

# Modeling Plant Life in Computer Graphics

## Environmental Response

Siggraph 2016 Course

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# Overview

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## Environmental response [20 minutes]

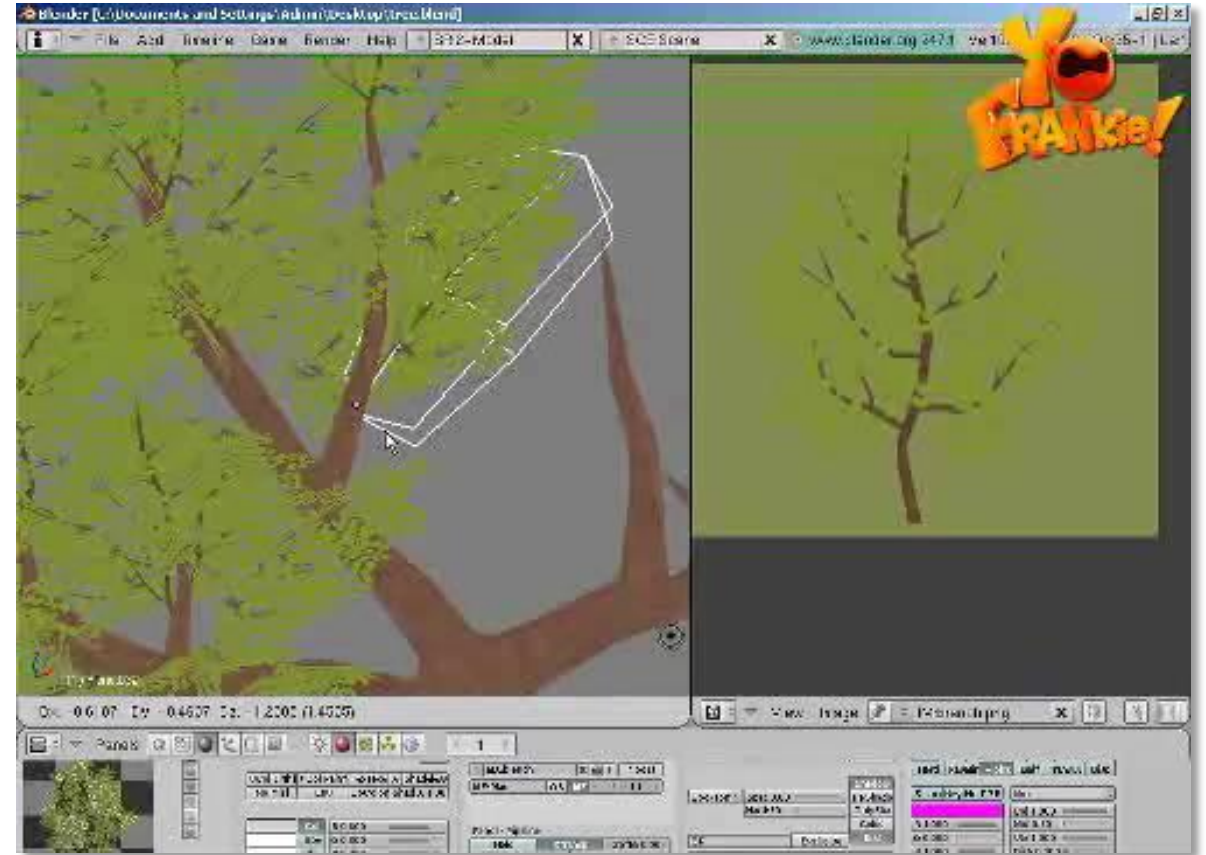
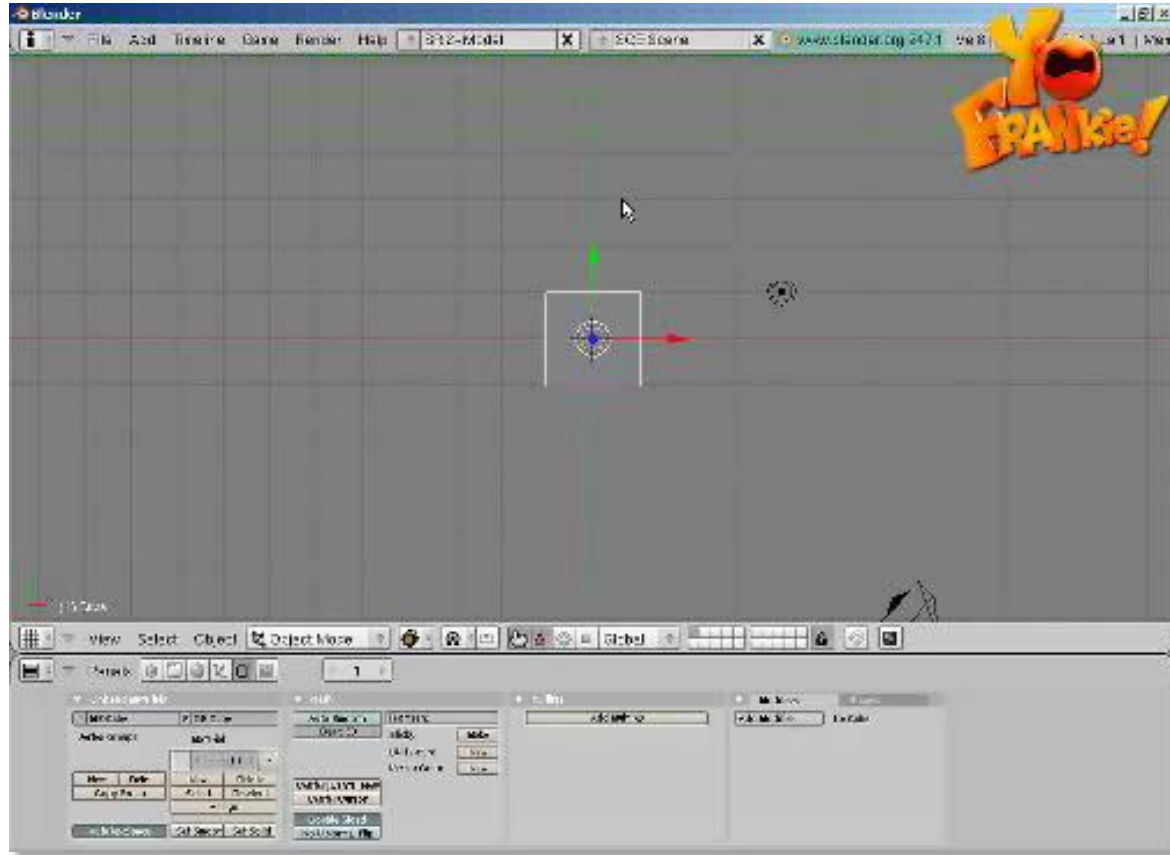
- Real-time sensitivity of tree models **(Pirk)**
- Capturing growth response **(Pirk)**
- Physics response to wind **(Pirk)**

# Tree models are static

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# 3D Tree Modeling



Pablo Vazquez - <http://vimeo.com/2956756>

# Plastic Trees: Interactive Self-Adapting Botanical Tree Models

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Pirk, S., Stava, O., Kratt, J., Said, M. A. M., Neubert, B., Mech, R., Benes, B., Deussen, O.  
**Plastic trees: interactive self-adapting botanical tree models.**  
ACM Trans. on Graph. 31, 4, 50:1–50:10, 2012.

