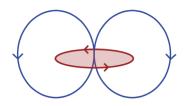
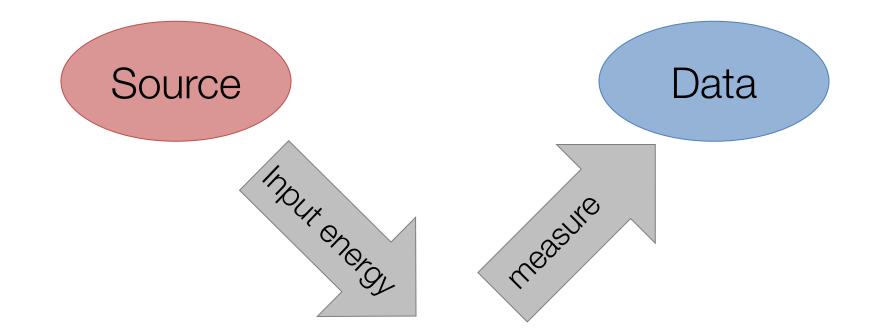
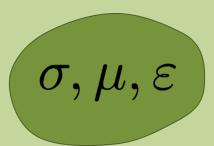
EM Induction



EM Survey & Physical Properties

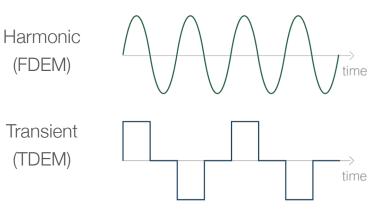


Physical Properties

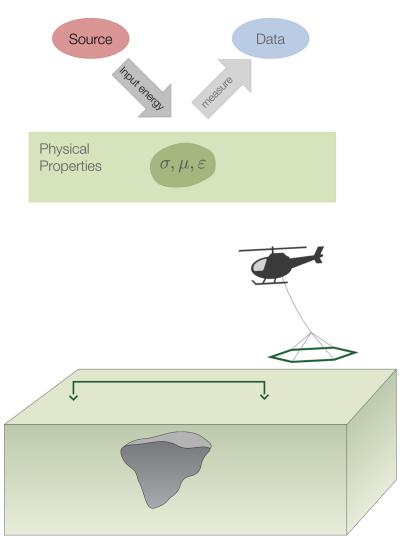


Electromagnetic Survey: Sources

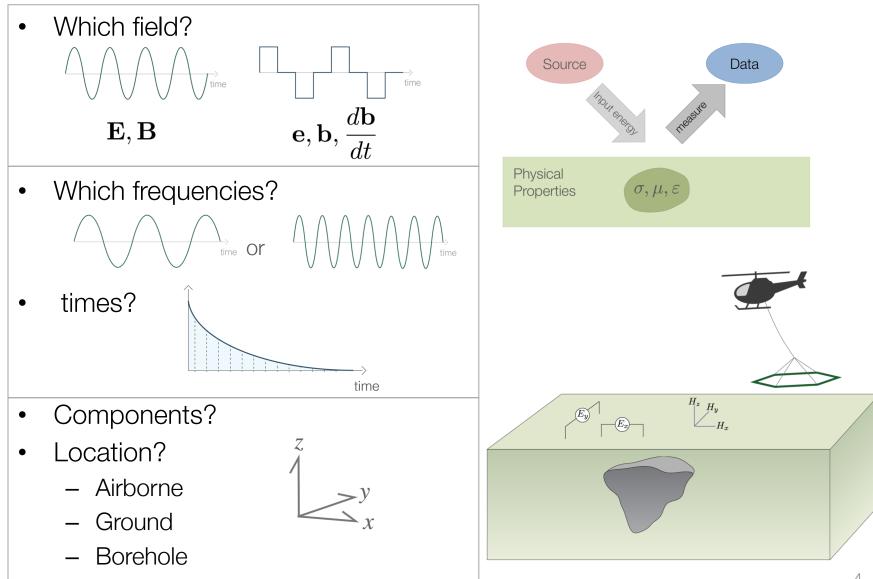
- Type
 - Inductive
 - Grounded
- Waveform



- Location
 - Airborne
 - Ground
 - Borehole



Electromagnetic Survey: Data

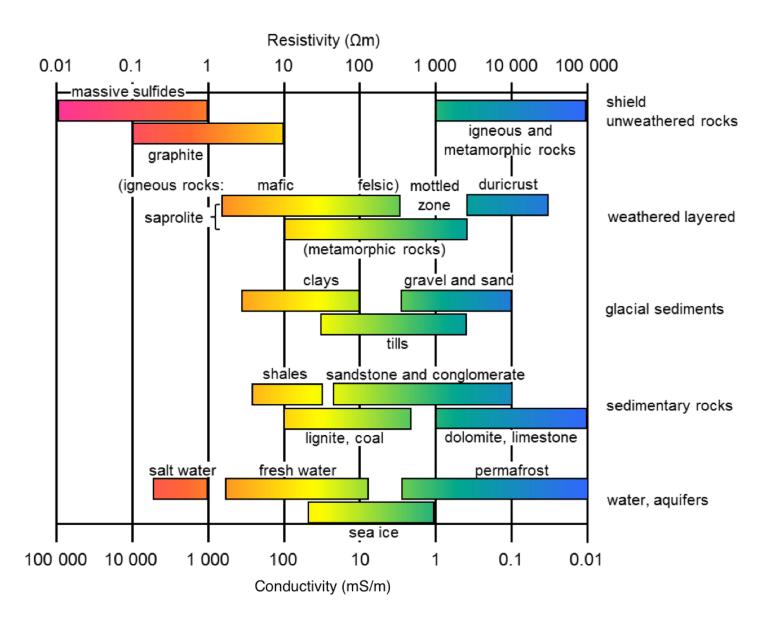


Basic Equations

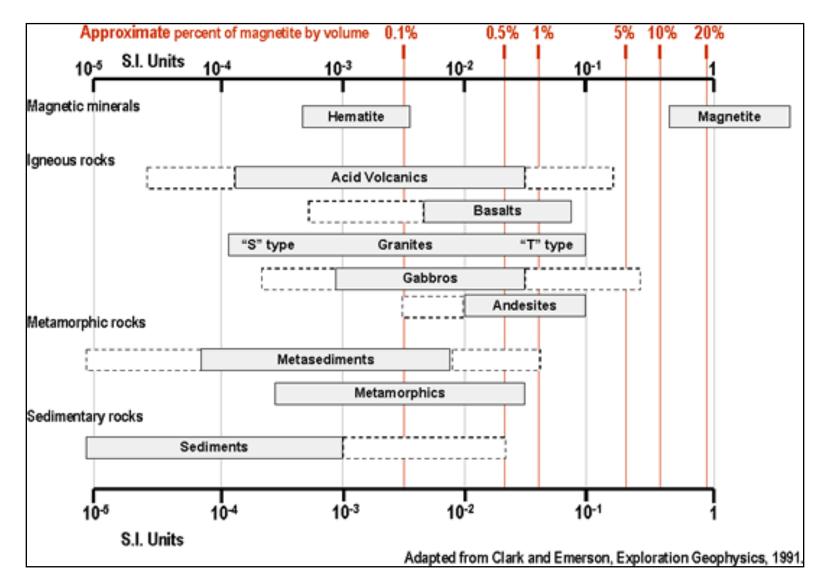
	Time	Frequency FDEM
Faraday's Law	$\nabla \times \mathbf{e} = -\frac{\partial \mathbf{b}}{\partial t}$	$ abla imes \mathbf{E} = -i\omega \mathbf{B}$
Ampere's Law	$ abla imes \mathbf{h} = \mathbf{j} + \frac{\partial \mathbf{d}}{\partial t}$	$ abla imes \mathbf{H} = \mathbf{J} + i\omega \mathbf{D}$
No Magnetic Monopoles	$\nabla \cdot \mathbf{b} = 0$	$\nabla \cdot \mathbf{B} = 0$
Constitutive Relationships	$\mathbf{j} = \sigma \mathbf{e}$	$\mathbf{J} = \sigma \mathbf{E}$
	$\mathbf{b}=\mu\mathbf{h}$	${f B}=\mu {f H}$
(non-dispersive)	$\mathbf{d} = \varepsilon \mathbf{e}$	$\mathbf{D} = arepsilon \mathbf{E}$

* Solve with sources and boundary conditions

Electrical Resistivity / Conductivity



Magnetic Susceptibility



Dielectric constant

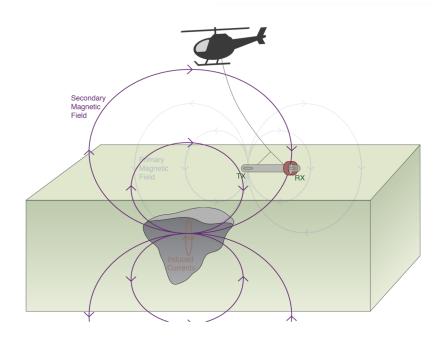
Material	Relative Permittivity	Conductivity (mS/m)	Average Velocity (m/ns)
Air	1	0	3
Fresh Water	80	0.5	0.033
Sea Water	80	3000	0.01
Ice	3-4	0.01	0.16
Dry Sand	3-5	0.01	0.15
Saturated Sand	20-30	0.1-1	0.06
Limestone	4-8	0.5-2	0.12
Shales	5-15	1-100	0.09
Silts	5-30	1-100	0.07
Clays	5-40	2-1000	0.06
Granite	4-6	0.01-1	0.13
Anhydrites	3-4	0.01-1	0.13

Quasi-static

	Time	Frequency FDEM
Faraday's Law	$\nabla \times \mathbf{e} = -\frac{\partial \mathbf{b}}{\partial t}$	$ abla imes \mathbf{E} = -i\omega \mathbf{B}$
Ampere's Law	$ abla imes \mathbf{h} = \mathbf{j} + rac{\partial \mathbf{d}}{\partial t}$	$ abla imes \mathbf{H} = \mathbf{J} + i\omega \mathbf{D}$
No Magnetic Monopoles	$\nabla \cdot \mathbf{b} = 0$	$\nabla \cdot \mathbf{B} = 0$
Constitutive Relationships (non-dispersive)	$\mathbf{j} = \sigma \mathbf{e}$	$\mathbf{J}=\sigma\mathbf{E}$
	$\mathbf{b} = \mu \mathbf{h}$	${f B}=\mu {f H}$
	$\mathbf{d} = \varepsilon \mathbf{e}$	$\mathbf{D} = arepsilon \mathbf{E}$

Basic Experiment

waveform

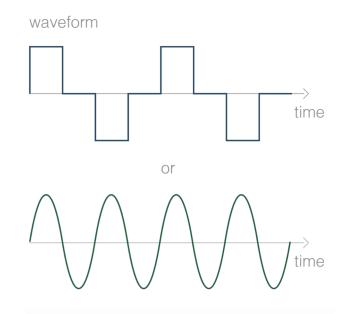


• Transmitter:

- Produces a primary magnetic field
- Exciting the target:
 - Time varying magnetic fields generate electric fields everywhere
 - Producing currents in conductors
- Receiver:
 - Induced currents produce secondary magnetic fields

Frequency vs time

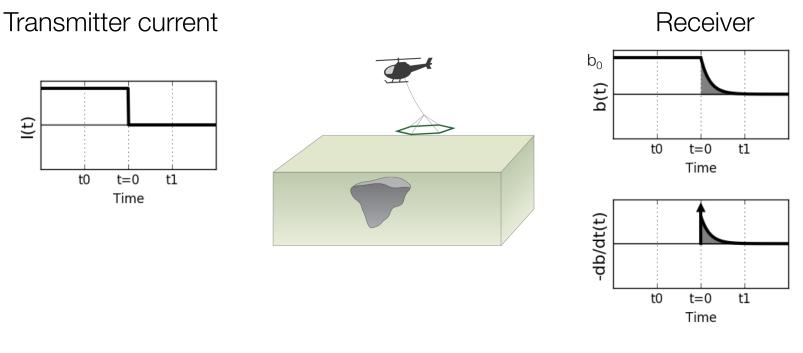
- Same physics
- Time domain is more intuitive for understanding the physics.



Outline

- TDEM: Currents and sounding curves for 1D earth
- Overview of inverse problem
- 1D inversion using SimPEG
- Effects of a background conductivity
- Conductive sphere in a halfspace
- 1D vs 3D inversions
- Examples where 3D inversion required?
- Frequency domain
- Summary

EM with Inductive Sources: Time Domain



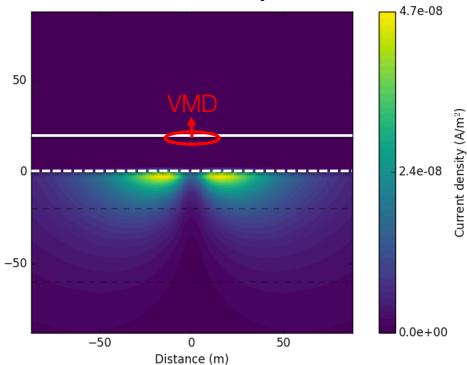
time	b	db/dt
t < 0	b_0	0
t = 0	b_0	$-b_0\delta(t)$
t > 0	secondary	secondary

 $\delta(t)$: Dirac-delta function

Footprint of Airborne EM system

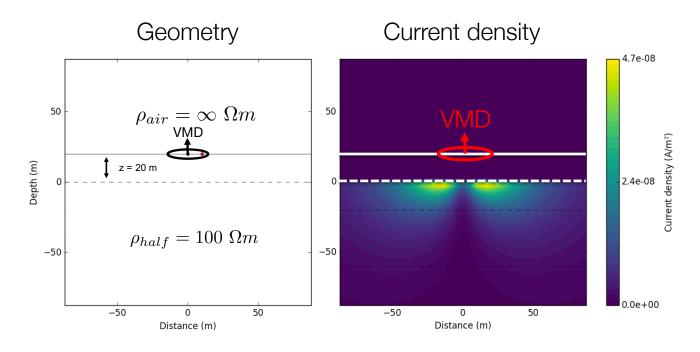
Depth (m)

- What volume of earth is "seen" by the airborne system?
 - Where are the currents?
- Currents depend on
 - Transmitter
 - Waveform: time or frequency
 - Background conductivity
- Simple case: loop source over homogeneous earth



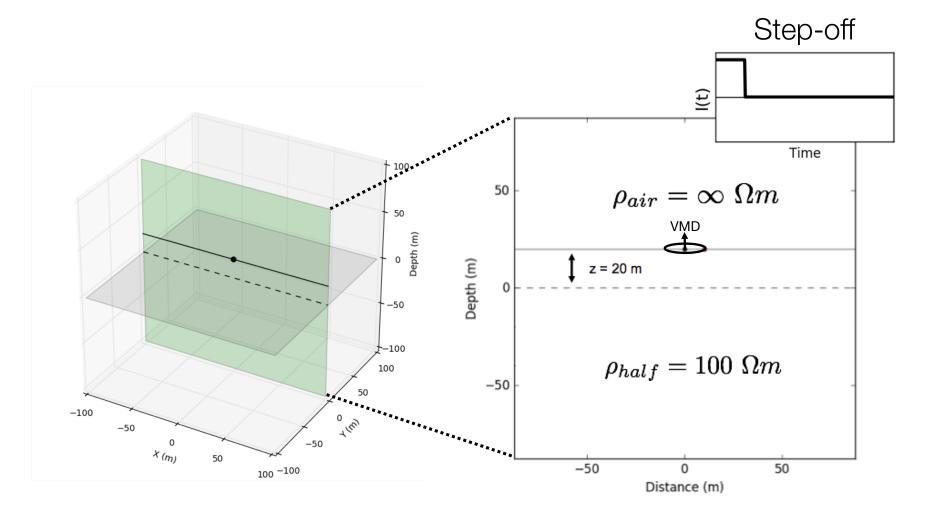
Current density

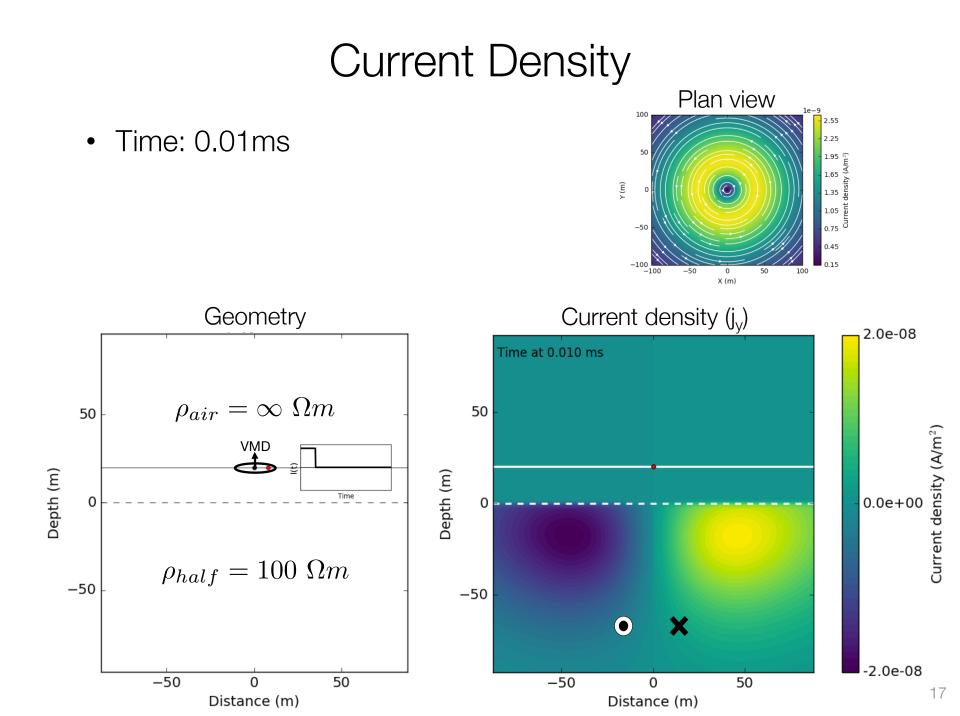
Vertical Magnetic Dipole (VMD)



- Some questions
 - Where, and how strong, are the currents?
 - How do they depend upon the conductivity?
 - What do the resulting magnetic fields look like?

