

Intro to college math: Chapter 2.4
Formulas

- * Formula — is an equation that contains more than one variable.
- * Solving for a variable — we isolate that variable on one side of the equal sign, and everything else will be on the other side.

1. Solve the following for the indicated variable. $4x + y = 2$ for y

$$\begin{array}{r} 4x + y = 2 \\ -4x \qquad -4x \\ \hline y = \boxed{2 - 4x} \end{array}$$

- * Since solving for y , we want y on one side + everything else on the other side of $=$
- * We cannot combine the 2 terms on the left, because 1 has an x and one doesn't.

2. Solve the following for the indicated variable. $y + 4 = -(x - 5)$ for y

$$\begin{array}{r} y + 4 = -(x - 5) \\ y + 4 = -x + 5 \\ -4 \qquad -4 \\ \hline y = \boxed{-x + 1} \end{array}$$

- * First, use distributive property to get rid of $()$.
- * Then move number on left to right by add / subtract. Be sure + combine it with like term.

3. Solve the following for the indicated variable.

$$y - 4 = \frac{1}{3}(x + 6) \text{ for } y$$

$$y - 4 = \frac{1}{3}(x + 6)$$

$$y - 4 = \frac{1}{3}x + 2$$

$$y = \frac{1}{3}x + 6$$

* First use the distributive property to get rid of the ().

* Then move the number on the left to the right so adding or subtracting. (Make sure to combine it with a like term.)

4. Solve the following for the indicated variable.

$$6x + 7y = 42$$

$$6x + 7y = 42$$

$$7y = 42 - 6x$$

$$y = 6 - \frac{6}{7}x$$

* Since we are solving for y, we must move the x's to the other side by adding or subtracting.

* Now, to get rid of the number in front of y, we divide everything by the number in front of y.

* Simplify if able. Use your calculator.

5. Use the formula $3x + 7y = 21$ to find y when:

a) $x = 7$

$$3x + 7y = 21$$

$$3(7) + 7y = 21$$

$$21 + 7y = 21$$

$$7y = 0$$

$$y = 0$$

* Replace x with number given.

* Then solve for y.

b) $x = 1$

$$3x + 7y = 21$$

$$3(1) + 7y = 21$$

$$3 + 7y = 21$$

$$7y = 18$$

$$y = \frac{18}{7}$$

c.) $x = 0$

$$3x + 7y = 21$$

$$3(0) + 7y = 21$$

$$0 + 7y = 21$$

$$\frac{7y}{7} = \frac{21}{7}$$

$$y = 3$$

d.) $x = -7$

$$3x + 7y = 21$$

$$3(-7) + 7y = 21$$

$$-21 + 7y = 21$$

$$+21 \quad +21$$

$$\frac{7y}{7} = \frac{42}{7}$$

$$y = 6$$

6. In the following exercise, use the formula $5x + 4y = 20$ solve for y

a.) when $x = 4$

$$5x + 4y = 20$$

$$5(4) + 4y = 20$$

$$20 + 4y = 20$$

$$-20 \quad -20$$

$$\frac{4y}{4} = \frac{0}{4}$$

$$y = 0$$

b.) In general, $y =$

$$5x + 4y = 20$$

$$-5x \quad -5x$$

$$\frac{4y}{4} = \frac{20 - 5x}{4}$$

$$y = 5 - \frac{5}{4}x$$

7. Solve the formula $3x - y = 2$ for y .

$$\begin{array}{r} 3x - y = 2 \\ \underline{-3x} \qquad \underline{-3x} \\ -y = 2 - 3x \\ \underline{-1} \qquad \underline{-1} \qquad \underline{-1} \\ y = -2 + 3x \end{array}$$

* move x 's to right by adding/subtracting

* Since there is a $(-)$ in front of " y ", we must divide everything by (-1) .

* Remember: $\frac{(-)}{(-)} = (+)$

8. Solve the formula $5x - y = 1$ for y .

$$\begin{array}{r} 5x - y = 1 \\ \underline{-5x} \qquad \underline{-5x} \\ -y = 1 - 5x \\ \underline{-1} \qquad \underline{-1} \qquad \underline{-1} \\ y = -1 + 5x \end{array}$$

* move x 's to right by adding/subtracting

* Since there is a $(-)$ in front of " y ", we must divide everything by (-1) .