# Environment Aware Trees



Automatic modification of 3D tree models





# Skeletal Graph

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## Skeletal Graph

- Branch Age
- Growth Rate

# Tree Analysis - Tropisms

Phototropism

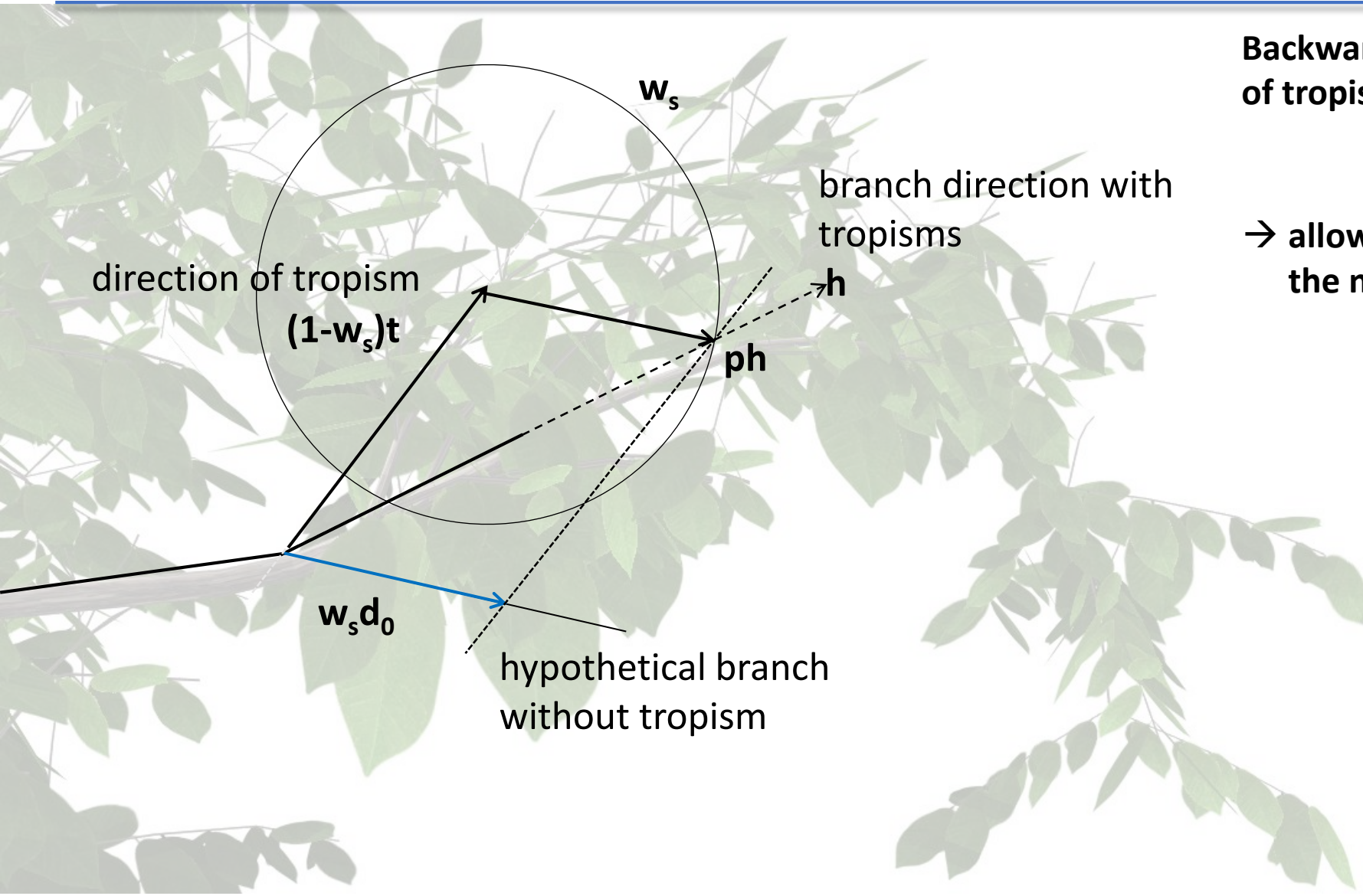


Gravitropism





# Inverse Tropism



Backward modeling to estimate influence of tropisms to the original model

→ allows to apply tropisms triggered by the new environment

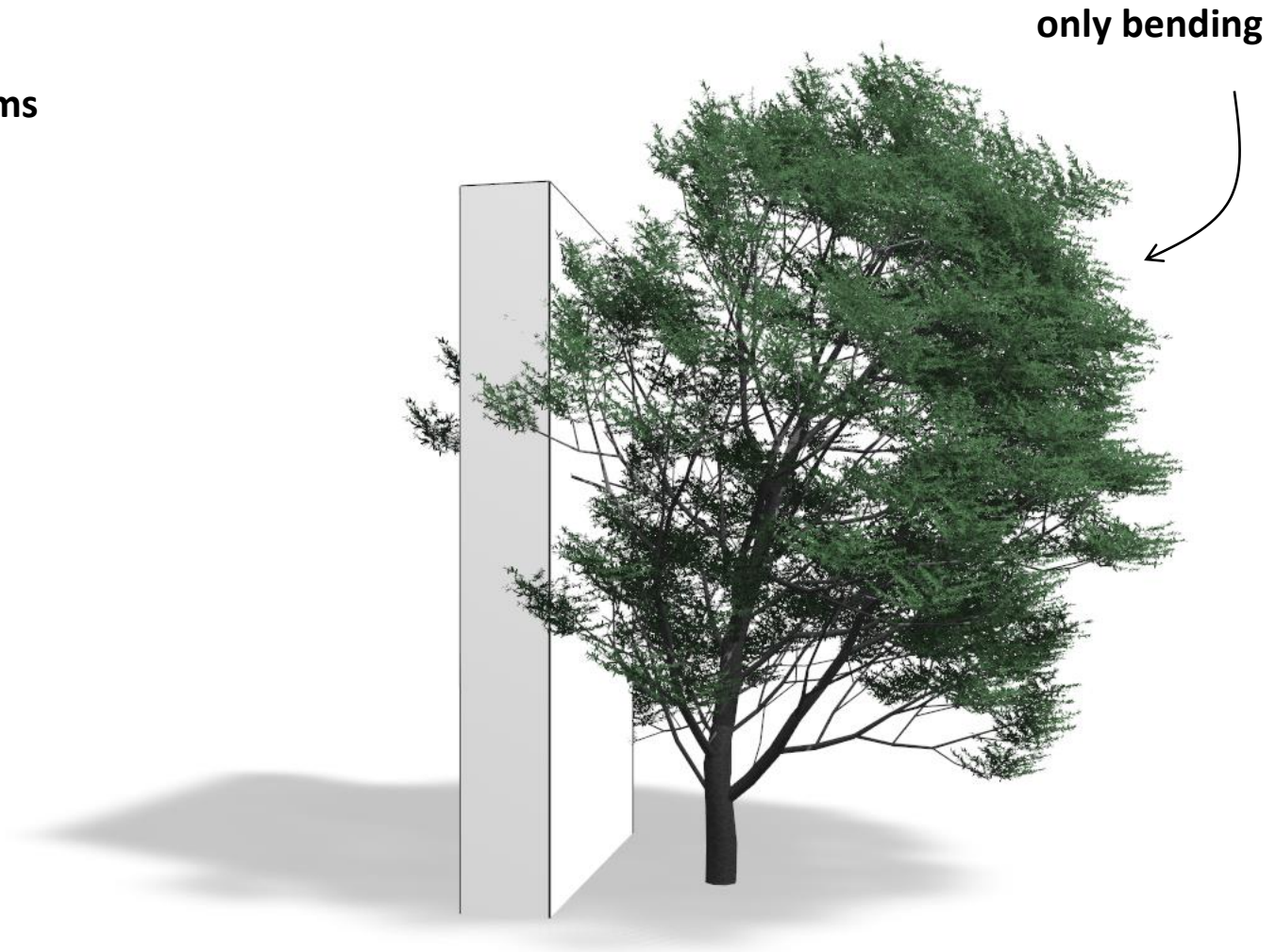
# Dynamic Interaction - Bending

**New Direction**

$$\vec{h} = w_s \vec{d}_0 + (1 - w_s) \frac{\sum w_\tau \vec{t}_\tau}{\sum w_\tau}$$

new direction  
start weight  
normalized direction  
weights of tropisms  
combination of tropisms

Transformations represent changes in the tree growth.



# Dynamic Interaction - Pruning

Approach similar to [Palubicki et al. 2009]

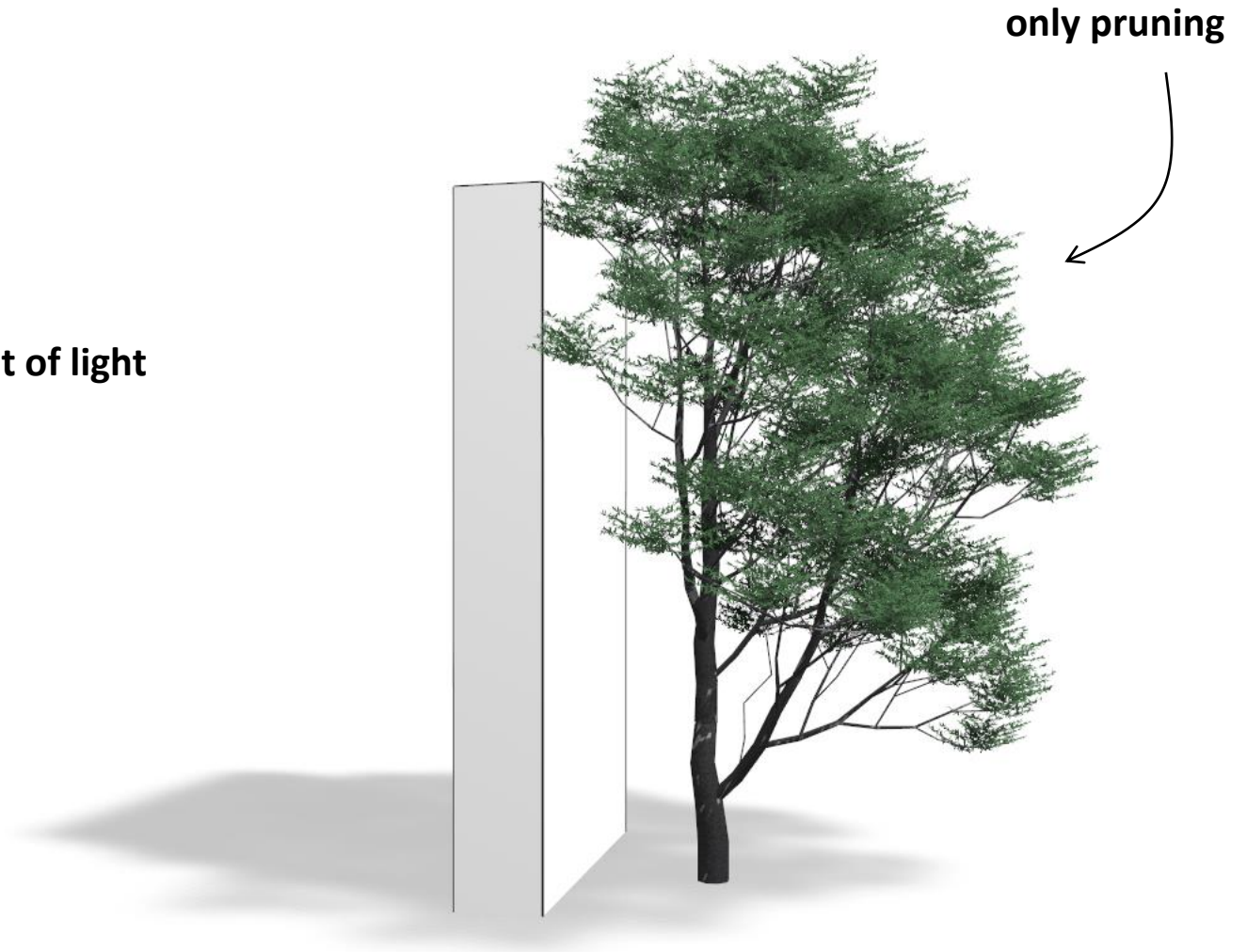
Amount of Light received by the leaf-cluster.

$$\varphi_{t_s} = \sum_{c \in C_s} 2\pi r_c^2 i_c$$

amount of resources (light)  $\nearrow$   
 $\nwarrow$  radius of a given cluster  
 $\longleftarrow$  normalized amount of light