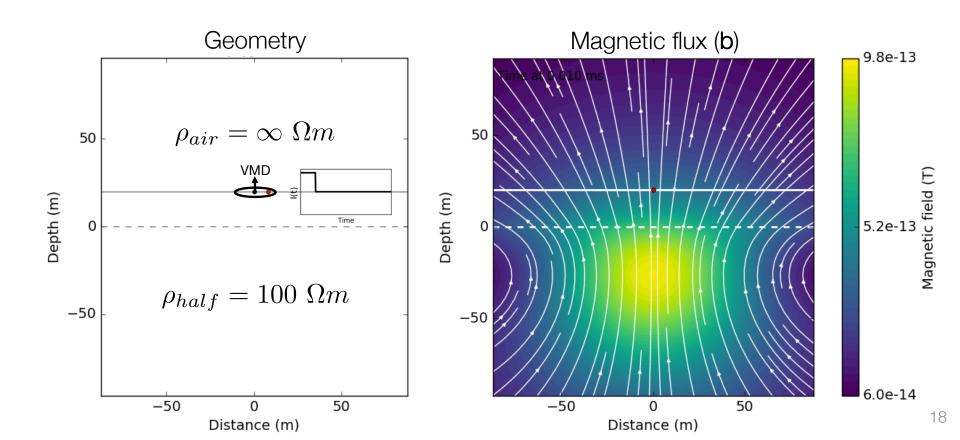
Vertical Magnetic Dipole over a halfspace (TDEM)





Magnetic flux density

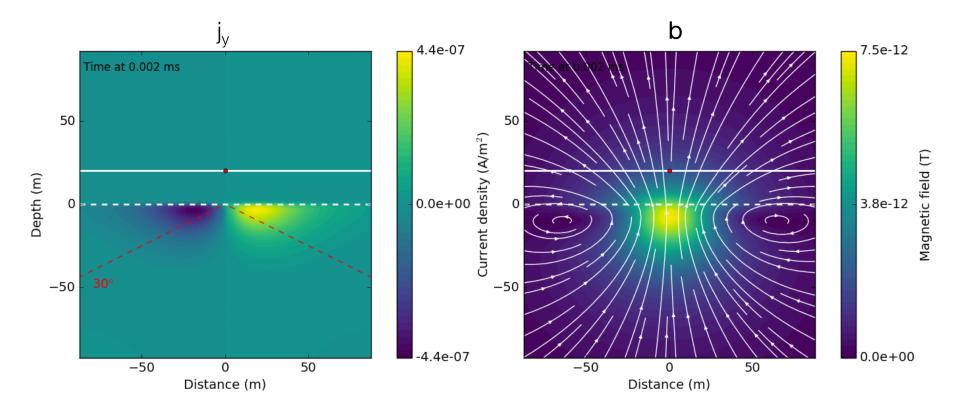
• Time: 0.01ms



• Time: 0.002ms

 $d = 1260 \sqrt{t\rho}$

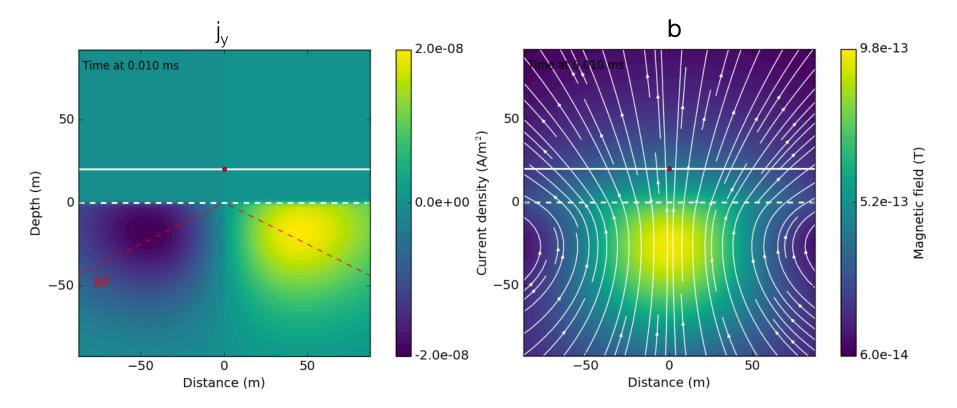
diffusion distance = 18 m



• Time: 0.01ms

$$d = 1260\sqrt{t\rho}$$

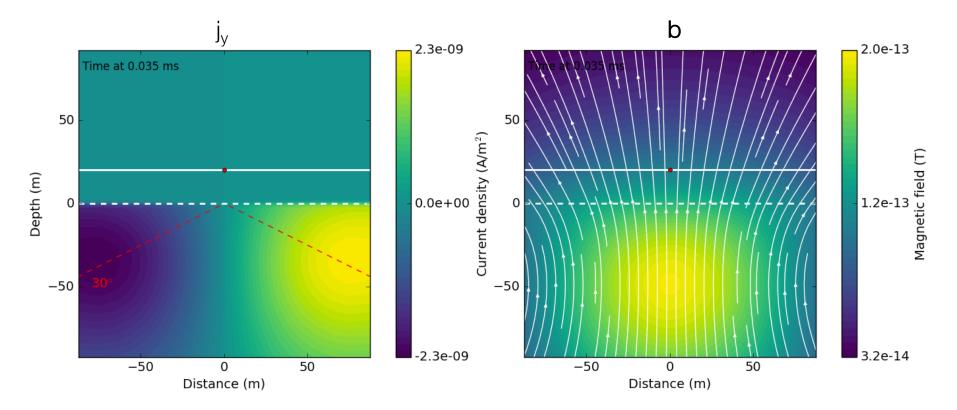
• diffusion distance = 38 m



• Time: 0.035ms

 $d = 1260\sqrt{t\rho}$

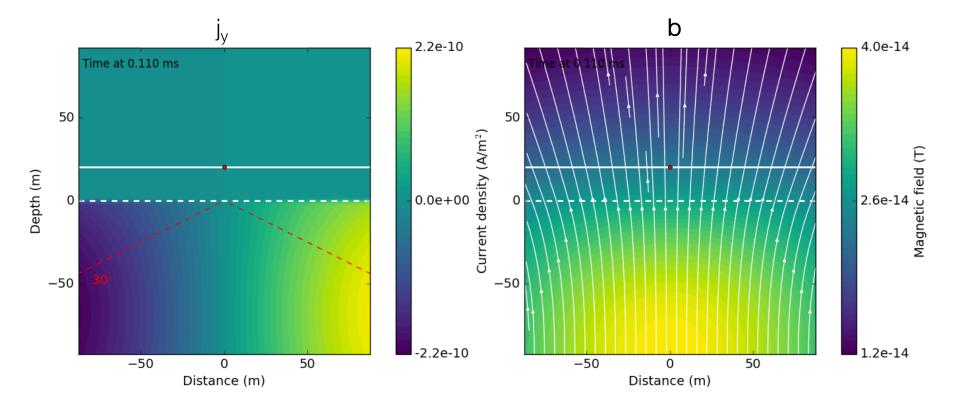
• diffusion distance = 75 m



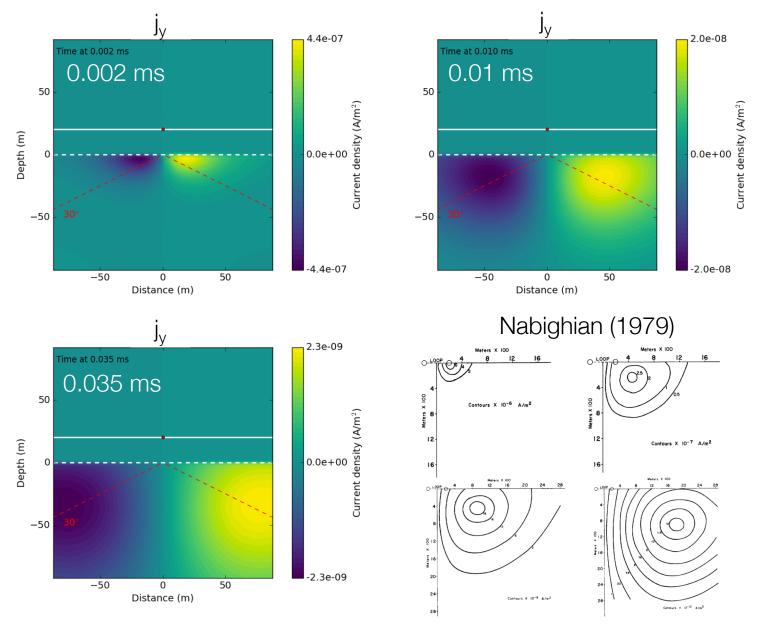
• Time: 0.110ms

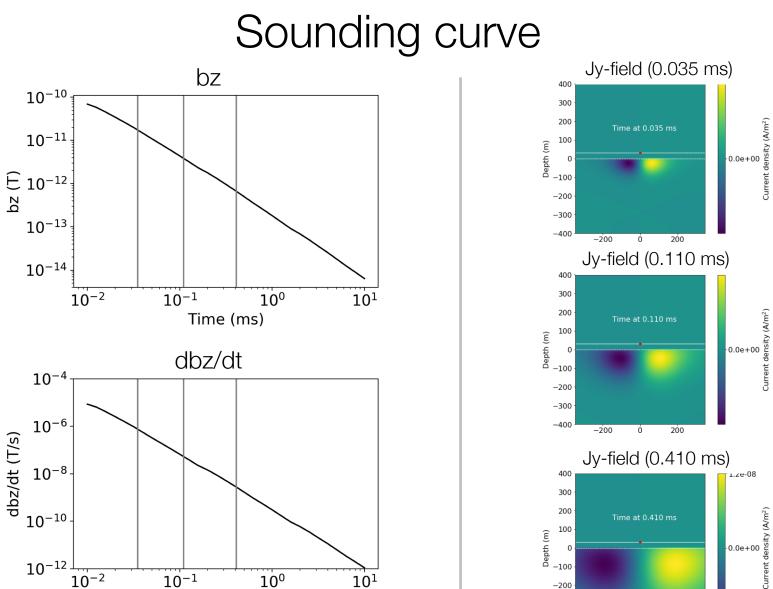
 $d=1260\sqrt{t\rho}$

diffusion distance = 132 m



Summary: propagation through time





Time (ms)

-300

-400

-200

200

0 Distance (m)

Important points

- Currents flow in same plane as transmitter currents
- Currents diffuse outward downward
- Each transmitter has a "footprint"
- Max resolution controlled by earliest time
- Depth of investigation controlled by latest time

magnetic field (on-time) 1.7e-08 50 Magnetic field (T) Depth (m) 8.6e-09 -50 50 -50 Distance (m) 4.4e-07 me at 0.002 ms 50 Current density (A/m²) Depth (m) 0.0e+00 -50 .**4e-07** -500 50

Distance (m)

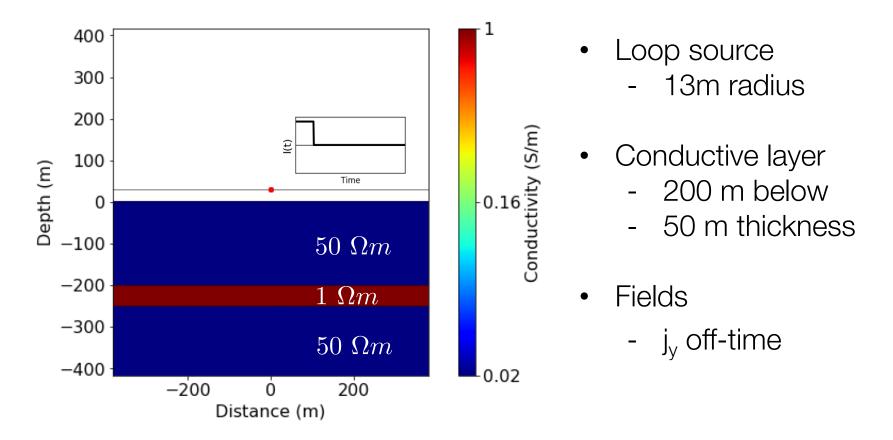
Important points

- Currents flow in same plane as transmitter currents
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- Max resolution controlled by earliest time
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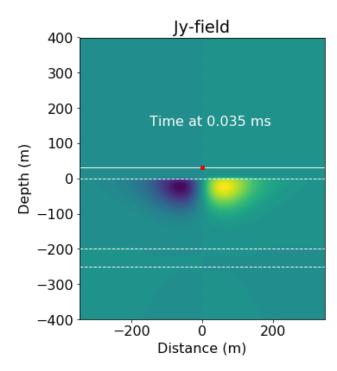
magnetic field (on-time) 1.7e-08 50 Magnetic field (T) Depth (m) 8.6e-09 -50 50 -50 Distance (m) 2.3e-09 me at 0.035 ms 50 Current density (A/m²) Depth (m) 0.0e+00 -50.3e-09 -500 50

Distance (m)

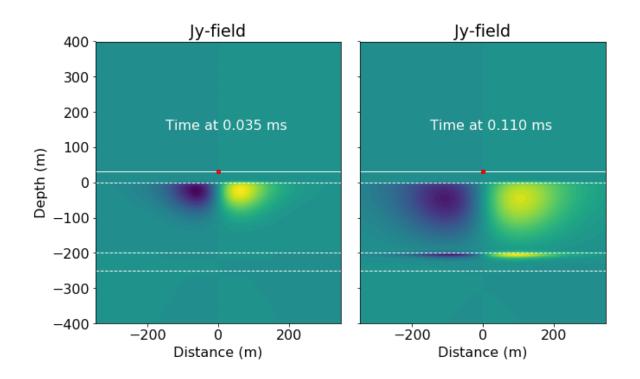
Conductive layer in a halfspace



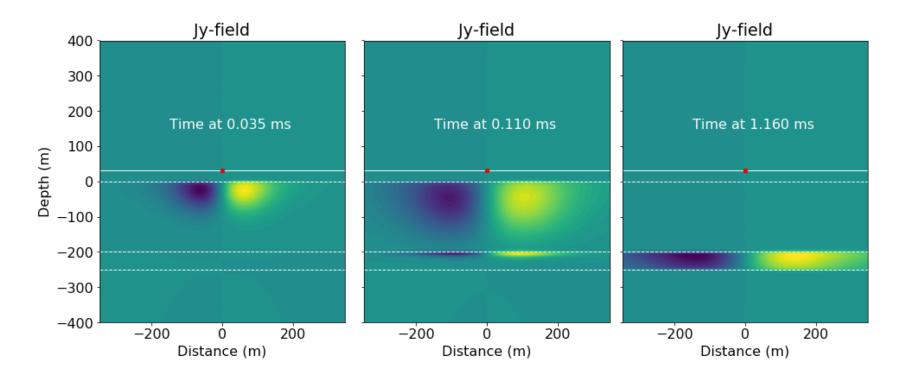
Layered earth currents (j_v)



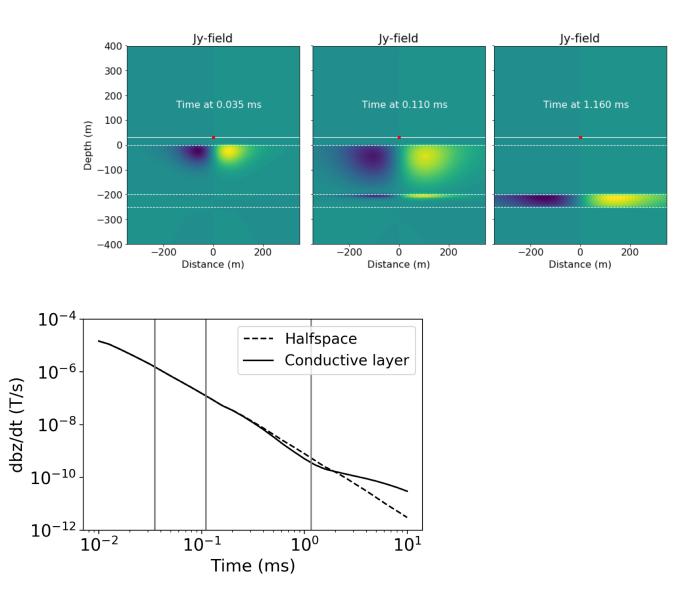
Layered earth currents (j_v)



