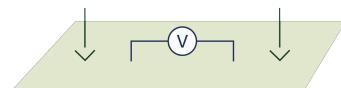
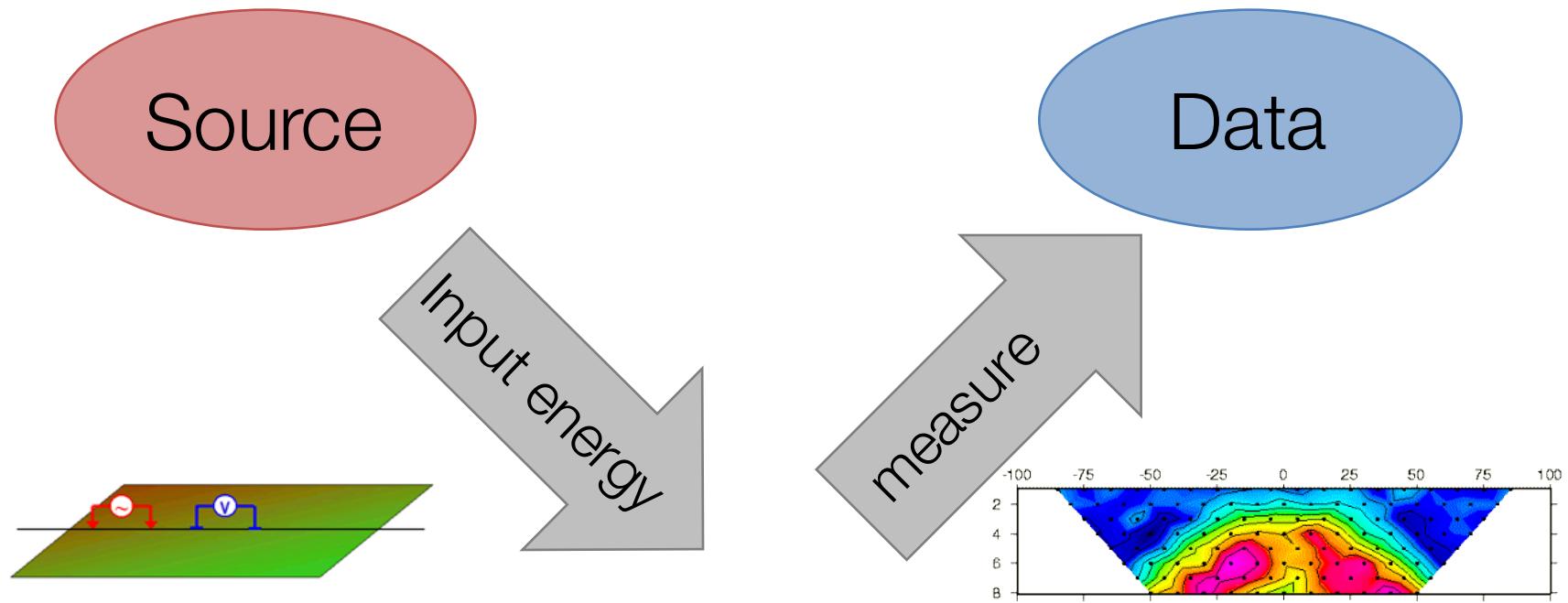


