

Lecture 9: Policy Gradients and Actor Critics

Hado van Hasselt

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Background reading: Sutton & Barto, 2018, Chapter 13



“Do not solve a more general problem as an intermediate step.”

— Vladimir Vapnik, 1998

If we care about optimal behaviour: why not learn a policy directly?



General overview

► Model-based RL

- + 'Easy' to learn a model (supervised learning)
- + Learns 'all there is to know' from the data
 - Uses compute & capacity on irrelevant details
 - Computing policy (=planning) is non-trivial and expensive (in compute)

► Value-based RL

- + Easy to generate policy (e.g., $\pi(a|s) = \mathcal{I}(a = \underset{a}{\operatorname{argmax}} q(s, a))$)
- + Close to true objective
- + Fairly well-understood, good algorithms exist
 - Still not the true objective:
 - May focus capacity on irrelevant details
 - Small value error can lead to larger policy error

► Policy-based RL

- + Right objective!
- More pros and cons on later slide



General overview

Model-based RL

Value-based RL

Policy-based RL

- ▶ All of these generalise in different ways
- ▶ Sometimes learning a model is easier (e.g., simple dynamics)
- ▶ Sometimes learning a policy is easier (e.g., “always move forward” is optimal)



Policy-Based Reinforcement Learning

- ▶ Previously we approximated parametric value functions

$$\begin{aligned}v_{\mathbf{w}}(s) &\approx v_{\pi}(s) \\ q_{\mathbf{w}}(s, a) &\approx q_{\pi}(s, a)\end{aligned}$$

- ▶ A policy can be generated from these values (e.g., greedy)
- ▶ In this lecture we directly parametrise the **policy** directly

$$\pi_{\theta}(a|s) = p(a|s, \theta)$$

- ▶ This lecture, we focus on **model-free** reinforcement learning



Value-based and policy-based RL: terminology

- ▶ **Value Based**

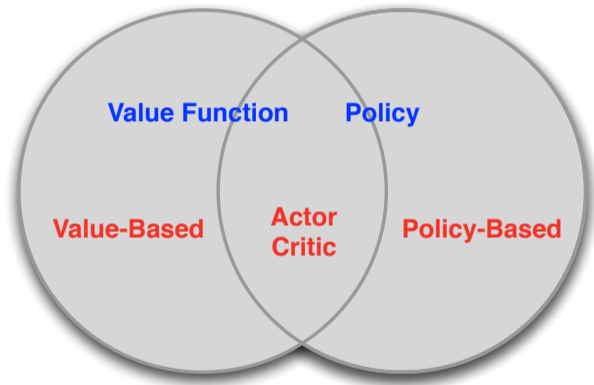
- ▶ Learn values
- ▶ Implicit policy (e.g. ϵ -greedy)

- ▶ **Policy Based**

- ▶ No values
- ▶ Learn policy

- ▶ **Actor-Critic**

- ▶ Learn values
- ▶ Learn policy



Advantages and disadvantages of policy-based RL

Advantages:

- ▶ True objective
- ▶ Easy extended to **high-dimensional** or **continuous** action spaces
- ▶ Can learn **stochastic** policies
- ▶ Sometimes policies are **simple** while values and models are complex
 - ▶ E.g., complicated dynamics, but optimal policy is always “move forward”

Disadvantages:

- ▶ Could get stuck in local optima
- ▶ Obtained knowledge can be **specific**, does not always generalise well
- ▶ Does not necessarily extract all useful information from the data (when used in isolation)



Benefits of stochastic policies



Stochastic policies

Why could we need stochastic policies?

