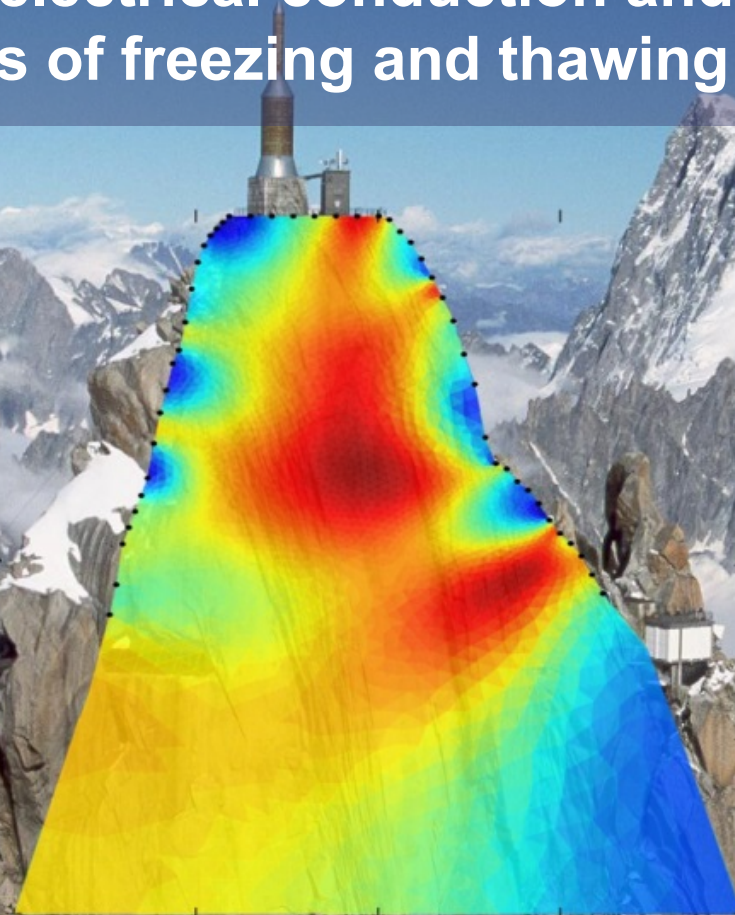


Low-frequency electrical conduction and polarization properties of freezing and thawing rocks

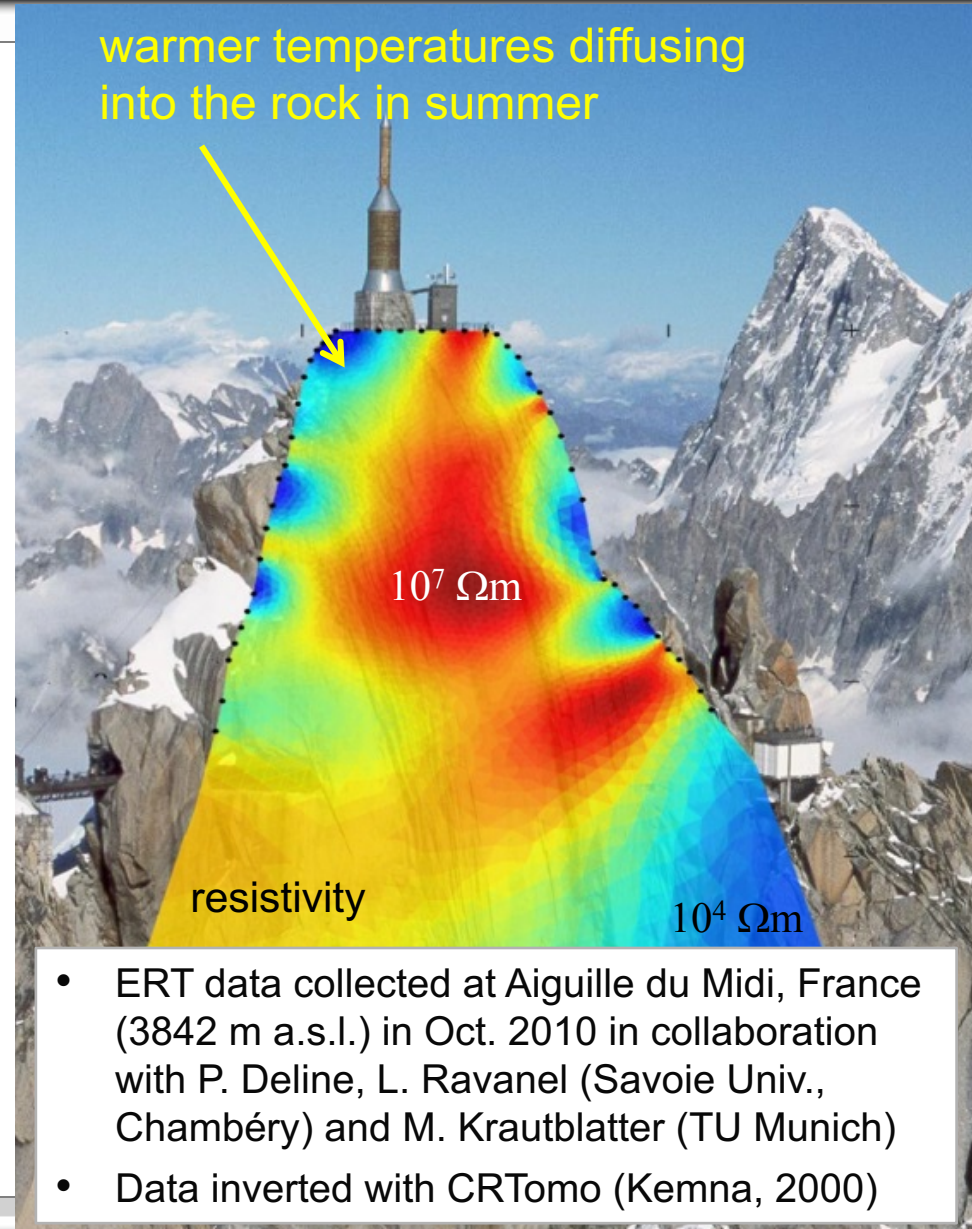


Andreas Kemna, Maximilian Weigand
Geodynamics/Geophysics, University of Bonn, Germany

