Supplementary Material for Anatomy of the first six months of COVID-19 Vaccination Campaign in Italy

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1 Model Definition

We report here the system of constitutive equations that defines the epidemic model. To simplify the notation we define the force of infection as 

\[ \lambda_k(t) = \beta \times \sigma_k(t) \times \left\{ \sum_{k'} \frac{\hat{C}_{kk'}(t)}{N_{k'}} \left[ I_{k'} + (1 - VE_k)(I_{k,1}^{V1} + I_{k,2}^{V2}) \right] \right\}, \]

where \( \beta \) is the transmission rate, \( \sigma_k(t) \) is the seasonality factor, \( \hat{C}_{kk'}(t) \) is the \( k,k' \) element of the contacts matrix with the reductions due to NPIs implemented, and the term in brackets is the probability of contacting an infectious individual in age group \( k' \) given the contact rates and the number of individuals per group. In the computational implementation, the model’s equations are integrated through chain binomial processes in order to ensure the discrete and stochastic nature of the transitions among compartments. Namely, at each time step \( t \) the number of individuals in age group \( k \) and compartment \( X \) transiting to compartment \( Y \) is sampled from \( Pr^{Bin}(X_k(t), p_{X_k \rightarrow Y_k}(t)) \), where \( p_{X_k \rightarrow Y_k}(t) \) is the transition probability. For the sake of readability we report below the ODE’s version of the constitutive
\[ S_k = -\lambda_k S_k - (1 + \psi)\lambda_k S_k - \Omega_{S_k}(t) \]
\[ S_k^{V1} = -(1 - V E_{S1})\lambda_k S_k^{V1} - (1 - V E_{S1}^{VOC})(1 + \psi)\lambda_k S_k^{V1} - \Delta_{V2}^{-1}S_k^{V1} + \Omega_{S_k}(t) \]
\[ S_k^{V2} = -(1 - V E_{S2})\lambda_k S_k^{V2} - (1 - V E_{S2}^{VOC})(1 + \psi)\lambda_k S_k^{V2} \]
\[ L_{WT,k} = \lambda_k S_k - \epsilon L_{WT,k} - \Omega_{L_{WT,k}}(t) \]
\[ L_{V1}^{VOC,k} = -(1 - V E_{S1})\lambda_k S_k^{V1} - \epsilon L_{V1}^{VOC,k} - \Delta_{V1}^{-1}L_{V1}^{VOC,k} + \Omega_{L_{V1}^{VOC,k}}(t) \]
\[ L_{V2}^{VOC,k} = -(1 - V E_{S2})\lambda_k S_k^{V2} + \Delta_{V1}^{-1}L_{V1}^{VOC,k} - \epsilon L_{V2}^{VOC,k} \]
\[ L_{VOC,k} = (1 + \psi)\lambda_k S_k - \epsilon L_{VOC,k} - \Omega_{L_{VOC,k}}(t) \]
\[ L_{V1}^{VOC,k} = -(1 - V E_{S1}^{VOC})(1 + \psi)\lambda_k S_k^{V1} - \epsilon L_{V1}^{VOC,k} - \Delta_{V1}^{-1}L_{V1}^{VOC,k} + \Omega_{L_{V1}^{VOC,k}}(t) \]
\[ L_{V2}^{VOC,k} = -(1 - V E_{S2}^{VOC})(1 + \psi)\lambda_k S_k^{V2} + \Delta_{V1}^{-1}L_{V1}^{VOC,k} - \epsilon L_{V2}^{VOC,k} \]
\[ I_{WT,k} = \epsilon L_{WT,k} - \mu I_{WT,k} \]
\[ I_{V1}^{VOC,k} = \epsilon L_{V1}^{VOC,k} - \mu I_{V1}^{VOC,k} \]
\[ I_{V2}^{VOC,k} = \epsilon L_{V2}^{VOC,k} - \mu I_{V2}^{VOC,k} \]
\[ R_{WT,k} = \mu(1 - IFR_k)I_{WT,k} - \Omega_{R_{WT,k}}(t) \]
\[ R_{V1}^{VOC,k} = \mu[1 - (1 - V E_{M1})IFR_k]I_{V1}^{VOC,k} - \Delta_{V2}^{-1}R_{V2}^{VOC,k} \]
\[ R_{V2}^{VOC,k} = \mu[1 - (1 - V E_{M2})IFR_k]I_{V2}^{VOC,k} + \Delta_{V1}^{-1}R_{V1}^{VOC,k} \]
\[ R_{VOC,k} = \mu(1 - IFR_k)I_{VOC,k} - \Omega_{R_{VOC,k}}(t) \]
\[ D_{V1}^{VOC,k} = \mu(1 - V E_{M1})IFR_kI_{V1}^{VOC,k} - \Delta_{V2}^{-1}D_{V2}^{VOC,k} \]
\[ D_{V2}^{VOC,k} = \mu(1 - V E_{M2})IFR_kI_{V2}^{VOC,k} - \Delta_{V1}^{-1}D_{V1}^{VOC,k} \]
\[ D_{VOC,k} = \mu IFR_kI_{VOC,k} - \Delta_{V1}^{-1}D_{VOC,k} \]
\[ D_{V1}^{VOC,k} = \mu(1 - V E_{M1})IFR_kI_{V1}^{VOC,k} - \Delta_{V2}^{-1}D_{V2}^{VOC,k} \]
\[ D_{V2}^{VOC,k} = \mu(1 - V E_{M2})IFR_kI_{V2}^{VOC,k} - \Delta_{V1}^{-1}D_{V1}^{VOC,k} \]
\[ D_{VOC,k} = \mu IFR_kI_{VOC,k} - \Delta_{V1}^{-1}D_{VOC,k} \]