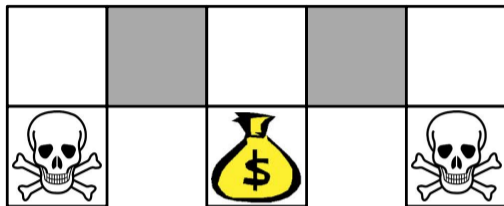
- ▶ In MDPs, there is always an optimal **deterministic** policy
- ▶ But, most problems are **not fully observable**
 - ▶ This is the common case, especially with function approximation
 - ▶ The optimal policy may then be stochastic
- ▶ Search space is smoother for stochastic policies \implies we can use gradients
- ▶ Provides some 'exploration' during learning



Stochastic Policy Example: Aliased Grid World



Example: Aliased Grid World



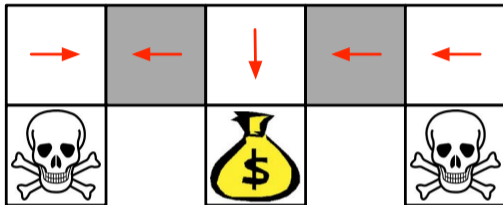
- ▶ The grey states look the same
- ▶ Consider features:

$$\phi(s) = \overbrace{\left(\underbrace{1}_{\text{up}} \quad \underbrace{0}_{\text{right}} \quad \underbrace{1}_{\text{down}} \quad \underbrace{0}_{\text{left}} \right)}^{\text{walls=state}}$$

- ▶ Compare **deterministic** and **stochastic** policies



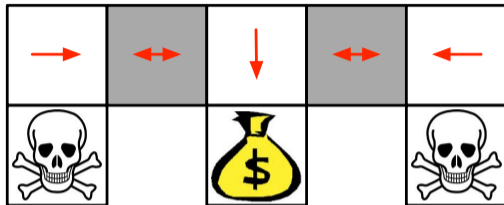
Example: Aliased Gridworld



- ▶ Under aliasing, an optimal **deterministic** policy will either
 - ▶ move left in both grey states (shown by red arrows)
 - ▶ or move right in both grey states
- ▶ Either way, it can get stuck and never reach the money



Example: Aliased Gridworld



- ▶ An optimal **stochastic** policy moves randomly left or right in grey states

$$\pi_{\theta}(\text{right} \mid \text{wall up and down}) = 0.5$$

$$\pi_{\theta}(\text{left} \mid \text{wall up and down}) = 0.5$$

- ▶ Will reach the goal state in a few steps with high probability
- ▶ Directly learning the policy parameters, we can learn an optimal stochastic policy
- ▶ Also when optimal policy does not give equal probability
(So this differs from random tie-breaking with values.)



Policy Learning Objective



Policy Objective Functions

- ▶ Goal: given **policy $\pi_\theta(s, a)$** , find best **parameters θ**
- ▶ How do we measure the quality of a policy π_θ ?
- ▶ In episodic environments we can use the **average total return per episode**
- ▶ In continuing environments we can use the **average reward per step**



Policy Objective Functions: Episodic

- **Episodic-return objective:**

$$\begin{aligned} J_G(\boldsymbol{\theta}) &= \mathbb{E}_{S_0 \sim d_0, \pi_{\boldsymbol{\theta}}} \left[\sum_{t=0}^{\infty} \gamma^t R_{t+1} \right] \\ &= \mathbb{E}_{S_0 \sim d_0, \pi_{\boldsymbol{\theta}}} [G_0] \\ &= \mathbb{E}_{S_0 \sim d_0} [\mathbb{E}_{\pi_{\boldsymbol{\theta}}} [G_t \mid S_t = S_0]] \\ &= \mathbb{E}_{S_0 \sim d_0} [v_{\pi_{\boldsymbol{\theta}}}(S_0)] \end{aligned}$$

where d_0 is the start-state distribution This objective equals the expected value of the start state



Policy Objective Functions: Average Reward

- **Average-reward objective**

$$\begin{aligned} J_R(\theta) &= \mathbb{E}_{\pi_\theta} [R_{t+1}] \\ &= \mathbb{E}_{S_t \sim d_{\pi_\theta}} \left[\mathbb{E}_{A_t \sim \pi_\theta(S_t)} [R_{t+1} \mid S_t] \right] \\ &= \sum_s d_{\pi_\theta}(s) \sum_a \pi_\theta(s, a) \sum_r p(r \mid s, a) r \end{aligned}$$

where $d_\pi(s) = p(S_t = s \mid \pi)$ is the probability of being in state s in the long run
Think of it as the ratio of time spent in s under policy π