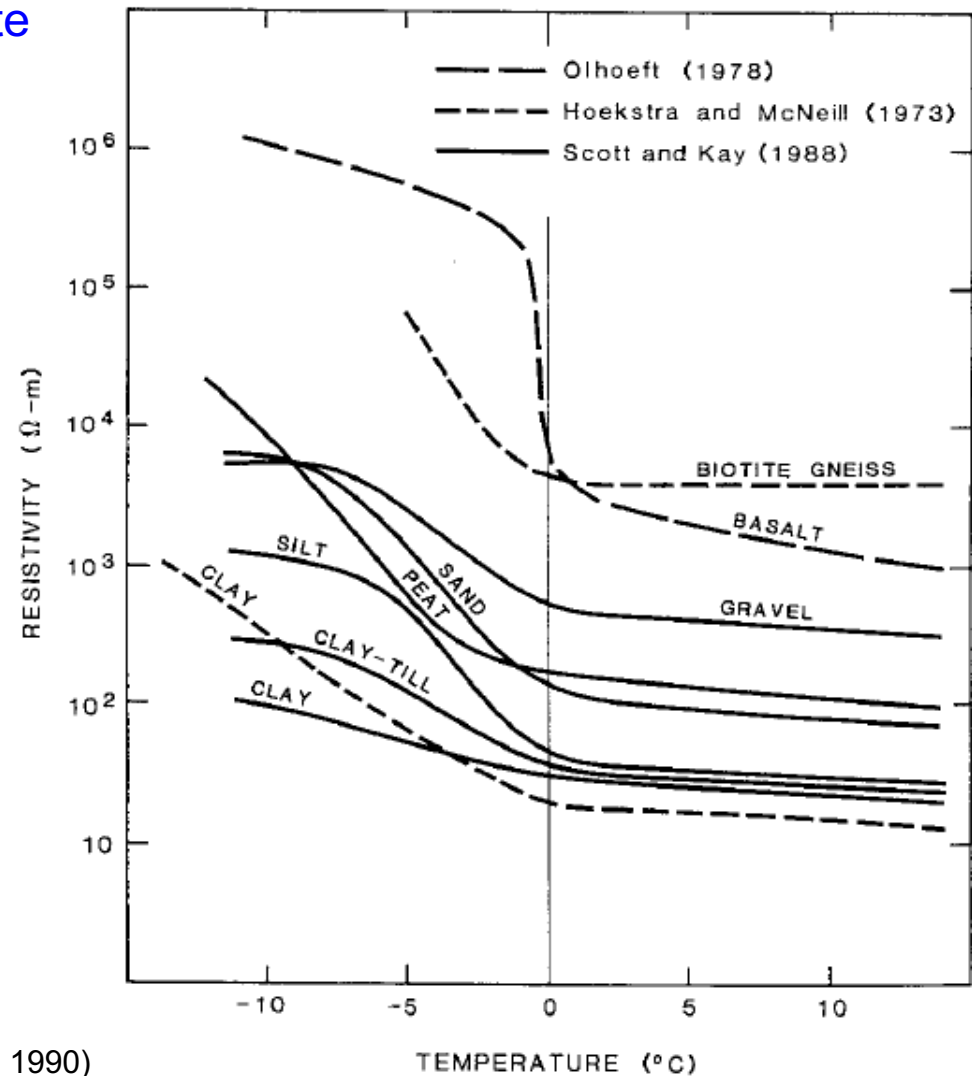
- **Electrical resistivity** of soils/rocks strongly dependent on water and ice content, and temperature
- **Electrical Resistivity Tomography (ERT)** increasingly used with a view to:
 - thermal state characterization and monitoring
 - quantification of water/ice content

See, e.g.:

Krautblatter et al. (S16, P31)
Magnin et al. (S7-1, 9:30)
Hauck (Plenary Lecture 3)



- Characterization of thermal state (frozen vs. unfrozen) based on resistivity difficult



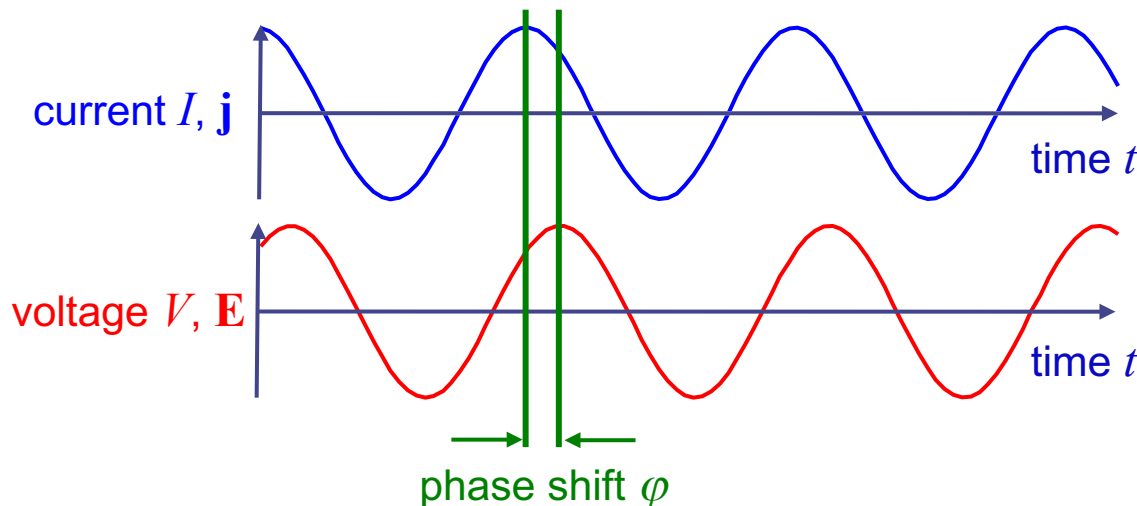
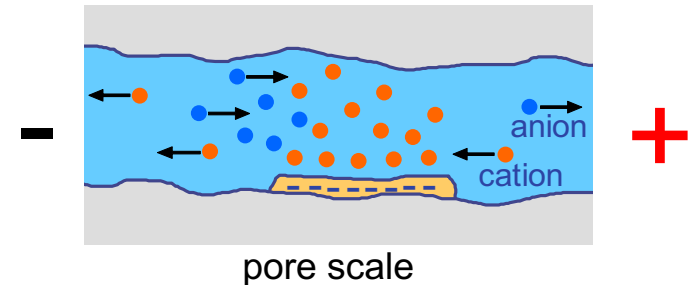
(Scott et al., 1990)

- Electrical **conduction** and **polarization** properties
- Measured as magnitude and phase (or real and imaginary components) of an effective complex conductivity (resistivity) or, alternatively, permittivity

$$\text{ice-free: } \sigma^*(\omega) = |\sigma| e^{i\varphi} = \sigma_{\text{DC}} + \sigma_{\text{surf}}^*(\omega)$$

$$\text{with ice: } \sigma^*(\omega) = \sigma_{\text{DC}} + \sigma_{\text{surf}}^*(\omega) + \sigma_{\text{ice}}^*(\omega)$$