Where the terms \( \Omega_{S_k}(t) \), \( \Omega_{L_{WT,k}}(t) \), \( \Omega_{R_{WT,k}}(t) \) describes the transition of individuals due to vaccination \( (1^{st} \text{ dose}) \). The number of individuals that receive the first dose at each time step is taken from real data \[ H \], while the distribution of doses among age groups depend on the strategy considered. For simplicity we did not included in the model the delay \( \Delta_Y \) between inoculation and actual vaccine protection. In Tab. \[ H \] we report a full list of parameters, their values and references.
<table>
<thead>
<tr>
<th>Symbol</th>
<th>Meaning</th>
<th>Value</th>
<th>Ref</th>
</tr>
</thead>
<tbody>
<tr>
<td>$\beta$</td>
<td>Transmission rate</td>
<td>fitted</td>
<td>2</td>
</tr>
<tr>
<td>$\epsilon$</td>
<td>Inverse of latency period</td>
<td>1 / 4 days</td>
<td>3, 4</td>
</tr>
<tr>
<td>$\mu$</td>
<td>Inverse of infectious period</td>
<td>1 / 2.5 days</td>
<td>3, 4</td>
</tr>
<tr>
<td>$C_{k,k'}$</td>
<td>Element of the contacts matrix</td>
<td>/</td>
<td>5</td>
</tr>
<tr>
<td>IFR</td>
<td>Infection Fatality Rate</td>
<td>Tab.</td>
<td>6</td>
</tr>
<tr>
<td>$\Delta$</td>
<td>Number of days between I $\rightarrow$ D and death reporting</td>
<td>fitted</td>
<td>7</td>
</tr>
<tr>
<td>$\psi$</td>
<td>Increased transmissibility of Alpha VOC</td>
<td>0.5</td>
<td>8, 9</td>
</tr>
<tr>
<td>$s(t)$</td>
<td>Seasonality modulation</td>
<td>time-varying</td>
<td>10</td>
</tr>
<tr>
<td>$VE_{S1}$</td>
<td>Vaccine efficacy against infection (1 dose)</td>
<td>Tab.</td>
<td>11</td>
</tr>
<tr>
<td>$VE_{S2}$</td>
<td>Vaccine efficacy against infection (2 dose)</td>
<td>Tab.</td>
<td>11</td>
</tr>
<tr>
<td>$VE_{M1}$</td>
<td>Vaccine efficacy against death if infected (1 dose)</td>
<td>Tab.</td>
<td>11</td>
</tr>
<tr>
<td>$VE_{M2}$</td>
<td>Vaccine efficacy against death if infected (2 dose)</td>
<td>Tab.</td>
<td>11</td>
</tr>
<tr>
<td>$VE_{VOC}^{S1}$</td>
<td>Vaccine efficacy against infection with Alpha VOC (1 dose)</td>
<td>Tab.</td>
<td>11</td>
</tr>
<tr>
<td>$VE_{VOC}^{S2}$</td>
<td>Vaccine efficacy against infection with Alpha VOC (2 dose)</td>
<td>Tab.</td>
<td>11</td>
</tr>
<tr>
<td>$VE_{VOC}^{M1}$</td>
<td>Vaccine efficacy against deaths if infected with Alpha VOC (1 dose)</td>
<td>Tab.</td>
<td>11</td>
</tr>
<tr>
<td>$VE_{VOC}^{M2}$</td>
<td>Vaccine efficacy against deaths if infected with Alpha VOC (2 dose)</td>
<td>Tab.</td>
<td>11</td>
</tr>
<tr>
<td>$VE_I$</td>
<td>Vaccine efficacy against further transmission</td>
<td>40%</td>
<td>11</td>
</tr>
<tr>
<td>$\Delta V_2$</td>
<td>Number of days for second inoculation</td>
<td>Tab.</td>
<td>11</td>
</tr>
</tbody>
</table>

Table 1: Interpretation of different parameters and their values.

<table>
<thead>
<tr>
<th>Age group</th>
<th>Infection Fatality Ratio (Salje et al)</th>
</tr>
</thead>
<tbody>
<tr>
<td>0-9</td>
<td>0.001%</td>
</tr>
<tr>
<td>10-19</td>
<td>0.001%</td>
</tr>
<tr>
<td>20-24</td>
<td>0.005%</td>
</tr>
<tr>
<td>25-29</td>
<td>0.005%</td>
</tr>
<tr>
<td>30-39</td>
<td>0.02%</td>
</tr>
<tr>
<td>40-49</td>
<td>0.05%</td>
</tr>
<tr>
<td>50-59</td>
<td>0.2%</td>
</tr>
<tr>
<td>60-69</td>
<td>0.7%</td>
</tr>
<tr>
<td>70-79</td>
<td>1.9%</td>
</tr>
<tr>
<td>80+</td>
<td>8.3%</td>
</tr>
</tbody>
</table>

Table 2: Age stratified infection fatality rate from Ref. [6]

<table>
<thead>
<tr>
<th>$VE_1 (VE_{S1})$</th>
<th>$VE_2 (VE_{S2})$</th>
<th>$\Delta V_2$</th>
</tr>
</thead>
<tbody>
<tr>
<td>Wild Type</td>
<td>Alpha</td>
<td>Wild Type</td>
</tr>
<tr>
<td>Pfizer</td>
<td>90% (80%)</td>
<td>50% (40%)</td>
</tr>
<tr>
<td>Moderna</td>
<td>90% (80%)</td>
<td>50% (40%)</td>
</tr>
<tr>
<td>AstraZeneca</td>
<td>70% (60%)</td>
<td>50% (40%)</td>
</tr>
<tr>
<td>Janssen</td>
<td>70% (60%)</td>
<td>50% (40%)</td>
</tr>
</tbody>
</table>

Table 3: Vaccine efficacy. We report the values of $VE$ and $VE_S$ in parenthesis. Using the relationship $VE = 1 - (1 - VE_S)(1 - VE_M)$ one can easily derive $VE_{M1}$ and $VE_{M2}$.