Policy Gradients



Policy Optimisation

- ▶ Policy based reinforcement learning is an **optimization** problem
- ▶ Find θ that maximises $J(\theta)$
- ▶ We will focus on **stochastic gradient ascent**, which is often quite efficient (and easy to use with deep nets)
- ▶ Some approaches do not use gradient
 - ▶ Hill climbing / simulated annealing
 - ▶ Genetic algorithms / evolutionary strategies



Policy Gradient

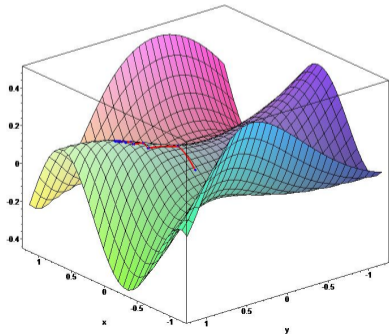
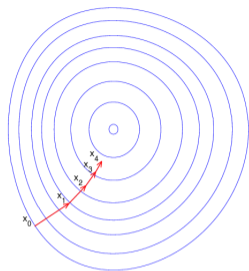
- ▶ Idea: ascent the gradient of the objective $J(\theta)$

$$\Delta\theta = \alpha \nabla_{\theta} J(\theta)$$

- ▶ Where $\nabla_{\theta} J(\theta)$ is the **policy gradient**

$$\nabla_{\theta} J(\theta) = \begin{pmatrix} \frac{\partial J(\theta)}{\partial \theta_1} \\ \vdots \\ \frac{\partial J(\theta)}{\partial \theta_n} \end{pmatrix}$$

- ▶ and α is a step-size parameter
- ▶ Stochastic policies help ensure $J(\theta)$ is smooth (typically/mostly)



Gradients on parameterized policies

- ▶ How to compute this gradient $\nabla_{\theta} J(\theta)$?
- ▶ Assume policy π_{θ} is differentiable almost everywhere (e.g., neural net)
- ▶ For average reward

$$\nabla_{\theta} J(\theta) = \nabla_{\theta} \mathbb{E}_{\pi_{\theta}} [R].$$

- ▶ How does $\mathbb{E}[R]$ depend on θ ?



Contextual Bandits Policy Gradient

- ▶ Consider a one-step case (a contextual bandit) such that $J(\theta) = \mathbb{E}_{\pi_\theta}[R(S, A)]$.
(Expectation is over d (states) and π (actions))
(For now, d does **not** depend on π)
- ▶ We cannot sample R_{t+1} and then take a gradient:
 R_{t+1} is just a number and does not depend on θ !
- ▶ Instead, we use the identity:

$$\nabla_{\theta} \mathbb{E}_{\pi_{\theta}}[R(S, A)] = \mathbb{E}_{\pi_{\theta}}[R(S, A) \nabla_{\theta} \log \pi(A|S)].$$

(Proof on next slide)

- ▶ The right-hand side gives an expected gradient that can be sampled
- ▶ Also known as REINFORCE (Williams, 1992)



The score function trick

Let $r_{sa} = \mathbb{E}[R(S, A) \mid S = s, A = a]$

$$\begin{aligned}\nabla_{\theta} \mathbb{E}_{\pi_{\theta}}[R(S, A)] &= \nabla_{\theta} \sum_s d(s) \sum_a \pi_{\theta}(a|s) r_{sa} \\ &= \sum_s d(s) \sum_a r_{sa} \nabla_{\theta} \pi_{\theta}(a|s) \\ &= \sum_s d(s) \sum_a r_{sa} \pi_{\theta}(a|s) \frac{\nabla_{\theta} \pi_{\theta}(a|s)}{\pi_{\theta}(a|s)} \\ &= \sum_s d(s) \sum_a \pi_{\theta}(a|s) r_{sa} \nabla_{\theta} \log \pi_{\theta}(a|s) \\ &= \mathbb{E}_{d, \pi_{\theta}}[R(S, A) \nabla_{\theta} \log \pi_{\theta}(A|S)]\end{aligned}$$



Contextual Bandit Policy Gradient

$$\nabla_{\theta} \mathbb{E}[R(S, A)] = \mathbb{E}[\nabla_{\theta} \log \pi_{\theta}(A|S) R(S, A)] \quad (\text{see previous slide})$$