$l_t$ : sum of distances

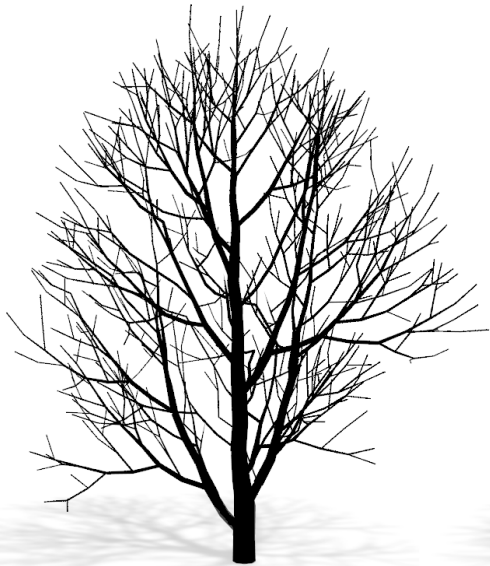
Branch is pruned when ratio  $\varphi_{t_s}/l_t < thres$



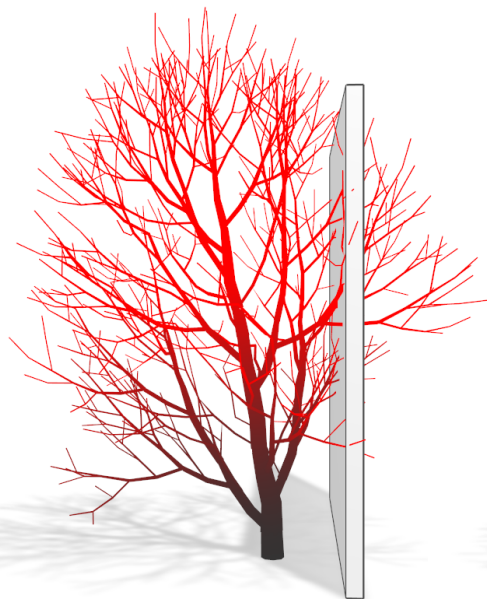


# Tree/Obstacle Interaction

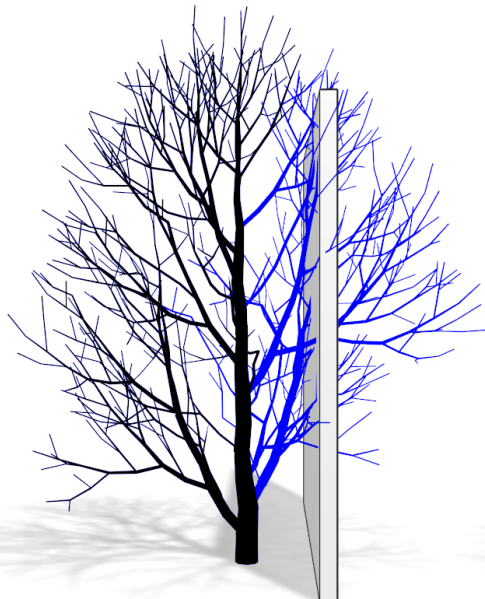
Original Model



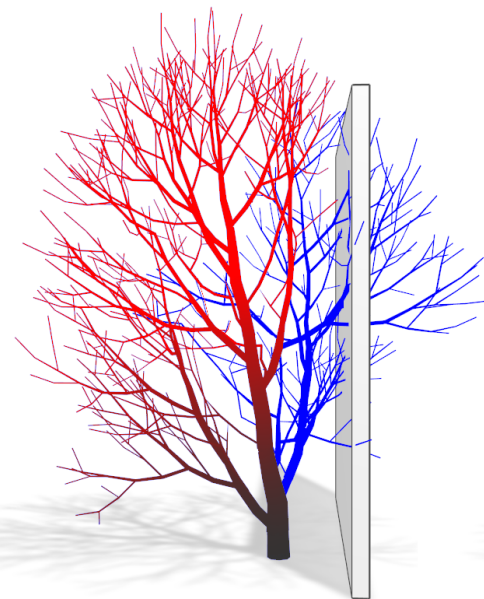
Bending



Pruning



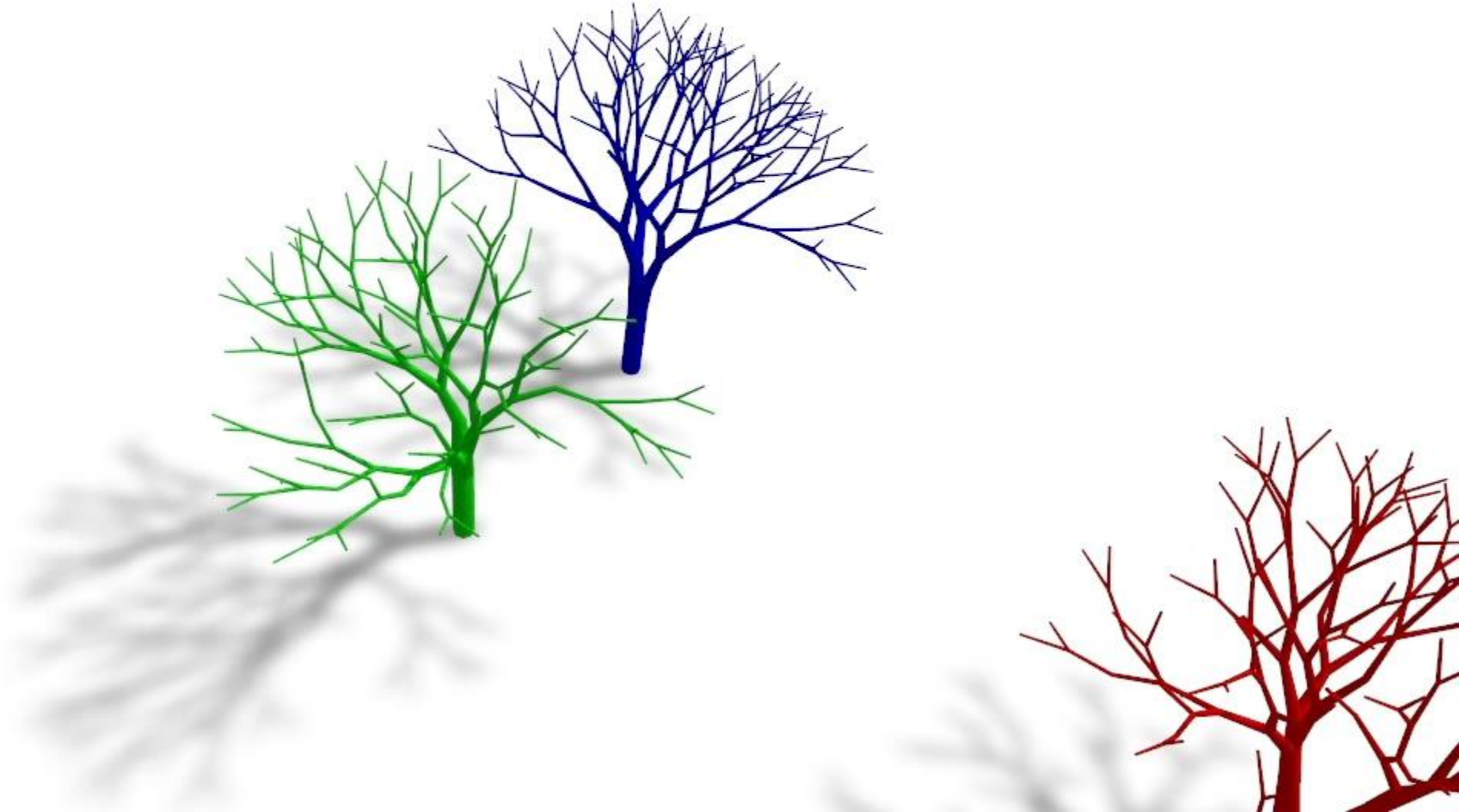
Bending + Pruning



Result



# Tree/Tree-Interaction





# Bending/Pruning Result

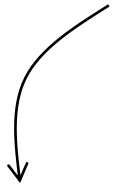
<http://www.flickr.com/photos/harveydogson/4095300141/>