### 1.1 Reproductive Number Calculation

We compute the reproductive number $R_t^*$ (where $t^*$ indicate the start of our simulations) of the model proposed using the Next Generation Matrix method [13]. We derive the $R_t^*$ without the compartments related to the vaccinated and to the Alpha VOC. Indeed, our simulations start well before both the arrival of vaccines and of the variant. Therefore, these compartments do not affect the initial stage of the epidemic. For simplicity, we also do not consider seasonality as this factor only implies a rescaling $R_t^* \rightarrow s(t^*)R_t^*$. We consider the $2K$ equations (where $K$ is the number of age groups) that describe the evolution in time of the number of infected individuals $L$ and $I$:
\[ \dot{L}_k = \lambda_k S_k - \epsilon L_k \]
\[ \dot{I}_k = \epsilon L_k - \mu I_k \]  

(2)

Where \( \lambda_k \) is the force of infection for age group \( k \) previously introduced. In matrix notation:

\[
\begin{bmatrix}
\frac{d L_1}{dt} \\
\vdots \\
\frac{d L_K}{dt}
\end{bmatrix} = 
\begin{bmatrix}
\lambda_1 S_1 \\
\vdots \\
\lambda_K S_K
\end{bmatrix} - 
\begin{bmatrix}
\epsilon L_1 \\
\vdots \\
\epsilon L_K
\end{bmatrix} - 
\begin{bmatrix}
\mu I_1 - \epsilon L_1 \\
\vdots \\
\mu I_K - \epsilon L_K
\end{bmatrix}
\]  

(3)

Then, we define the disease free equilibrium (DFE) for age group \( k \) as \((S_k, L_k, I_k, R_k) \simeq (N_k - \tilde{R}_k, 0, 0, \tilde{R}_k)\)

where \( \tilde{R}_k \) is the residual immunity from previous waves. We define the two matrices \( F \) and \( V \) as follows:

\[
F_{ij} = \frac{\partial F_i}{\partial \theta_j} \bigg|_{DFE}
\]

\[
V_{ij} = \frac{\partial V_i}{\partial \theta_j} \bigg|_{DFE}
\]

(4)

These can be written as:

\[
F = 
\begin{bmatrix}
0 & \ldots & 0 & \beta \frac{(N_1 - \tilde{R}_1) C_{11}}{N_1} & \ldots & \beta \frac{(N_1 - \tilde{R}_1) C_{1K}}{N_K} \\
\vdots & \ddots & \vdots & \ddots & \ddots & \ddots \\
0 & \ldots & 0 & \beta \frac{(N_K - \tilde{R}_K) C_{K1}}{N_1} & \ldots & \beta \frac{(N_K - \tilde{R}_K) C_{KK}}{N_K} \\
0 & \ldots & 0 & 0 & \ldots & 0
\end{bmatrix}
\]

(5)

\[
V = 
\begin{bmatrix}
\epsilon & \ldots & 0 & 0 & \ldots & 0 \\
\vdots & \ddots & \vdots & \ddots & \ddots & \ddots \\
0 & \ldots & \epsilon & 0 & \ldots & 0 \\
-\epsilon & \ldots & 0 & \mu & \ldots & 0 \\
\vdots & \ddots & \vdots & \ddots & \ddots & \ddots \\
0 & \ldots & -\epsilon & 0 & \ldots & \mu
\end{bmatrix}
\]

(6)

The reproductive number is defined as \( R_t = \rho(FV^{-1}) \), where \( \rho(\cdot) \) indicates the spectral radius (i.e., leading eigenvalue). First, we compute \( V^{-1} \). We recognize that \( V \) and \( F \) can be written in blocks as:

\[
F = 
\begin{bmatrix}
0 & \beta \tilde{C} \\
0 & 0
\end{bmatrix}
\]

\[
V = 
\begin{bmatrix}
\epsilon \mathbb{1} & 0 \\
-\epsilon \mathbb{1} & \mu \mathbb{1}
\end{bmatrix}
\]

(7)

Where \( \tilde{C} \) is the contacts matrix weighted by the relative susceptible population in different age groups (i.e. \( \tilde{C}_{ij} = \frac{N_j - \tilde{R}_j}{N_j} C_{ij} \)), \( \mathbb{1} \) is the \( K \times K \) identity matrix, and 0 indicates a \( K \times K \) matrix with zero elements. The inverse of \( V \) is:

\[
V^{-1} = 
\begin{bmatrix}
1/\epsilon \mathbb{1} & 0 \\
1/\mu \mathbb{1} & 1/\mu \mathbb{1}
\end{bmatrix}
\]

(8)

The next step consists in computing the product \( FV^{-1} \):

\[
FV^{-1} = 
\begin{bmatrix}
0 & \beta \tilde{C} \\
0 & 0
\end{bmatrix} 
\begin{bmatrix}
1/\epsilon \mathbb{1} & 0 \\
1/\mu \mathbb{1} & 1/\mu \mathbb{1}
\end{bmatrix} = 
\begin{bmatrix}
\beta \tilde{C}/\mu & \beta \tilde{C}/\mu \\
0 & 0
\end{bmatrix}
\]

(9)
Finally, we are left with finding the spectral radius of $FV^{-1}$ (i.e., its largest eigenvalue). The eigenvalue problem can be written as $\text{det}(FV^{-1} - \lambda I) = 0$. Given the structure of $FV^{-1}$, and since we are interested in non-trivial solutions ($\lambda \neq 0$), the problem reduces to:

$$\text{det}[\beta \hat{C}/\mu - \lambda I] = 0$$ (10)

Therefore $R_t^* = \rho(FV^{-1}) = \beta \rho(\hat{C})/\mu$. In the main text we assumed that $\bar{R}_k << N_k$, therefore we approximate the disease free equilibrium as $(S_k, L_k, I_k, R_k) \simeq (N_k, 0, 0, 0)$. This assumption holds in our case since the initial number of recovered across all age brackets is generally smaller than 10% of the total population.
2 Model Calibration