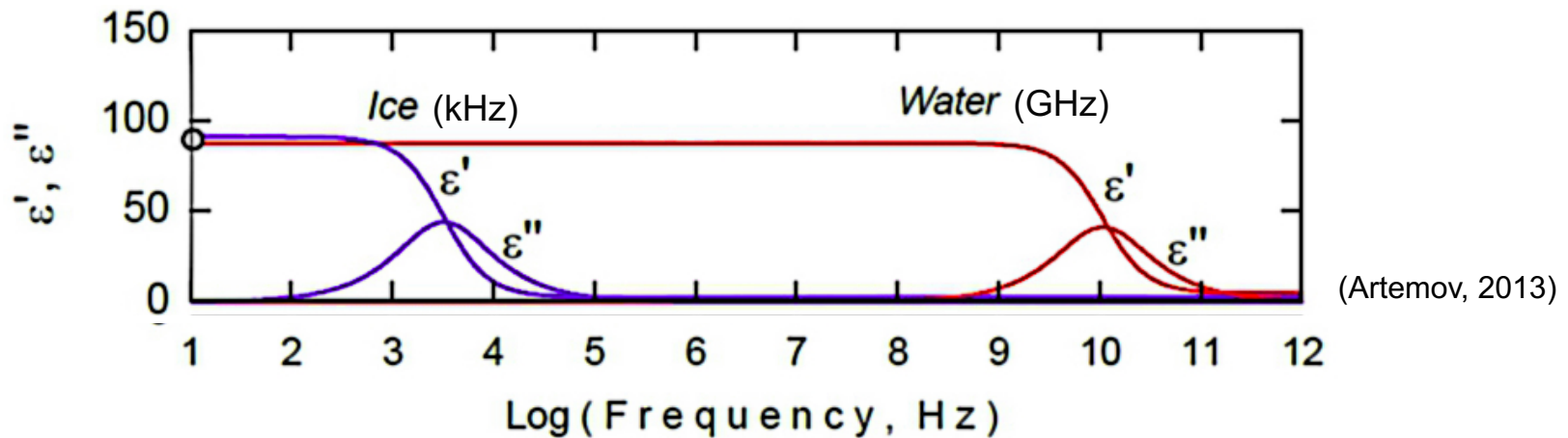
$$\sigma^* = \sigma_{\text{DC}} + i\omega\epsilon^* = 1/\rho^*, \quad i^2 = -1$$



- **Polarization of ice** (polarization of point defects in the crystal lattice) at much lower frequencies than polarization of water

ε' : real component of ε^*

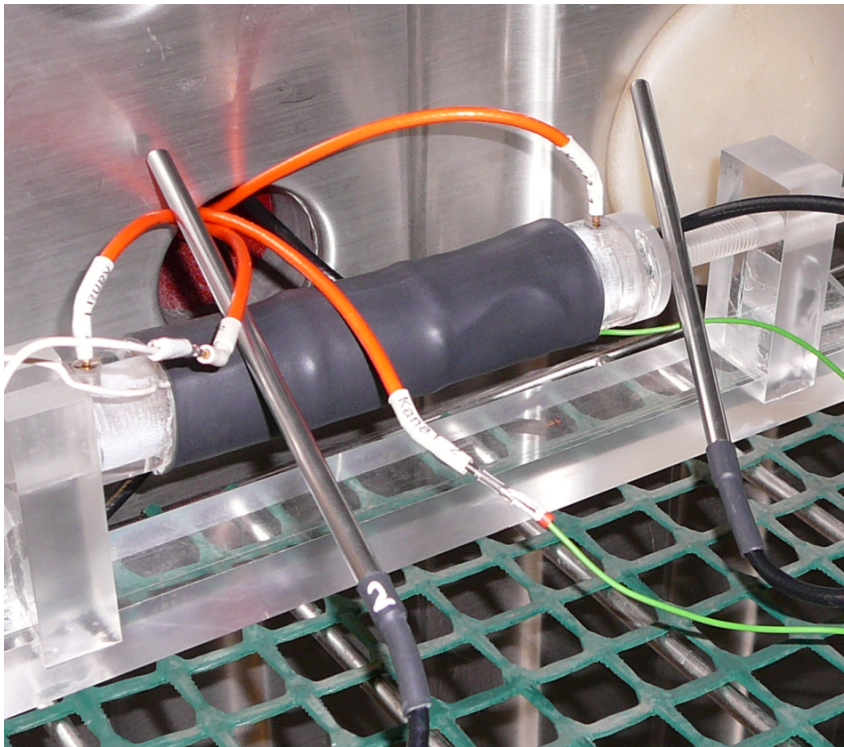
ε'' : imaginary component of ε^*



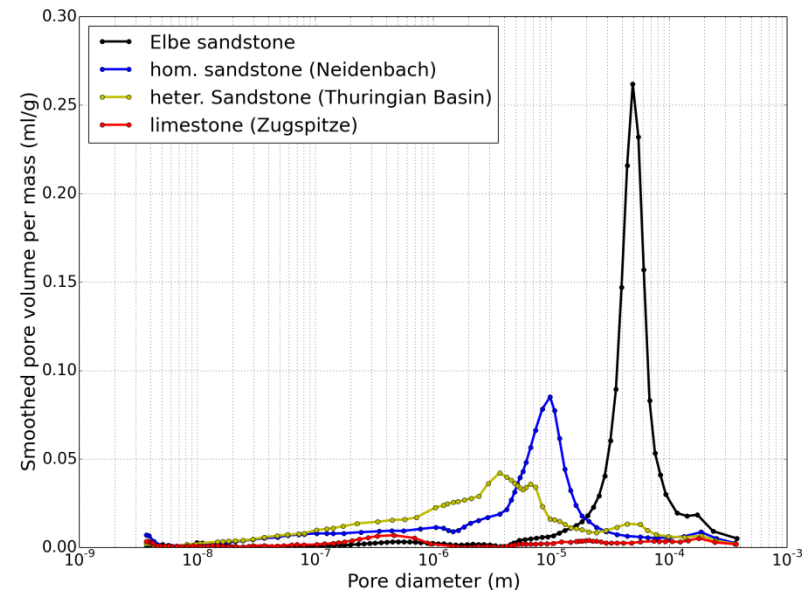
measurement range of
Spectral Induced Polarization
(SIP) method
(extension of ERT)

