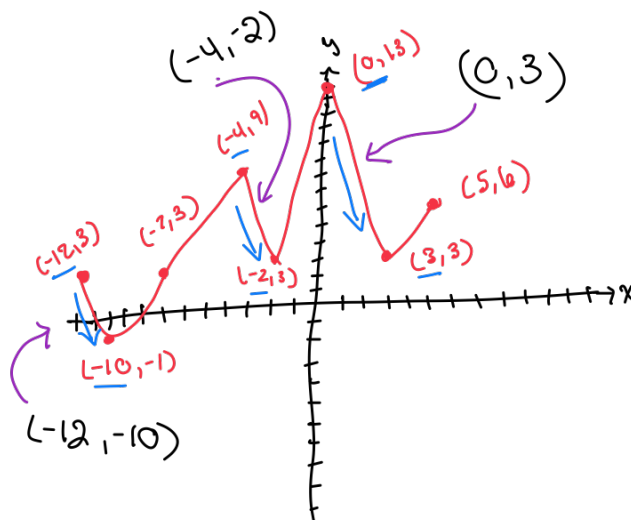


- * Look at the line between the points. If the line slants up \nearrow , then it is increasing.
 * If the line slants down \searrow , then it's decreasing.

3. List the intervals on which f is decreasing.

$(-12, -10), (-4, -2), (0, 3)$

- * Start on the left side of the graph. Trace the graph with your finger.
 * Find the point where the graph begins to go down. Write down the " x " number. Then trace the graph until it starts to turn and go up, and write down that number.
 * Keep following the graph and doing the same thing.



4. Use the graph of the function f given below to answer the questions.

* Is there a local minimum at $x = 4$?

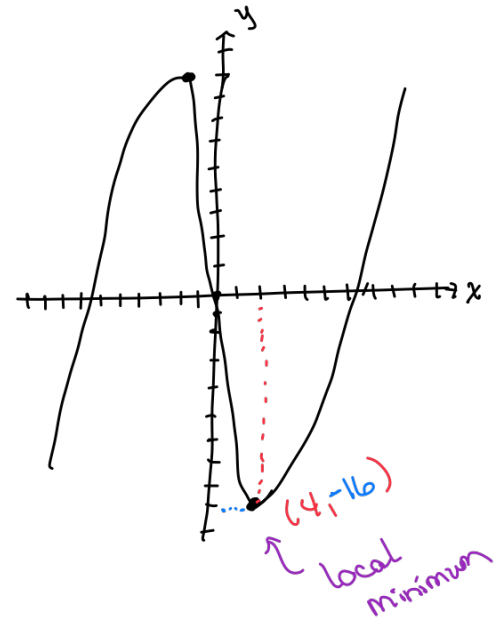
yes, there is a local minimum at $x = 4$

* To find the local minimum, find where the graph has a valley.
Write down what the x value is at that point.

The local minimum is

$$y = -16$$

* This is the y value at that point.



5. Use the graph of the function f given below to answer the questions.

Local maximum:

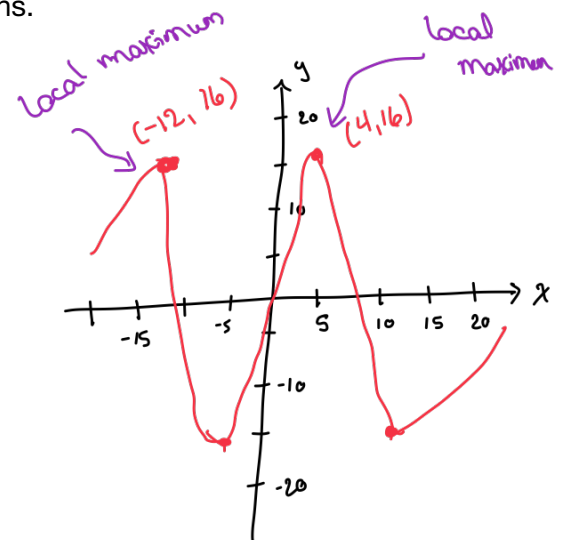
$$x = -12, 4$$

* The x -value of each pair.