We calibrate the free parameters of the model using an Approximate Bayesian Computation (ABC) technique \[14, 15\]. We define the prior distributions of the free parameters \( P(\theta) \), a number accepted sets \( N \), an error metric \( m(E, E') \), and a tolerance \( \delta \). We start sampling a set of parameters \( \theta \) from \( P(\theta) \) and generate an instance of the model using these parameters. Then, using the chosen error metric we compare an output quantity \( E' \) of the model with the corresponding real quantity \( E \): if \( m(E, E') < \delta \) then we accept the set \( \theta \), otherwise we reject it. We repeat this accept/reject step until \( N \) parameter sets are accepted. The empirical distribution of the accepted sets is an approximation of their real posterior distribution. We produce model’s projections sampling parameters sets from the pool of accepted sets and generating an ensemble of possible epidemic trajectories. We then compute median and confidence intervals on this ensemble. In this work, we consider the following free parameters and priors:

- \( \beta \), we explore values of the transmission rate parameter such that the associated \( R_t = \rho(\tilde{C})s(t)\mu \) on the first simulation day \( \sim U(1.2, 2.0) \) \[2\] (where \( \tilde{C} \) is the contacts matrix weighted by the relative population in different age groups and \( \rho(\cdot) \) is the leading eigenvalue; see Sec. 1.1);
- \( \Delta \sim U(14, 25) \). The calibration range is informed by Ref. \[7\];
- \( \alpha_{\text{min}} \sim U(0.5, 1.0) \), in doing so we explore values from strong (0.5) to absent (1.0) seasonality;
- we select initial conditions from an ensemble of realistic estimates from GLEAM. Each estimate has the number of individuals of different age groups in different compartments (\( S \), \( L \), \( I \), \( R \)) on the start of the simulation (2020/09/01).

The model is calibrated separately for each of the six regions considered. We set the calibration period to 2020/09/01-2021/07/05. We consider weekly deaths as output quantity and the weighted mean absolute percentage error (wMAPE) as error metric. We also set the number of accepted sets \( N = 3000 \) and the weighted mean absolute percentage error (wMAPE) as error metric. We also set the number of accepted sets \( N = 3000 \) and the weighted mean absolute percentage error (wMAPE) as error metric. For the different basins, we represent in Fig. 1 the number of weekly real and simulated deaths (median and 90% CI). We obtain a median wMAPE of 0.23 for North West, 0.26 for North East, 0.25 for Center, 0.18 for South, 0.30 for Sicily, and of 0.40 for Sardinia. In the Supplementary Information we report the posterior distributions of the free parameters obtained through the ABC calibration.

In Fig. 2 are shown the posterior distributions of the parameters calibrated through the ABC rejection algorithm \[14, 15\] for each region. In particular, we report the effective reproductive number \( R_t \) on the first simulation day, the delay (expressed in days) in deaths \( \Delta \), the seasonality parameter \( \alpha_{\text{min}} \), and the initial number of infected (\( I \) plus \( L \) individuals) and recovered per 100'000 at the start of the simulation.
Figure 1: **Calibration Results.** Simulated (median and 90% CI) and observed cumulative number of deaths.

Figure 2: **Posterior distributions of parameters obtained through ABC calibration.** Each boxplot summarises the distribution of the parameter showing median, interquartile range (IQR), and minimum and maximum values defined respectively as $Q_1 – 1.5IQR$ and $Q_3 + 1.5IQR$ (where $Q_1$ and $Q_3$ are the first and third quartile).
3 Modeling non-pharmaceutical interventions: school closures

We model variations in contacts in schools as follows. First, we identify two phases. Before 2020/11/06, interventions from the Italian Government were mostly at the national level and different regions followed the same rules and recommendations. During this first phase, we use data from the Oxford COVID-19 Government Response Tracker [18] to model contacts variation in schools. We consider three indexes from this report about school closure (school$_{idx}$), workplace closure (work$_{idx}$), and stay at home requirements (stayhome$_{idx}$). These indexes vary daily and are provided at the national level. They can assume discrete values from 0 (no measures) to 3 (maximum restrictions). We define the parameters $w_s(t)$ and $\alpha(t)$ as follows:

1. $school_{idx}(t) = 0 \rightarrow w_s(t) = 1.0, \alpha(t) = 1.0$
2. $school_{idx}(t) = 1 \rightarrow w_s(t) = 0.5, \alpha(t) = 1.0$
3. $school_{idx}(t) = 2 \rightarrow w_s(t) = 1.0, \alpha(t) = 0.3444$
4. $school_{idx}(t) = 3$ and $NOT(work_{idx}(t) \geq 2$ and $stayhome_{idx}(t) \geq 2) \rightarrow w_s(t) = 1.0, \alpha(t) = 0.3444$
5. $school_{idx}(t) = 3$ and $(work_{idx}(t) \geq 2$ and $stayhome_{idx}(t) \geq 2) \rightarrow w_s(t) = 0.0, \alpha(t) = 1.0$

Finally, we model the impact of school closing on contacts on day $t$ multiplying the school layer $C_{school}$ (the elements describing contacts between 0 – 24 years old individuals of the overall contacts matrix $C$) by $w_s(t)$ and by $\alpha(t)$. The two indexes are introduced to modify contacts that the younger age groups may have at school but also in other settings. The idea behind our approach is to define increasingly higher risk levels according to the policies implemented. The first case, for example, refers to a situation with no restrictions in place, therefore contacts in schools are not affected. When instead $school_{idx}(t) = 1$ some restrictions are in place, school closing or hybrid teaching mode and additional NPIs in classroom are recommended resulting in significant differences compared to normal operations [16]. We assume this would result in significant reduction of contacts in school. When $school_{idx}(t) = 2$ we introduce a reduction factor on the contacts of 0 – 24 years which is taken from Ref. [17], where authors studied the impact of school closure on contacts patterns among younger population. In the fourth case, strict closure policies on school are in place ($school_{idx}(t) = 3$) but younger age groups may still meet in different context apart from school (i.e., the work from home and the stay at home indexes are not at the maximum value). We assume that this would result in the same contacts reduction of the previous cases. Finally, when closure is required at all levels we send to zero the layer of contacts in schools.