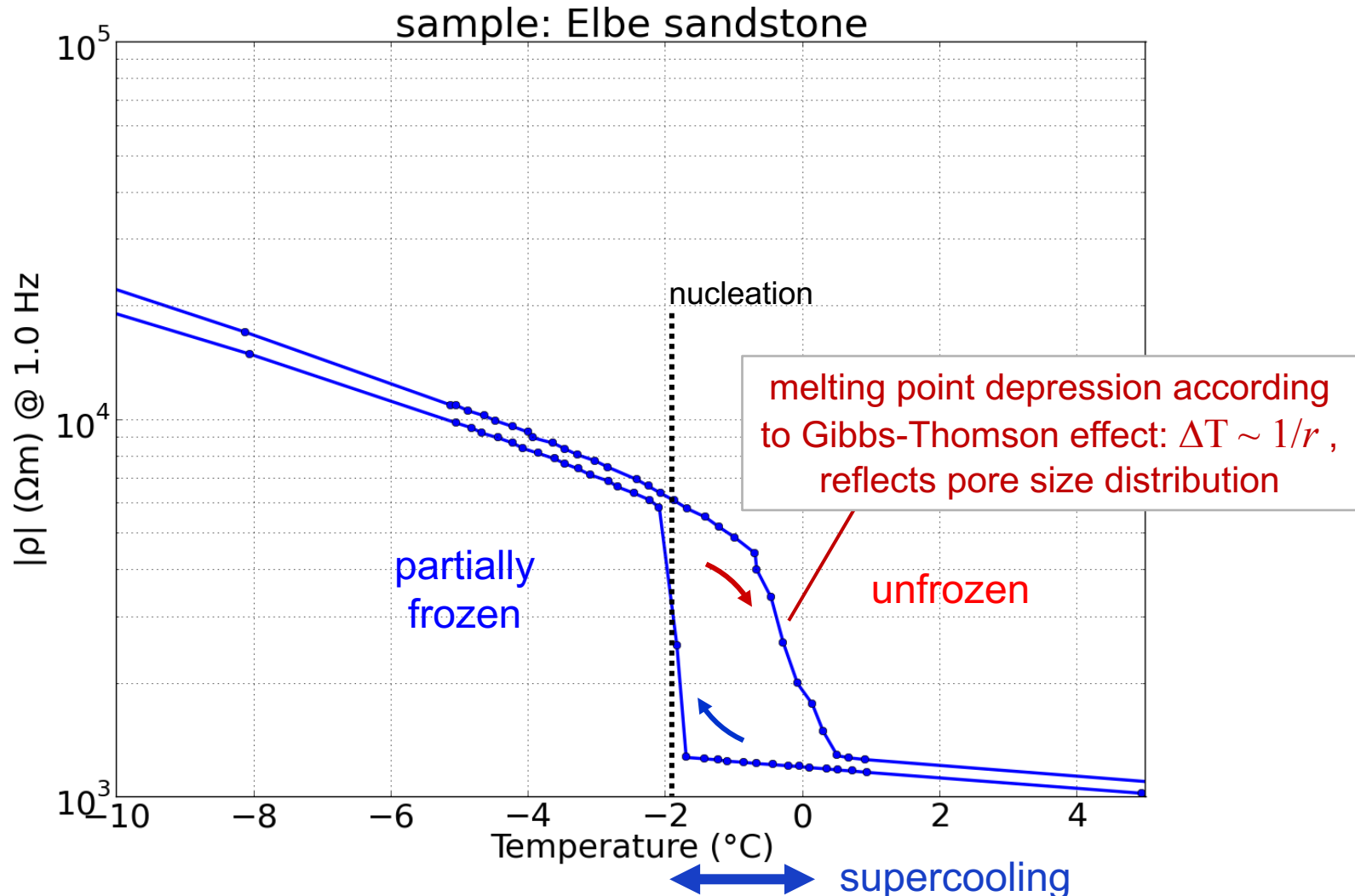
**Electrical polarization
measure of ice content?**

- SIP measurements on 6 sandstone and limestone samples (saturated with deionized water, different pore sizes/porosity)
- Frequency range: 1 mHz to 45 kHz
- +10 to −40 °C, waiting for thermal equilibrium at each temperature step



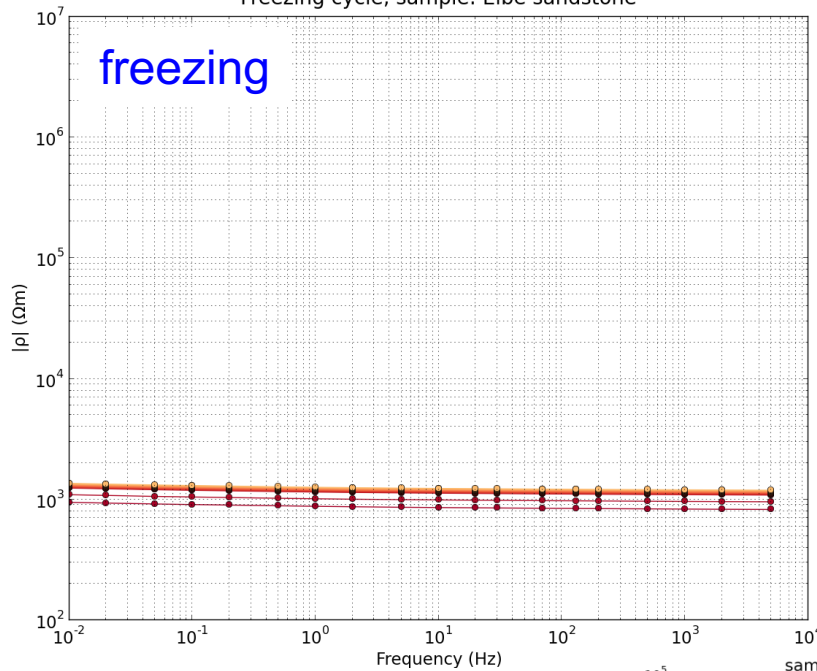
10 cm





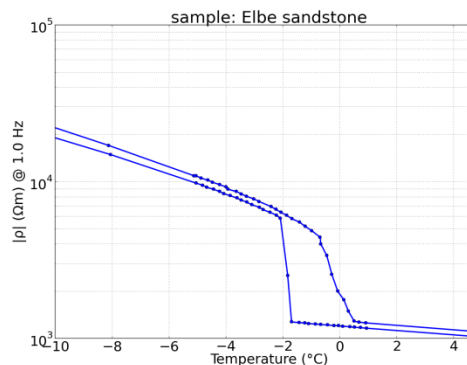
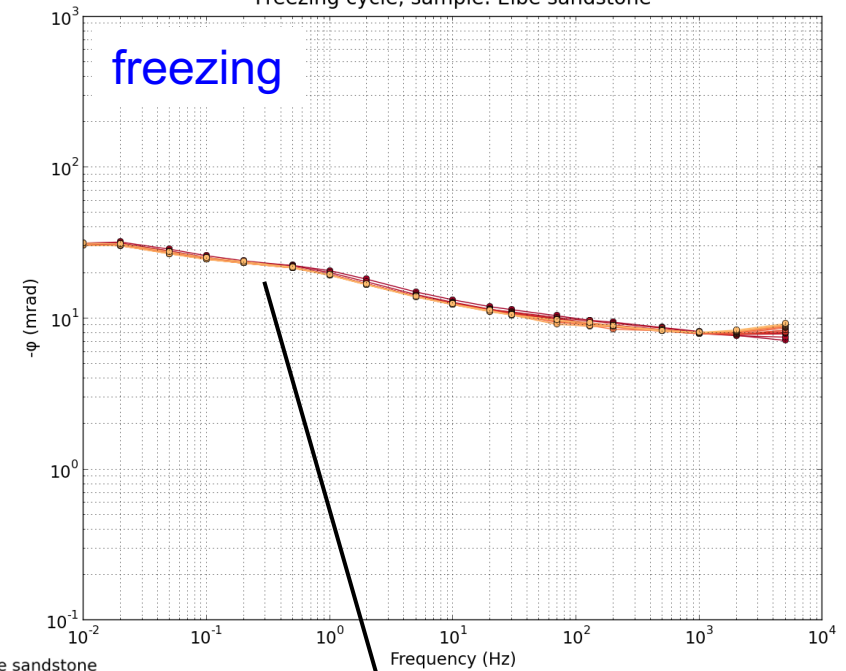
resistivity magnitude