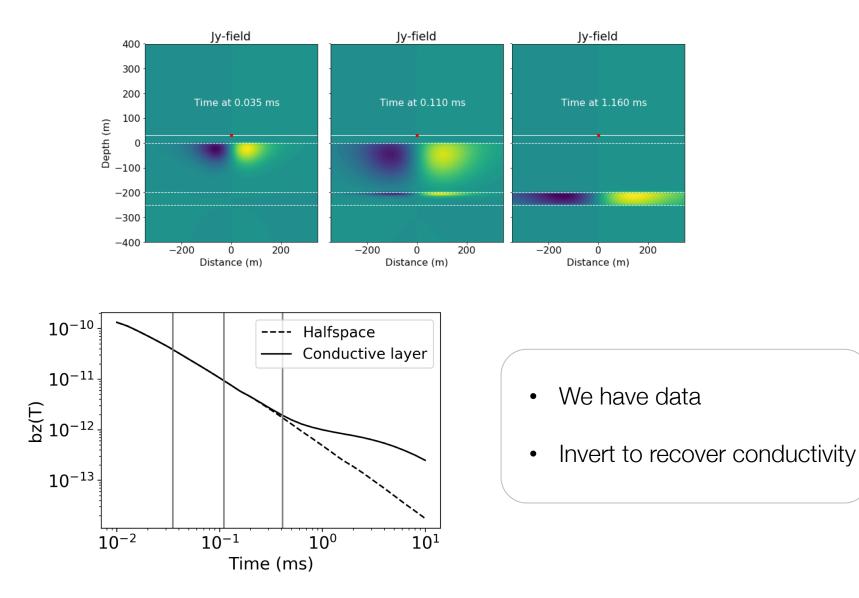
Layered earth currents (j_y)



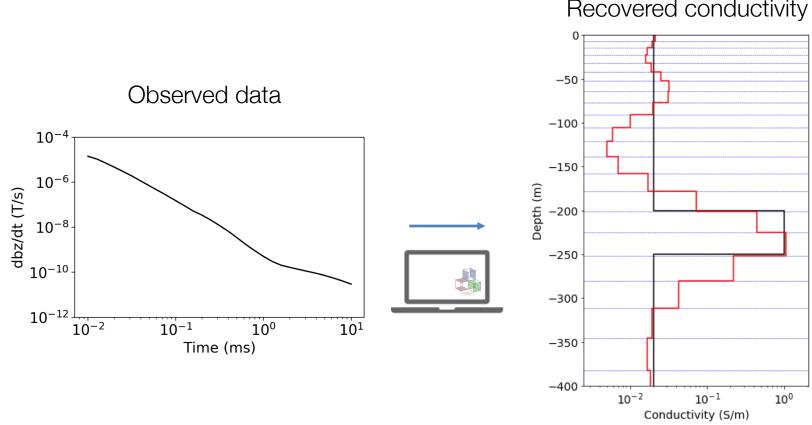
Sounding curve (bz)



Sounding curve (dbz/dt)

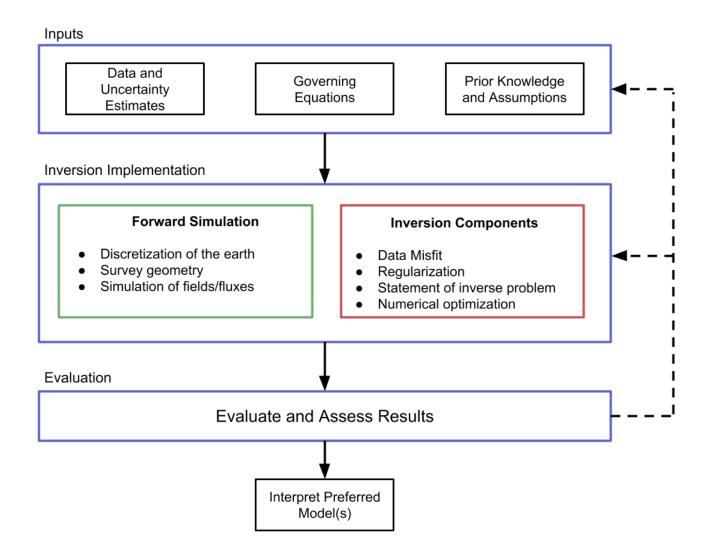


Inversion



Recovered conductivity

Inversion flow chart



Inverse problem

• Minimize

$$\phi(\mathbf{m}) = \phi_d(\mathbf{m}) + \beta \phi_m(\mathbf{m})$$

subject to $\mathbf{m}_{lower} < \mathbf{m} < \mathbf{m}_{upper}$

Data misfit

$$\phi_d(\mathbf{m}) = \frac{1}{2} ||\mathbf{W}_d(F[\mathbf{m}] - \mathbf{d}_{obs})||_2^2.$$
Regularization

$$\phi_m(\mathbf{m}) = \frac{1}{2} ||\mathbf{W}_m(\mathbf{m} - \mathbf{m}_{ref})||_2^2.$$
Tikhonov curve

 ϕ_m

Regularization and a-priori information

$$\phi_m(\mathbf{m}) = \frac{1}{2} \|\mathbf{W}_m(\mathbf{m} - \mathbf{m}_{ref})\|_2^2.$$

Inversion Parameters: (model)

- conductivities 1D, 2D, or 3D
- linear or log

. . .

- geometrical parameters

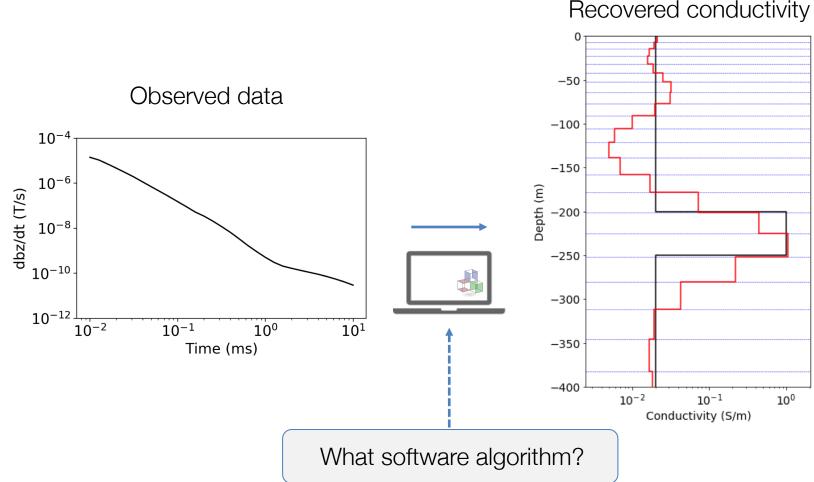
- Smallness
- Smoothness
- Cell weight
- Face weight

..

Reference model Norms

- L_p: 0<p<2
- L2 (smooth)
- L0 (sparse)

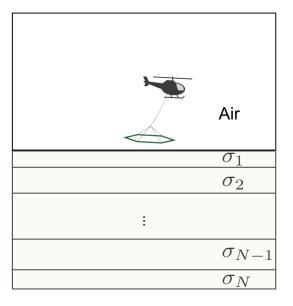
Inversion



Recovered conductivity

SimPEG-EM1D inversion code

Layered conductivity



- Pseudo-analytic solution
 - Similar to UBC EM1DFM and EM1DTM
- Multiple sources
 - ~100,000 sources
- 1D inversion for each sounding

AEM data -5.1e-03 -4.5e-03 -3.9e-03 -3.3e-03 -2.7e-03

- Spatial constraint
 - Ask for horizontally smooth model
 - Use Delaunay triangulation
 - Similar to AarhusInv
- Effective tool to invert large scale AEM data

-2.1e-03

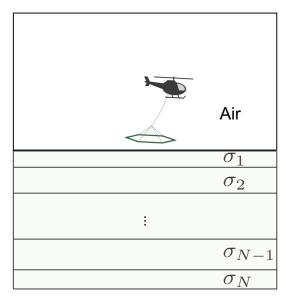
-1.5e-03

- 9.0e-04

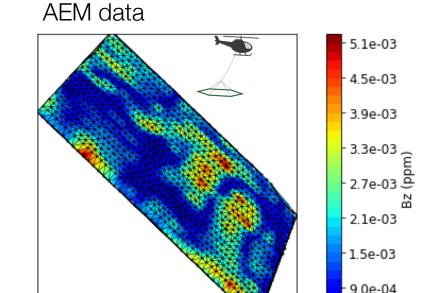
3.0e-04

SimPEG-EM1D inversion code

Layered conductivity



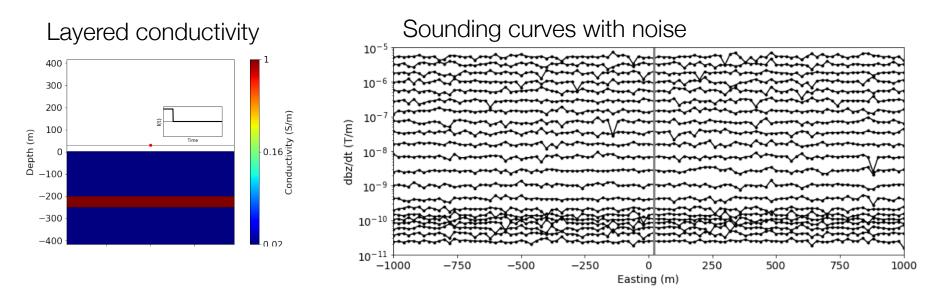
- Pseudo-analytic solution
 - Similar to UBC EM1DFM and EM1DTM
- Multiple sources
 - ~100, 000 sources
- 1D inversion for each sounding



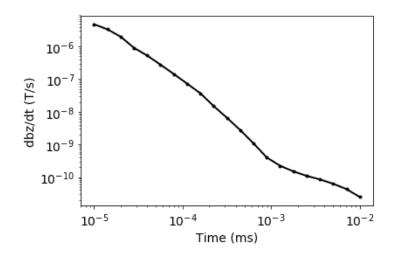
- Spatial constraint
 - Ask for horizontally smooth model
 - Use Delaunay triangulation
 - Similar to AarhusInv
- Effective tool to invert large scale AEM data

3.0e-04

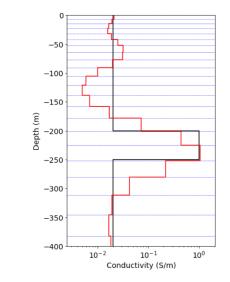
Layered Earth: 1D inversion



Observed data at a single sounding

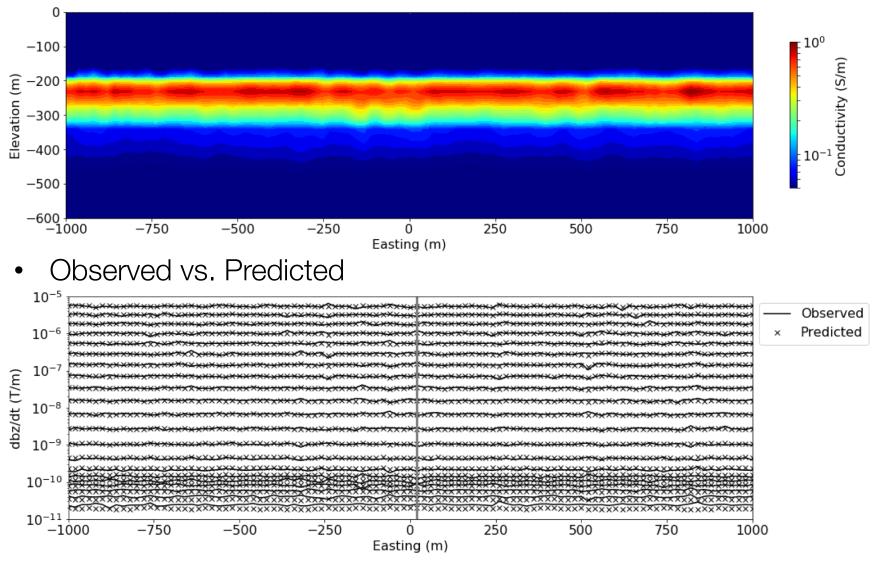


Recovered conductivity



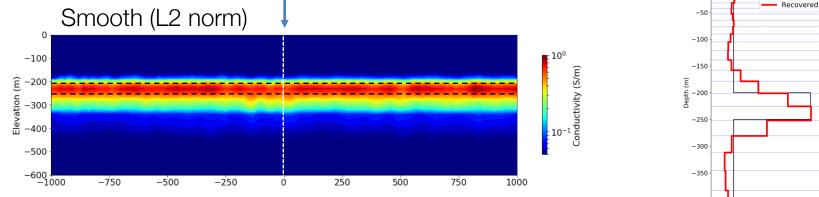
1D inversion

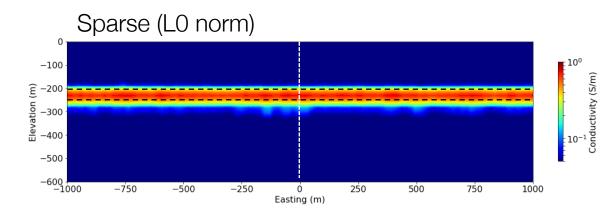


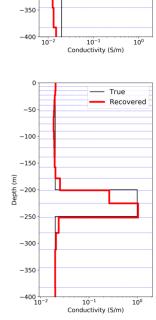


Different regularization function

$$\phi_m(\mathbf{m}) = \frac{1}{2} \|\mathbf{W}_m(\mathbf{m} - \mathbf{m}_{ref})\|_2^2 \longleftarrow$$

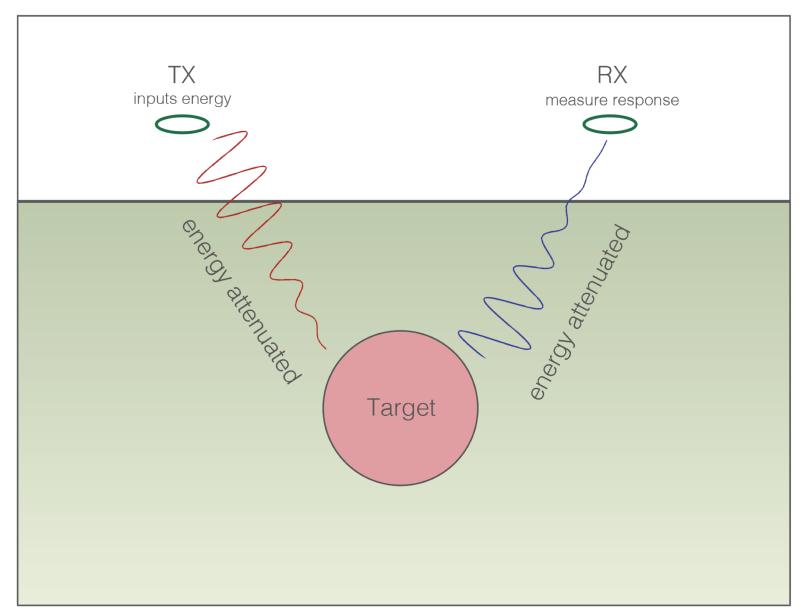






True

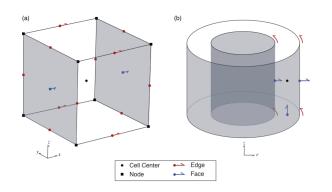
EM effects with 3D structure: Conductive sphere



Cyl Code

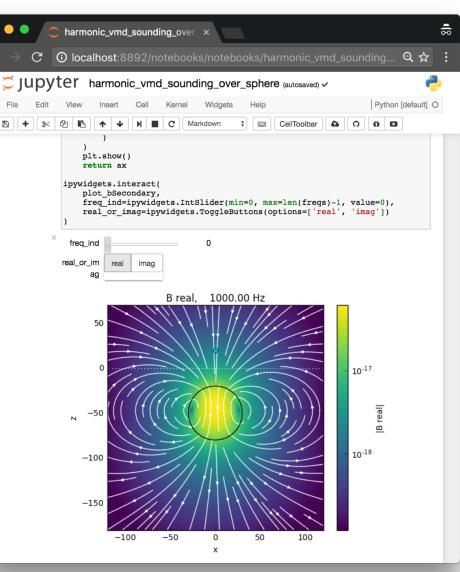


- Finite Volume EM
 - Frequency and Time

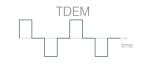


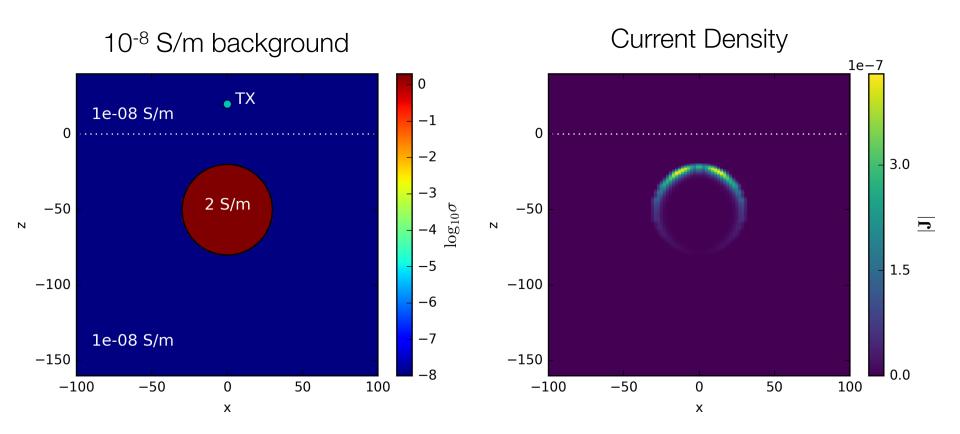
- Built on SimPEG
- Open source, available at: <u>http://em.geosci.xyz/apps.html</u>
- Papers Cockett et al, 2015