After 2020/11/06, the Italian government introduced a tier system in which different NUTS2 regions were assigned to one of four risk levels (from 0, lowest risk, to 4 highest risk) [18]. Different tiers are associated with increasingly more restrictive measures. Because of our spatial resolution, first we define the risk tier at the NUTS1 level as the weighted average (according to the population) of the risk levels of the component NUTS2 regions (rounded to the nearest integer). For example, for NUTS1 region $R$, the risk tier at time $t$ is:

$$TIER_R(t) = \left\lfloor \frac{\sum_{r \in R} p_r \cdot TIER_r(t)}{\sum_{r \in R} p_r} \right\rfloor$$

(11)

Where the summation runs over all NUTS2 regions $r$ which are part of NUTS1 region $R$, and $p_r$ is the population of NUTS2 region $r$ taken from official sources [19]. Finally, we define the parameters $w_s(t)$ and $\alpha(t)$ similarly to what we did before for the first phase:

1. $TIER_R(t) = 0 \rightarrow w_s(t) = 0.5, \alpha(t) = 1.0$
2. $TIER_R(t) = 1 \rightarrow w_s(t) = 0.5, \alpha(t) = 1.0$
3. $TIER_R(t) = 2 \rightarrow w_s(t) = 1.0, \alpha(t) = 0.3444$
4. $TIER_R(t) = 3 \rightarrow w_s(t) = 0.0, \alpha(t) = 1.0$

Then the contacts matrix for school on day $t$ is again obtained by the multiplying $C_{school}$ by $w_s(t)$ and by $\alpha(t)$ the contact rates between 0 – 24 years old individuals.
4 Italian Regions

In Fig. 3 we report some demographic and epidemiological characteristics of the different Italian regions under study. In Fig. 3A we show the distribution (%) of individuals in different age groups. We observe that, in general, the population is younger in South Italy and Sicily even tough the difference with other regions is extremely limited. Fig. 3B reports the estimated date (median and 90% CI) of the first Alpha VOC importation estimated by the Global Epidemic and Mobility model (GLEAM [10 20 21]). Importations are highly synchronized across regions. Indeed, across the board, the initial seeding of the variant happened throughout October 2020, and slightly later (early November 2020) in Sardinia. Fig. 3C shows the attack rate (i.e., cumulative incidence per 100) as reported by official surveillance and as estimated by GLEAM on the 2020/09/01 (start of our simulations). We notice good accordance between modeling estimates and official data. As expected, estimated attack rates are generally much higher than reported ones (∼10×). We notice significant differences among regions. Sicily, Sardinia, and South Italy feature a smaller attack rate with respect to Center, and especially North East and North West. We also characterize regions according to the unfolding of the vaccine rollout in Fig. 3D, where it is reported the cumulative number of first doses administered per 100. The evolution of the number of doses given is extremely similar across regions with some difference at the end of the period of observation (e.g., Sicily has a slightly smaller number of doses given respect to other regions). Finally, Fig. 3E and Fig. 3F shows population size and density. Northwest is the most numerous and densely populated region. The number of individuals and their density in North East, South, and Center are comparable. Finally, Sicily and Sardinia are less populated (they are NUTS2 regions), but while Sardinia is also less densely populated, Sicily has a high population density (similar to Northeast, Center, and Sicily).
Figure 3: **Characteristics of Italian regions under study.** A) Distribution of individuals among age groups. B) Date of estimated first importation of Alpha VOC (median and 90% CI). C) Attack rate on 2020/09/01 (start of the simulation) as reported by official surveillance and as estimated by modeling. D) Cumulative number of first doses administered. E) Population size. F) Population density.
5 Vaccine Hesitancy

In the main text we assumed that in the counterfactual scenarios (strategy 2 and strategy 3) all individuals are willing to receive the vaccines. Despite Italy showing very high rates of vaccine acceptance (as of 2021/10/19 85.7% received at least one dose [22]), this is an optimistic assumption. Therefore, we repeat here part of the analyses considering that a fraction of the population do not want to receive the vaccine. In Fig. 4 we show the total number of averted deaths and infections (median and IQR) for strategy 2 (prioritizing the elderly) and 3 (prioritizing the younger) for different values of hesitancy (i.e., the percentage of the population that refuses vaccines). We assume that hesitant individuals are homogeneously distributed among age groups. The horizontal dashed lines indicate the number of averted deaths/infections for the two strategies in the case of no hesitancy as presented in the main text. We observe, overall, a negligible effects of hesitancy. The explanation for such a small impact is that, as of 2021/07/05, only 58% of the population received at least one dose of vaccine in Italy. Therefore, the number of doses distributed in our simulations are not high enough to make the values of hesitancy considered significant. This also explains why we only observe an impact on model’s outputs when considering averted deaths by strategy 2. In this scenario, we notice a decline in the number of averted deaths as the value of hesitancy grows. Indeed, since in this case we proceed in strictly decreasing age order between 50-80+, the values of hesitancy can play a role for older age groups that also feature higher IFRs.

![Averted Deaths (Country) - Effects of Hesitancy](image1)

![Averted Infections (Country) - Effects of Hesitancy](image2)

Figure 4: Effects of vaccine hesitancy
6 Different Transmissibility of Alpha Variant

In the main text we assumed the variant Alpha to be 50\% (i.e., $\psi = 0.5$) more infectious than the wild type circulating previously, in line with available estimates [8, 9]. Nonetheless, we provide a sensitivity analysis to the results considering different values of $\psi$. In particular, we consider here $\psi = 0.3$ and $\psi = 0.6$. We repeat the calibration step for the two additional values of $\psi$. We note a need to increase the ABC tolerance in the case of $\psi = 0.6$ for convergence reasons. In Tab. 4 we report the obtained wMAPE between simulated and reported weekly deaths for the three values of $\psi$. We notice how the calibration with $\psi = 0.5$ gives in general better results.