# Tree/Tree-Interaction

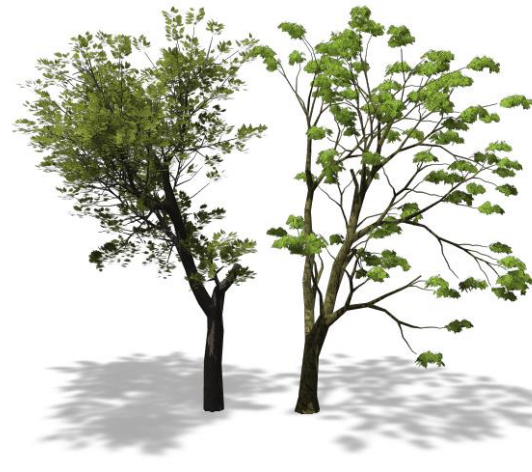
Static Models



Bending and Pruning



Strong Pruning

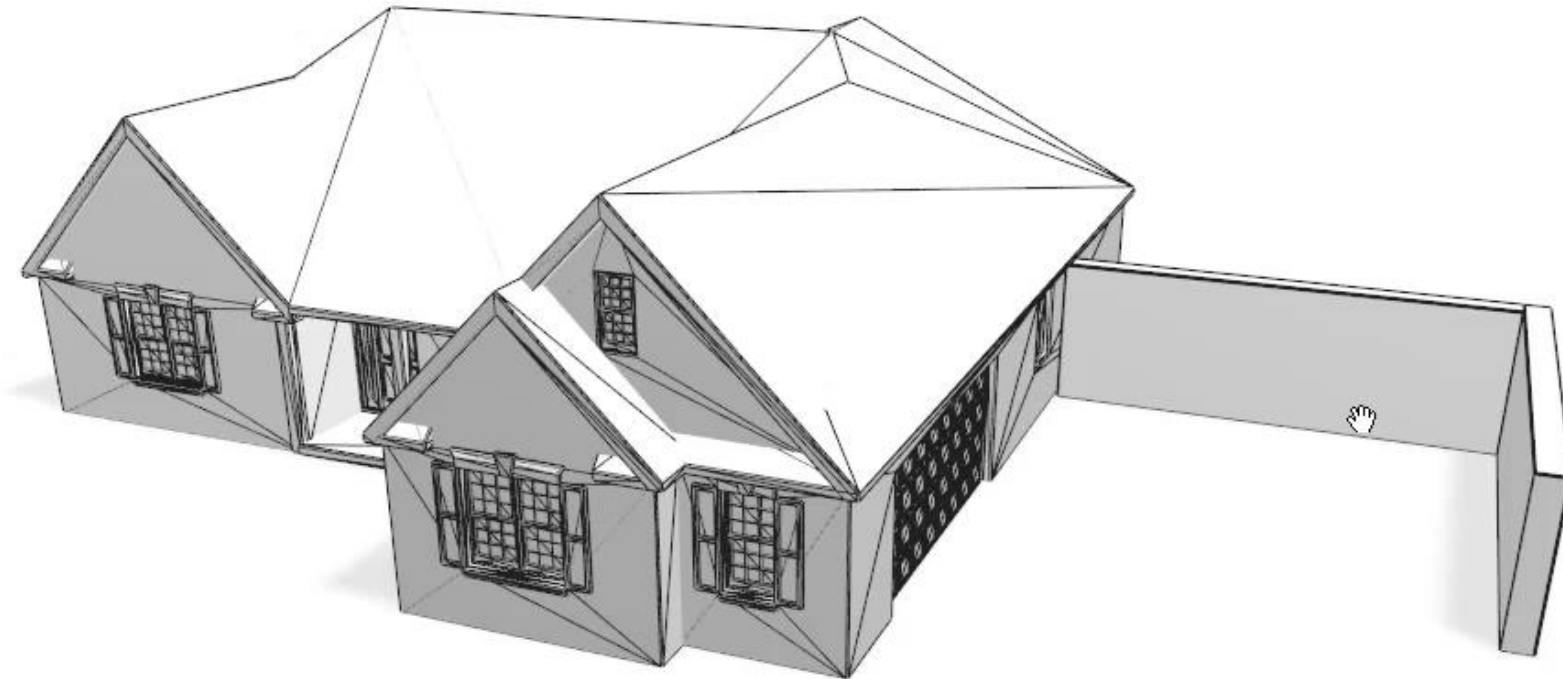


Exaggerated Bending



# Editing

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# Capturing and Animating the Morphogenesis of Polygonal Tree Models

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Pirk, S., Niese, T., Deussen, O., Neubert, B.

**Capturing and animating the morphogenesis of polygonal tree models.**

ACM Trans. on Graph. 31, 6, 169:1–169:10, 2012.

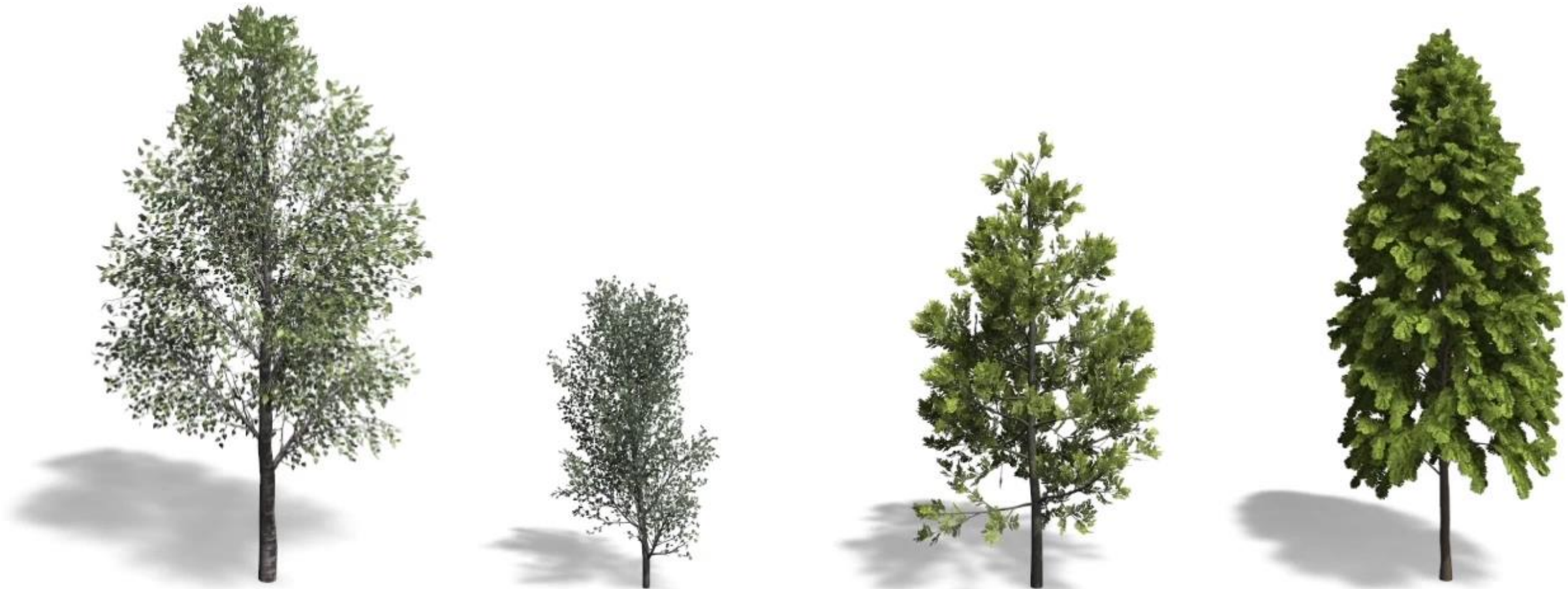






# Continuous Animations of Growth

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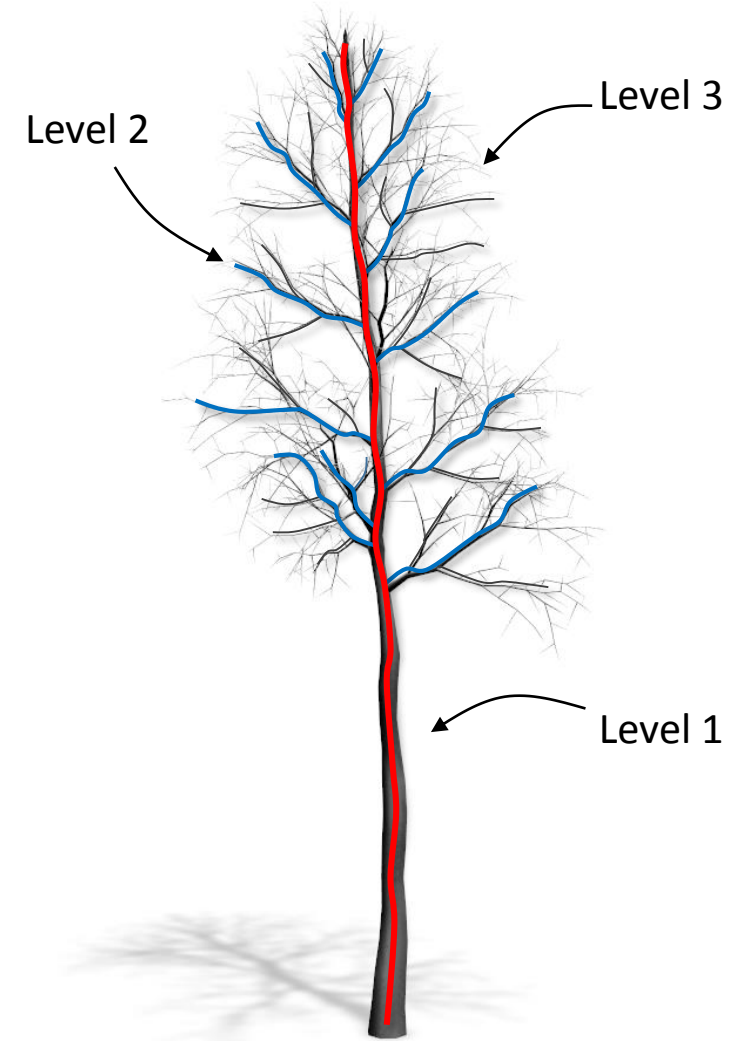
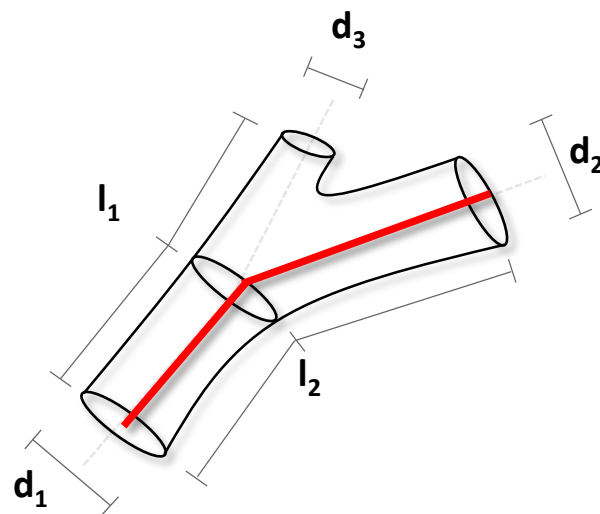


# Gravelius Order

Ordering method for identifying hierarchies.

Determine main trunk based on angle between branches.

Also considering length and thickness of a branch.



# Pipe Model Theory

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[Shinozaki et al. 1964]

Plant forms emerge from vascular systems.

Assembly of leaf units connecting the leaves to the root.

Provides us with branch radii.

