

**Practice with Examples**

For use with pages 264–270

**GOAL**

Solve quadratic equations by finding square roots and use quadratic equations to solve real-life problems

**VOCABULARY**

If  $b^2 = a$ , then  $b$  is a **square root** of  $a$ . A positive number  $a$  has two square roots,  $\sqrt{a}$  and  $-\sqrt{a}$ . The symbol  $\sqrt{\quad}$  is a **radical sign**,  $a$  is the **radicand**, and  $\sqrt{a}$  is a **radical**.

**Rationalizing the denominator** is the process of eliminating square roots in the denominator of a fraction.

**EXAMPLE 1****Using Properties of Square Roots**

Simplify the expression.

a.  $\sqrt{99} = \sqrt{9} \cdot \sqrt{11} = 3\sqrt{11}$

b.  $\sqrt{6} \cdot \sqrt{8} = \sqrt{48} = \sqrt{16} \cdot \sqrt{3} = 4\sqrt{3}$

c.  $\sqrt{\frac{3}{25}} = \frac{\sqrt{3}}{\sqrt{25}} = \frac{\sqrt{3}}{5}$

d.  $\sqrt{\frac{36}{5}} = \frac{\sqrt{36}}{\sqrt{5}} = \frac{6}{\sqrt{5}} \cdot \frac{\sqrt{5}}{\sqrt{5}} = \frac{6\sqrt{5}}{5}$

**Exercises for Example 1**

Simplify the expression.

1.  $\sqrt{60}$

2.  $\sqrt{2} \cdot \sqrt{18}$

3.  $\sqrt{\frac{81}{121}}$

**EXAMPLE 2****Solving a Quadratic Equation**

Solve  $\frac{x^2}{6} - 4 = 10$ .

**SOLUTION**

$$\frac{x^2}{6} - 4 = 10$$

Write original equation.

$$\frac{x^2}{6} = 14$$

Add 4 to each side.

$$x^2 = 84$$

Multiply both sides by 6.

$$x = \pm\sqrt{84}$$

Take square roots of both sides.

$$x = \pm 2\sqrt{21}$$

Simplify.

The solutions are  $2\sqrt{21}$  and  $-2\sqrt{21}$ .

LESSON  
**5.3**  
CONTINUED

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### Exercises for Example 2

Solve the equation.

4.  $4x^2 - 5 = -1$

5.  $12 - 2y^2 = 4$

6.  $\frac{p^2}{4} - 3 = 33$

### EXAMPLE 3 Solving a Quadratic Equation

Solve  $5(x - 7)^2 = 135$ .

$$5(x - 7)^2 = 135$$

Write original equation.

$$(x - 7)^2 = 27$$

Divide both sides by 5.

$$x - 7 = \pm\sqrt{27}$$

Take the square roots of both sides.

$$x - 7 = \pm 3\sqrt{3}$$

Simplify.

$$x = 7 \pm 3\sqrt{3}$$

Add 7 to both sides.

The solutions are  $7 + 3\sqrt{3}$  and  $7 - 3\sqrt{3}$ .

### Exercises for Example 3

Solve the equation.

7.  $(y + 3)^2 = 9$

8.  $(w - 1)^2 = 196$

9.  $-2(x - 3)^2 = -12$

10.  $(r - 8)^2 = 50$

11.  $5(x - 3)^2 = 50$

12.  $\frac{1}{3}(z + 3)^2 = 5$

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### EXAMPLE 4 Modeling a Falling Object's Height with a Quadratic Function

A person is trapped in a building 120 feet above the ground and wants to land on a rescue team's air cushion. How long before the person reaches safety?

#### SOLUTION

Use the falling object model  $h = -16t^2 + h_0$ , where  $h$  is the height (in feet) of the object after  $t$  seconds and  $h_0$  is the object's initial height.

$$\begin{array}{ll} 0 = -16t^2 + 120 & \text{Substitute 120 for } h_0 \text{ and 0 for } h. \\ -120 = -16t^2 & \text{Subtract 120 from each side.} \end{array}$$

$$\frac{120}{16} = t^2 \quad \text{Divide each side by } -16.$$

$$\sqrt{\frac{120}{16}} = t \quad \text{Take positive square root.}$$

$$2.7 \approx t \quad \text{Use a calculator.}$$

The person will reach safety in about 2.7 seconds.

#### Exercises for Example 4

13. A coyote is standing on a cliff 254 feet above a roadrunner. If the coyote drops a boulder from the cliff, how much time does the roadrunner have to move out of its way?

14. An apple falls from a branch on a tree 30 feet above a man sleeping underneath. When will the apple strike the man?