Freezing cycle, sample: Elbe sandstone

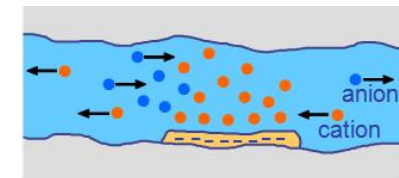


resistivity phase

Freezing cycle, sample: Elbe sandstone

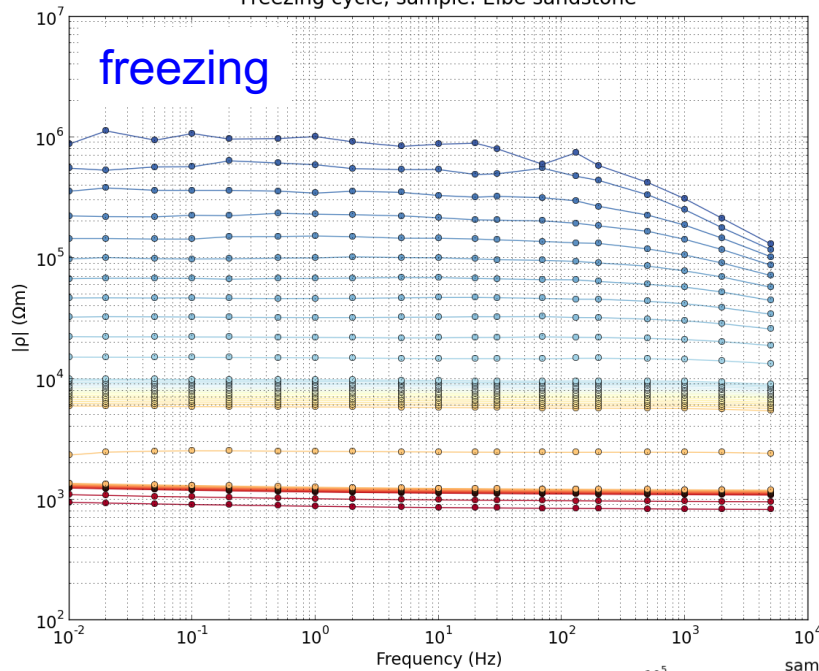


polarization at
mineral-water interfaces



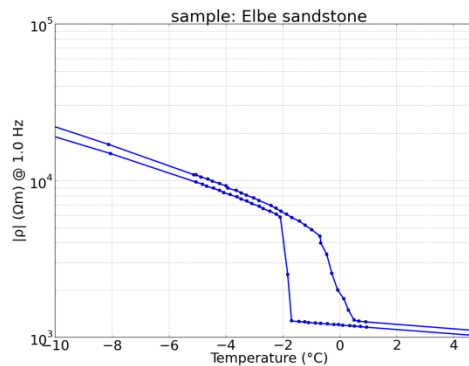
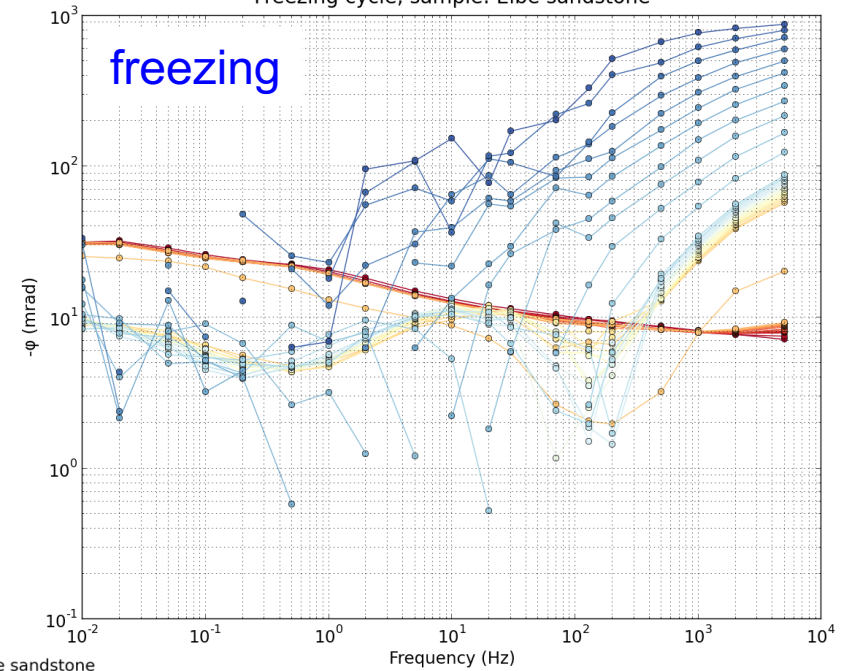
resistivity magnitude