The local maxima are:

$$16, 16$$

* The y -values of each pair



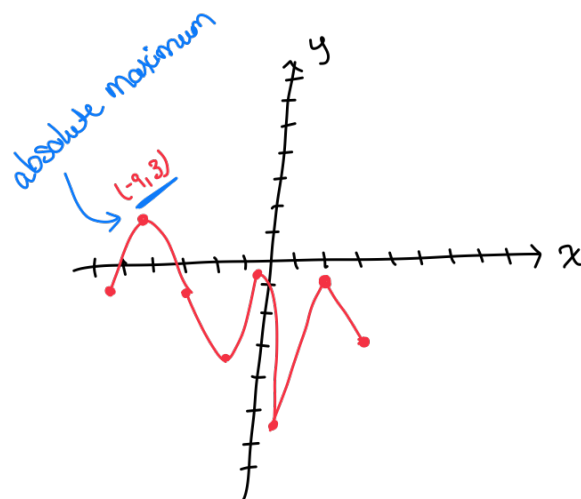
6. Find the absolute maximum of f on $[-11, 6]$.

The absolute maximum of f is

$$f(-9) = 3$$

x y

* This is the highest point on the graph.



7. Use the graph to find:

a) The values of x at which f has a local maximum is:

$$x = 0$$

The local maximum is

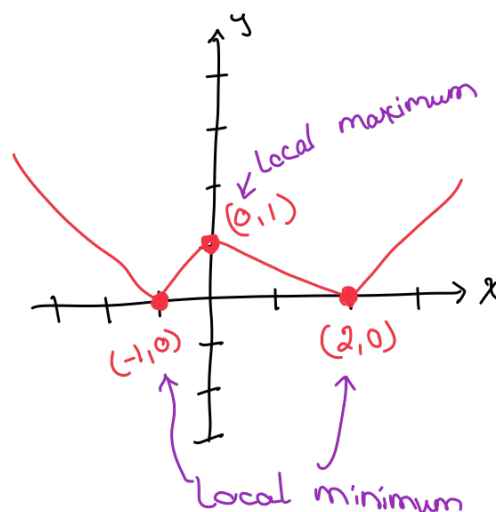
$$y = 1$$

b) The values at which x has a local minimum is

$$x = -1, 2$$

The local minimum are

$$y = 0, 0$$



* local maximum is any mountain top

* local minimum is any valley point

8. Use the given graph of the function f to find the following:

- a) Find the values of x at which f has a local maximum.

$$x = \boxed{\frac{\pi}{2}}$$

Find the local maximum.

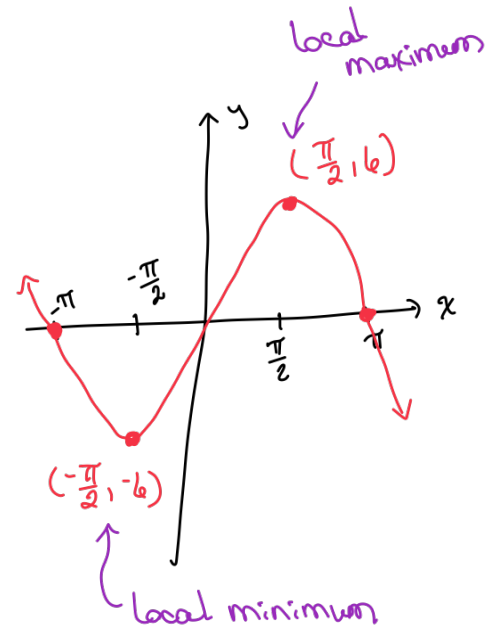
The local maximum is $\boxed{6}$

- b) Find the values of x at which f has a local minimum.

$$x = \boxed{-\frac{\pi}{2}}$$

Find the local minimum.

The local minimum is $\boxed{-6}$



9. Determine algebraically whether the given function is even, odd, or neither.

$$f(x) = -9x^3 + 3x$$

write equation down twice.

$$\begin{aligned} f(x) &= -9x^3 + 3x \\ &= -9(1)^3 + 3(1) \\ &= -6 \end{aligned}$$

Replace x with (1)

$$\begin{aligned} f(x) &= -9x^3 + 3x \\ &= -9(-1)^3 + 3(-1) \\ &= 6 \end{aligned}$$

Replace x with (-1)

$\boxed{\text{Odd}}$

* Replace each x with a 1.

* Then type in calculator.

* Then write down equation again, but replace x with a (-1) .