Heagy et al, 2017

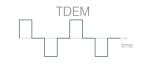


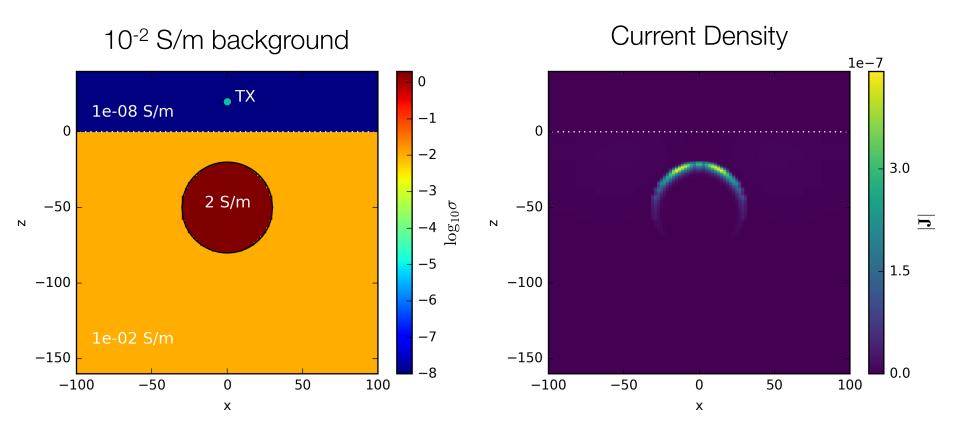
- Buried, conductive sphere
- Vary background conductivity
- Time: 10⁻⁵ s



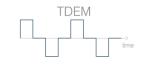


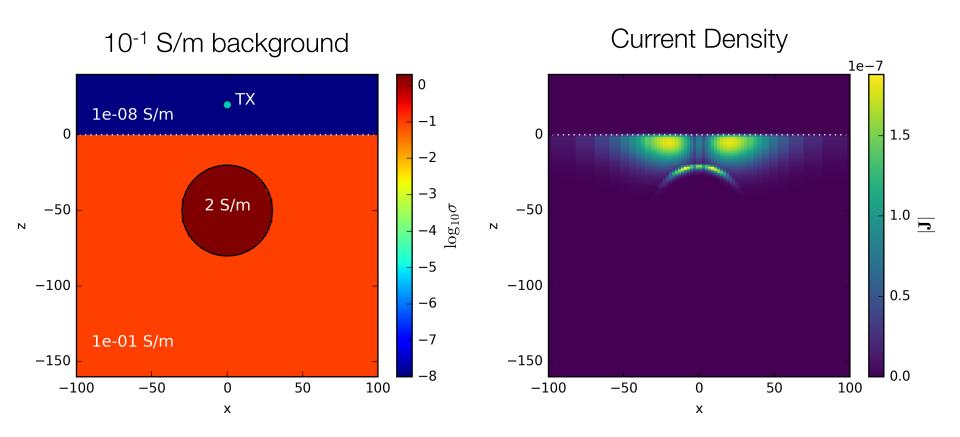
- Buried, conductive sphere
- Vary background conductivity
- Time: 10⁻⁵ s



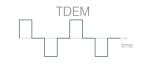


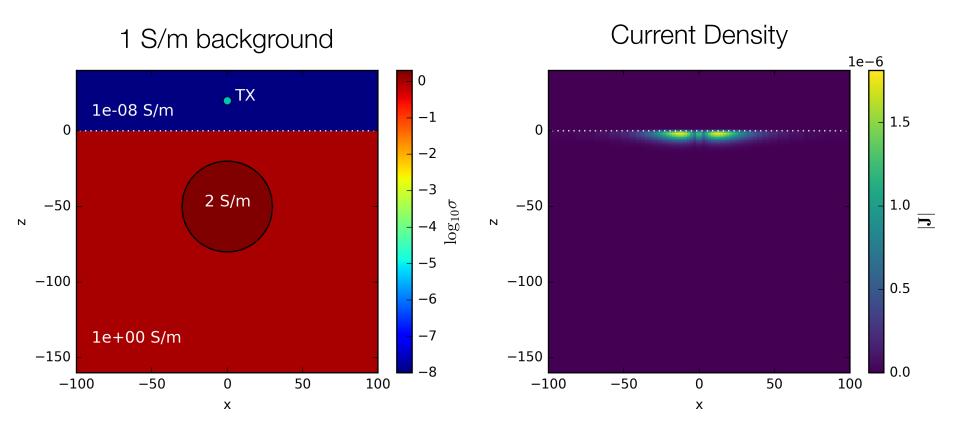
- Buried, conductive sphere
- Vary background conductivity
- Time: 10⁻⁵ s

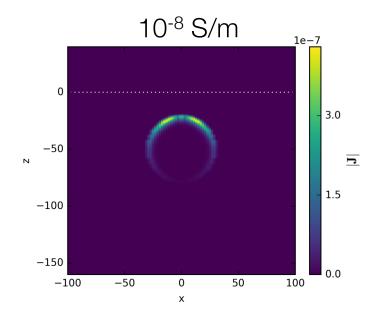




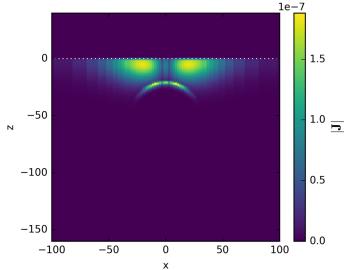
- Buried, conductive sphere
- Vary background conductivity
- Time: 10⁻⁵ s

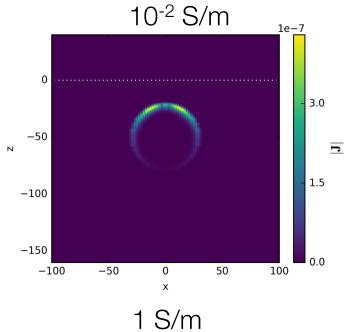


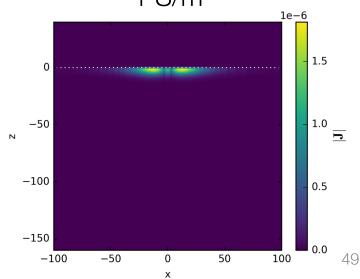




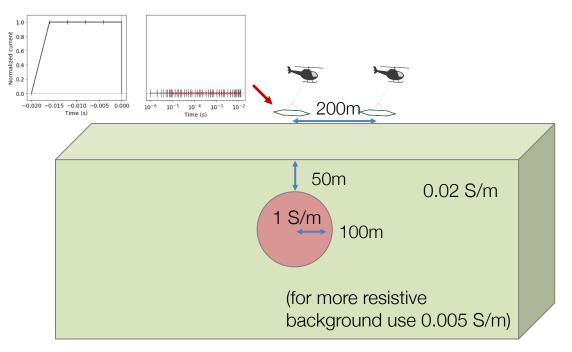






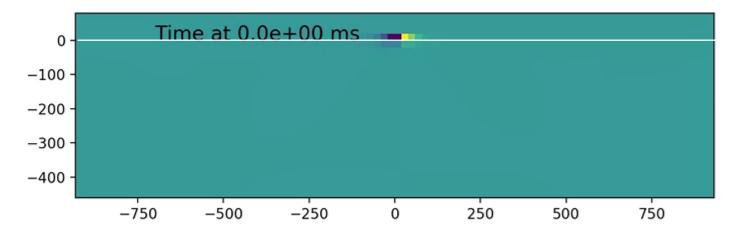


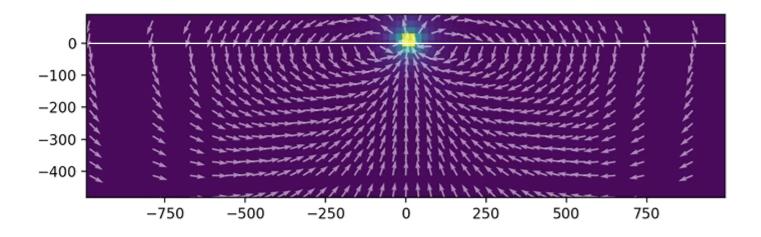
Conductive sphere in a halfspace



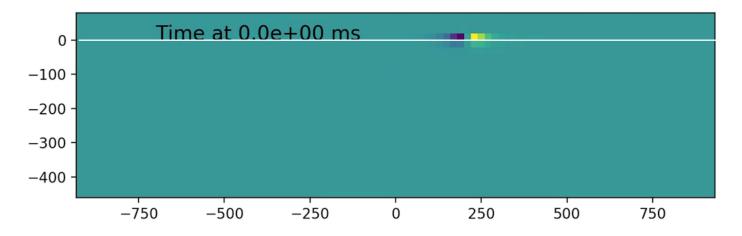
- Explore fields
- Generate synthetic data (3D simulation)
- Invert in 1D (artefacts?)
- Invert in 3D

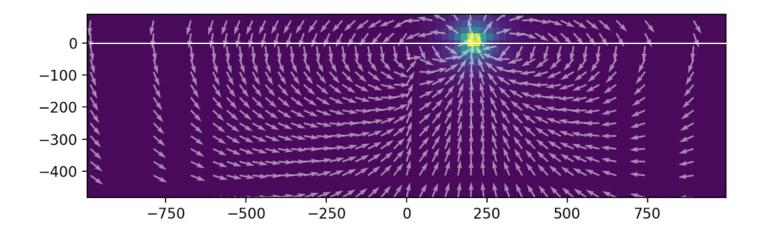
Currents and Magnetic Field (x=0m)



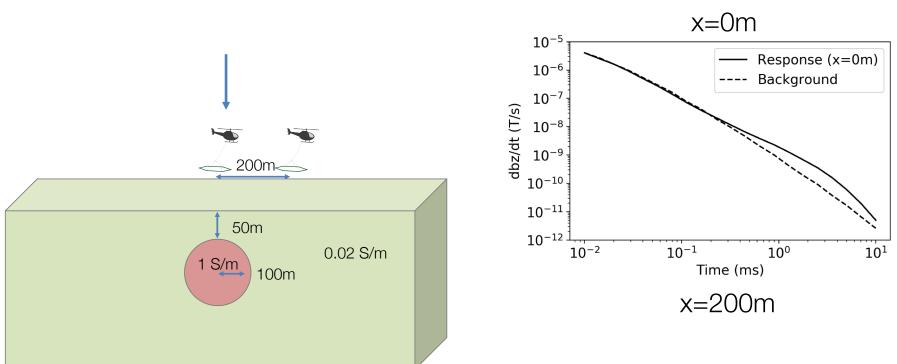


Currents and Magnetic Field (x=200m)



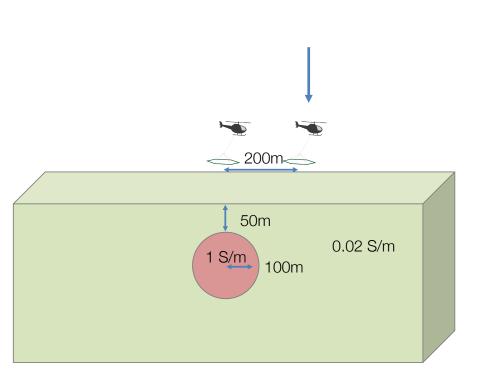


Soundings

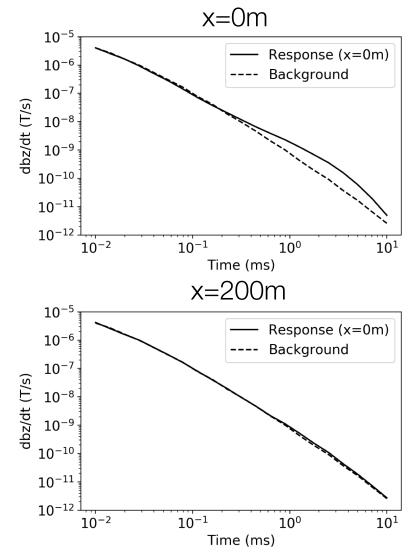


Responses are differ due to conductive sphere

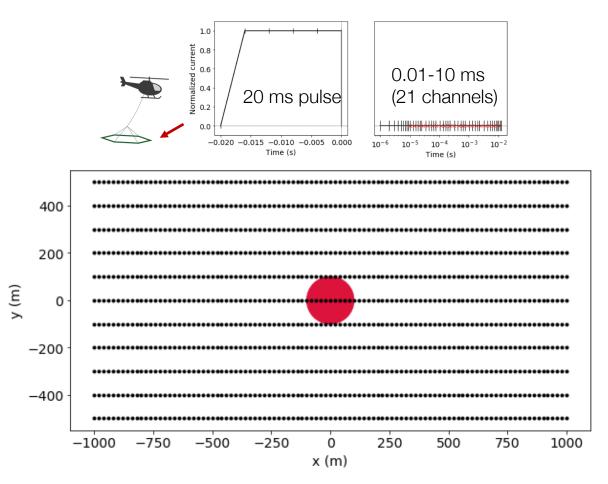
Soundings



Responses are differ due to conductive sphere



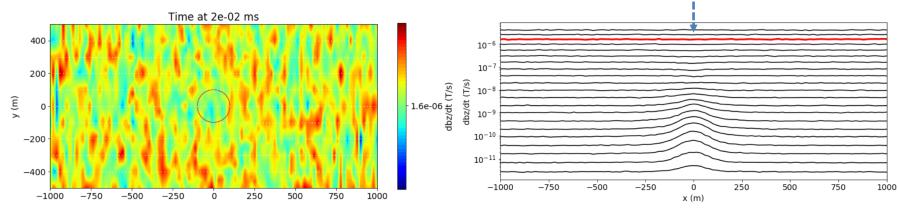
AEM survey over a sphere

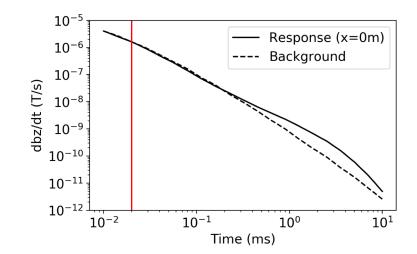


- Loop source
 - 13m radius
 - 30 m height
- Survey geometry
 - 11 lines
 - 100 line spacing
 - # of sounding: 1111
- Data
 - dbz/dt
 - 2% noise