<table>
<thead>
<tr>
<th>$\psi$</th>
<th>North West</th>
<th>North East</th>
<th>Center</th>
<th>South</th>
<th>Sicily</th>
<th>Sardinia</th>
</tr>
</thead>
<tbody>
<tr>
<td>0.3</td>
<td>0.33</td>
<td>0.32</td>
<td>0.32</td>
<td>0.28</td>
<td>0.29</td>
<td>0.33</td>
</tr>
<tr>
<td>0.5</td>
<td>0.23</td>
<td>0.26</td>
<td>0.25</td>
<td>0.18</td>
<td>0.30</td>
<td>0.40</td>
</tr>
<tr>
<td>0.6</td>
<td>0.28</td>
<td>0.23</td>
<td>0.32</td>
<td>0.27</td>
<td>0.46</td>
<td>0.57</td>
</tr>
</tbody>
</table>

Table 4: wMAPE between simulated and reported weekly deaths for different $\psi$

In Fig. 5A we show averted deaths and infections at the subnational and national level. We observe how figures are lower when considering $\psi = 0.3$. This is expected. Indeed a less transmissible variant causes a milder wave in our simulations with no vaccine and therefore the difference with the simulations with vaccine administered is smaller. For the opposite reason, the number of averted deaths and infections is higher, instead, in the case of $\psi = 0.6$. At the national level, we estimate vaccines would have averted 12,896 ($IQR: [7,002 - 19,254]$) deaths for $\psi = 0.3$ and 39,242 ($IQR: [24,539 - 53,543]$) with $\psi = 0.6$. As discussed in the main for $\psi = 0.5$ we have instead 29,350 ($IQR: [16,454 - 42,826]$). Similarly, the estimated number of averted infections would have been 2,383,158 ($IQR: [748,270 - 4,130,513]$) with $\psi = 0.3$ and 4,815,666 ($IQR: [2,411,182 - 7,207,004]$) with $\psi = 0.6$. For $\psi = 0.5$ we have instead 4,256,332 ($IQR: [1,675,564 - 6,980,070]$).

In Fig. 5B we report the national prevalence of Alpha for the three values of $\psi$. When $\psi = 0.5$, we get a wMAPE of 0.34 and a Pearson correlation coefficient $\rho = 0.84$ ($p < 0.001$) between the simulated prevalence and the one reported by genomic surveillance [23]. When $\psi = 0.3$ we get poorer results (wMAPE = 0.53, $\rho = 0.70$), and when $\psi = 0.6$ we get slightly better performance (wMAPE = 0.31, $\rho = 0.86$).
Figure 5: Sensitivity analysis on $\psi$. A) Averted deaths and infections at subnational and national level for different values of $\psi$. B) National prevalence of the Alpha variant as simulated with different $\psi$ and as reported by genomic surveillance.
7 Increased Mortality for the Alpha Variant

In the main text we assumed the same Infection Fatality Ratio (IFR) for both the wild type and the Alpha variant. Nonetheless, previous works showed that the Alpha variant may also be associated with higher severity [24, 25]. To estimate how this impacts our findings we repeat here the analysis considering $IFR_{\text{Alpha}} = 1.5 IFR_{\text{wild type}}$, where $IFR_{\text{wild type}}$ is the one used in the main text and is taken from Ref. [6], and the 1.5 factor is in line with previous works [24, 25].

In Fig. 6 we show averted deaths and infections using the same IFR for wild type and Alpha and using the higher IFR for Alpha. We observe that our findings are not significantly impacted by the change of the IFR. Overall, when the higher IFR for Alpha is considered we estimate a slightly higher number of averted deaths. For example, at the national level we estimate vaccines averted 29,350 (IQR: [16,454 – 42,826]) deaths when considering the same IFR for both strains, and 34,578 (IQR: [19,449 – 50,314]) when considering a higher IFR for Alpha.

Figure 6: Sensitivity analysis on Alpha variant IFR. Averted deaths and infections at subnational and national level considering the same IFR for both wild type and Alpha and a higher IFR for Alpha.
The Role of Asymptomatic and Recovered on Vaccinations

In the main text we assumed that all individuals but the infectious ($I$) can receive the vaccine. The real vaccination rollout in Italy, however, was more complex in terms of allocation. For example, individuals who recovered from the disease generally received only dose after at least three months from recovery and no more than six (then extended to twelve) \[26\]. At the same time, since vaccines were not officially preceded by a test, asymptomatic individuals may have received the vaccine as well. To assess how much the different allocation of vaccines among compartments can affect our result, we propose here the following analysis. In line with available estimates, we consider that 40% of all infections in our simulations are asymptomatic \[27, 28\]. Then, we assume that 40% of infectious individuals $I$ (i.e., the asymptomatic) can also receive the vaccines. We also assume that only 40% of recovered can receive the vaccine. Said differently, we assume that symptomatic recovered do not receive the vaccine. We note how this is an extreme scenario in which all asymptomatic infectious are eligible for vaccine and none of the symptomatic recovered are. The goal here is indeed to test the extent to which our results are impacted by different choices of allocation of vaccines among compartments.

In Fig. 7 we show averted deaths and infections using the allocation of vaccines among compartments presented in the main text and the one just described. We see that the change of allocation does not significantly impact our findings. For example, the number of averted deaths with the new allocation is 35,404 ($IQR: [21, 577 − 50, 200]$), while in the main text we obtained 29,350 ($IQR: [16, 454 − 42, 826]$). The higher number of averted deaths may be due to the fact that, with the new allocation among compartments, vaccines are given only to a fraction of the recovered and as result more doses are administered to susceptibles individuals.