Freezing cycle, sample: Elbe sandstone



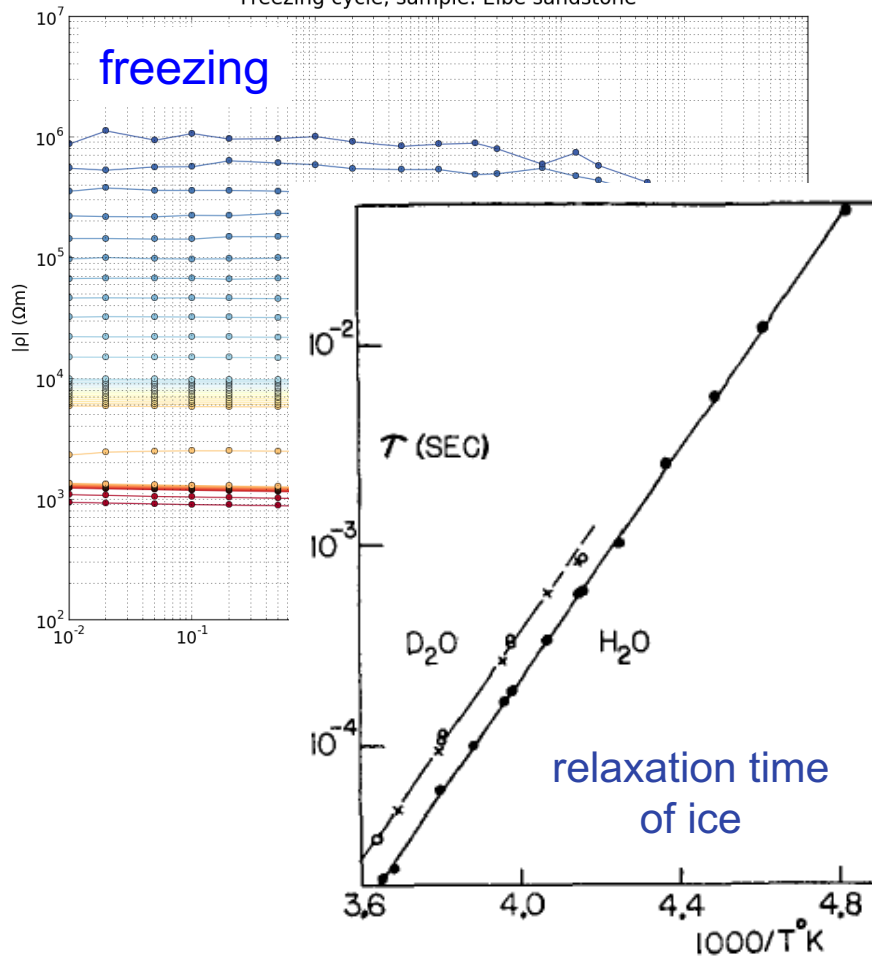
resistivity phase

Freezing cycle, sample: Elbe sandstone



resistivity magnitude

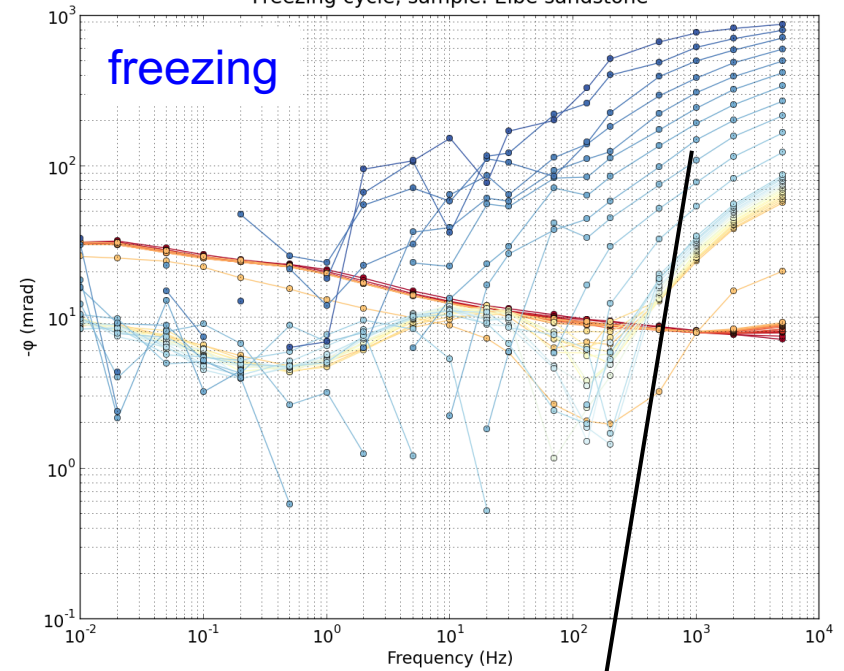
Freezing cycle, sample: Elbe sandstone



(Auty and Cole, 1952)

resistivity phase

Freezing cycle, sample: Elbe sandstone



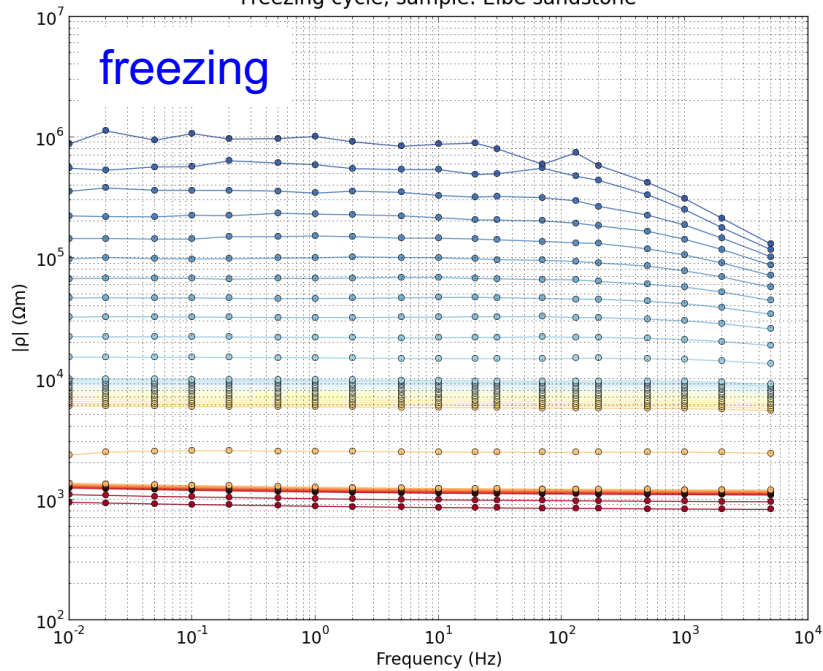
polarization response of ice

$$\sigma_{ice}^*(\omega) = \sigma_{\infty} \left(1 - \frac{m}{1 + i\omega\tau} \right)$$

(m : chargeability)

