

Arco Duplo

Prof. Dé
Matemática

Arco Duplo

Como calcular $\sin(2x)$, $\cos(2x)$ e $\tg(2x)$?

$$\sin(x+x) = \sin x \cos x + \sin x \cos x$$

$$\sin(2x) = 2 \cdot \sin x \cos x$$

$$\cos(x+x) = \cos x \cos x - \sin x \sin x$$

$$\cos(2x) = \cos^2 x - \sin^2 x$$

$$\tg(x+x) = \frac{\tg x + \tg x}{1 - \tg x \tg x}$$

$$\tg(2x) = \frac{2 \cdot \tg x}{1 - \tg^2 x}$$

Arco Duplo

$$\sin(2x) = 2 \cdot \sin x \cdot \cos x$$

$$\cos(2x) = \cos^2 x - \sin^2 x$$

$$\tan(2x) = \frac{2 \cdot \tan x}{1 - \tan^2 x}$$

Arco Duplo

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Considere: $\sin x - \cos x = \sqrt{a}$, com $a > 0$.

Logo, $\sin 2x$ é igual a:

a. $1 - a$

b. $a - 1$

c. a

d. $a + 1$

e. $2a$

$$(\sin x - \cos x)^2 = (\sqrt{a})^2$$

$$\sin^2 x - 2\sin x \cdot \cos x + \cos^2 x = a$$

$$1 - 2\sin x \cdot \cos x = a$$

$$1 - a = 2\sin x \cdot \cos x$$

$$\sin 2x = 1 - a$$

$$\sin^2 x + \cos^2 x = 1$$

$$\sin 2x = 2 \cdot \sin x \cdot \cos x$$

Arco Duplo

$$x = 22^\circ 30'$$

Encontre o valor de $(\sin 22^\circ 30' + \cos 22^\circ 30')^2$

$$(\sin 22^\circ 30' + \cos 22^\circ 30')^2$$

$$(\sin x + \cos x)^2$$

$$\sin^2 x - 2\sin x \cdot \cos x + \cos^2 x$$

$$1 - 2\sin x \cdot \cos x$$

$$1 - \sin 2x$$

$$1 - \sin 2(22^\circ 30')$$

$$\sin^2 x + \cos^2 x = 1$$

$$1 - \sin 45^\circ = 1 - \frac{\sqrt{2}}{2}$$

$$(\sin 22^\circ 30' + \cos 22^\circ 30')^2 = \frac{2 - \sqrt{2}}{2}$$

Arco Duplo

(UFSC) Na figura a seguir determine a medida do segmento AB, em cm, sabendo que $\sin a = 0,6$.