# Angle/Radii Interpolation



## Angle Interpolation

Current Angle

Initial Angle

$$\vartheta_{\alpha} = \frac{\alpha_i - \alpha_{init}}{\Delta t}$$

Angular Velocity

Duration

## Radii Interpolation

Child Radii

Power Law of Branching

$$r_p = \left( \frac{\sum r_i^u}{b^p} \right)^{\frac{1}{u}}$$

Current Radius

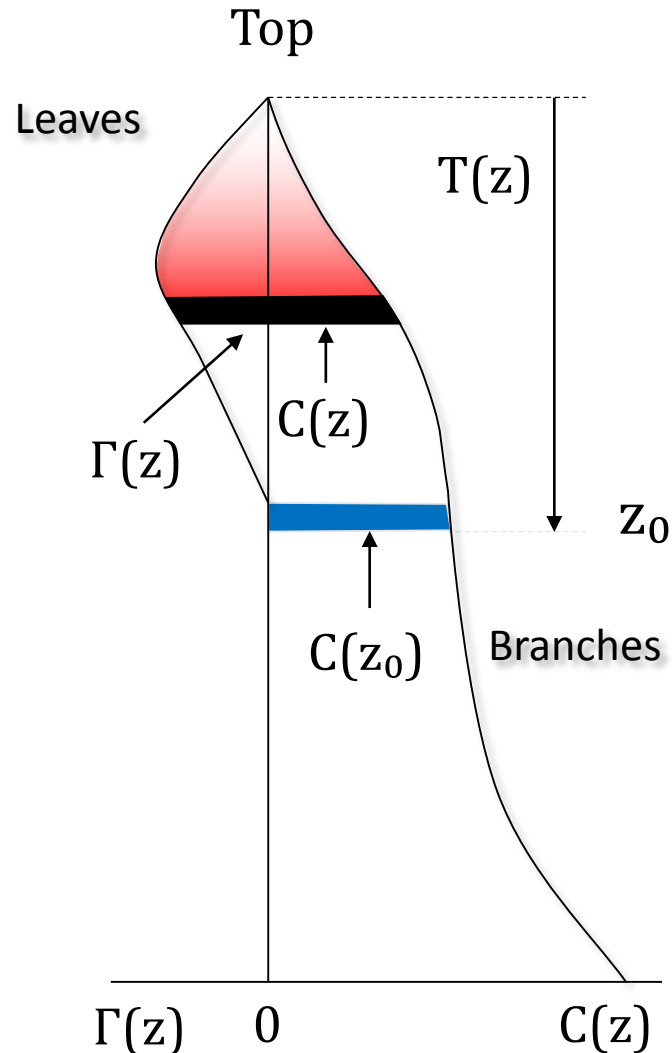
Original Model Coefficient

# Angle/Radii Interpolation





# Profile Diagram



Similar Among Plant Communities.

Represents vertical distribution of leaves.

Distribution of leaves needs to be consistent.

→ Tells us where geometry is missing.

→ How to measure densities?

[Chiba 1990, Chiba 1991]

# Measuring Densities

## Stratified Clipping (STC)

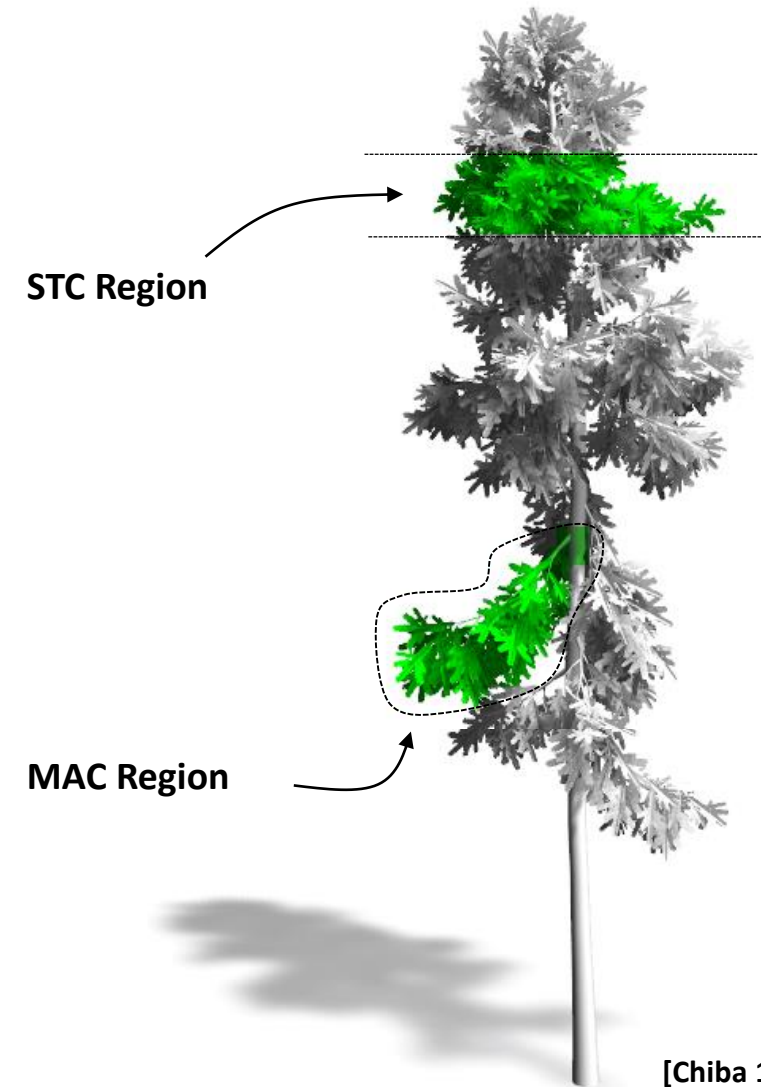
Vertical range of the tree is selected.

All branches and leaves in this region are used for measuring biomass.

## Main Axis Cutting (MAC)

Part of the main axis is selected.

All branches and leaves attached to this part are used for measuring biomass.



# Crown Ratio

Add geometry where no information was available in the original model.

Remove geometry during animation to maintain plausibility and to eventually reach the input.

**Crown Ratio**

**Overlap Region**



# Growth-based Editing

Individual Growth  
of Branches







## Windy Trees: Modeling Stress Response for Developmental Tree Models

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Pirk, S., Niese, T., Hädrich, T., Benes, B., and Deussen. O.

**Windy trees: computing stress response for developmental tree models.**

ACM Trans. Graph. 33, 6, Article 204 ,11 pages, 2014.

# Tree/Wind Interaction

Render the Possibilities  
SIGGRAPH 2016



# Wind as Developmental Factor

Alex Bamford



Rich Price



Walberth Mascarenha



Fedderica Gentile



# Windy Trees



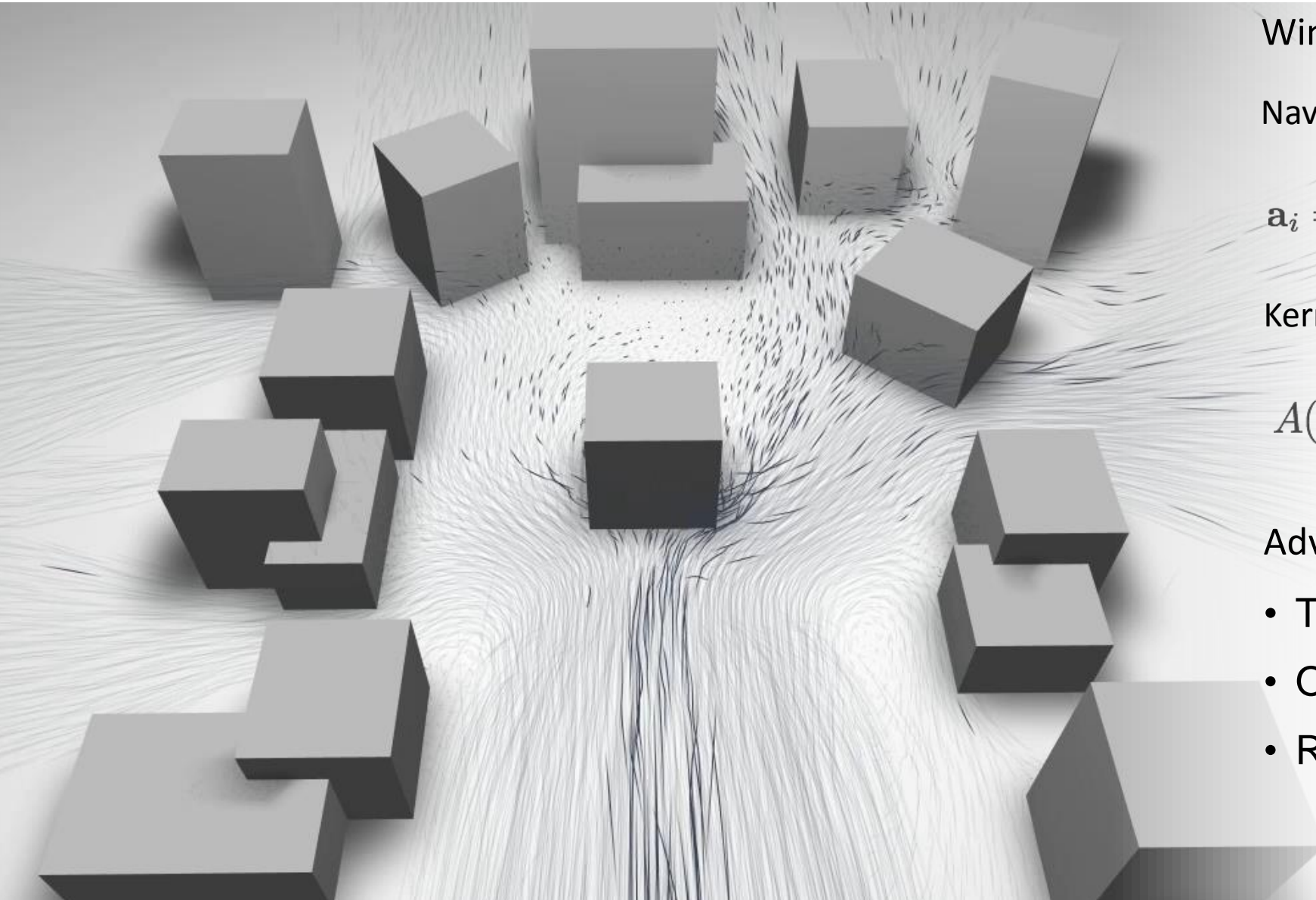


# Growth Model

- Pipe Model Theory
- Gravelius Order
- Branching Angles
- Branch Radii
- Growth Rate



