

Intro to college math: Chapter 2.4  
Formulas

- \* Formula — is an equation that contains more than one variable.
- \* Solving for a variable — we isolate that variable on one side of the equal sign, and everything else will be on the other side.

1. Solve the following for the indicated variable.  $4x + y = 2$  for  $y$

$$\begin{array}{r} 4x + y = 2 \\ -4x \qquad -4x \\ \hline y = \boxed{2 - 4x} \end{array}$$

\* Since solving for  $y$ , we want  $y$  on one side + everything else on the other side of  $=$

\* We cannot combine the 2 terms on the left, because 1 has an  $x$  and one doesn't.

2. Solve the following for the indicated variable.  $y + 4 = -(x - 5)$  for  $y$

$$\begin{array}{r} y + 4 = -(x - 5) \\ y + 4 = -x + 5 \\ -4 \qquad -4 \\ \hline y = \boxed{-x + 1} \end{array}$$

\* First, use distributive property to get rid of  $( )$ .

\* Then move number on left to right by add / subtract. Be sure + combine it with like term.

3. Solve the following for the indicated variable.

$$y - 4 = \frac{1}{3}(x + 6) \text{ for } y$$

$$y - 4 = \frac{1}{3}(x + 6)$$

$$y - 4 = \frac{1}{3}x + 2$$

$$y = \frac{1}{3}x + 6$$

\* First use the distributive property to get rid of the ().

\* Then move the number on the left to the right so adding or subtracting. (Make sure to combine it with a like term.)

4. Solve the following for the indicated variable.

$$6x + 7y = 42$$

$$6x + 7y = 42$$

$$7y = 42 - 6x$$

$$y = 6 - \frac{6}{7}x$$

\* Since we are solving for y, we must move the x's to the other side by adding or subtracting.

\* Now, to get rid of the number in front of y, we divide everything by the number in front of y.

\* Simplify if able. Use your calculator.

5. Use the formula  $3x + 7y = 21$  to find y when:

a)  $x = 7$

$$3x + 7y = 21$$

$$3(7) + 7y = 21$$

$$21 + 7y = 21$$

$$7y = 0$$

$$y = 0$$

\* Replace x with number given.

\* Then solve for y.

b)  $x = 1$

$$3x + 7y = 21$$

$$3(1) + 7y = 21$$

$$3 + 7y = 21$$

$$7y = 18$$

$$y = \frac{18}{7}$$

c.)  $x = 0$

$$3x + 7y = 21$$

$$3(\underline{0}) + 7y = 21$$

$$0 + 7y = 21$$

$$\begin{array}{r} 7y = 21 \\ \underline{-7} \quad \underline{7} \end{array}$$

$$y = 3$$

d.)  $x = -7$

$$3x + 7y = 21$$

$$3(\underline{-7}) + 7y = 21$$

$$\begin{array}{r} -21 + 7y = 21 \\ \underline{+21} \quad \underline{+21} \end{array}$$

$$\begin{array}{r} 7y = 42 \\ \underline{-7} \quad \underline{7} \end{array}$$

$$y = \boxed{6}$$

6. In the following exercise, use the formula  $5x + 4y = 20$  solve for  $y$

a.) when  $x = 4$

$$5x + 4y = 20$$

$$5(\underline{4}) + 4y = 20$$

$$\begin{array}{r} 20 + 4y = 20 \\ \underline{-20} \quad \underline{-20} \end{array}$$

$$\begin{array}{r} 4y = 0 \\ \underline{-4} \quad \underline{4} \end{array}$$

$$y = \boxed{0}$$

b.) In general,  $y =$

$$5x + 4y = 20$$

$$\begin{array}{r} -5x \quad -5x \\ \hline 4y = 20 - 5x \\ \underline{-4} \quad \underline{-4} \quad \underline{-4} \end{array}$$

$$y = \boxed{5 - \frac{5}{4}x}$$

7. Solve the formula  $3x - y = 2$  for  $y$ .

$$\begin{array}{r} 3x - y = 2 \\ \underline{-3x} \quad \underline{-3x} \\ -y = 2 - 3x \\ \underline{-1} \quad \underline{-1} \quad \underline{-1} \\ y = -2 + 3x \end{array}$$

\* move  $x$ 's to right by adding/subtracting

\* Since there is a  $(-)$  in front of ' $y$ ', we must divide everything by  $(-1)$ .

\* Remember:  $\frac{(-)}{(-)} = (+)$

8. Solve the formula  $5x - y = 1$  for  $y$ .

$$\begin{array}{r} 5x - y = 1 \\ \underline{-5x} \quad \underline{-5x} \\ -y = 1 - 5x \\ \underline{-1} \quad \underline{-1} \quad \underline{-1} \\ y = -1 + 5x \end{array}$$

\* move  $x$ 's to right by adding/subtracting

\* Since there is a  $(-)$  in front of ' $y$ ', we must divide everything by  $(-1)$ .