- ▶ This is something we **can** sample
- ▶ Our stochastic policy-gradient update is then

$$\theta_{t+1} = \theta_t + \alpha R_{t+1} \nabla_{\theta} \log \pi_{\theta_t}(A_t | S_t).$$

- ▶ In expectation, this is the following the actual gradient
- ▶ So this is a pure (unbiased) stochastic gradient algorithm
- ▶ Intuition: increase probability for actions with high rewards



Policy gradients: reduce variance

- ▶ Note that, in general

$$\begin{aligned}\mathbb{E} [b \nabla_{\theta} \log \pi(A_t | S_t)] &= \mathbb{E} \left[\sum_a \pi(a | S_t) b \nabla_{\theta} \log \pi(a | S_t) \right] \\ &= \mathbb{E} \left[b \nabla_{\theta} \sum_a \pi(a | S_t) \right] \\ &= \mathbb{E} [b \nabla_{\theta} 1] \qquad = 0\end{aligned}$$

- ▶ This is true if b does not depend on the action (but it can depend on the state)
- ▶ Implies we can subtract a **baseline** to reduce variance

$$\theta_{t+1} = \theta_t + \alpha (R_{t+1} - b(S_t)) \nabla_{\theta} \log \pi_{\theta_t}(A_t | S_t).$$

- ▶ We will also use this fact in proofs below



Example: Softmax Policy

- ▶ Consider a softmax policy on action preferences $h(s, a)$ as an example
- ▶ Probability of action is proportional to exponentiated weight

$$\pi_{\theta}(a|s) = \frac{e^{h(s,a)}}{\sum_b e^{h(s,b)}}$$

- ▶ The gradient of the log probability is

$$\nabla_{\theta} \log \pi_{\theta}(A_t|S_t) = \underbrace{\nabla_{\theta} h(S_t, A_t)}_{\text{gradient of preference}} - \underbrace{\sum_a \pi_{\theta}(a|S_t) \nabla_{\theta} h(S_t, a)}_{\text{expected gradient of preference}}$$



Policy Gradient Theorem



Policy Gradient Theorem

- ▶ The policy gradient approach also applies to (multi-step) MDPs
- ▶ Replaces reward R with long-term return G_t or value $q_\pi(s, a)$
- ▶ There are actually two policy gradient theorems (Sutton et al., 2000):
average return per episode & **average reward per step**



Policy gradient theorem (episodic)

Theorem

For any differentiable policy $\pi_{\theta}(s, a)$, let d_0 be the starting distribution over states in which we begin an episode. Then, the policy gradient of $J(\theta) = \mathbb{E}[G_0 \mid S_0 \sim d_0]$ is

$$\nabla_{\theta} J(\theta) = \mathbb{E}_{\pi_{\theta}} \left[\sum_{t=0}^T \gamma^t q_{\pi_{\theta}}(S_t, A_t) \nabla_{\theta} \log \pi_{\theta}(A_t | S_t) \mid S_0 \sim d_0 \right]$$

where

$$\begin{aligned} q_{\pi}(s, a) &= \mathbb{E}_{\pi}[G_t \mid S_t = s, A_t = a] \\ &= \mathbb{E}_{\pi}[R_{t+1} + \gamma q_{\pi}(S_{t+1}, A_{t+1}) \mid S_t = s, A_t = a] \end{aligned}$$



Policy gradients on trajectories

- ▶ Policy gradients do **not** need to know the MDP dynamics
- ▶ Kind of surprising; shouldn't we know how the policy influences the states?



