Vijay Nicole

Essentials of
Business Mathematics & Statistics

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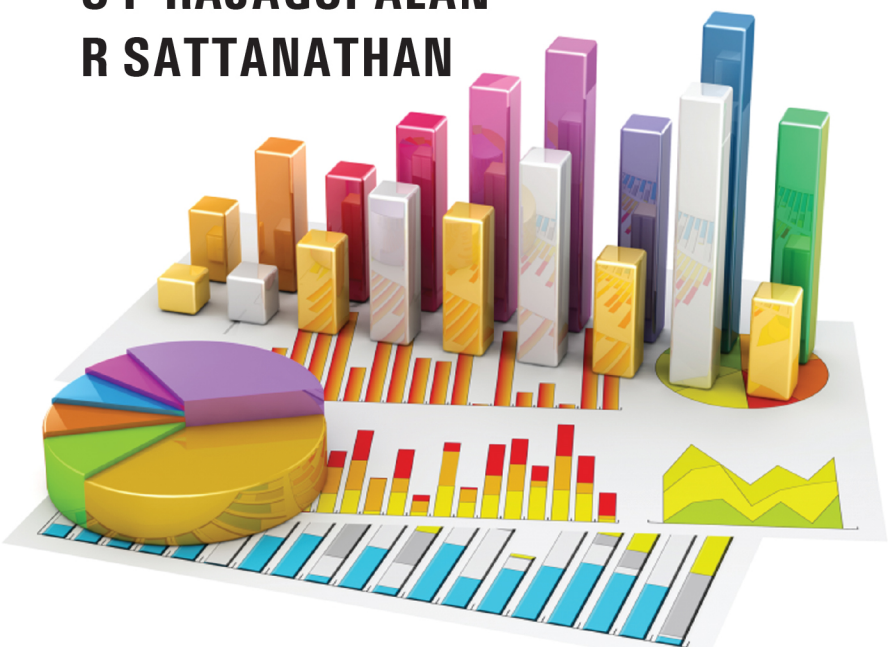

Essentials of Business Mathematics and Statistics

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