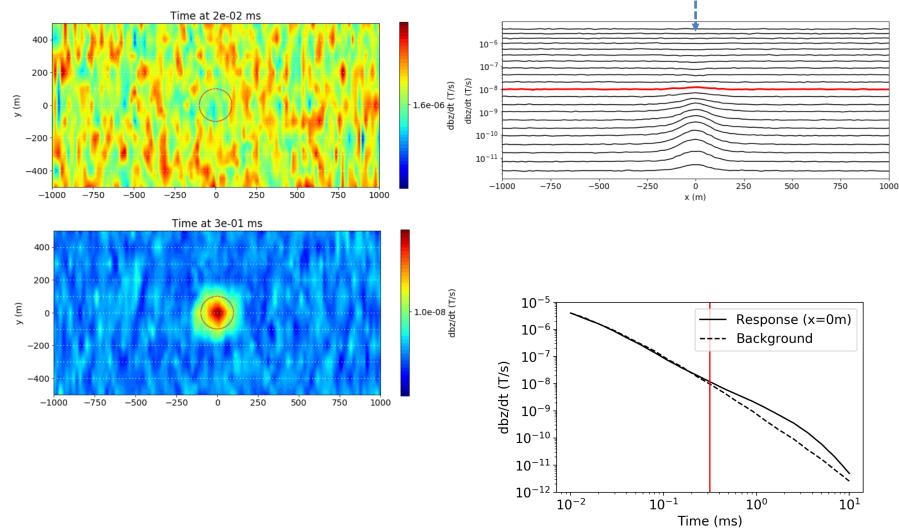
UBC-TDOctree code

Data map, profile, and decay

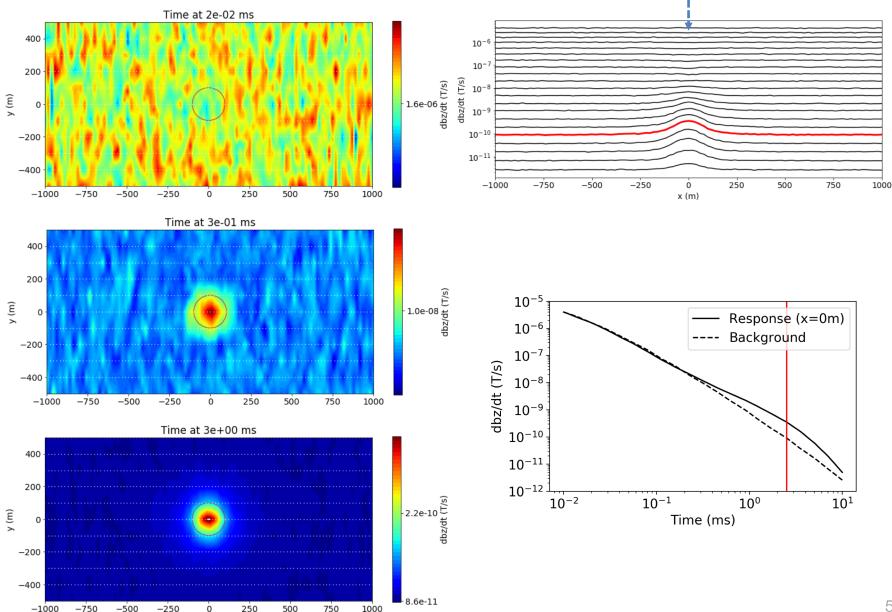




Data map, profile, and decay

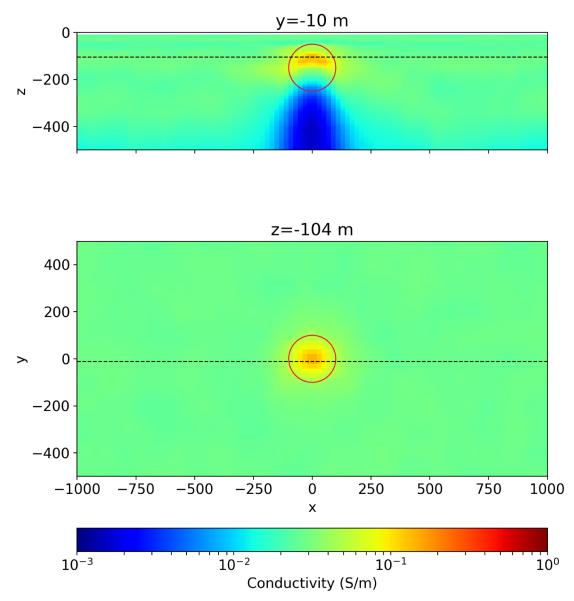


Data map, profile, and decay



x (m)

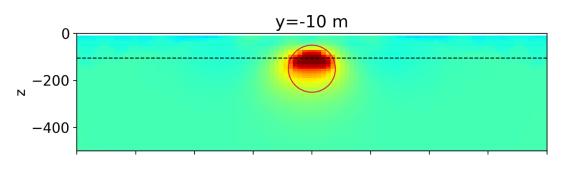
1D inversion

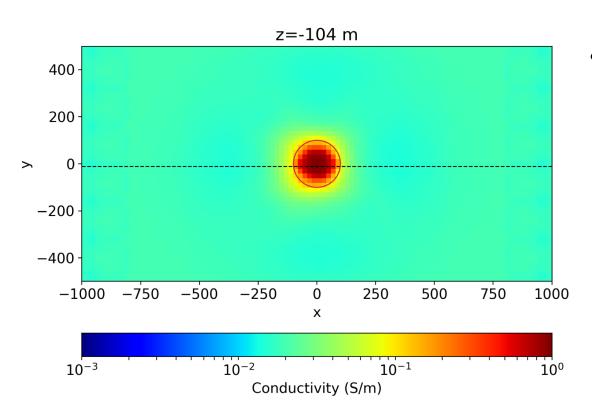


- Start: 0.02 S/m
- Reach target misfit (rms=1)
- Conductor at correct depth
- Underestimate conductivity value (max = 0.15 S/m)
- Resistive artifact below

Can 3D make it better?

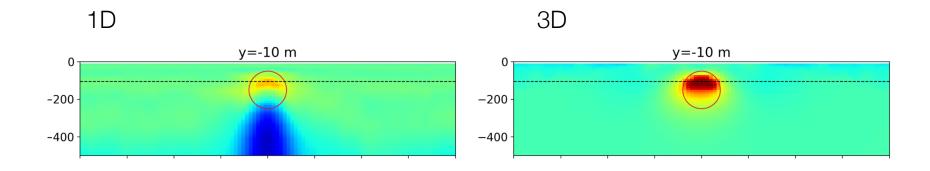
3D inversion

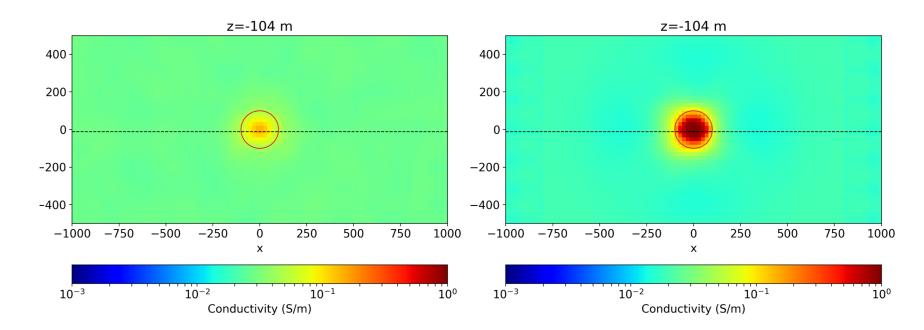




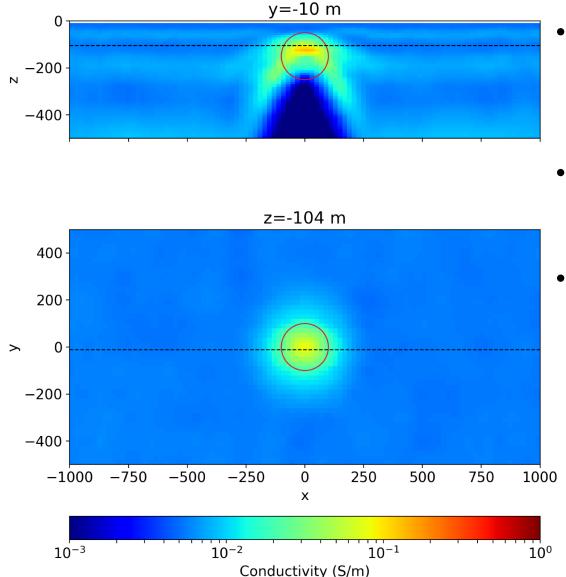
- Use 1D conductivity as an initial model
- Closer to the true
 conductivity (1S/m)
- No resistive artifact

Comparison 1D and 3D





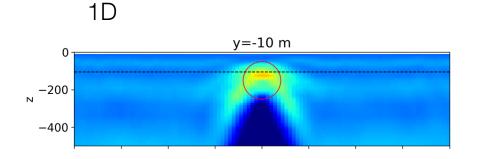
More resistive background.

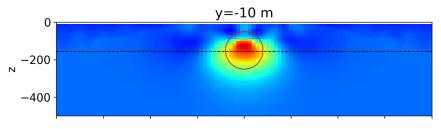


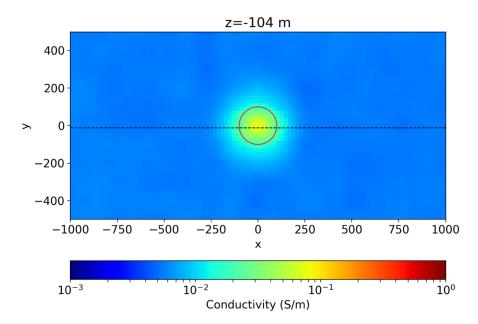
- Decrease background conductivity
 - 0.02 → 0.005 S/m
- Pronounced pant-legs (larger foot-print)
- Resistive artefact beneath conductor.

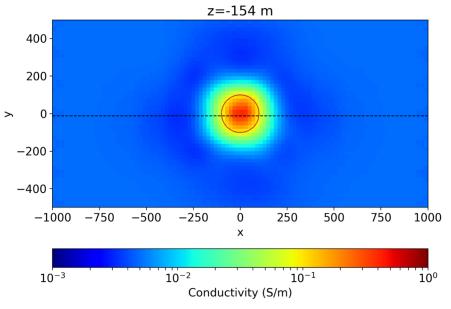
Comparison 1D and 3D

ЗD





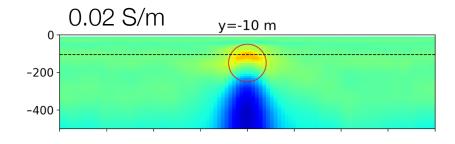


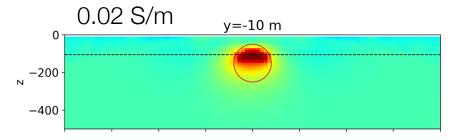


63

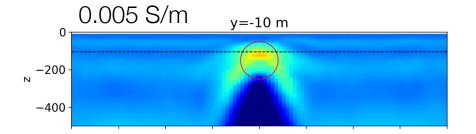
Inversion with different backgrounds

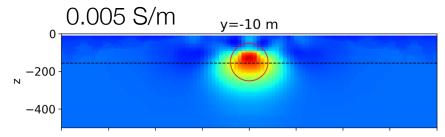
1D





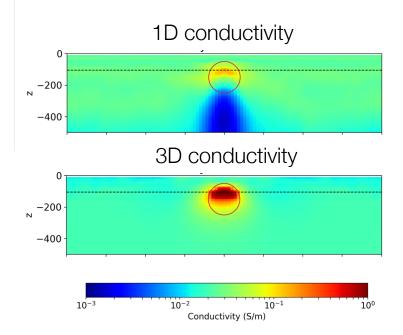
3D





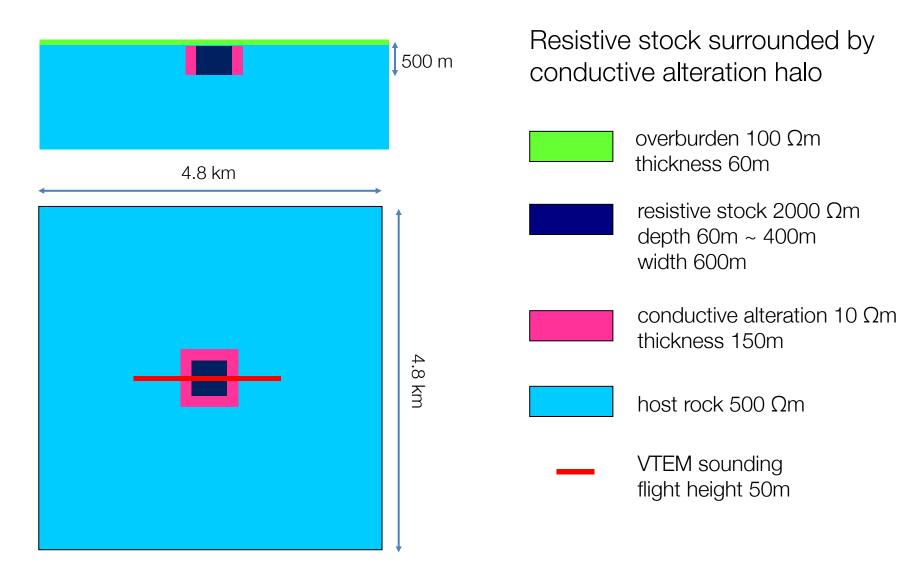
When is 3D inversion required?

- Depends upon the goal:
 - target detection?
 - detailed structure/
 - What resolution scale is needed?

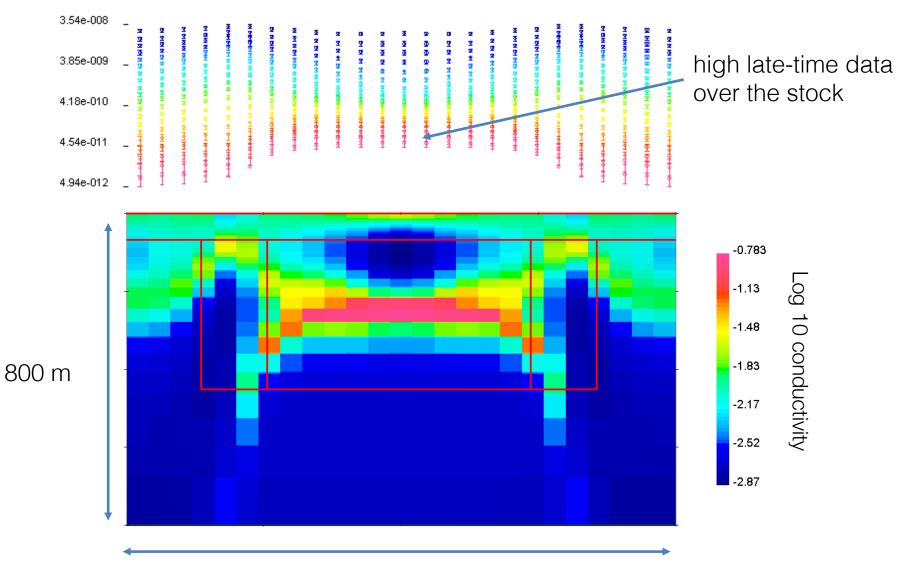


- Some other generic cases:
 - compact resistor
 - topography
 - general 3D structure with different scale lengths

Compact resistor in porphyry deposit

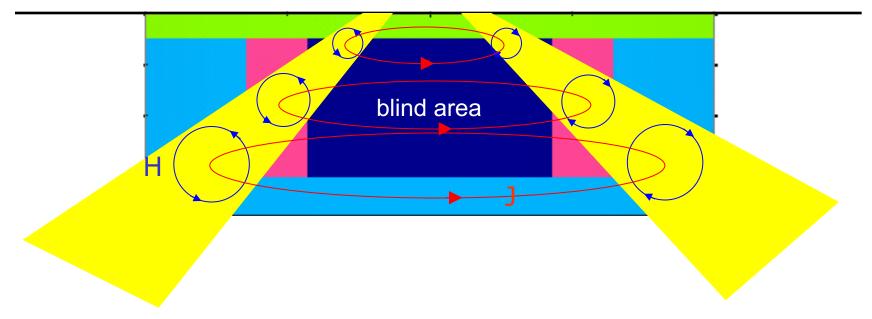


1D Inversion of 3D Synthetic Data



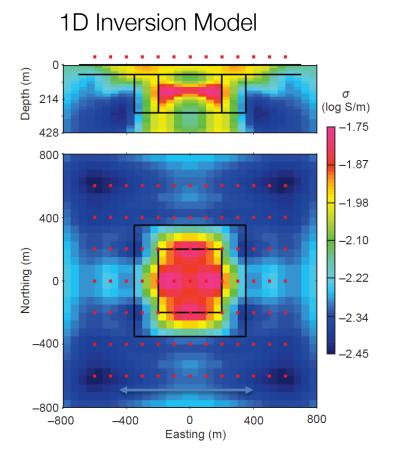
What is wrong with 1D inversion?