Episodic policy gradients: proof

- ▶ Consider trajectory $\tau = S_0, A_0, R_1, S_1, A_1, R_1, S_2, \dots$ with return $G(\tau)$

$$\nabla_{\theta} J_{\theta}(\pi) = \nabla_{\theta} \mathbb{E}[G(\tau)] = \mathbb{E}[G(\tau) \nabla_{\theta} \log p(\tau)] \quad (\text{score function trick})$$

$$\begin{aligned} \nabla_{\theta} \log p(\tau) &= \nabla_{\theta} \log \left[p(S_0) \pi(A_0|S_0) p(S_1|S_0, A_0) \pi(A_1|S_1) \cdots \right] \\ &= \nabla_{\theta} \left[\log p(S_0) + \log \pi(A_0|S_0) + \log p(S_1|S_0, A_0) + \log \pi(A_1|S_1) + \cdots \right] \\ &= \nabla_{\theta} \left[\log \pi(A_0|S_0) + \log \pi(A_1|S_1) + \cdots \right] \end{aligned}$$

So:

$$\nabla_{\theta} J_{\theta}(\pi) = \mathbb{E}_{\pi} \left[G(\tau) \nabla_{\theta} \sum_{t=0}^T \log \pi(A_t|S_t) \right]$$



Episodic policy gradients: proof (continued)

$$\begin{aligned}\nabla_{\boldsymbol{\theta}} J_{\boldsymbol{\theta}}(\pi) &= \mathbb{E}_{\pi}[G(\tau) \sum_{t=0}^T \nabla_{\boldsymbol{\theta}} \log \pi(A_t | S_t)] \\ &= \mathbb{E}_{\pi}\left[\sum_{t=0}^T G(\tau) \nabla_{\boldsymbol{\theta}} \log \pi(A_t | S_t)\right] \\ &= \mathbb{E}_{\pi}\left[\sum_{t=0}^T \left(\sum_{k=0}^T \gamma^k R_{k+1}\right) \nabla_{\boldsymbol{\theta}} \log \pi(A_t | S_t)\right] \\ &= \mathbb{E}_{\pi}\left[\sum_{t=0}^T \left(\sum_{k=t}^T \gamma^k R_{k+1}\right) \nabla_{\boldsymbol{\theta}} \log \pi(A_t | S_t)\right] \\ &= \mathbb{E}_{\pi}\left[\sum_{t=0}^T \left(\gamma^t \sum_{k=t}^T \gamma^{k-t} R_{k+1}\right) \nabla_{\boldsymbol{\theta}} \log \pi(A_t | S_t)\right] \\ &= \mathbb{E}_{\pi}\left[\sum_{t=0}^T (\gamma^t G_t) \nabla_{\boldsymbol{\theta}} \log \pi(A_t | S_t)\right] &= \mathbb{E}_{\pi}\left[\sum_{t=0}^T \gamma^t q_{\pi}(S_t, A_t) \nabla_{\boldsymbol{\theta}} \log \pi(A_t | S_t)\right]\end{aligned}$$



Episodic policy gradients algorithm

$$\nabla_{\theta} J_{\theta}(\pi) = \mathbb{E}_{\pi} \left[\sum_{t=0}^T \gamma^t q_{\pi}(S_t, A_t) \nabla_{\theta} \log \pi(A_t | S_t) \right]$$

- ▶ We can sample this, given a whole episode
- ▶ Typically, people pull out the sum, and split up this into separate gradients, e.g.,

$$\Delta \theta_t = \gamma^t G_t \nabla_{\theta} \log \pi(A_t | S_t)$$

such that $\mathbb{E}_{\pi} [\sum_t \Delta \theta_t] = \nabla_{\theta} J_{\theta}(\pi)$

- ▶ Typically, people ignore the γ^t term, use $\Delta \theta_t = G_t \nabla_{\theta} \log \pi(A_t | S_t)$
- ▶ This is actually okay-ish — we just partially pretend on each step that we could have started an episode in that state instead (alternatively, view it as a slightly biased gradient)



Policy gradient theorem (average reward)

Theorem

For any differentiable policy $\pi_{\theta}(s, a)$, the policy gradient of $J(\theta) = \mathbb{E}[R | \pi]$ is

$$\nabla_{\theta} J(\theta) = \mathbb{E}_{\pi} [q_{\pi_{\theta}}(S_t, A_t) \nabla_{\theta} \log \pi_{\theta}(A_t | S_t)]$$

where

$$q_{\pi}(s, a) = \mathbb{E}_{\pi} [R_{t+1} - \rho + q_{\pi}(S_{t+1}, A_{t+1}) | S_t = s, A_t = a]$$

$$\rho = \mathbb{E}_{\pi} [R_{t+1}] \quad (\text{Note: global average, not conditioned on state or action})$$