# Smoothed Particle Hydrodynamics (SPH)



Wind Simulation

Navier Stokes - Acceleration

$$\mathbf{a}_i = \frac{d\mathbf{v}_i}{dt} = \frac{-\nabla p + \mu \nabla^2 \mathbf{v} + \rho \mathbf{g}}{\rho_i}$$

Kernel Smoothing Function

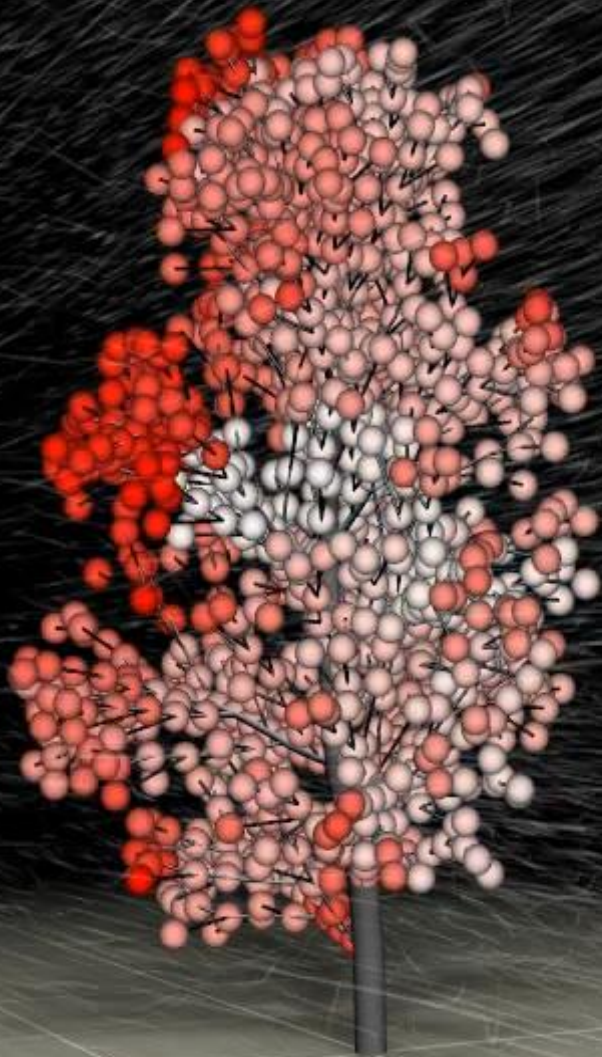
$$A(\mathbf{x}) = \sum_{j=1}^N \frac{m_j}{\rho_j} A_j W(\mathbf{x} - \mathbf{x}_j, h)$$

Advantages

- Tracking of individual collisions
- Occlusion handling (wind shadow)
- Real-time simulation



# Sensor Particles





# Two-Way Coupling





# Force Model for Branches

Torque

$$N = I \frac{d\omega}{dt}$$

Moment of Inertia (rod)

$$I = \frac{mr^2}{3}$$

$$F_W = S_b \sigma v$$

Wind Force

$$D = -(\hat{\omega} \times \hat{e}) \mu \omega |\omega|$$

Damping Force

$$\mathbf{F} = \mathbf{F}_W + \mathbf{R} + \mathbf{D} + \mathbf{P} + \mathbf{L}$$