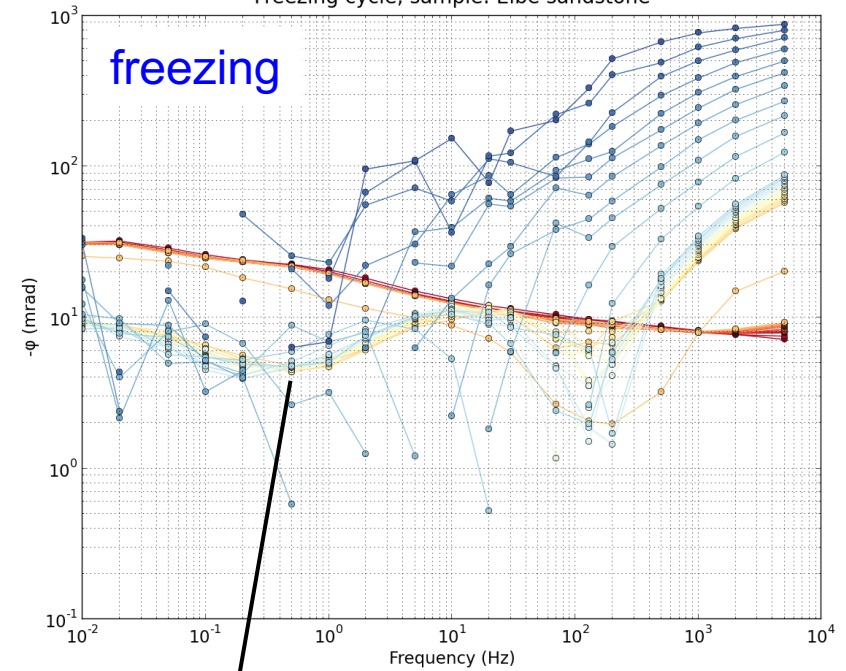
resistivity magnitude

Freezing cycle, sample: Elbe sandstone

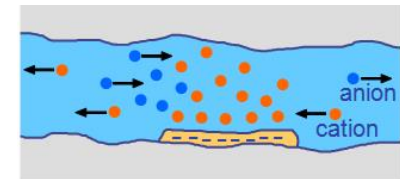


resistivity phase

Freezing cycle, sample: Elbe sandstone

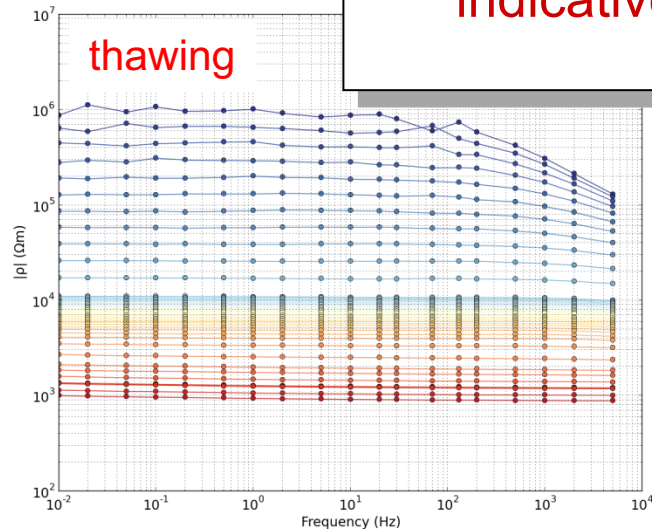
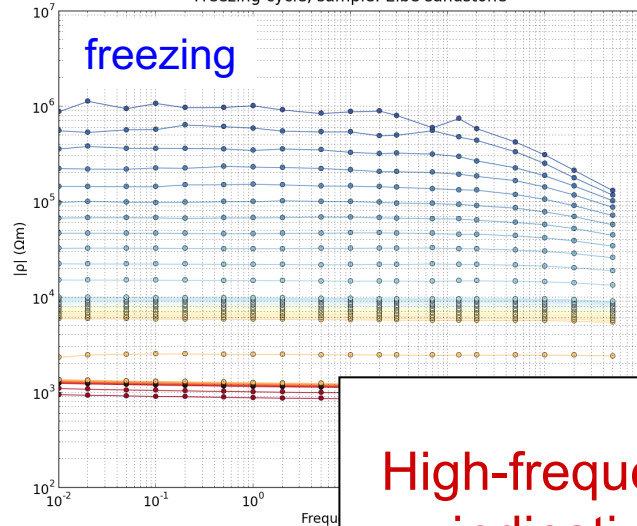


decrease of polarization at
mineral-water interfaces



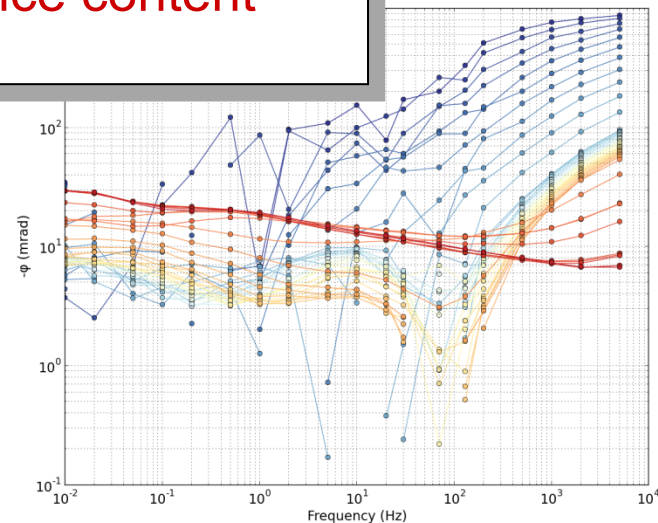
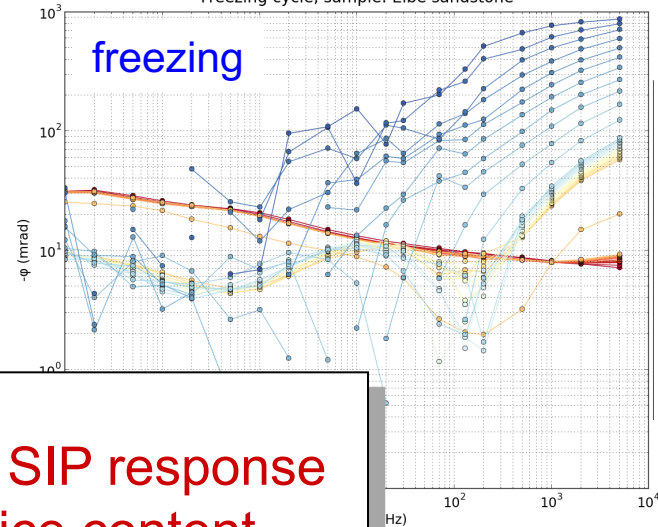
resistivity magnitude