Baseline with behavioral reactions

In the main text, the impact of vaccines is measured respect to a baseline that has everything equal but for the presence of vaccines. This approach allows us to isolate the impact of vaccines alone on the epidemic trajectory. Nonetheless, we acknowledge that the NPIs observed during the rollout were contingent to the improved epidemiological condition to which vaccines contributed in a substantial way. In the absence of vaccines, a worsening of the epidemiological conditions would have likely led to both
bottom-up (i.e., self-initiated) and top-down (i.e., government mandated) behavioral reactions [29]. As result, the baseline is a pessimistic estimate since it does not account for possible NPIs enforcement in response to rises in infections and fatalities in case of no vaccinations.

Here, we present a second baseline without vaccines in which we also model behavioral reactions. It is important to stress that we will never know what it could have happened in the spring of 2021 without vaccines, so any scenario aiming to account for behavioral changes it is speculative. Bearing this in mind we proceed as follows. First, we define a threshold for the introduction of tougher restrictive measures. As mentioned in the main text, on 2020/11/06 the Italian government introduced a risk-level system to adopt more targeted and timely countermeasures according to the local epidemic conditions. Therefore, for each of our six regions, we compute the average number of deaths on the days when the region was moved to the highest risk level (indicated as “red zone”). We call this quantity \( D_{\text{red zone}}^i \). Second, we compute the average contacts matrix \( C_{\text{red zone}}^i \) observed during the days when in region \( i \) were in place the rules of the highest risk level. Finally, we follow this simple approach: in the simulation without vaccines administered, if the number of daily deaths in region \( i \) exceeds \( D_{\text{red zone}}^i \) - and the region is not already in the highest risk level - we use the contacts matrix \( C_{\text{red zone}}^i \) instead of the one computed following actual mobility change and policy interventions. We apply this check after 2021/03/01 since it is around this date that the epidemic trajectories with and without vaccines start to visibly diverge.

We stress how this threshold approach to model NPIs enforcement has many limitations. For example, the system of risk-levels developed in Italy depended on many parameters and not just on deaths [18]. Also, we consider a single threshold, while in reality multiple thresholds associated with increasingly higher risk levels were defined. As result, our approach is admittedly simplistic to represent the complexity of individual and collective response to epidemics [30]. Nonetheless, it captures the possible evolution of NPIs in a hypothetical scenario using historical real data and allows us to assess the impact of this on our findings.

In Fig. 8 we compare the evolution of weekly deaths as reported by official sources and as simulated by our model. We consider the case in which i) vaccines are administered according to the real data, ii) no vaccines are administered, iii) no vaccines are administered but NPIs are put in place to counter the uptick of cases and deaths. As expected, in this last scenario we observe less deaths with respect to the simple baseline considered in the main. Nonetheless, it is important to stress how also in this case the death toll is worse with respect to the case with vaccines.

In Tab. 5 and Tab. 6 we compare the number of averted deaths and infections by vaccines with respect to the two no-vaccine baselines in different regions. Not surprisingly, we observe that total number of averted deaths with respect to the new baseline is diminished, from 29,4064 (IQR: [16, 571; 42,830]) to 12,676 (IQR: [2,795; 22,887]). At the same time, we also obtain a much lower number of averted infections (547,554 IQR: [−1,540,752; 2,701,933] respect to 4,306,913 IQR: [1,656,934; 6,990,557]).

Figure 8: Evolution of weekly deaths in Italy under different scenarios. We show the number of weekly deaths in Italy as reported by official sources and simulated by our model. We consider different vaccination scenarios: i) data-driven vaccination (solid line), ii) no vaccine (dashed line), and iii) no vaccine with possible behaviour reaction (dash-dotted line).
Table 5: Averted deaths - No vaccine baseline comparison

<table>
<thead>
<tr>
<th></th>
<th>No Vaccine Baseline</th>
<th>No Vaccine + Behavior Reaction Baseline</th>
</tr>
</thead>
<tbody>
<tr>
<td>North West</td>
<td>9047 [5525, 1249]</td>
<td>4672 [2052, 7480]</td>
</tr>
<tr>
<td>North East</td>
<td>3143 [750, 596]</td>
<td>3128 [532, 594]</td>
</tr>
<tr>
<td>Center</td>
<td>6431 [4077, 873]</td>
<td>2469 [733, 410]</td>
</tr>
<tr>
<td>South</td>
<td>7892 [4745, 112]</td>
<td>1464 [75, 352]</td>
</tr>
<tr>
<td>Sicily</td>
<td>2263 [1246, 331]</td>
<td>720 [56, 138]</td>
</tr>
<tr>
<td>Sardinia</td>
<td>629 [228, 1095]</td>
<td>222 [-24, 44]</td>
</tr>
<tr>
<td>Italy (total)</td>
<td>29406 [16571, 4283]</td>
<td>12676 [2795, 2288]</td>
</tr>
</tbody>
</table>

Table 6: Averted infections - No vaccine baseline comparison

<table>
<thead>
<tr>
<th></th>
<th>No Vaccine Baseline</th>
<th>No Vaccine + Behavior Reaction Baseline</th>
</tr>
</thead>
<tbody>
<tr>
<td>North West</td>
<td>1011733 [269085, 17337]</td>
<td>260,281 [-390544, 886551]</td>
</tr>
<tr>
<td>North East</td>
<td>506441 [43955, 993421]</td>
<td>467160 [11869, 100859]</td>
</tr>
<tr>
<td>Center</td>
<td>875658 [460490, 1284045]</td>
<td>75351 [-222365, 368548]</td>
</tr>
<tr>
<td>South</td>
<td>1289381 [571882, 2044919]</td>
<td>-269856 [-745282, 201937]</td>
</tr>
<tr>
<td>Sicily</td>
<td>451476 [243112, 652044]</td>
<td>6086 [-134485, 155195]</td>
</tr>
<tr>
<td>Sardinia</td>
<td>172223 [68409, 282335]</td>
<td>8532 [-53945, 63195]</td>
</tr>
<tr>
<td>Italy (total)</td>
<td>4306913 [1656934, 690955]</td>
<td>547554 [-154075, 629193]</td>
</tr>
</tbody>
</table>

