## Combinatorial Information Distance\*

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## Abstract

Let |A| denote the cardinality of a finite set A. For any real number x define t(x)=x if  $x\geq 1$  and 1 otherwise. For any finite sets A,B let  $\delta(A,B)=\log_2\big(t\left(\left|B\cap\overline{A}\right||A|\right)\big)$ . We define a new cobinatorial distance  $d(A,B)=\max\big\{\delta\left(A,B\right),\delta\left(B,A\right)\big\}$  which may be applied to measure the distance between binary strings of different lengths. The distance is based on a classical combinatorial notion of information introduced by Kolmogorov.

Keywords: Set distance, Lempel-Ziv complexity, Combinatorial entropy, Set entropy, Binary sequences

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