

Intro to College Math: Chapter 7.2
Multiply/Divide Rational Expressions

1. Multiply or divide as indicated. Be sure to reduce all answers to lowest terms.

$$\frac{2a-8}{a^3} \cdot \frac{a^4}{6a-24}$$

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$$\frac{2(\cancel{a-4})}{a^3} \cdot \frac{a^4}{6(\cancel{a-4})}$$

$$\frac{2a^4}{6a^3} =$$

$$\frac{1}{3} a^{4-3} =$$

$$\boxed{\frac{1}{3} a}$$

← First factor out what each group has in common, if able.
← Then cancel out what is the same on top and bottom

← Write down what's left.
← type numbers (fraction) into calculator to reduce.

← for like variables, subtract exponents (since it is division problem)

2. Multiply or divide as indicated. Be sure to reduce all answers to lowest terms.

$$\frac{a^2-a}{4a} \cdot \frac{5a^2}{a^3-4a}$$

$$\frac{a^2-a}{4a} \cdot \frac{5a^2}{a^3-4a}$$

$$\frac{\cancel{a}(a-1)}{4a} \cdot \frac{5a^2}{\cancel{a}(a-4)}$$

$$a^{2-1} = a \leftarrow \frac{5a^2(a-1)}{4a(a-4)}$$

$$\boxed{\frac{5a(a-1)}{4(a-4)}}$$

← First factor out what each group has in common, if able.
← Then cancel out what is the same on top and bottom

← Write down what's left.
← for like variables, subtract exponents (since it is division problem)

← Rewrite

3. Multiply and simplify. You may leave the denominator in factored form.

$$\frac{x+4}{x^2+12x+32} \cdot \frac{x+8}{2}$$

$$\frac{x+4}{x^2+12x+32} \cdot \frac{x+8}{2}$$

$(x+4)(x+8)$ 32
 1 · 32
 2 · 16
 4 · 8

← first factor the polynomial. Write down the last number to the side, + list the pairs of numbers that multiply together to get that number.
 • Then determine which pair add or subtract to get the middle number.

$$\frac{\cancel{x+4}}{(\cancel{x+4})(\cancel{x+8})} \cdot \frac{\cancel{x+8}}{2} =$$

← Rewrite problem with factored polynomial.
 ← cancel out what top + bottom have in common.

$$\boxed{\frac{1}{2}}$$

← write down what's left over.
 * If there's nothing on top of fraction, put a "1".

4. Simplify.

$$\frac{y^2+7y-18}{y^2+5y+6} \cdot \frac{y+2}{y+9}$$

$$\frac{(y-2)(y+9)}{y^2+5y+6} \cdot \frac{y+2}{y+9}$$

$y^2+7y-18$
 18
 1 · 18
 2 · 9
 3 · 6
 y^2+5y+6
 $(y+2)(y+3)$
 6
 1 · 6
 2 · 3

← first factor the polynomials. Write down the last number to the side, + list the pairs of numbers that multiply together to get that number.
 • Then determine which pair add or subtract to get the middle number.

$$\frac{(y-2)(\cancel{y+9})}{(\cancel{y+2})(y+3)} \cdot \frac{\cancel{y+2}}{\cancel{y+9}}$$

← Rewrite problem with factored polynomial.
 ← cancel out what top + bottom have in common.

$$\boxed{\frac{(y-2)}{(y+3)}}$$

← Write down what's left over.

5. Simplify. $\frac{a^2 + 5a + 4}{a^2 - 3a - 40} \div \frac{a+4}{a+5}$

* We don't divide fractions! Change to multiplication + flip 2nd fraction upside down (reciprocal)

$(a+1)(a+4)$
 $\frac{a^2 + 5a + 4}{a^2 - 3a - 40} \cdot \frac{a+5}{a+4}$
 $(a+5)(a-8)$

Factoring process for $a^2 + 5a + 4$:
 Pairs of numbers that multiply to 4: $1 \cdot 4$ (sum 5), $2 \cdot 2$ (sum 4).
 Pairs of numbers that multiply to -40: $1 \cdot 40$, $2 \cdot 20$, $4 \cdot 10$, $5 \cdot 8$ (sum -3).