Restoration Force

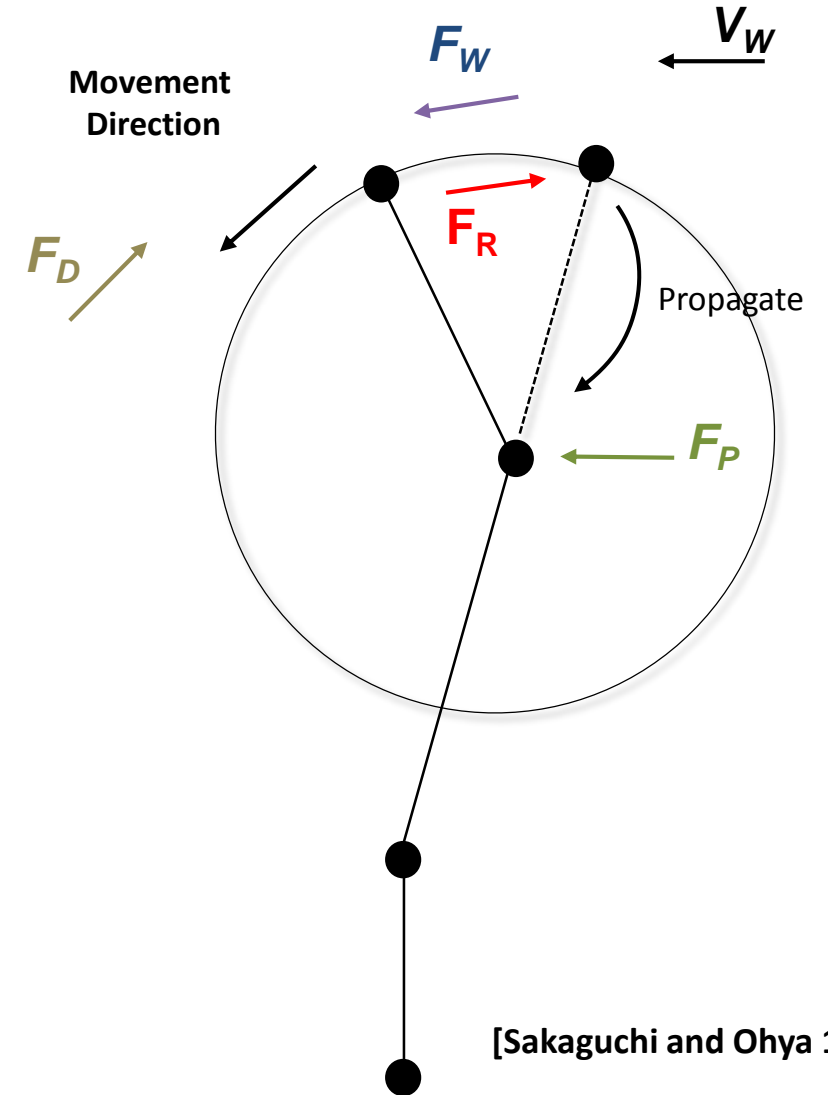
$$R = d_r k \alpha$$

Propagation Force

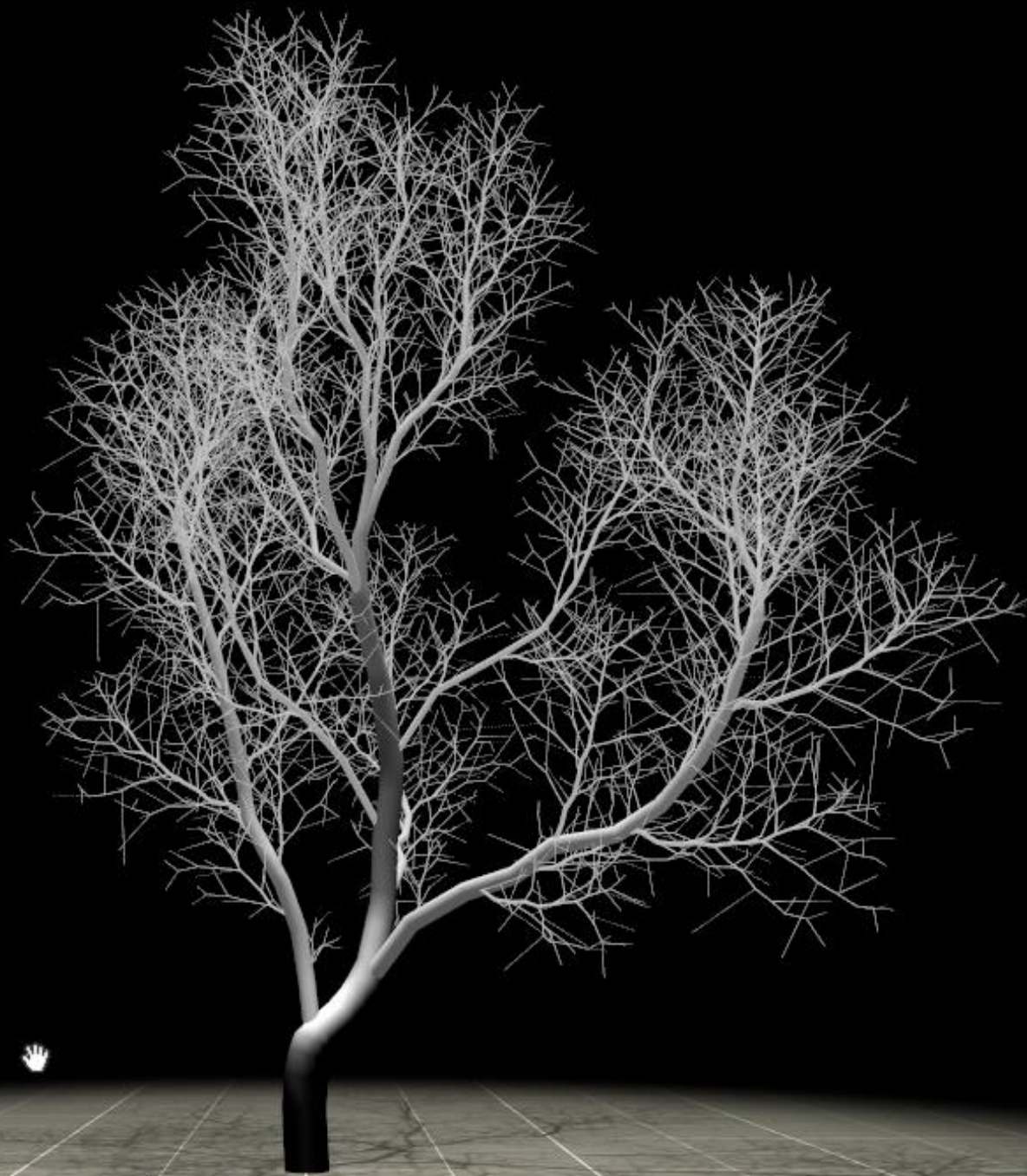
$$P_{i-1} = - \sum k_i F_{Ri}$$

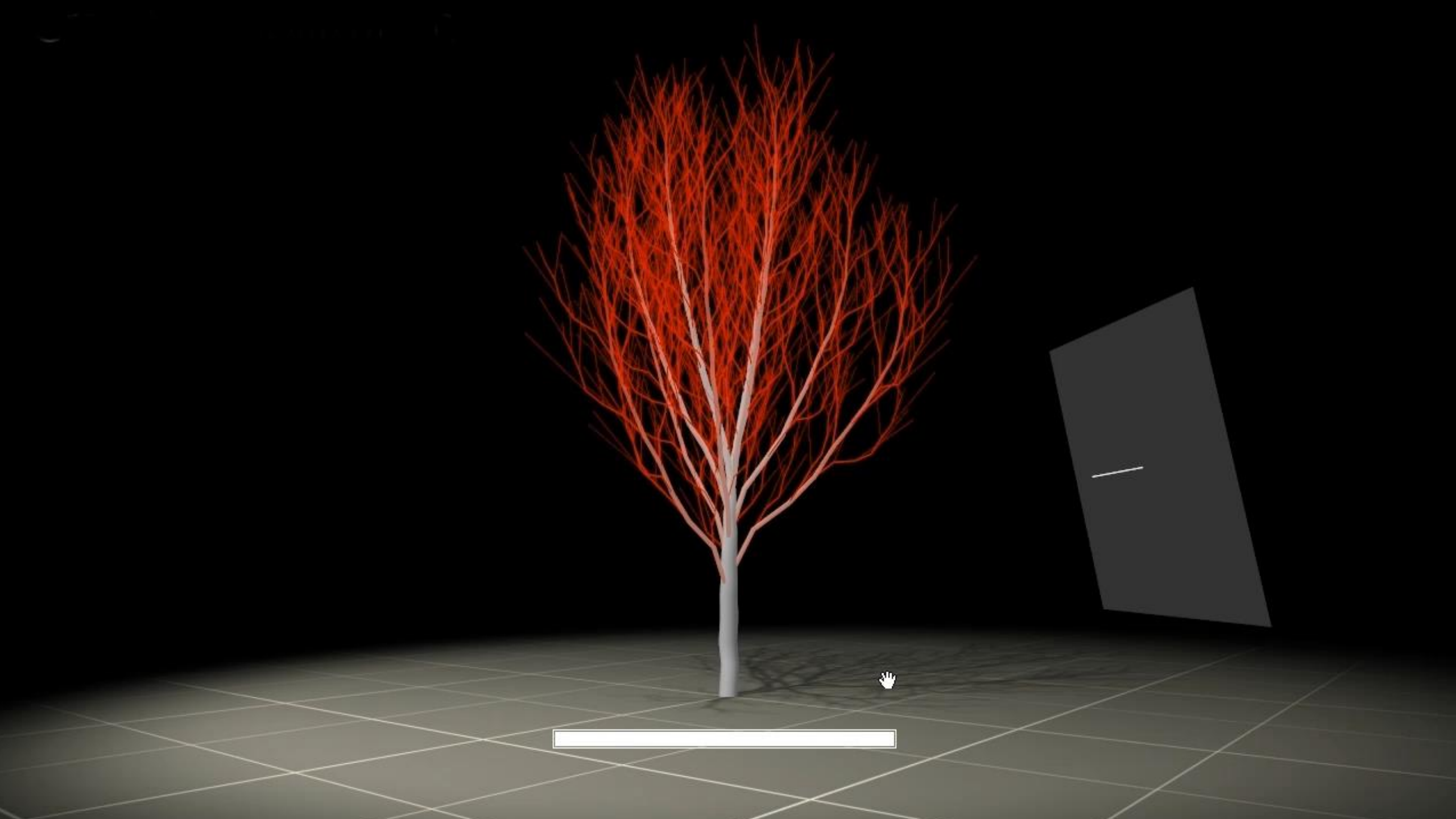
Leaf Force

$$L = S_l \sigma v c$$



[Sakaguchi and Ohya 1999]





# Breaking of Branches

- Branch breaks when the acting forces exceed a certain level of stress
- Wood is a highly inhomogeneous material
- Approximating Young's Modulus and Hook's law

Young's Modulus Coefficient

Bending Moment

Stress

$$\sigma = \frac{4cM}{3\pi r^2}$$

Stress (Young's Modulus)

$$\sigma_{max} = d^3 p$$

Material Property

Branch Thickness

Branch Radius

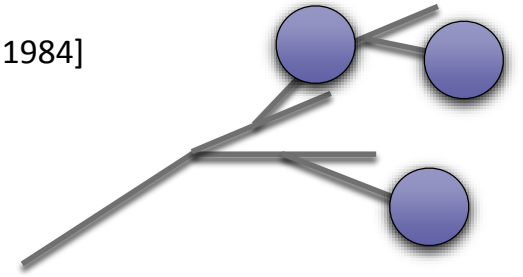




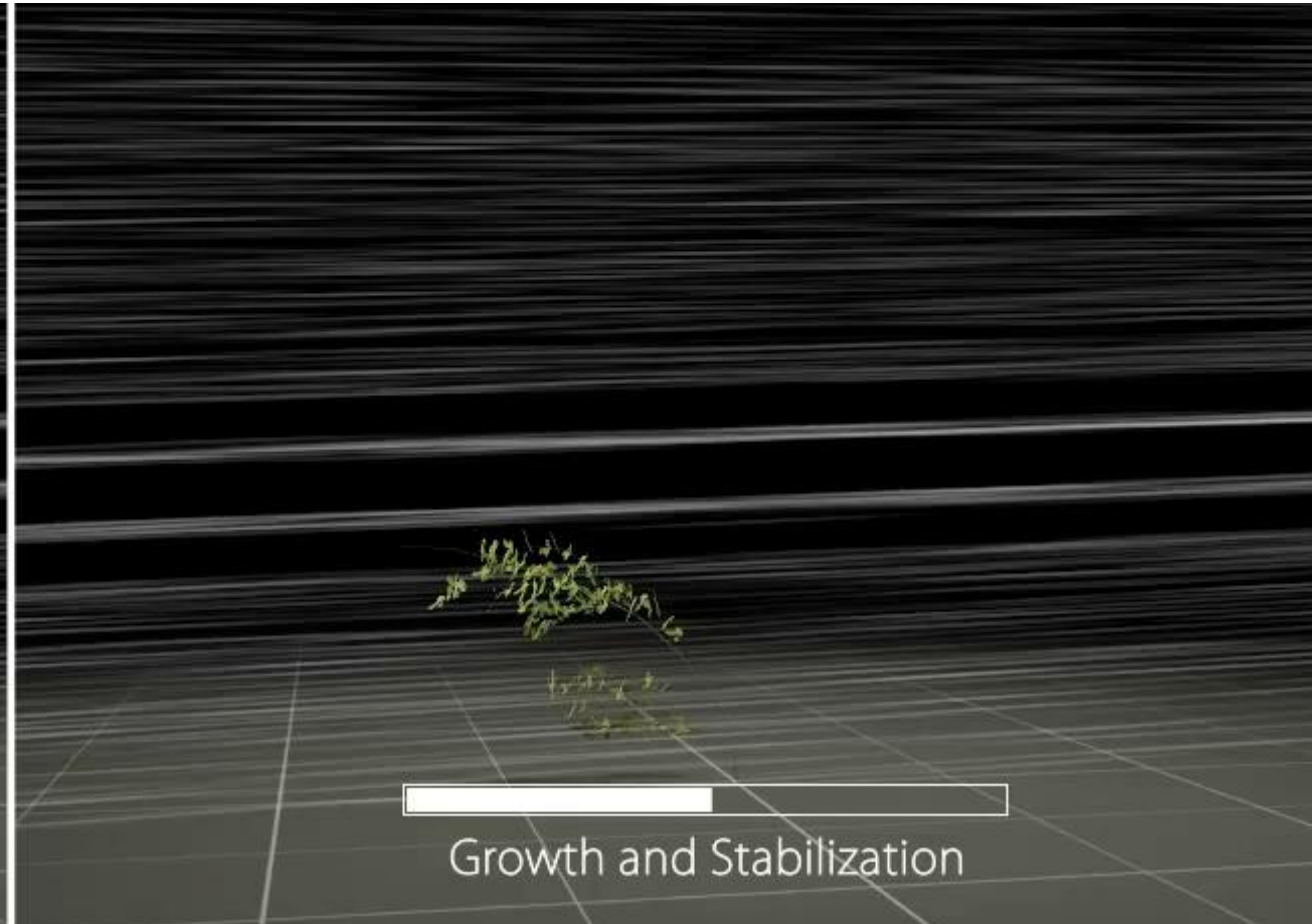
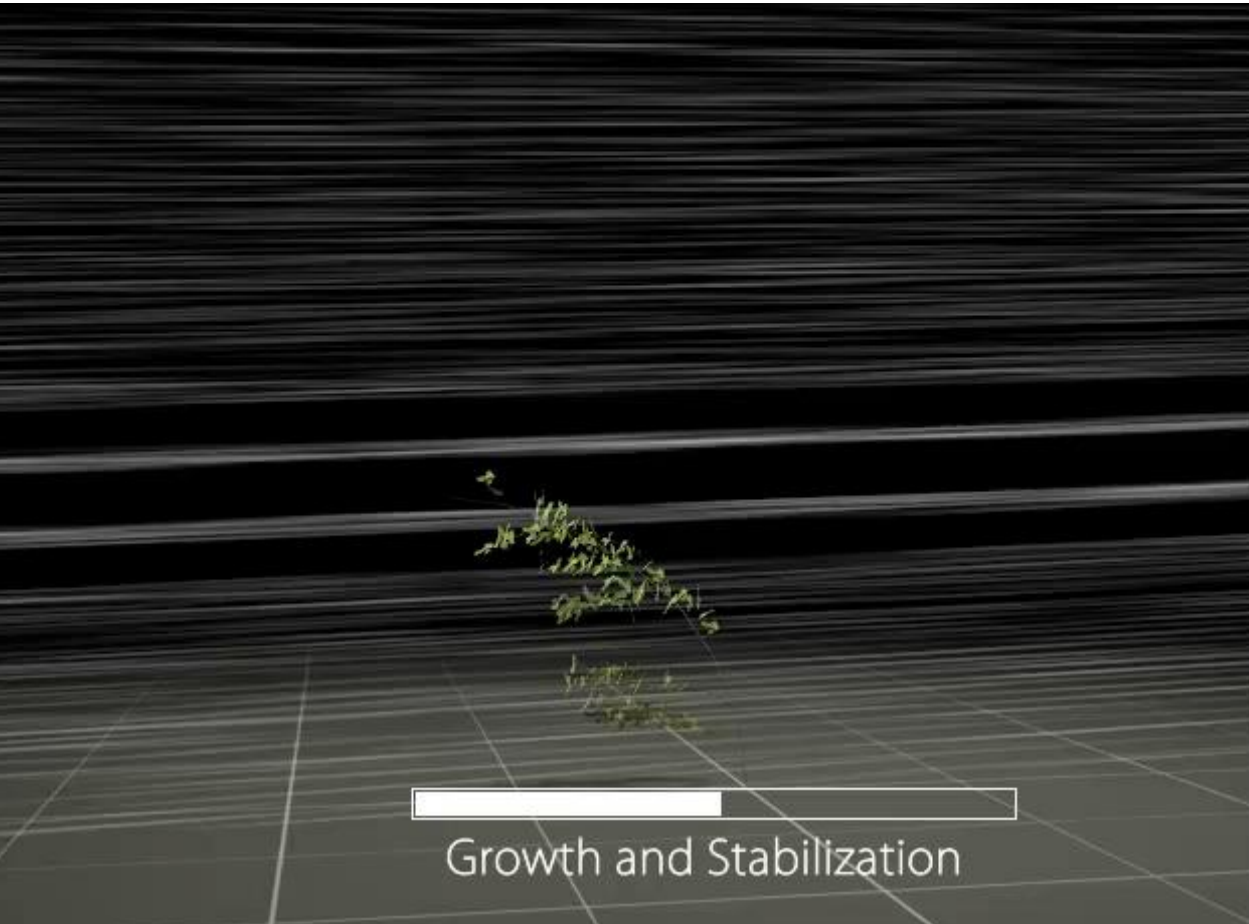
# Bud Abrasion and Drying