(Expectation is over both states and actions)



Policy gradient theorem (average reward)

Alternatively (but equivalently):

Theorem

For any differentiable policy $\pi_{\theta}(s, a)$, the policy gradient of $J(\theta) = \mathbb{E}[R | \pi]$ is

$$\nabla_{\theta} J(\theta) = \mathbb{E}_{\pi} [R_{t+1} \sum_{n=0}^{\infty} \nabla_{\theta} \log \pi_{\theta}(A_{t-n} | S_{t-n})]$$

(Expectation is over both states and actions)



Actor Critics



Policy gradients: reduce variance

- ▶ Recall $\mathbb{E}_\pi[b(S_t)\nabla \log \pi(A_t|S_t)] = 0$, for any $b(S_t)$ that does not depend on A_t
- ▶ A common baseline is $v_\pi(S_t)$

$$\nabla_{\theta} J_{\theta}(\pi) = \mathbb{E} \left[\sum_{t=0} \gamma^t (q_{\pi}(S_t, A_t) - v_{\pi}(S_t)) \nabla_{\theta} \log \pi(A_t|S_t) \right]$$

- ▶ Typically, we estimate $v_w(s) \approx v_\pi(s)$ explicitly, and sample

$$q_{\pi}(S_t, A_t) \approx G_t$$

- ▶ We can minimise variance further by **bootstrapping**, e.g., $G_t = R_{t+1} + \gamma v_w(S_{t+1})$
- ▶ More on these techniques in the next lecture



Critics

- ▶ A critic is a value function, learnt via **policy evaluation**:
What is the value $v_{\pi_{\theta}}$ of policy π_{θ} for current parameters θ ?
- ▶ This problem was explored in previous lectures, e.g.
 - ▶ Monte-Carlo policy evaluation
 - ▶ Temporal-Difference learning
 - ▶ n -step TD



Actor-Critic

Critic Update parameters \mathbf{w} of $v_{\mathbf{w}}$ by TD (e.g., one-step) or MC

Actor Update θ by policy gradient

function ONE-STEP ACTOR CRITIC

Initialise s, θ

for $t = 0, 1, 2, \dots$ **do**

Sample $A_t \sim \pi_{\theta}(S_t)$

Sample R_{t+1} and S_{t+1}

$\delta_t = R_{t+1} + \gamma v_{\mathbf{w}}(S_{t+1}) - v_{\mathbf{w}}(S_t)$

[one-step TD-error, or **advantage**]

$\mathbf{w} \leftarrow \mathbf{w} + \beta \delta_t \nabla_{\mathbf{w}} v_{\mathbf{w}}(S_t)$

[TD(0)]

$\theta \leftarrow \theta + \alpha \delta_t \nabla_{\theta} \log \pi_{\theta}(A_t | S_t)$

[Policy gradient update (ignoring γ^t term)]



Policy gradient variations

- ▶ Many extensions and variants exist
- ▶ Take care: bad policies lead to bad data
- ▶ This is different from supervised learning
(where learning and data are independent)



Increasing robustness with trust regions

- ▶ One way to increase stability is to **regularise**
- ▶ A popular method is to **limit the difference between subsequent policies**
- ▶ For instance, use the Kullbeck-Leibler divergence:

$$\text{KL}(\pi_{\text{old}} \parallel \pi_{\theta}) = \mathbb{E} \left[\int \pi_{\text{old}}(a \mid S) \log \frac{\pi_{\theta}(a \mid S)}{\pi_{\text{old}}(a \mid S)} da \right].$$

(Expectation is over states)

- ▶ A divergence is like a distance between distributions
- ▶ Then maximise $J(\theta) - \eta \text{KL}(\pi_{\text{old}} \parallel \pi_{\theta})$, for some hyperparameter η
c.f. **TRPO** (Schulman et al. 2015), **PPO** (Abbeel & Schulman 2016), **MPO** (Abdolmaleki et al. 2018)



