

Intro to College Math: Chapter 11.1
Simplifying Radical Expressions

* Rational Exponent Property: the quantity of $x^{1/n}$ is the nth root of x.

ex.) $x^{1/n} = \sqrt[n]{x}$

* Properties of Exponents:

* $a^r \cdot a^s = a^{r+s}$

* $(a^r)^s = a^{r \cdot s}$

* $(ab)^r = a^r b^r$

* $a^{-r} = \frac{1}{a^r}$

* $\left(\frac{a}{b}\right)^r = \frac{a^r}{b^r}$

* $\frac{a^r}{a^s} = a^{r-s}$

* $a^{1/r} = \sqrt[r]{a}$

1. Simplify using absolute values if necessary.

$\sqrt{64x^4}$

$\sqrt{64x^4}$

$\sqrt{64} \cdot \sqrt{x^4}$

$8 \cdot x^{\frac{4}{2}}$

$8 \cdot x^{4 \div 2}$ ← Divide

$8x^2$

* First, rewrite the problem separating the number from the variable.

* Then take the square root of the number.

* For the variable, make a fraction for the exponent.

• The exponent that was under $\sqrt{\quad}$ goes on top.

• Little exponent outside $\sqrt{\quad}$ goes on bottom.
(if no number outside, use "2")

2. Simplify. $-\sqrt{49x^8}$

$$-\sqrt{49x^8}$$

$$-\sqrt{49} \cdot \sqrt{x^8}$$

$$-7 \cdot x^{\frac{8}{2}}$$

$$-7 \cdot x^{8 \div 2}$$

$$\boxed{-7x^4}$$

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(if no number outside, use "2")

3. Assume all variables are positive, and find the following root.

$$\sqrt[3]{343x^3}$$

$$\sqrt[3]{343x^3}$$

$$\sqrt[3]{343} \cdot \sqrt[3]{x^3}$$

$$7 \cdot x^{\frac{3}{3}}$$

$$7 \cdot x^{3 \div 3}$$

$$\boxed{7x}$$

* First, rewrite the problem separating the number from the variable.

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• Little exponent outside $\sqrt{\quad}$ goes on bottom.
(if no number outside, use "2")

To type into calculator:

- * type the little number outside the $\sqrt{\quad}$ first.
- * then press the "2nd" button
- * then press the "^" button
- * then typed in the number under the $\sqrt{\quad}$
- * then press enter.

4. Assume all variables are positive, and find the following root.

$$\sqrt[5]{32 x^{15} y^{15}}$$

$$\begin{aligned} & \sqrt[5]{32 x^{15} y^{15}} \\ & \sqrt[5]{32} \cdot \sqrt[5]{x^{15}} \cdot \sqrt[5]{y^{15}} \\ & 2 \cdot x^{\frac{15}{5}} \cdot y^{\frac{15}{5}} \\ & 2 \cdot x^{15 \div 5} \cdot y^{15 \div 5} \\ & \boxed{2 x^3 y^3} \end{aligned}$$

Divide

* First, rewrite the problem separating the number from the variable.

* Then take the square root of the number.

* For the variable, make a fraction for the exponent.

• The exponent that was under $\sqrt{\quad}$ goes on top.

• Little exponent outside $\sqrt{\quad}$ goes on bottom.
(if no number outside, use "2")

5. Assume all variables are positive, and find the following root.

$$\sqrt[4]{16 x^8 y^4}$$

$$\begin{aligned} & \sqrt[4]{16 x^8 y^4} \\ & \sqrt[4]{16} \cdot \sqrt[4]{x^8} \cdot \sqrt[4]{y^4} \\ & 2 \cdot x^{\frac{8}{4}} \cdot y^{\frac{4}{4}} \\ & 2 \cdot x^{8 \div 4} \cdot y^{4 \div 4} \\ & \boxed{2 x^2 y} \end{aligned}$$

Divide

* First, rewrite the problem separating the number from the variable.