10 Impact of vaccine protection delays distributions and second doses administration

We propose an alternative version of the model in which we use a different distribution of the delays between inoculation and actual vaccine protection. As explained previously, in the main text we considered an average period of $\Delta_V = 14$ days between inoculation (of both 1st and 2nd dose) and vaccine protection. This means that a person receiving a dose on day $t$ will be protected, on average, on day $t + \Delta_V$. In practice, individuals receiving the vaccine are moved to a temporary compartment, and transition to the final compartment of vaccinated with a rate $1/\Delta_V$. Consider the following example. The number of susceptible individuals receiving the first dose on day $t$ is taken from real data. These individuals are moved to the temporary compartment $S_1^{V_1}$. In this compartment they still have no vaccine protection, therefore they can get infected at the same rate as the susceptibles. Then, $S_1^{V_1}$ eventually transition to the vaccinated compartment $S_1^{V_2}$ with a rate $1/\Delta_V$. Also this transition is regulated by a binomial sample: $P_{bin}(S_1^{V_1}(t), 1/\Delta_V)$. The result is that, the times spent in the temporary compartment $S_1^{V_1}$ will be exponentially distributed with scale parameter $1/\Delta_V$ (mean $\Delta_V$ and variance $\Delta_V^2$).

To assess the impact of this modeling choice, we propose here a model in which vaccine protection delays follow an Erlang distribution with shape parameter $n$. Indeed, while the standard formulation of compartmental models assume that the time spent in different compartments is exponentially distributed, distributions might be narrower and centred around the mean. The Erlang distribution is equivalent to a sequence of independent and identically distributed exponential distributions. Therefore, we modify the modeling setup including additional temporary compartments. Consider the previous example. In this new formulation of the model, susceptible individuals that receive the first dose move to the temporary compartment $S_1^{V_1}$, where they are still not protected by vaccines. Then, they transition to the next temporary compartment $S_2^{V_1}$ at rate $n/\Delta_V$, where $n$ is shape parameter and the number of temporary compartments. Finally, the individuals in $S_2^{V_1}$ transition to the compartment of the vaccinated with one dose $S_3^{V_1}$. Following this approach, we obtain that the time spent in the temporary compartments is distributed according to an Erlang distribution with shape parameter $n$ and scale parameter $1/\Delta_V$ (mean $\Delta_V$ and variance $\Delta_V^2/n$). In Fig. 5, we show the Erlang distribution for different values of $n$. We see that for $n = 1$ we get the exponential distribution, while for higher values the distribution is narrower and more peaked around the mean.

For simplicity, here we set $n = 2$. This implies defining two temporary compartments ($S_1^{V_1}$ and $S_2^{V_1}$ according to the previous example), in which each individual spends on average 7 days. As an additional sensitivity check to the modeling of vaccinations, here we also consider real data for second
doses. Indeed, in the main text we informed the number of daily first doses with real data from official sources, while we modeled the second inoculation introducing transitions happening at rate $1/\Delta V_2$, with $\Delta V_2$ depending on the vaccine manufacturer. This was done to simplify the model. Here, to assess the impact of this choice we inform the model also with the number of second doses administered per day by age group and manufacturer.

![Erlang Distribution](image)

**Figure 9:** Erlang distribution for several shape parameters. Plot is adapted from Ref. [31]. Solid vertical line indicates the average stage duration $\Delta V = 14$ days.

In Fig. 10 we compare different strategies in terms of averted deaths and infections using the modeling setup just described. We see that the main findings are unaltered. Indeed, the strategy prioritizing the elderly (strategy 2) generally implies more averted deaths, followed by the actual strategy and the strategy prioritizing 20-49 age groups (strategy 3). When considering averted infections, instead, the order is inverted: strategy 3 guarantees less infections, followed by the actual strategy and strategy 2. The overall national figures are also very similar to those obtained in the main text. For example, we estimate here that the actual strategy averted 31,314 ($IQR: [18, 247 - 44,621]$) deaths compared to 29,350 ($IQR: [16, 454 - 42,826]$) as reported in the main text.
Figure 10: Comparison of vaccine allocation strategies with Erlang distributed vaccine protection delays. A) Averted COVID-19 deaths and infections, both at subnational and national level (medians and interquartile ranges are reported). B) Percentage reduction of the Infection Fatality Rate as of 2021/07/05. In all panels, actual strategy denotes an allocation strategy that follows the observed allocation as it unfolded during the pandemic, strategy 2 considers the case where vaccines are allocated in decreasing age order starting from the 80+, strategy 3 considers the case in which vaccines are first allocated to the age groups 20–49 and then homogeneously to the rest of the population, and no-vaccine denotes the counterfactual scenario in which vaccines were not administered. In both panel we report the statistical significance of the Kruskal-Wallis H-test comparing different scenarios as follows: ****: \( p \text{value} \leq 10^{-4} \), ***: \( 10^{-4} < p \text{value} \leq 10^{-3} \), **: \( 10^{-3} < p \text{value} \leq 10^{-2} \), *: \( 10^{-2} < p \text{value} \leq 0.05 \), and otherwise blank if \( p > 0.05 \).
References


[26] Aggiornamento indicazioni sulla Vaccinazione dei soggetti che hanno avuto un’infezione da SARS-CoV-2. [https://redas.services.siag.it/covidArticlesAttachment?attachId=1116555](https://redas.services.siag.it/covidArticlesAttachment?attachId=1116555), 2021.