← first factor the polynomials. Write down the last number to the side, + list the pairs of numbers that multiply together to get that number.
 * Then determine which pair add or subtract to get the middle number.

$\frac{(a+1)(a+4)}{(a+5)(a-8)} \cdot \frac{a+5}{a+4}$

← Rewrite problem with factored polynomial.
 ← Cancel out what top + bottom have in common.

$\frac{a+1}{a-8}$

← Write down what's left over.

6. Multiply or divide as indicated. Be sure to reduce all answers to lowest terms.

$\frac{y^2 + 6y + 5}{4y + 20} \div \frac{4y + 4}{y + 5}$

* We don't divide fractions! Change to multiplication + flip 2nd fraction upside down (reciprocal)

$(y+1)(y+5)$
 $\frac{y^2 + 6y + 5}{4y + 20} \cdot \frac{y+5}{4y+4}$
 $4(y+5)$ $4(y+1)$

Factoring process for $y^2 + 6y + 5$:
 Pairs of numbers that multiply to 5: $1 \cdot 5$ (sum 6).

← Factor each numerator & denominator if possible.

$\frac{(y+1)(y+5)}{4(y+5)} \cdot \frac{y+5}{4(y+1)}$

← Rewrite problem with factored polynomial.
 ← Cancel out what top + bottom have in common.

$\frac{y+5}{4 \cdot 4} = \frac{y+5}{16}$

← write down what's left over & simplify

7. Simplify. $\frac{a^2 + 17a + 72}{a^2 + 6a + 8} \div \frac{a+8}{a+4}$

* We don't divide fractions! Change to multiplication & flip 2nd fraction upside down (reciprocal)

Factor each numerator & denominator if possible.

$$\frac{(a+8)(a+9)}{(a+2)(a+4)} \cdot \frac{a+4}{a+8}$$

Factoring process for $a^2 + 17a + 72$:
 $\begin{array}{l} 1 \cdot 72 \\ 2 \cdot 36 \\ 3 \cdot 24 \\ 4 \cdot 18 \\ 6 \cdot 12 \\ 8 \cdot 9 \end{array}$
 Factoring process for $a^2 + 6a + 8$:
 $\begin{array}{l} 1 \cdot 8 \\ 2 \cdot 4 \end{array}$

$$\frac{(a+8)(a+9)}{(a+2)(a+4)} \cdot \frac{a+4}{a+8}$$

← Rewrite problem with factored polynomial
 ← Cancel out what top & bottom have in common.

$$\boxed{\frac{a+9}{a+2}}$$

← Write down what's left over

8. Multiply or divide as indicated. Be sure to reduce all answers to lowest terms.

$$\frac{a^2 - 4a + 4}{a-2} \div \frac{a^2 - 4}{a+2}$$

* We don't divide fractions! Change to multiplication & flip 2nd fraction upside down (reciprocal)

Factor each numerator & denominator if possible.

$$\frac{(a-2)(a-2)}{a-2} \cdot \frac{a+2}{(a-2)(a+2)}$$

Factoring process for $a^2 - 4a + 4$:
 $\begin{array}{l} 1 \cdot 4 \\ 2 \cdot 2 \end{array}$
 Factoring process for $a^2 - 4$:
 $\sqrt{a^2} = a$, $\sqrt{4} = 2$
 $(a-2)(a+2)$

← Factor each numerator & denominator if possible.

$$\frac{(a-2)(a-2)}{a-2} \cdot \frac{a+2}{(a-2)(a+2)}$$

← Rewrite problem with factored polynomial
 ← Cancel out what top & bottom have in common.

$$\frac{1}{1} = \boxed{1}$$

← If everything cancels out, then the answer is "1".