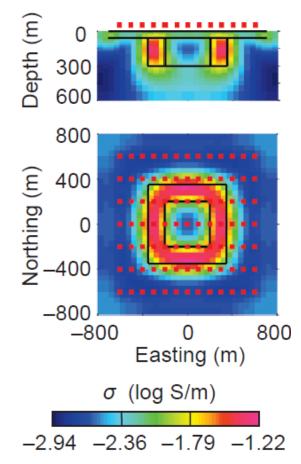


Footprint sensitive to conducting halo around the stock

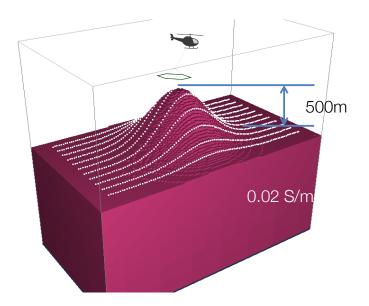
1D VS 3D: Mt. Milligan Synthetic Model



3D Inversion Model

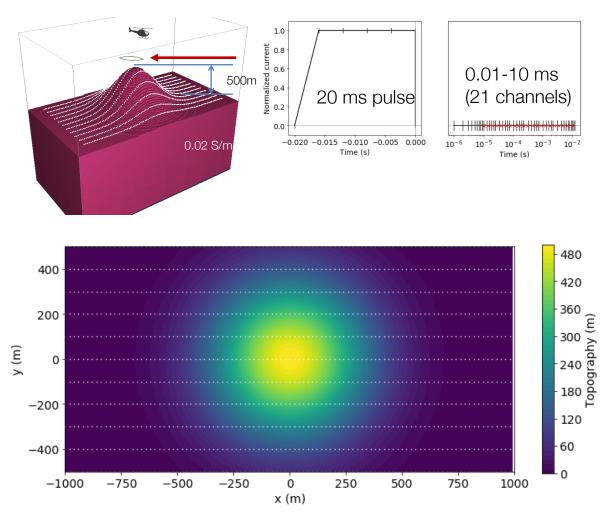


Topography



- Explore fields
- Generate synthetic data (3D simulation)
- Invert in 1D (artefacts?)
- Invert in 3D

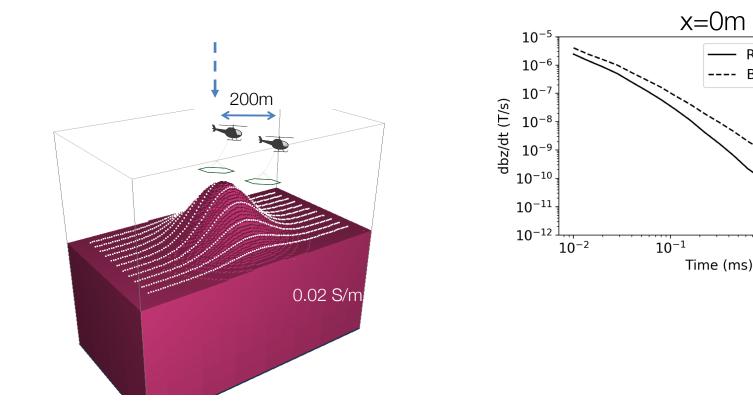
AEM surveys over topography



- Loop source
 - 13m radius
 - 30 m height
- Survey geometry
 - 11 lines
 - 100 line spacing
 - # of sounding: 1111
- Data
 - dbz/dt
 - 2% noise

UBC-TDOctree code

Soundings



Responses are differ due to conductive sphere

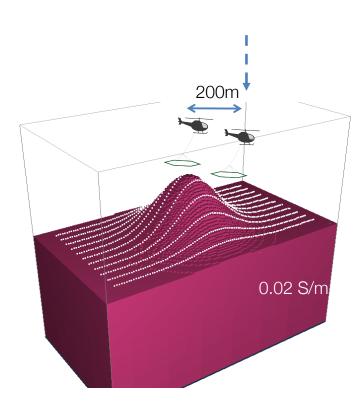
Response (x=0m)

10¹

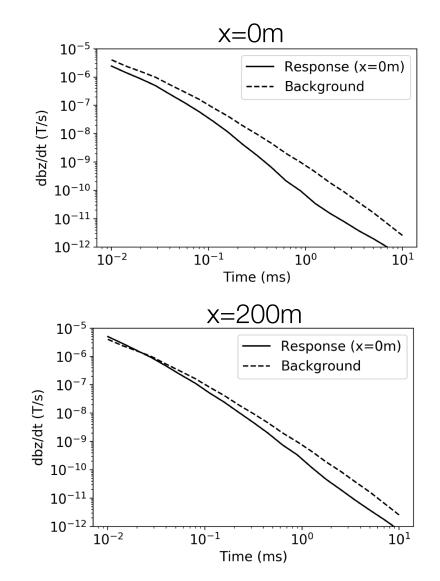
---- Background

10⁰

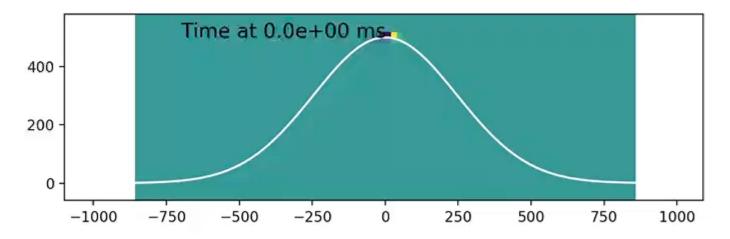
Soundings

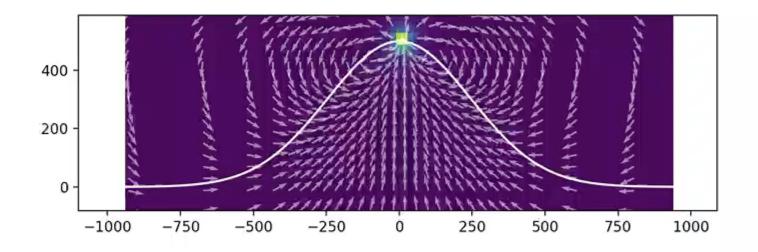


Responses are differ due to conductive sphere

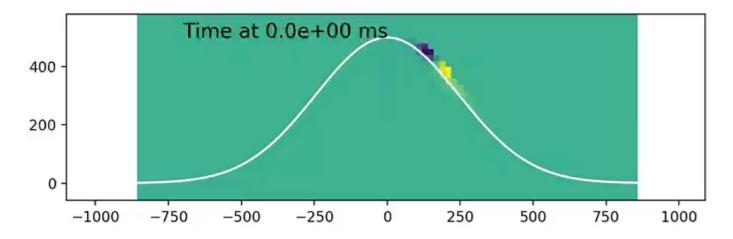


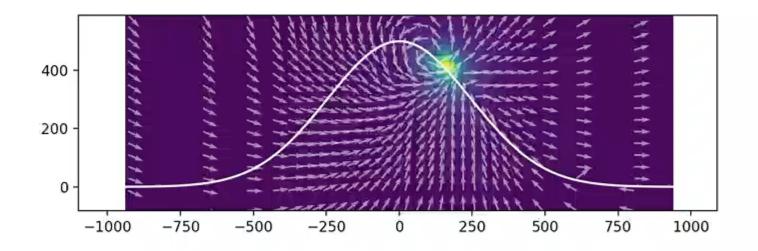
Currents and Magnetic Fields (x=0m)



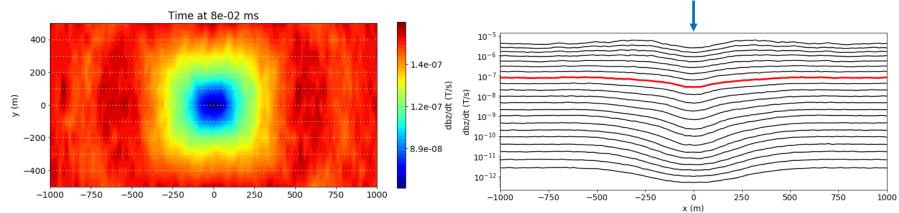


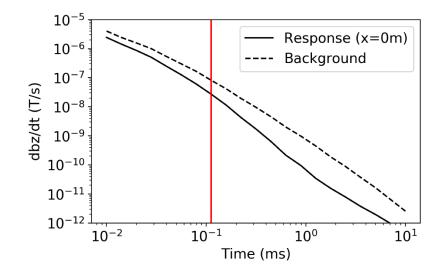
Currents and Magnetic Fields (x=200m)



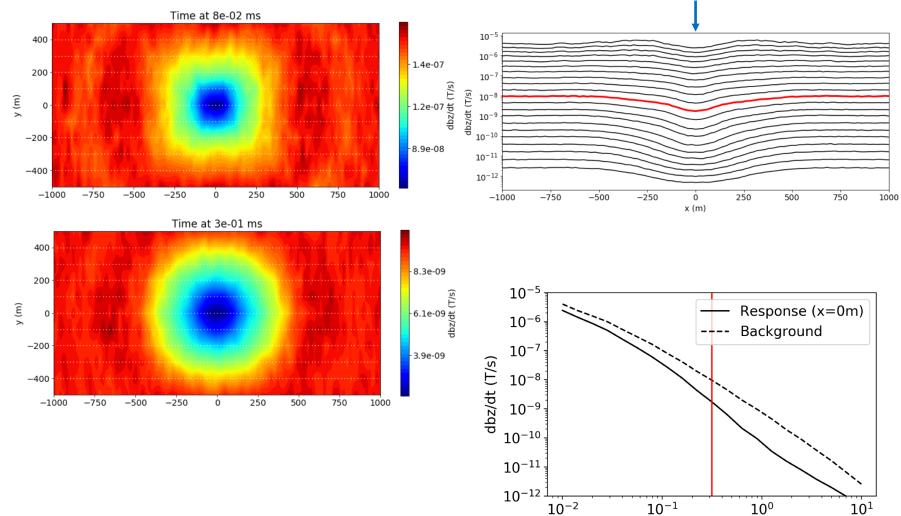


Data map, profile, and decay



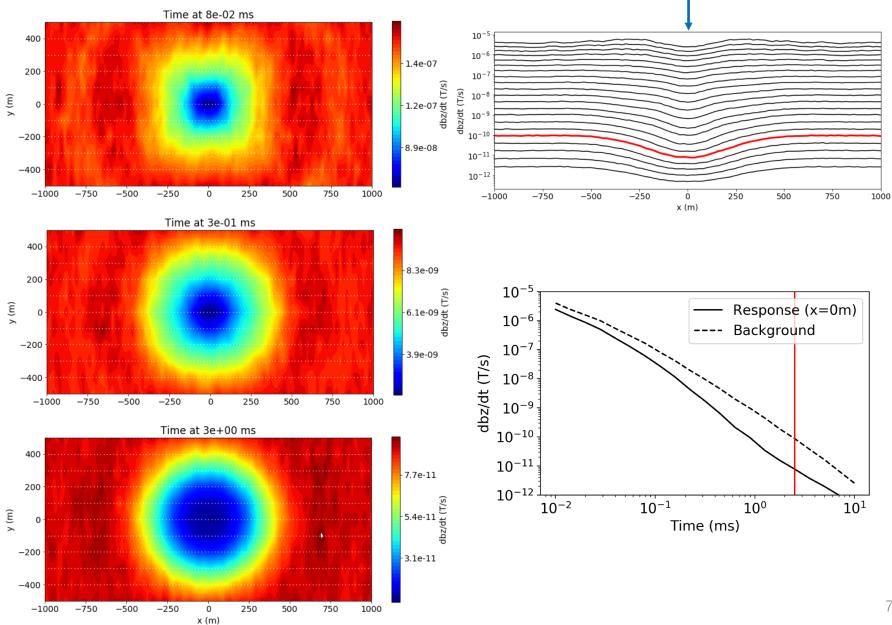


Data map, profile, and decay

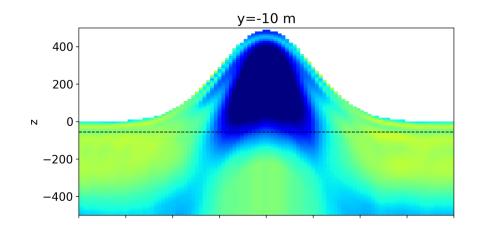


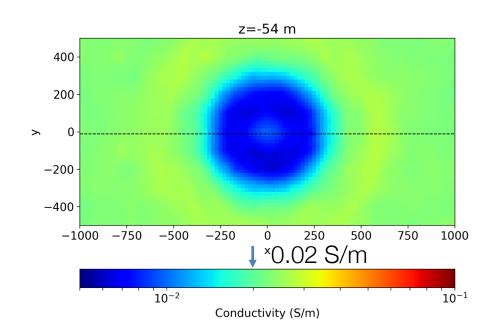
Time (ms)

Data map, profiles, and sounding curves



1D inversion

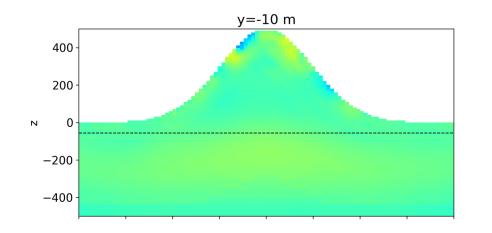




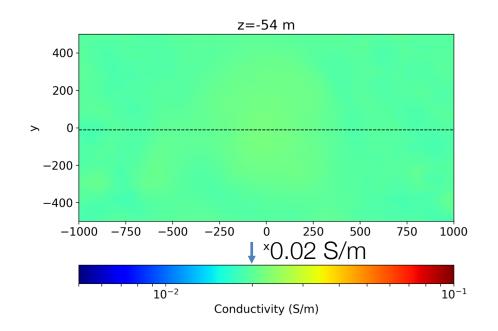
- Start from 0.02 S/m background
- Reached target misfit (rms=1)
- Large resistor below topography

Need to invert in 3D!

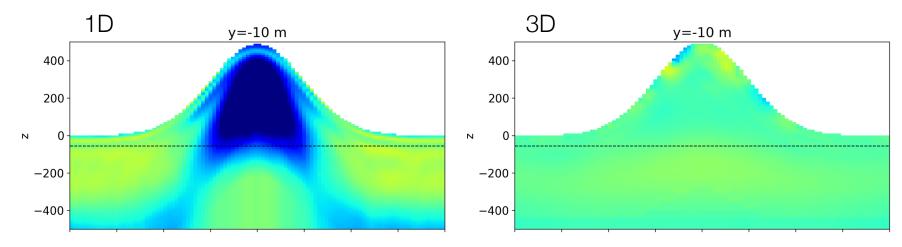
3D inversion

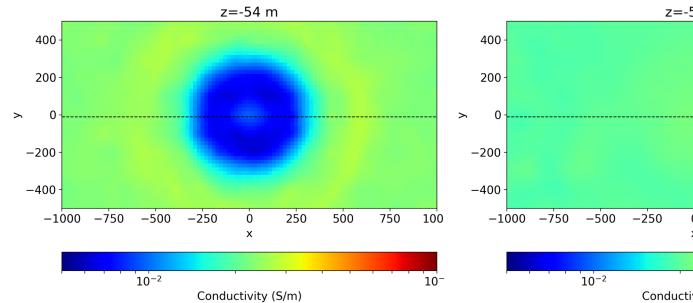


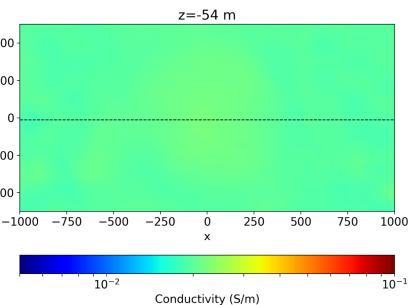
- Start from 0.01 S/m background
- Reached target misfit (rms=1)