Even:

If numbers are exact same

Odd:

If number are the same but have different signs

10. Determine algebraically whether the given function is even, odd, or neither.

$$g(x) = -3x^3 - 2$$

Replace x with (1)

$$\begin{aligned} g(x) &= -3x^3 - 2 \\ &= -3(1)^3 - 2 \\ &= -5 \end{aligned}$$

write down equation twice

$$\begin{aligned} g(x) &= -3x^3 - 2 \\ &= -3(-1)^3 - 2 \\ &= 1 \end{aligned}$$

Replace x with (-1)

Neither

- * Replace each x with a 1.
- * Then type in calculator.
- * Then write down equation again, but replace x with a (-1) .

Even:

If numbers are exact same

Odd:

If number are the same but have different signs

11. Determine algebraically whether the given function is even, odd, or neither.

$$f(x) = \sqrt[7]{6x}$$

Replace x with (1)

$$\begin{aligned} f(x) &= \sqrt[7]{6x} \\ &= \sqrt[7]{6(1)} \\ &= 1.2917 \end{aligned}$$

Replace x with (-1)

$$\begin{aligned} f(x) &= \sqrt[7]{6x} \\ &= \sqrt[7]{6(-1)} \\ &= -1.2917 \end{aligned}$$

Odd

Even:

If numbers are exact same

Odd:

If number are the same but have different signs

12. Determine algebraically whether the given function is even, odd, or neither.

$$f(x) = \frac{5}{x^{16}}$$

Replace x with 1

$$\begin{aligned} f(x) &= \frac{5}{x^{16}} \\ &= \frac{5}{(1)^{16}} \\ &= 5 \end{aligned}$$

Replace x with (-1)

$$\begin{aligned} f(x) &= \frac{5}{x^{16}} \\ &= \frac{5}{(-1)^{16}} \\ &= 5 \end{aligned}$$

Even

Even:

If numbers are exact same

Odd:

If number are the same but have different signs

13. Find the average rate of change of $f(x) = 2x^2 + 5$ over the following intervals.

a. From 2 to 4

Replace x with # for b

$$\frac{2x^2 + 5 - (2x^2 + 5)}{b - a}$$

Replace x with # for a

$$\frac{2(4)^2 + 5 - (2(2)^2 + 5)}{4 - 2} = 12$$

Type into calculator

average Rate of change formula:

$$\frac{f(b) - f(a)}{b - a}$$

Replace x 's with # for b

Replaces x 's with # for a

$$\frac{\text{equation} - (\text{equation})}{b - a}$$

b. From 4 to 6

Replace x with # for b

$$\frac{2x^2 + 5 - (2x^2 + 5)}{b - a}$$

Replace x with # for a

$$\frac{2(6)^2 + 5 - (2(4)^2 + 5)}{6 - 4} = 20$$

Type into calculator

c. From 2 to 5

Replace x with # for b

$$\frac{2x^2 + 5 - (2x^2 + 5)}{b - a}$$

Replace x with # for a

$$\frac{2(5)^2 + 5 - (2(2)^2 + 5)}{5 - 2} = 14$$

Type into calculator

14. Find the average rate of change of $f(x) = x^3 - 7x + 7$ over the following intervals.

$$f(x) = x^3 - 7x + 7$$

$$\frac{f(b) - f(a)}{b - a}$$

A. From -7 to -5

Replace x 's with # for b

$$\frac{x^3 - 7x + 7 - (x^3 - 7x + 7)}{b - a}$$

Replace x 's with # for a

$$\frac{(-5)^3 - 7(-5) + 7 - ((-7)^3 - 7(-7) + 7)}{-5 - (-7)} = \boxed{102}$$

Type into calculator

B. From -1 to 5

Replace x 's with # for b

$$\frac{x^3 - 7x + 7 - (x^3 - 7x + 7)}{b - a}$$

Replace x 's with # for a

$$\frac{(5)^3 - 7(5) + 7 - ((-1)^3 - 7(-1) + 7)}{5 - (-1)} = \boxed{14}$$

Type into calculator

C. From 5 to 8

Replace x 's with # for b

$$\frac{x^3 - 7x + 7 - (x^3 - 7x + 7)}{b - a}$$

Replace x 's with # for a

$$\frac{(8)^3 - 7(8) + 7 - (5^3 - 7(5) + 7)}{8 - 5} = \boxed{122}$$

Type into calculator