

Name: _____

Date: _____

Calculus Chapter 3 Test

1) State the Derivative of each of the following functions

a) $y = x^n$

d) $y = \sin x$

b) $y = e^x$

e) $y = \cos x$

c) $y = b^x$

f) $y = \tan x$

#2 – 18 Calculate the derivative of each

1) $f(x) = \frac{x^2 - x + 2}{\sqrt{x}}$

2) $f(x) = (x^2 + 3)^2$

3) $f(x) = x^4 + 3x^{3/2} - 5 - 2x^{-2}$

$$4) f(x) = (3x^2 - 5x)e^x$$

$$5) f(x) = \left(\frac{1}{x^2} - \frac{3}{x^4}\right)(x + 5x^3)$$

$$6) f(x) = \frac{x^3 + 3x}{x^2 - 4x + 3}$$

$$7) f(\theta) = \theta \cos \theta \sin \theta$$

$$8) f(x) = \frac{\cot x}{e^x}$$

$$9) f(x) = \sec x$$

$$10) \quad f(x) = (5x^6 + 2x^3)^4$$

$$11) \quad f(\theta) = e^{\tan \theta}$$

$$12) \quad f(x) = \sqrt{1 + xe^{-2x}}$$

$$13) \quad x^2 - 4xy + y^2 = 4$$

$$14) \quad e^{\frac{x}{y}} = x - y$$

$$15) \quad \sin(xy) = \cos(x + y)$$

$$16) \quad f(x) = \ln(1 + x - x^3)$$

17) $f(x) = 2^x \log_2 x$

18) $f(x) = \sqrt{\frac{x-1}{x^4+1}}$

19) If a snowball melts so that its surface area decreases at a rate of $1 \frac{\text{cm}^2}{\text{min}}$ find the rate at which the diameter decreases when the diameter is 10 cm.

20) Find the linear approximation of the function $f(x) = \sqrt{1-x}$ at $a=0$ and use it to approximate the numbers $\sqrt{0.9}$ and $\sqrt{0.99}$. sketch a graph of the function and its tangent line to illustrate this approximation.