

Matemática

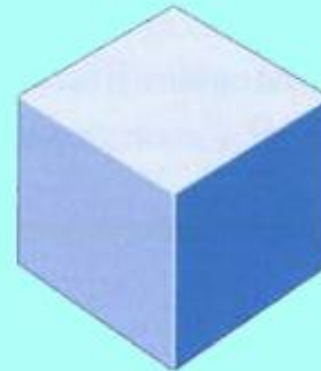


Poliedros

Poliedro Regular

As faces são polígonos regulares,
todos idênticos.

Todos os ângulos poliédricos são
idênticos entre si.



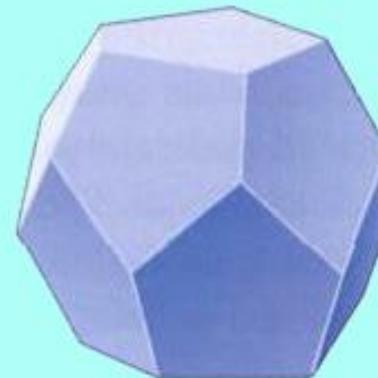
Cubo



Octaedro



Tetraedro



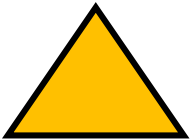
Dodecaedro




Icosaedro

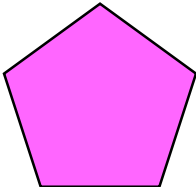
Os cinco sólidos regulares.


Poliedros de Platão

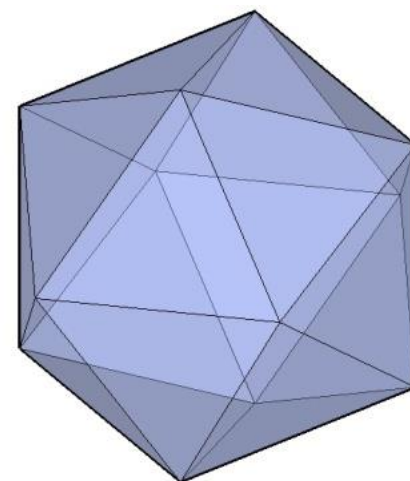
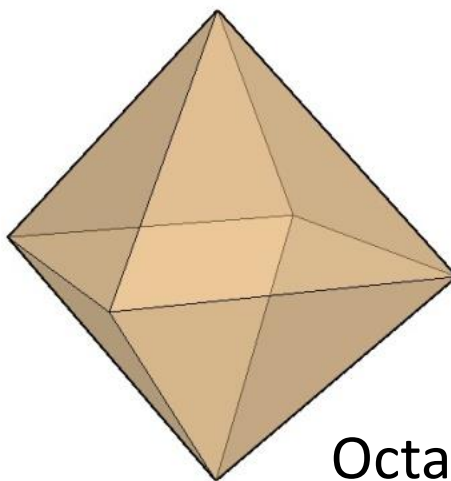
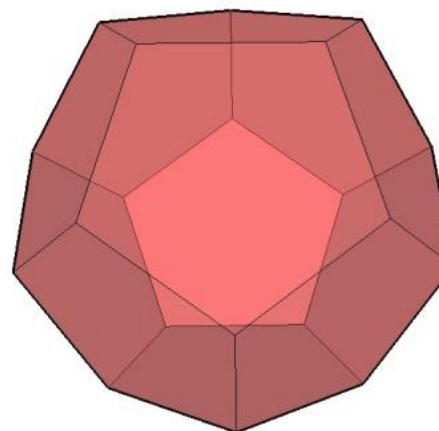
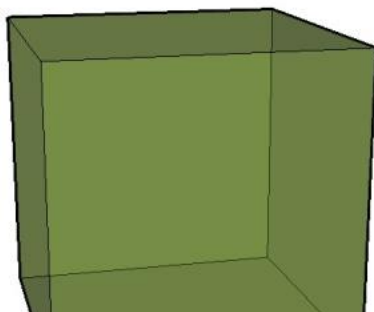
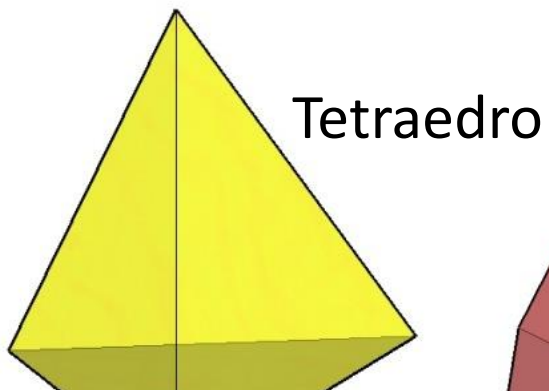
TETRAEDRO → 4 