* Then take the square root of the number.

* For the variable, make a fraction for the exponent.

• The exponent that was under $\sqrt{\quad}$ goes on top.

• Little exponent outside $\sqrt{\quad}$ goes on bottom.
(if no number outside, use "2")

6. Assume all variables are positive, and find the following root.

$$\sqrt[3]{-8x^{15}y^{12}}$$

$$\sqrt[3]{-8x^{15}y^{12}}$$

$$\sqrt[3]{-8} \cdot \sqrt[3]{x^{15}} \cdot \sqrt[3]{y^{12}}$$

$$-2 \cdot x^{5/3} \cdot y^{4/3}$$

$$-2 \cdot x^{15 \div 3} \cdot y^{12 \div 3}$$

$$\boxed{-2x^5y^4}$$

* First, rewrite the problem separating the number from the variable.

* Then take the square root of the number.

* For the variable, make a fraction for the exponent.

• The exponent that was under $\sqrt{\quad}$ goes on top.

• Little exponent outside $\sqrt{\quad}$ goes on bottom.
(if no number outside, use "2")

7. Simplify. Assume variables are positive.

$$\sqrt{16u^7g^8}$$

$$\sqrt{16u^7g^8}$$

$$\sqrt{16} \cdot \sqrt{u^7} \cdot \sqrt{g^8}$$

$$4 \cdot u^{7/2} \cdot g^{8/2}$$

$$4 \cdot u^{7 \div 2} \cdot g^{8 \div 2}$$

$$4 \cdot u^{3.5} \cdot g^4$$

cannot have a decimal in exponent. so....
Rethink $u^{7/2}$

$$u \cdot u \cdot u \cdot u \cdot u \cdot u \cdot u$$

$$u^3 \sqrt{u}$$

$$\boxed{4g^4u^3\sqrt{u}}$$

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• Little exponent outside $\sqrt{\quad}$ goes on bottom.
(if no number outside, use "2")

← Rethink:

$$u^{7/2}$$

• Write down the variable the number of times the top # says.

• Then the bottom # tells you how many to put in a group + circle.

• Count the circled groups, + that number becomes exponent.

• Any leftovers go back under the $\sqrt{\quad}$.

8. Simplify. Assume all variables are nonnegative.

$$\sqrt{16a^{11}b^{15}}$$

$$\sqrt{16a^{11}b^{15}}$$

$$\sqrt{16} \cdot \sqrt{a^{11}} \cdot \sqrt{b^{15}}$$

$$4 \cdot a^{11/2} \cdot b^{15/2}$$

$$4 \cdot a^{11 \div 2} \cdot b^{15 \div 2}$$

$$4 \cdot a^{5.5} \cdot b^{7.5}$$

cannot have a decimal in exponent. so....
Rethink

$$a^{11/2} =$$

$$\underbrace{a \cdot a}_1 \cdot \underbrace{a \cdot a}_2 \cdot \underbrace{a \cdot a}_3 \cdot \underbrace{a \cdot a}_4 \cdot \underbrace{a \cdot a}_5$$

$$a^5 \sqrt{a}$$

← Rethink:

$$a^{7/2}$$

• Write down the variable the number of times the top # says.

• Then the bottom # tells you how many to put in a group + circle.

• Count the circled groups, + that number becomes exponent.

• Any leftovers go back under the $\sqrt{}$.

$$b^{15/2} =$$

$$\underbrace{b \cdot b}_1 \cdot \underbrace{b \cdot b}_2 \cdot \underbrace{b \cdot b}_3 \cdot \underbrace{b \cdot b}_4 \cdot \underbrace{b \cdot b}_5 \cdot \underbrace{b \cdot b}_6 \cdot b$$

$$b^7 \sqrt{b}$$

$$4 \cdot a^5 \sqrt{a} \cdot b^7 \sqrt{b}$$

$$4a^5 b^7 \sqrt{ab}$$