

# Mock Set 1 Paper 02 Calculator — Solutions

Foundation Tier — Total Marks: 80

Time allowed: 1 hour and 30 minutes

# Instructions

This document provides worked solutions to all questions from the mock paper. Use this for revision and checking your methods.

## **Solutions**

## Question 1

#### Answer

4, 6

## Explanation

A factor divides the number exactly.

Factors of 24 are 1, 2, 3, 4, 6, 8, 12, 24.

Any two of these are acceptable (e.g., 4 and 6).

## Question 2

## Answer

 $\frac{4}{5}$ 

## ${\bf Explanation}$

$$0.8 = \frac{8}{10}$$

Simplify by dividing top and bottom by 2:  $\frac{8}{10} = \frac{4}{5}$ .

## Question 3

## Answer

 $450~\mathrm{cm}$ 

#### Explanation

 $1~\mathrm{metre} = 100~\mathrm{cm}$ 

 $4.5 \text{ metres} = 4.5 \times 100 = 450 \text{ cm}$ 

Answer

25

Explanation

Square numbers are:  $1, 4, 9, 16, 25, 36, 49, \dots$ 

Between 10 and 50, we have 16, 25, 36, 49.

One example is 25.

## Question 5

Answer

120

Explanation

$$50\% = \frac{50}{100} = \frac{1}{2}$$

 $Half \ of \ 240 = 120$ 

## Question 6

Answer

£12

Explanation

Total pay = 48, total hours = 4

Pay per hour  $=\frac{48}{4}=12$ 

## ${\bf Question}~7$

## Question 7(a)

#### Answer

Cylinder

## Explanation

This shape has two equal circular faces and one curved surface, which makes it a cylinder.

## Question 7(b)

#### Answer

Sketch of a rectangular prism

## Explanation

Draw a 3D shape with 6 rectangular faces, opposite faces equal in size.

## Question 8

## Answer

Yes

#### Explanation

Footballs:  $4 \times £8.50 = £34$ 

Hockey sticks: 6 sticks = 3 packs at £24 = £72

Cricket bats:  $3 \times £21 = £63$ Tennis balls: £6 for 6 = £6

Total = £(34 + 72 + 63 + 6) = £ $175 \le$  £ $180 \Rightarrow$  Yes, he can buy everything.

#### Answer

RP, RS, RC, BP, BS, BC, GP, GS, GC

## Explanation

Shirts: Red (R), Blue (B), Green (G)

Ties: Plain (P), Striped (S), Checked (C)

List all combinations:

RP, RS, RC, BP, BS, BC, GP, GS, GC

#### Question 10

## Answer

5:7

## Explanation

Number of green marbles = 35, Number of yellow marbles = 49.

Ratio (green: yellow) = 35:49.

Divide both numbers by their greatest common divisor (GCD) which is 7:

 $35 \div 7 = 5$ ,  $49 \div 7 = 7$ .

 $\therefore$  Simplest form is 5:7.

## Question 11

## Question 11(a)

#### Answer

unlikely

#### Explanation

 $P(\text{picking an Ace}) = \frac{4}{52} = \frac{1}{13}$ , which is small, so 'unlikely'.

## Question 11(b)

#### Answer

evens

#### Explanation

 $P(\text{picking a red card}) = \frac{26}{52} = \frac{1}{2}, \text{ so 'evens'}.$ 

## Question 12

## Answer

 $216~\mathrm{km}$ 

## Explanation

 $\mathrm{Distance} = \mathrm{Speed} \times \mathrm{Time}$ 

$$=72\times3=216~\mathrm{km}$$

## Question 13

## Question 13(a)

#### Answer

She multiplied each dimension twice instead of once; correct area is  $7 \times 3 = 21 \text{ cm}^2$ .

## Explanation

Area =  $7 \times 3 = 21 \text{ cm}^2$ , not  $7 \times 3 \times 7 \times 3$ .

