

PREDICATE CALCULUS: RULES

GENERAL AND PARTICULAR

General:

Universal quantifier $\forall x$

Variables designated by "y", that refer to things in general

Particular:

Existential quantifier $\exists x$

Constants designated by "a" that refer to a particular thing

QUANTIFICATION RULES

$\forall E$ (UI): Universal Elimination/Instantiation. Two forms (variables and constants).

Variable: $\forall x(Fx) / \vdash Fy$

Constant: $\forall x(Fx) / \vdash Fa$

$\forall I$ (UG): Universal Introduction/Generalization.

One form (only variables, not constants):

Variable: $Fy / \vdash \forall x(Fx)$

Constant: impermissible (e.g., $Fa / \vdash \forall x(Fx)$)

$\exists I$ (EG): Existential Introduction/Generalization.

Two forms (variables and constants).

Variable: $Fa / \vdash \exists x(Fx)$

Constant: $Fy / \vdash \exists x(Fx)$

$\exists E$ (EI): Existential Elimination/Instantiation. One form (only constants, not variables). Also, existential name "a" must be a new name that has not occurred in any previous line.

Variable: impermissible (e.g., $\exists x(Fx) / \vdash Fy$)

Constant: $\exists x(Fx) / \vdash Fa$

OTHER RULES

Quantifier Equivalence Rules (Quantifier Exchange QE)

$\forall x(Fx) :: \sim \exists x \sim (Fx)$

$\sim \forall x(Fx) :: \exists x \sim (Fx)$

$\forall x \sim (Fx) :: \sim \exists x(Fx)$

$\sim \forall x \sim (Fx) :: \exists x(Fx)$

Identity (ID)

$Fx, x=y / \vdash Fy$