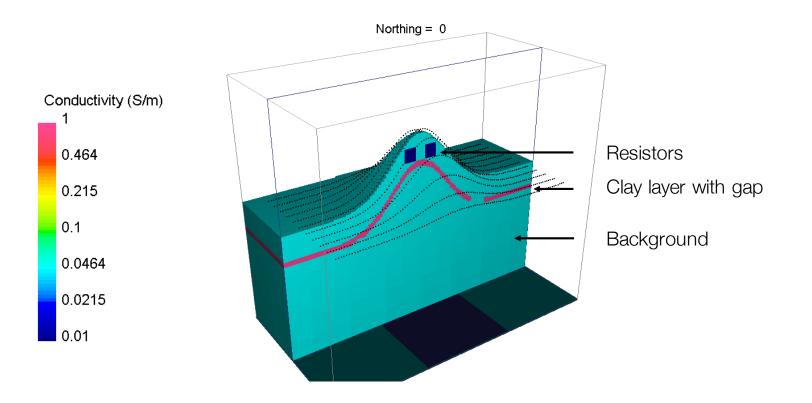
Comparison 1D and 3D





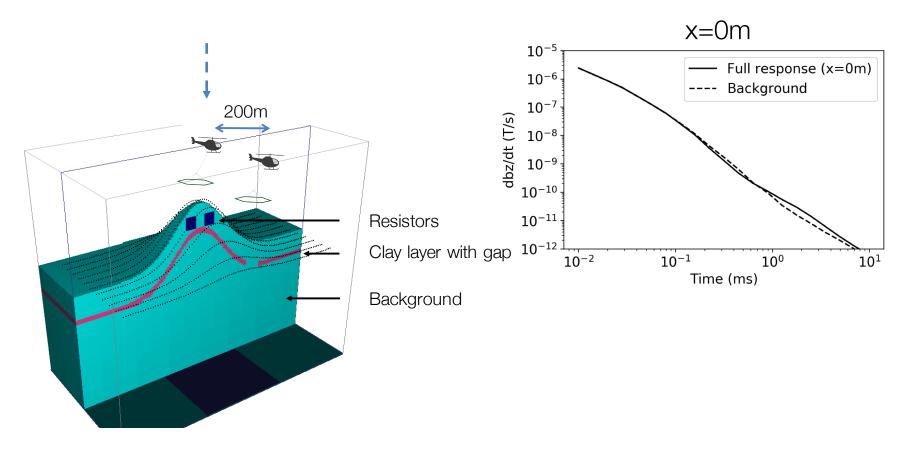


Geologic structures below topography

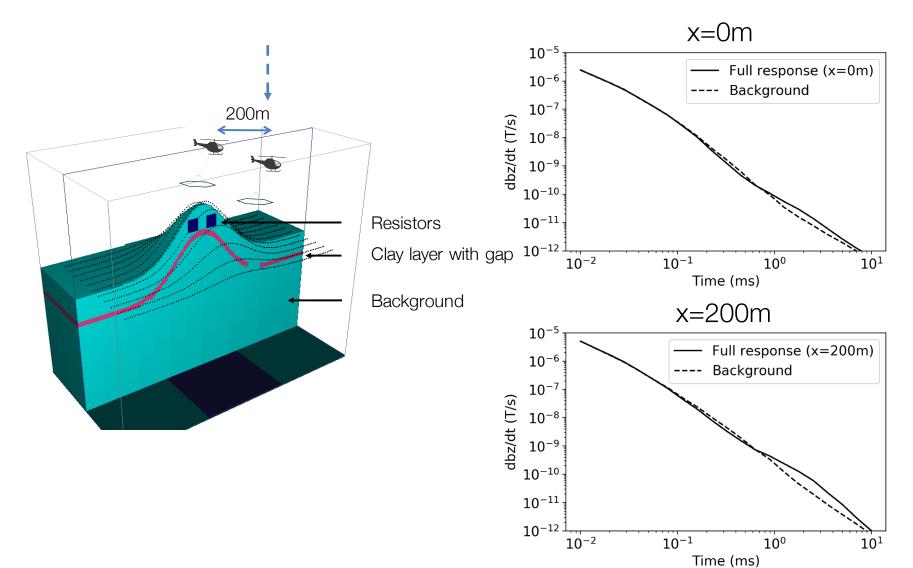


- Generate synthetic data (3D simulation)
- Invert in 1D
- Invert in 3D

Sounding curves

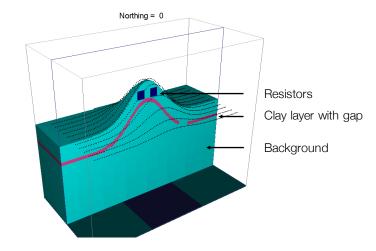


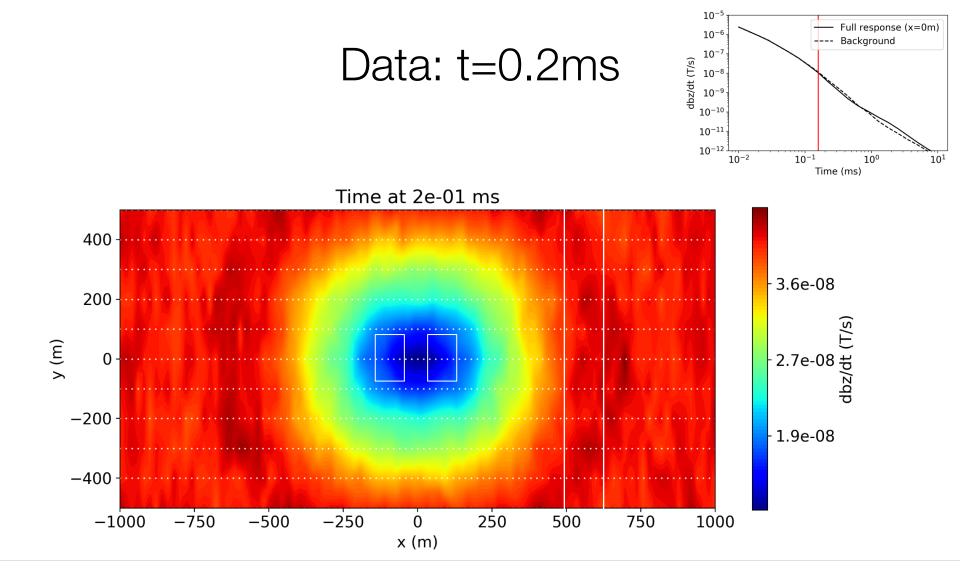
Sounding curves

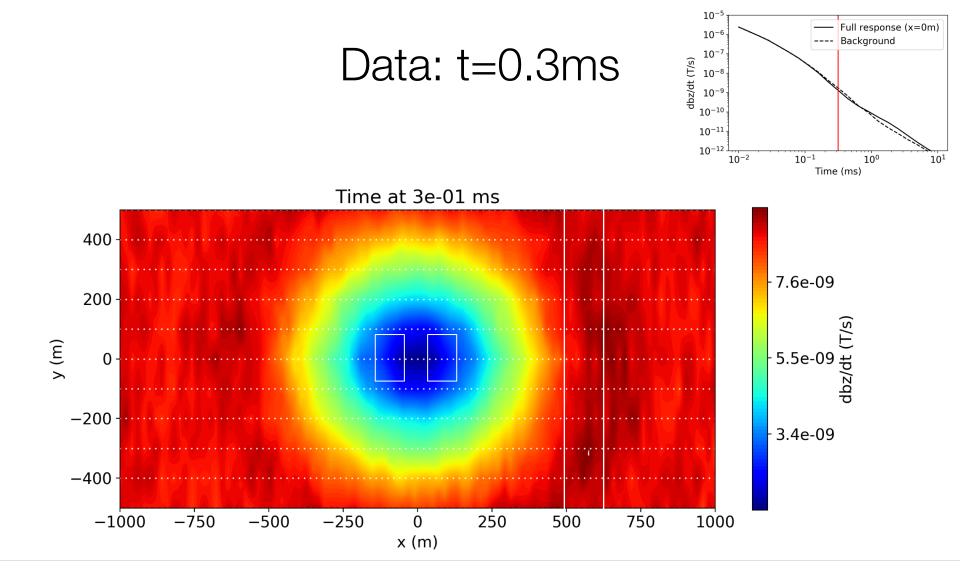


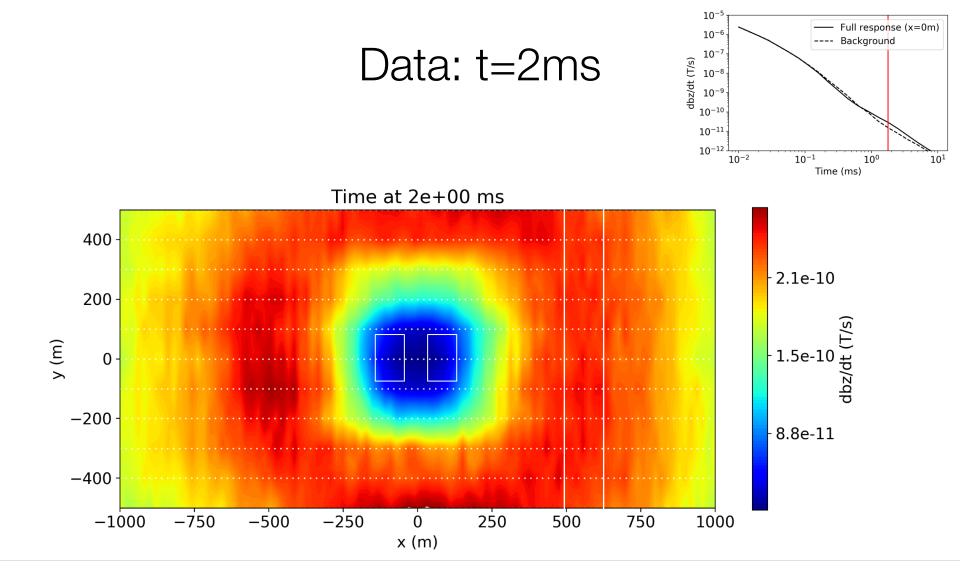
Questions

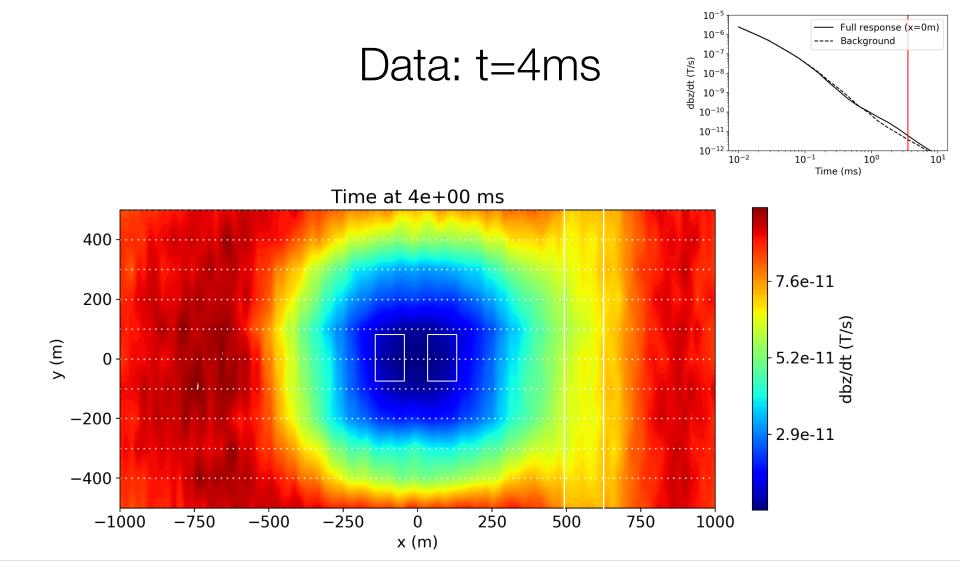
- Can we detect signals from:
 - Conductive clay layer
 - Resistors
- Can we see the gap in the clay layer?
- How do we invert these data?
 - Is 1D inversion effective?
 - Do we need 3D inversion?
 - How much information can we extract?

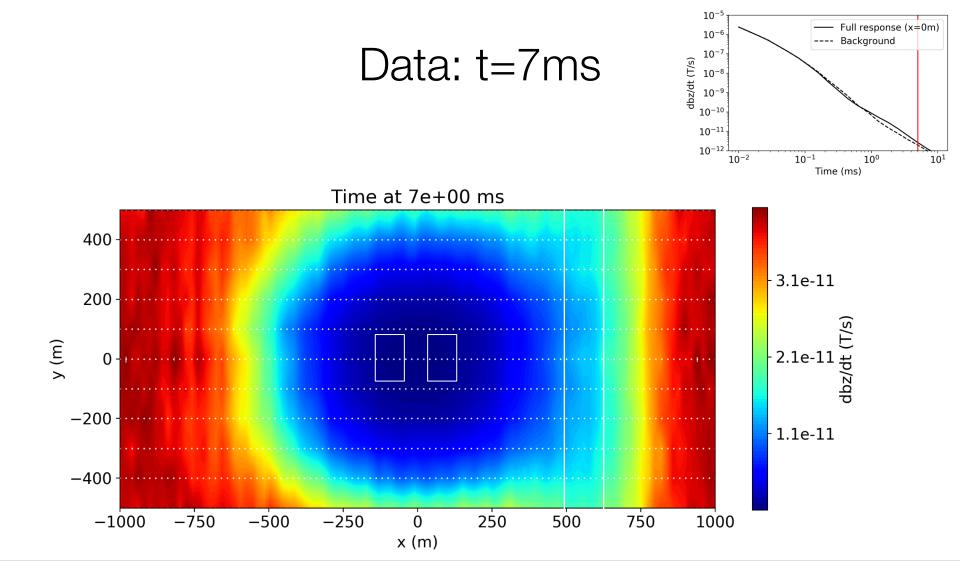




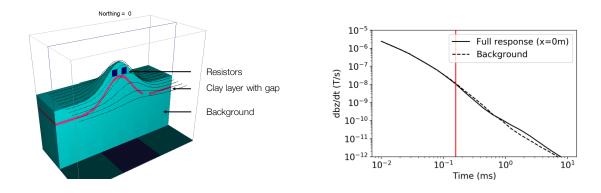


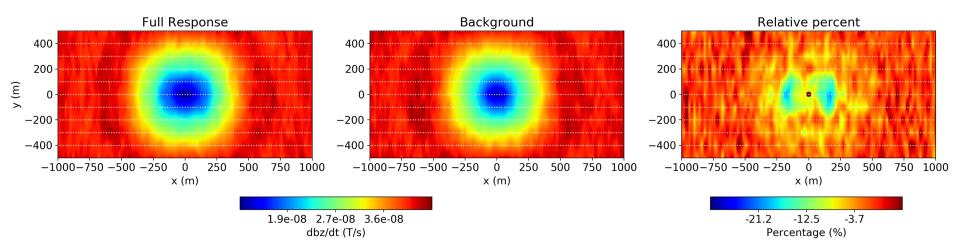




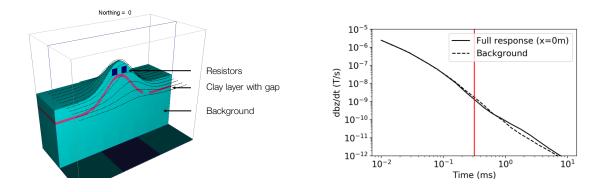


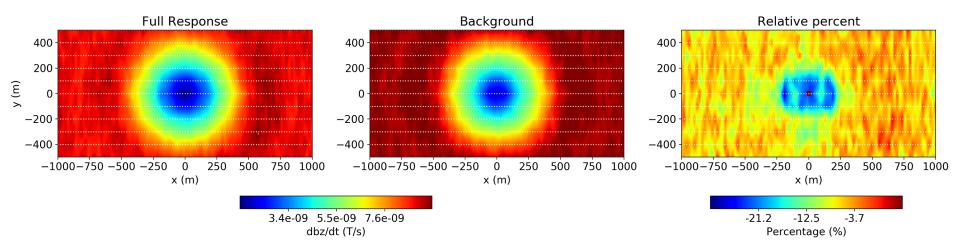
Time at 0.2ms



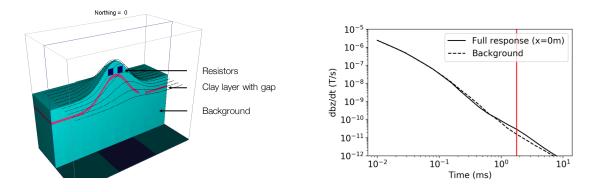


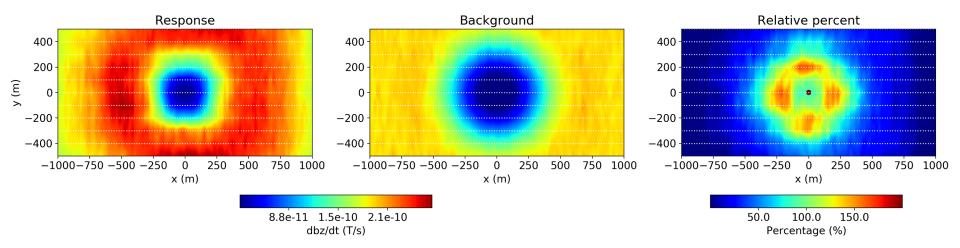
Time at 0.3ms



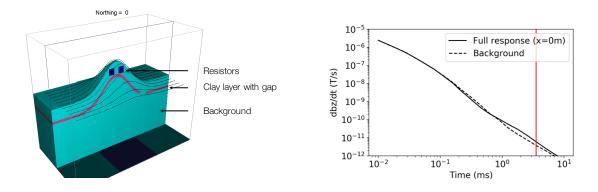


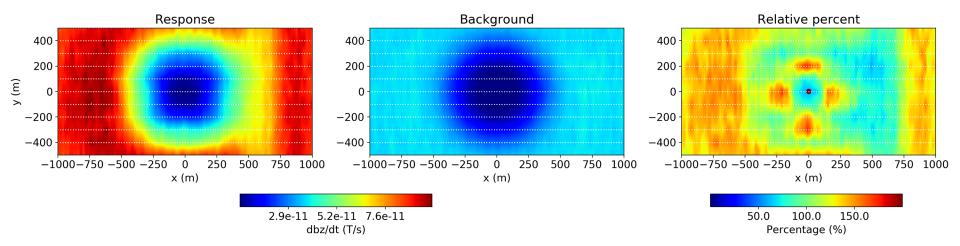
Time at 2ms



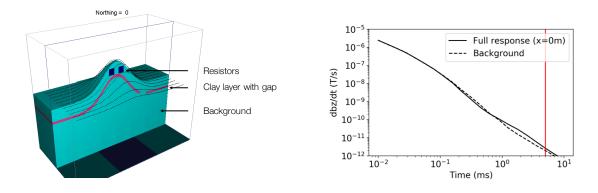


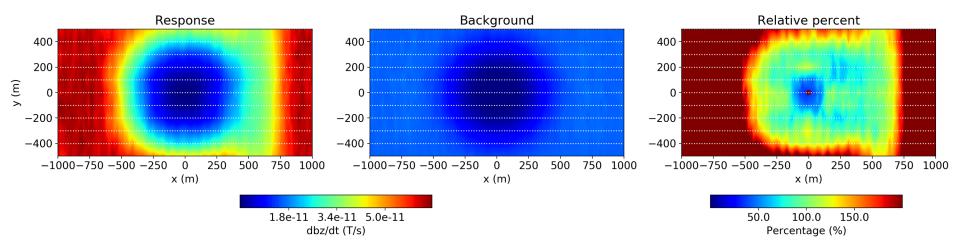
Time at 4ms



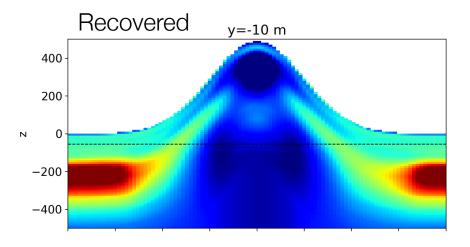


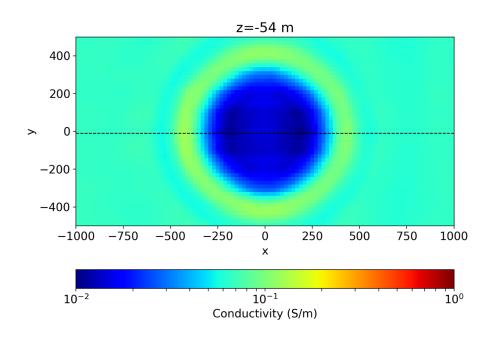
Time at 7ms





1D inversion

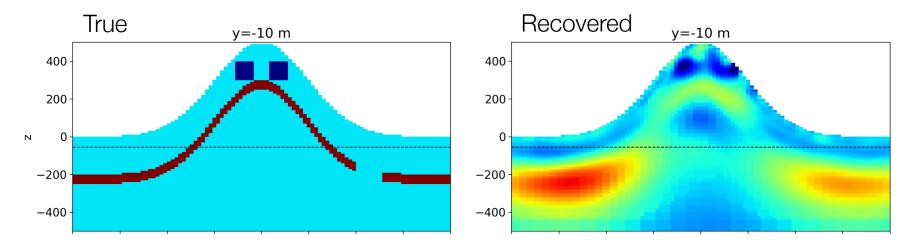


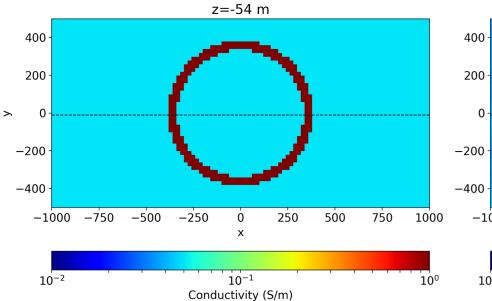


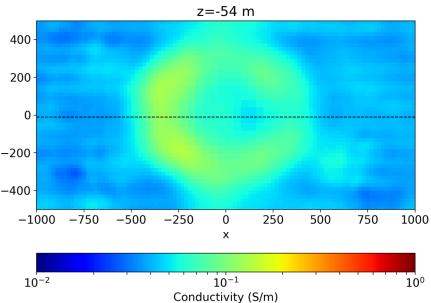
- Background: 0.02 S/m
- Reached target misfit (rms=1)
- Large resistor below topography
- Clay layers away from topography.