## Question 13(b)

#### Answer

Area should be in  $cm^2$ , not cm.

## Explanation

Area is measured in square units;  $42~\mathrm{cm}$  is a length, not an area.

#### Answer

£7.90

#### Explanation

Let rice cost per kg = r, beans cost per kg = b.

$$4r = 5.60 \Rightarrow r = 1.40$$
.

$$3r + 7b = 10.15 \Rightarrow 4.20 + 7b = 10.15 \Rightarrow 7b = 5.95 \Rightarrow b = 0.85.$$

$$2r + 6b = 2(1.40) + 6(0.85) = 2.80 + 5.10 = 7.90.$$

#### Question 15

#### Answer

£56.40

#### Explanation

Liam gets 65% of £120 =  $0.65 \times 120 = 78$ .

He spends 28% of £78 =  $0.28 \times 78 = 21.84$ .

Money left = 78 - 21.84 = 56.40.

#### Question 16

## Answer

23

## Explanation

Total people = 150. Children =  $64 \Rightarrow \text{Adults} = 86$ .

Football total = 28: children  $12 \Rightarrow$  adults 16.

Basketball total = 70: adults  $41 \Rightarrow$  children 29.

Let children choosing tennis = x. Adults choosing tennis = 9.

Given: children choosing tennis = adults choosing rugby (y), so x = y.

Rugby total = 150 - 28 - 70 - (9 + x) = 43 - x.

Children total:  $12 + 29 + x + ((43 - x) - y) = 64 \Rightarrow 84 - y = 64 \Rightarrow y = 20$ .

Hence x = 20, Rugby total = 43 - x = 23.

## Question 17a

#### Question 18

## Answer

(a) 
$$\frac{12.5 + 7.3}{5.4 \times 3.2} = \frac{19.8}{17.28} \approx 1.1458333333$$

(b) To 2 decimal places: 1.15

#### Explanation

Numerator: 12.5 + 7.3 = 19.8. Denominator:  $5.4 \times 3.2 = 17.28$ .

Division:  $19.8 \div 17.28 \approx 1.1458333333$ .

Rounded to 2 d.p.: 1.15.

#### Question 19

#### Answer

 $115^{\circ}$ 

## ${\bf Explanation}$

Since  $DE \parallel AC$  and CD is a transversal, the interior angles on the same side are supplementary.  $x + 65^{\circ} = 180^{\circ} \implies x = 115^{\circ}$ .

#### Answer

(3,0) and sketch a smooth curve.

Plot 
$$(-2,5),(-1,0),(0,-3),(1,-4),(2,-1)$$

## Explanation

Use  $y = x^2 - 2x - 3$ . Compute for each x:

$$x = -2: 4 + 4 - 3 = 5.$$
  $x = -1: 1 + 2 - 3 = 0.$   $x = 0: 0 - 0 - 3 = -3.$ 

$$x = 1: 1 - 2 - 3 = -4.$$
  $x = 2: 4 - 4 - 3 = -3.$   $x = 3: 9 - 6 - 3 = 0.$ 

Plot the points and join with a smooth U-shaped curve.

#### Question 21

#### Answer

Reflection in the line y = x.

#### Explanation

Triangles A and B are congruent, so the transformation is isometric.

Their orientation is reversed, so it is not a translation or rotation of 180°.

Checking corresponding vertices shows  $(a, b) \mapsto (b, a)$ , so each point is mirrored across y = x.

 $\therefore$  the single transformation is a reflection in the line y = x.

#### Question 22

#### Question 22(a)

#### Answer

9a + 11

#### Explanation

$$4(a+3) = 4a + 12, \quad 5(a-1) = 5a - 5,$$

$$4a + 12 + 5a - 5 = 9a + 7.$$

Question 22(b)

Answer

7y(y-6)

Explanation

HCF of  $14y^2$  and 42y is 7y,

$$14y^2 - 42y = 7y(y - 6).$$

Question 22(c)

Answer

$$\frac{q+8}{5}$$

Explanation

$$q=5p-8 \Rightarrow q+8=5p \Rightarrow p=\frac{q+8}{5}.$$

## Question 23

Answer

32

Explanation

Total cost = 85 + 150 + 95 = 330.