Continuous action spaces



Continuous actions

- ▶ Pure value-based RL can be non-trivial to extend to **continuous action spaces**
 - ▶ How to approximate $q(s, a)$?
 - ▶ How to compute $\max_a q(s, a)$?
- ▶ When directly updating the policy parameters, continuous actions are easier
- ▶ Most algorithms discussed today can be used for discrete and continuous actions
- ▶ Note: exploration in high-dimensional continuous spaces can be challenging



Example: Gaussian policy

- ▶ As example, consider a **Gaussian policy**
- ▶ E.g., mean is some function of state $\mu_{\theta}(s)$
- ▶ For simplicity, let's consider fixed variance of σ^2 (can be parametrized as well)
- ▶ Policy is Gaussian, $A_t \sim \mathcal{N}(\mu_{\theta}(S_t), \sigma^2)$
(here μ_{θ} is the mean — not to be confused with the behaviour policy!)
- ▶ The gradient of the log of the policy is then

$$\nabla_{\theta} \log \pi_{\theta}(s, a) = \frac{A_t - \mu_{\theta}(S_t)}{\sigma^2} \nabla \mu_{\theta}(s)$$

- ▶ This can be used, for instance, in REINFORCE / actor critic



Example: Policy gradient with Gaussian policy

- ▶ Gaussian policy gradient update:

$$\begin{aligned}\boldsymbol{\theta}_{t+1} &= \boldsymbol{\theta}_t + \beta(G_t - v(S_t))\nabla_{\boldsymbol{\theta}} \log \pi_{\boldsymbol{\theta}}(A_t|S_t) \\ &= \boldsymbol{\theta}_t + \beta(G_t - v(S_t))\frac{A_t - \mu_{\boldsymbol{\theta}}(S_t)}{\sigma^2}\nabla\mu_{\boldsymbol{\theta}}(S_t)\end{aligned}$$

- ▶ Intuition: if return was high, move $\mu_{\boldsymbol{\theta}}(S_t)$ toward A_t



Gradient ascent on value

- ▶ Policy gradients work well, but do not strongly exploit the critic
- ▶ If values generalise well, perhaps we can rely on them more?
 1. Estimate $q_w \approx q_\pi$, e.g., with Sarsa
 2. Define **deterministic actor**: $A_t = \pi_\theta(S_t)$
 3. Improve actor (**policy improvement**) by **gradient ascent on the value**:

$$\Delta\theta \propto \frac{\partial Q_\pi(s, a)}{\partial \theta} = \frac{\partial Q_\pi(s, \pi_\theta(S_t))}{\partial \pi_\theta(S_t)} \frac{\partial \pi_\theta(S_t)}{\partial \theta}$$

- ▶ Known under various names:
 - “Action-dependent heuristic dynamic programming” (ADHDP; Werbos 1990, Prokhorov & Wunsch 1997)
 - “Gradient ascent on the value” (van Hasselt & Wiering 2007)
 - These days, mostly know as: “**Deterministic policy gradient**” (DPG; Silver et al. 2014)
- ▶ It's a form of **policy iteration**



Continuous actor-critic learning automaton (Cacla)

We can also define the error in action space, rather than parameter space

1. $a_t = \text{Actor}_\theta(S_t)$ (get current (continuous) action proposal)
2. $A_t \sim \pi(\cdot | S_t, a_t)$ (e.g., $A_t \sim \mathcal{N}(a_t, \Sigma)$) (explore)
3. $\delta_t = R_{t+1} + \gamma v_w(S_{t+1}) - v_w(S_t)$ (compute TD error)
4. Update $v_w(S_t)$ (e.g., using TD) (policy evaluation)
5. If $\delta_t > 0$, update $\text{Actor}_\theta(S_t)$ towards A_t (policy improvement)

$$\theta_{t+1} \leftarrow \theta_t + \beta(A_t - a_t) \nabla_{\theta_t} \text{Actor}_{\theta_t}(S_t)$$

6. If $\delta_t \leq 0$, do not update Actor_θ

Note: update magnitude does not depend on the value magnitude

Note: don't update 'away' from 'bad' actions



Video

(Peng, Berseth, van de Panne 2016)



End of Lecture