Need to invert in 3D

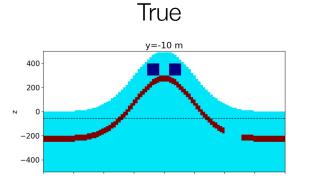
3D inversion

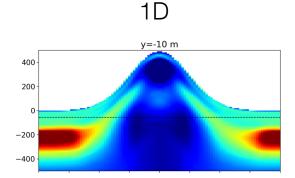


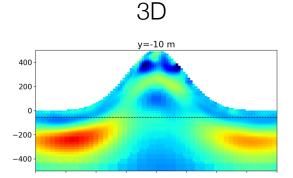


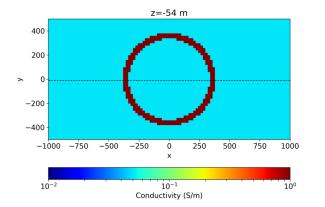


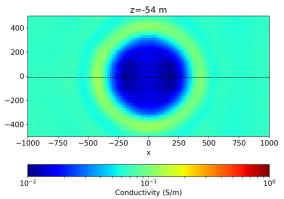
Comparison 3D and 1D

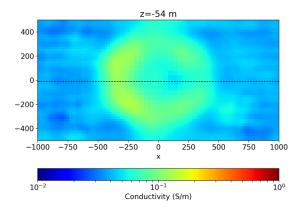




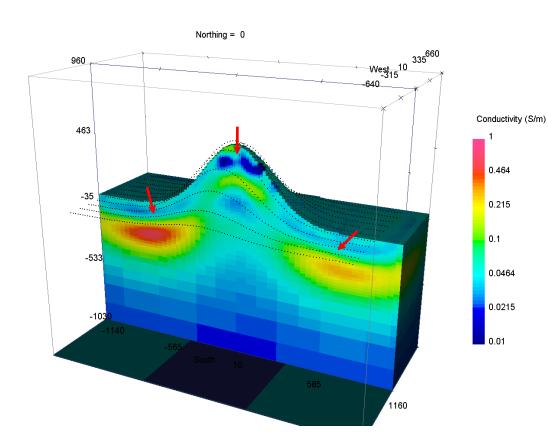








3D view



- Imaged main features in 3D
 - Deep clay layer
 - Resistors

3D view

0.464

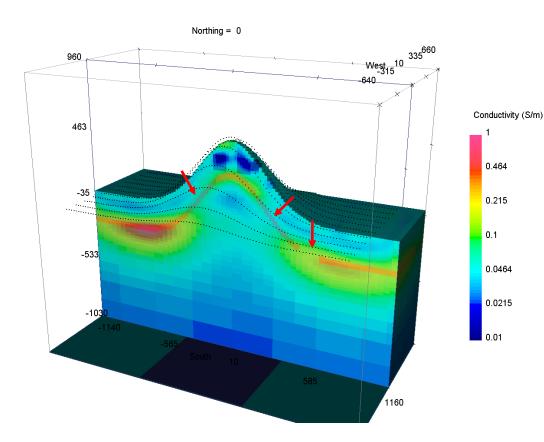
0.215

0.1

0.0464

0.0215

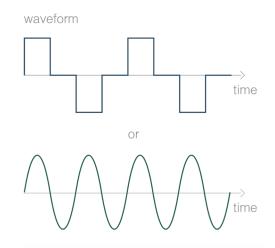
0.01



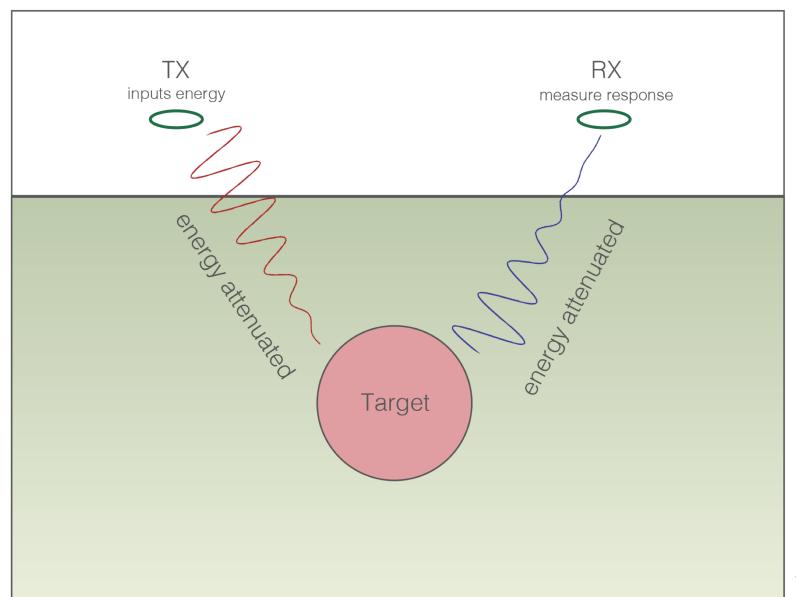
- Imaged
 - Deep clay layer
 - Resistors
- Less sensitive to clay layer on the slopes of the mountain
 - Poor coupling
- Gap in the clay
 - slight indication
 - Requires some a priori information to resolve

Frequency Domain

- Same physics as time domain
- Challenging because primary field is always on
- Currents are partitioned into in-phase and quadrature portions.
- Consider a sphere in a buried background

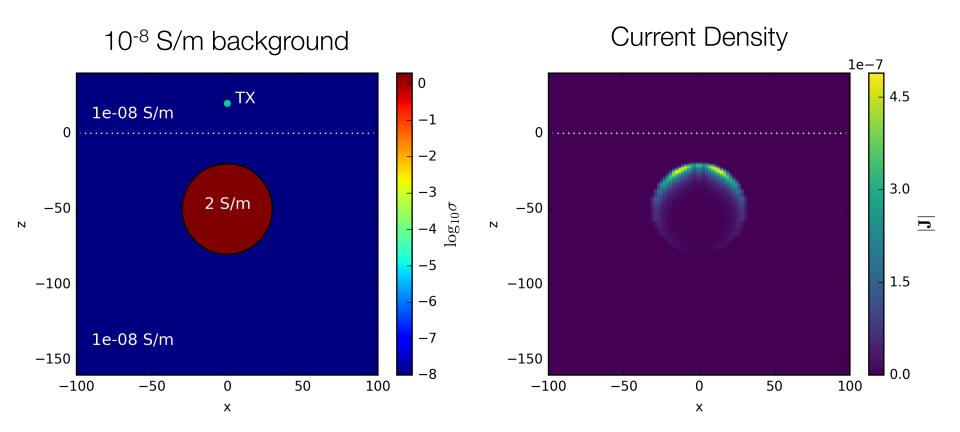


Conductive sphere in a uniform background

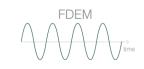


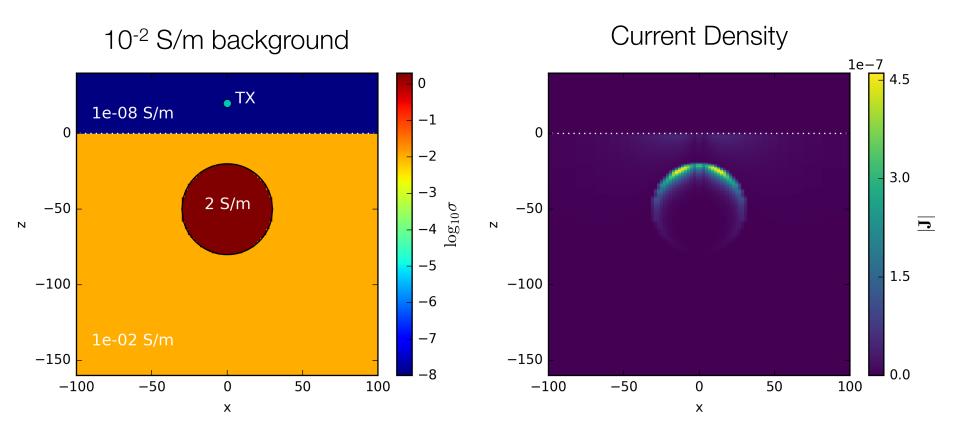
- Buried, conductive sphere
- Vary background conductivity
- Frequency: 10⁴ Hz



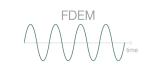


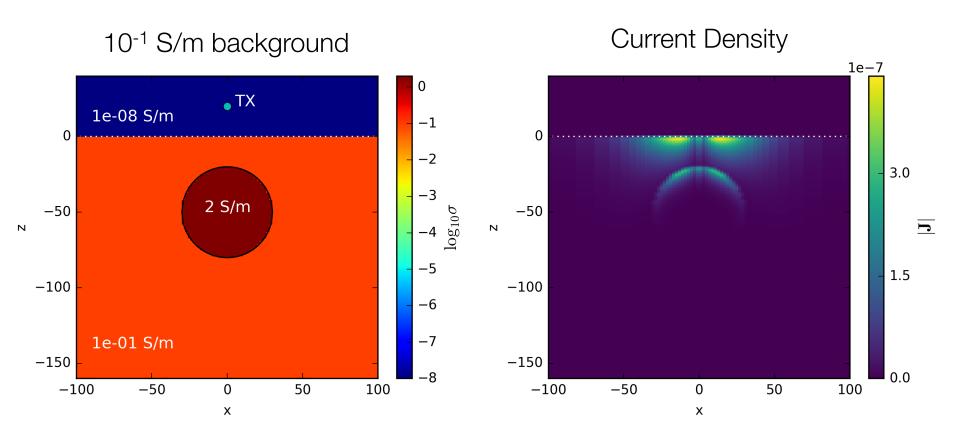
- Buried, conductive sphere
- Vary background conductivity
- Frequency: 10⁴ Hz





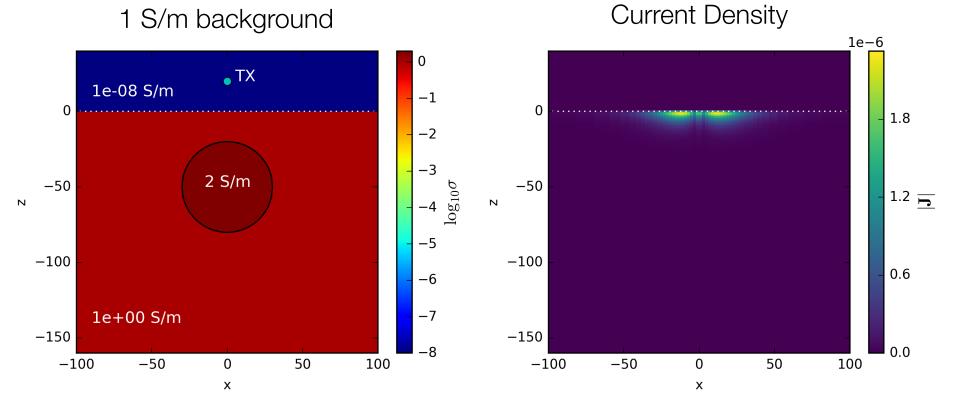
- Buried, conductive sphere
- Vary background conductivity
- Frequency: 10⁴ Hz

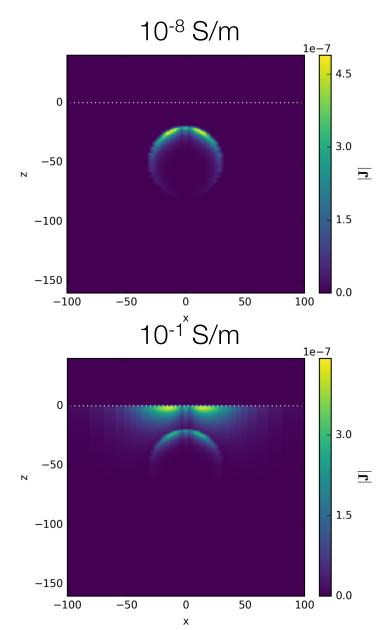


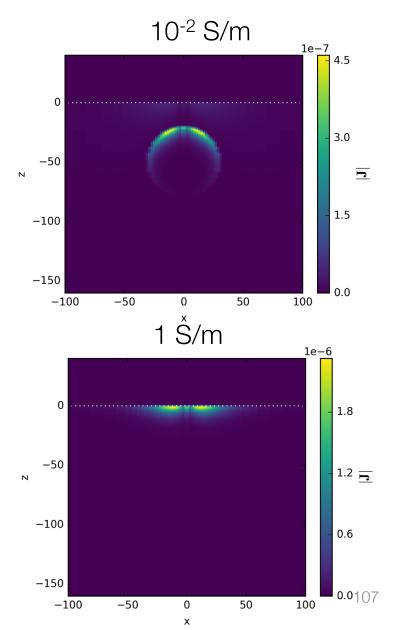


- Buried, conductive sphere
- Vary background conductivity
- Frequency: 10⁴ Hz





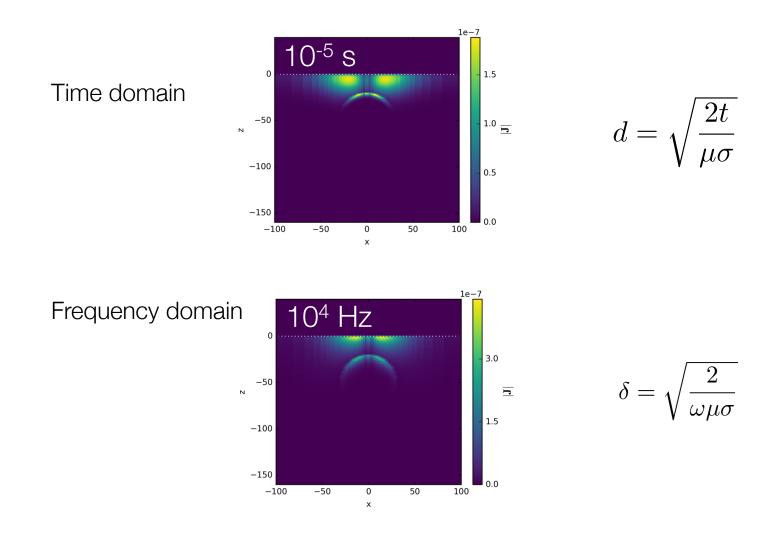




10⁴ Hz

Summary: frequency vs. time

Physics is same, but looking field in time domain is more intuitive in general



Summary

- Fundamentals of EM induction
- Fields and fluxes in 3D to aid understanding
- Generic examples where 3D can be important
 - buried conductor
 - buried resistor
 - topography
 - complex structure
- Frequency vs time domain



EM Induction

Field Examples

Computation

Open Source Software