Tickets sold =  $60 \times 7.25 = 435$ .

Profit = 435 - 330 = 105.

Percentage profit =  $\frac{105}{330} \times 100 \approx 31.82\%$  (32% to the nearest whole number).

## Answer

 $\pounds 5310.74$ 

## Explanation

 $Principal = 5000, \ Rate = 3.05\% = 0.0305, \ Time = 2 \ years.$ 

Amount =  $5000 \times (1 + 0.0305)^2$ 

- $=5000 \times (1.0305)^2$
- $=5000\times1.062148025$
- = 5310.74.

## Question 25

## Answer

8

## Explanation

$$7y - 10 = 38 - y$$

$$7y + y - 10 = 38$$

$$8y - 10 = 38$$

$$8y = 38 + 10$$

$$8y = 48$$

$$y = 8$$

#### Answer

£18

#### Explanation

Initial ratio: 5:3:4, Ben's share =3k = ninety

k = 30.

Alex: 5k = 150, Ben: 90, Carl: 4k = 120.

Final ratio: 4:5:3, let multiplier be m.

Alex: 4m, Ben: 5m, Carl: 3m.

Total initially: 150 + 90 + 120 = 360, total finally: 12m.

 $12m = 360 \Rightarrow m = 30.$ 

Final shares: Alex: 120, Ben: 150, Carl: 90.

Carl had initially 120, now 90, so he gave away 30. Of this, Alex's loss is 150 - 120 = 30, so all of Carl's loss went to

Actually, Ben had 90, now 150, so gained 60. Alex had 150, now 120, so lost 30. The remaining 30 gained by Ben car

Carl gave to Ben: 18

#### Question 27

## Answer

 $065^{\circ}$ 

#### Explanation

Bearings are measured clockwise from north.

If the bearing from X to Y is  $245^{\circ}$ ,

then the bearing from Y to X is  $245^{\circ} + 180^{\circ} = 425^{\circ}$ .

Since this is greater than  $360^{\circ}$ , subtract  $360^{\circ} \Rightarrow 065^{\circ}$ .

#### Answer

85

## Explanation

Volume of cylinder  $V = \pi r^2 h = \pi (18)^2 (50) = \pi \cdot 324 \cdot 50 = \pi \cdot 16200$ 

 $V \approx 50893.8 \text{ cm}^3 = 50.8938 \text{ L} \quad (1 \text{ L} = 1000 \text{ cm}^3).$ 

 $\mathrm{Time} = \frac{50.8938}{0.60} = 84.823\dots \ \mathrm{minutes} \ \Rightarrow \ \boxed{85 \ \mathrm{minutes}} \ \mathrm{(nearest \ minute)}.$ 

#### Question 29

#### Answer

 $14.3~\mathrm{cm}$ 

## Explanation

In right-angled  $\triangle ABC$ ,  $\angle C=37^{\circ}$  and the side adjacent to  $\angle C$  is BC=19 cm.

$$\tan(37^{\circ}) = \frac{\text{opposite}}{\text{adjacent}} = \frac{AB}{19}.$$

 $AB = 19 \tan(37^{\circ}) \approx 19 \times 0.7536 = 14.317...$  cm.

To 3 s.f.: 14.3 cm.

## Question 30

## Answer

$$x = 2, y = -1$$

## Explanation

$$2x + y = 3 \quad (1)$$

$$5x + 3y = 7 \quad (2)$$

Multiply (1) by 3: 
$$6x + 3y = 9$$
 (3)

$$(3) - (2): \quad (6x - 5x) + (3y - 3y) = 9 - 7$$

x = 2

Substitute into (1): 2(2) + y = 3

 $4 + y = 3 \quad \Rightarrow \quad y = -1$