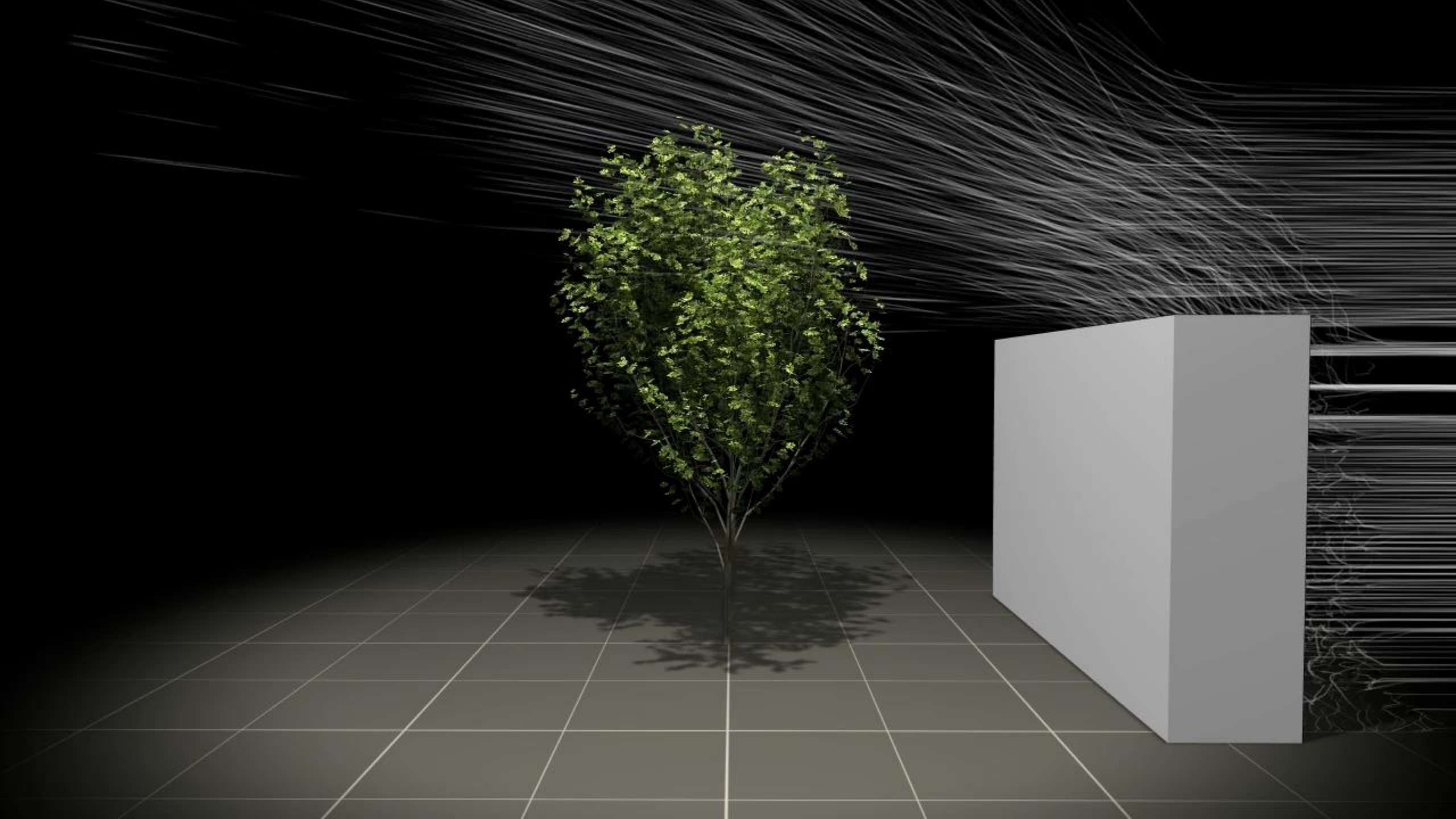
- Wind dries out or abrades buds
- Detect particles and neighboring branches
- User-defined threshold to terminate buds

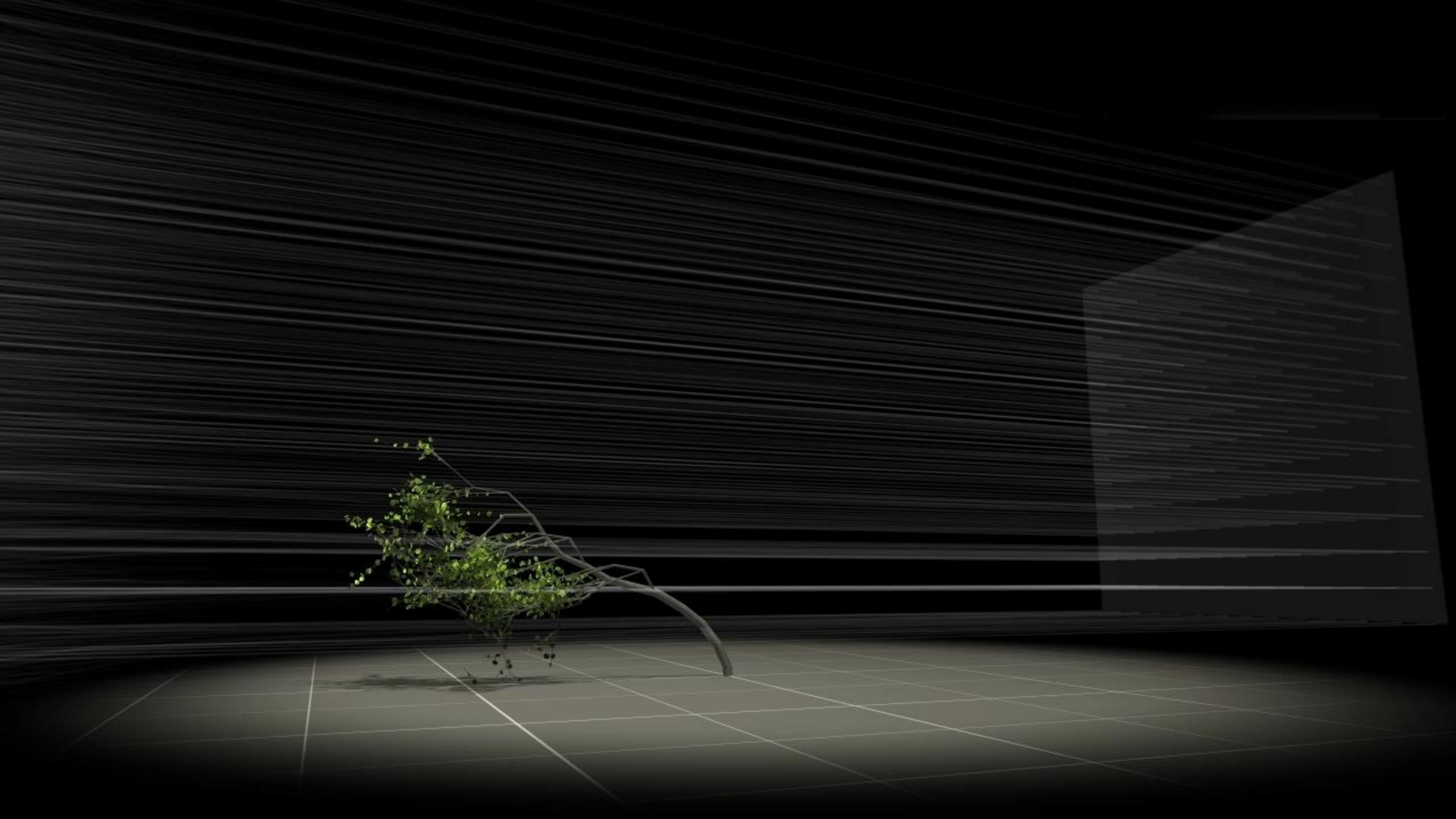
[Putz and Parker 1984]



Off On









5 x faster