HEXAEDRO → 6 

OCTAEDRO → 8 

DODECAEDRO → 12 

ICOSAEDRO → 20 



Poliedros

Teorema de Euler

$$V + F = A + 2 \quad \text{Poliedros Fechados}$$

Teorema de Cauchy

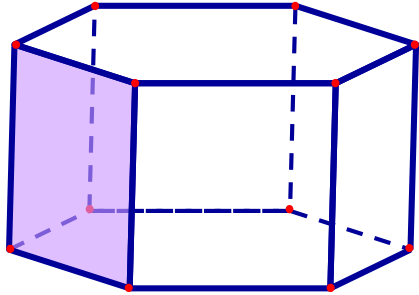
$$V + F = A + 1 \quad \text{Poliedros Abertos}$$

Soma dos Ângulos Internos das Faces

$$S = 360^\circ (V - 2)$$

UFSC - ADAPTADO

Qual a quantidade de vértices, arestas e faces de um poliedro limitado por seis faces quadrangulares e duas faces hexagonais?



$$\begin{array}{r} 6F_4 \\ + \\ 2F_6 \\ \hline F = 8 \end{array}$$

$$A = \frac{6(4) + 2(6)}{2}$$

$$A = \frac{24 + 12}{2} \quad \boxed{A = 18}$$

$$\begin{array}{r} V + 8 = 18 + 2 \\ V = 12 \end{array}$$

Um poliedro possui cinco ângulos triédricos, cinco ângulos tetraédricos e um pentaédrico, determine as arestas, faces e vértices.

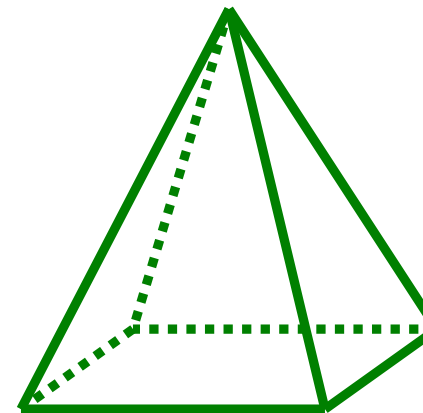
$$\begin{array}{r}
 5V(3) \\
 + 5V(4) \\
 + 1V(5) \\
 \hline
 \boxed{V = 11}
 \end{array}$$

$$A = \frac{5(3) + 5(4) + 1(5)}{2}$$

$$A = \frac{15 + 20 + 5}{2} \quad \boxed{A = 20}$$

$$V + F = A + 2$$

$$11 + F = 20 + 2 \quad \boxed{F = 11}$$



FUVEST

Um poliedro de 16 vértices possui 8 faces triangulares e faces quadrangulares, quantas arestas ele possui

$$\begin{array}{r} 8F(3) \\ + \\ XF(4) \\ \hline F = 8 + X \end{array}$$

$$A = \frac{8(3) + X(4)}{2}$$

$$A = \frac{24 + 4X}{2}$$

$$A = 12 + 2X$$

$$V + F = A + 2$$

$$16 + 8 + X = 12 + 2X + 2$$

$$X = 10$$

$$A = 32$$