Freezing cycle, sample: Elbe sandstone



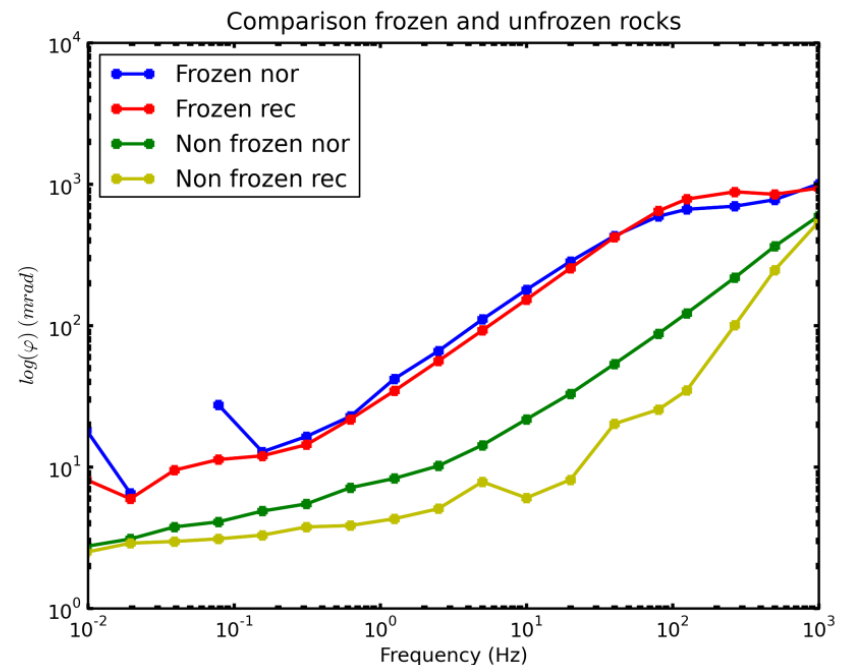
resistivity phase

Freezing cycle, sample: Elbe sandstone



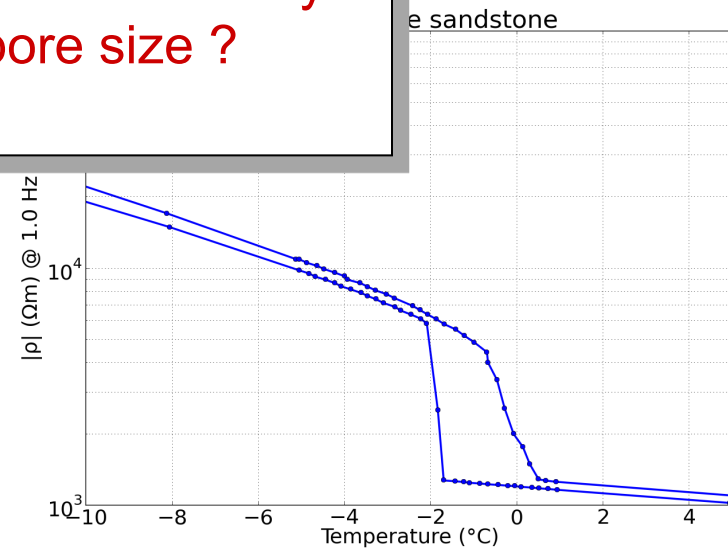
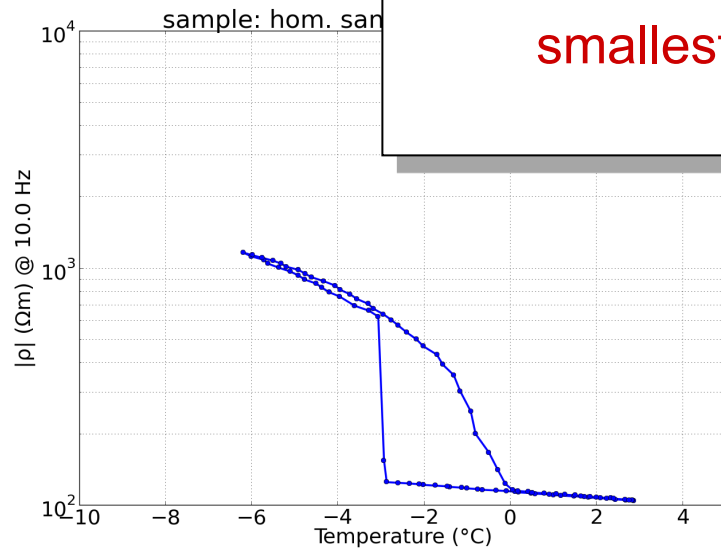
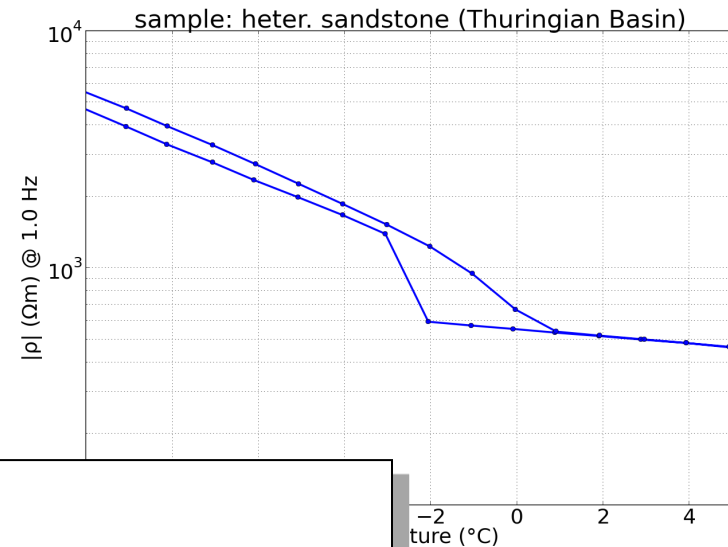
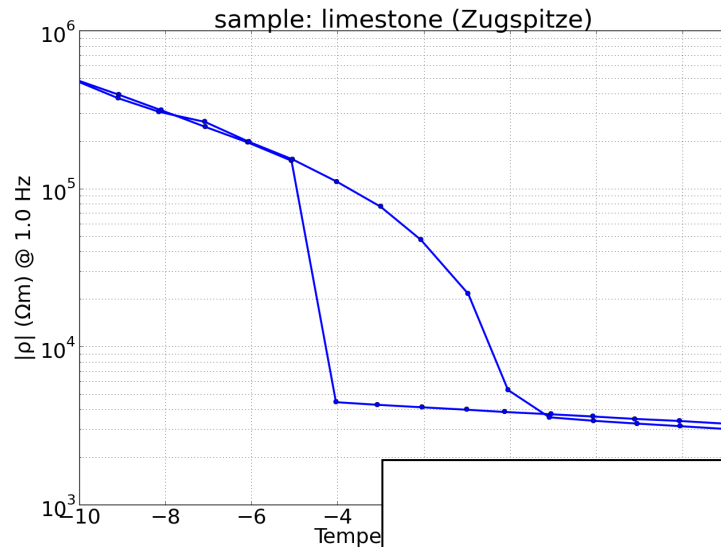
High-frequency SIP response
indicative of ice content

- Development of **SIP model** for partially frozen rocks:
 - matrix/ice/water fractions dependent on temperature and pore size (Gibbs-Thomson effect)
 - representation of polarization based on Debye decomposition into relaxation time distribution
- Analysis of **SIP field data** measured at the Zugspitze (German Alps)



- Resistivity and SIP of investigated rock samples exhibit **freeze-thaw hysteresis**
- Ice polarization response represents **indicator for thermal state** (frozen vs. unfrozen) of rocks, provides access to **presence and amount of ice**
- Hysteretic behaviour of SIP strongly depends on considered frequency due to change of spectral shape during freezing/thawing
- Electrical hysteresis must be taken into account if temperature is to be inferred from ERT/SIP images (e.g. in the course of permafrost monitoring)

Resistivity hysteresis for different samples



Ice nucleation controlled by
smallest pore size ?