# DC Resistivity



# DC Resistivity Survey



$$\rho$$

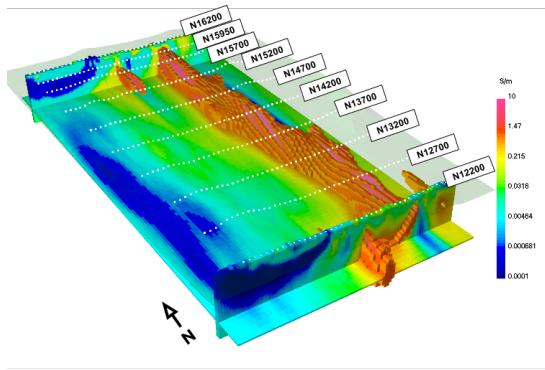
$$\rho = 1/\sigma$$

$\rho$  : resistivity

$\sigma$  : electrical conductivity

# Motivation

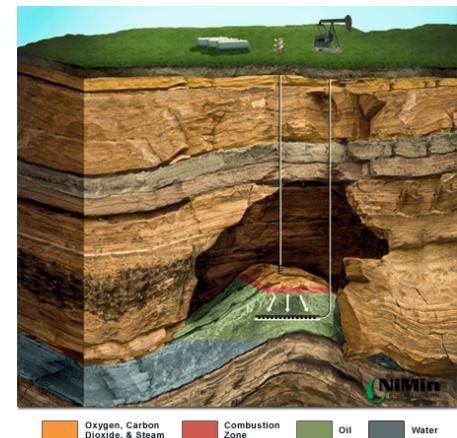
Minerals



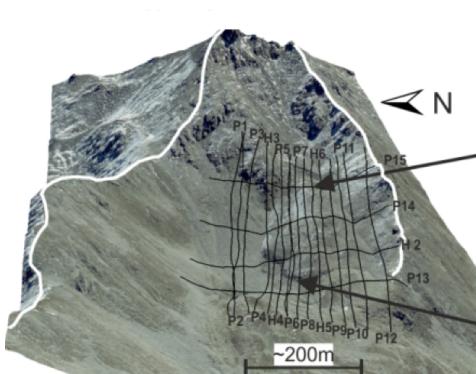
Water inflow in mine



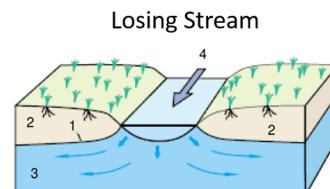
Oil and Gas



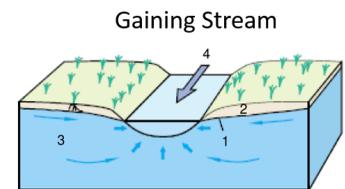
Geotechnical



Groundwater

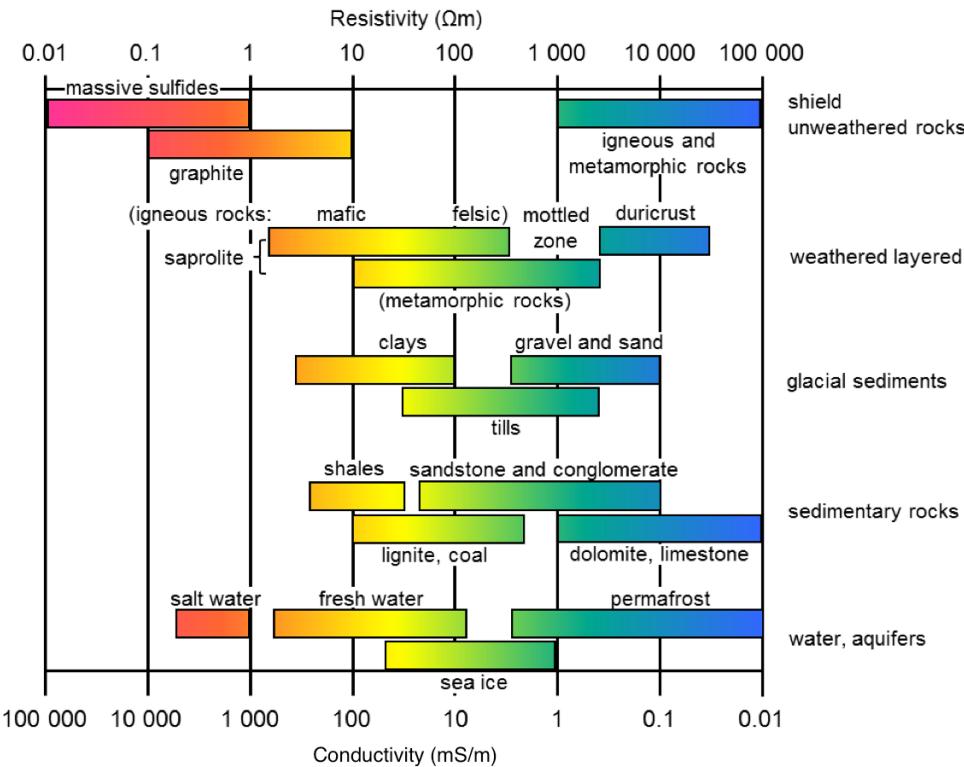


1 – Water table    2 – Unsaturated zone    3 – Saturated zone    4 – Flow direction



# Electrical conductivity

- DC resistivity is sensitive to:
  - $\sigma$ : Conductivity [S/m]
  - $\rho$ : Resistivity [ $\Omega\text{m}$ ]
  - $\sigma = 1/\rho$
- Varies over many orders of magnitude
- Depends on many factors:
  - Rock type
  - Porosity
  - Connectivity of pores
  - Nature of the fluid
  - Metallic content of the solid matrix



# Outline

- Basic experiment
- Currents, charges, potentials and apparent resistivities
- Soundings, profiles and arrays
- Data, pseudosections and inversion
- Sensitivity
- Survey Design
- Case History – Mt Isa
- Effects of background resistivity

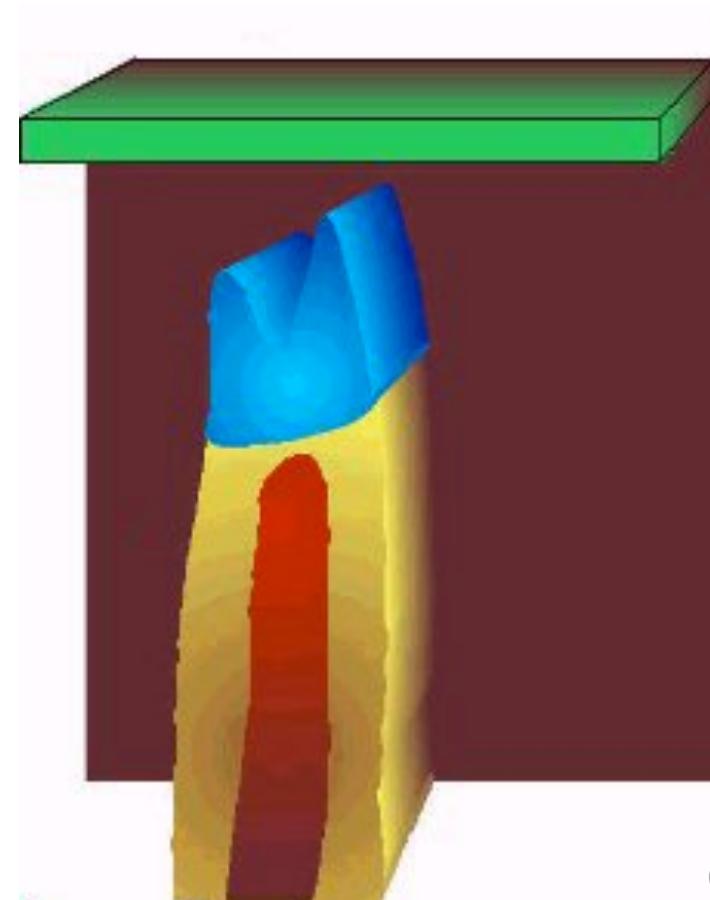
# Basic Experiment

- **Target:**

- Ore body. Mineralized regions less resistive than host

Elura Orebody Electrical resistivities

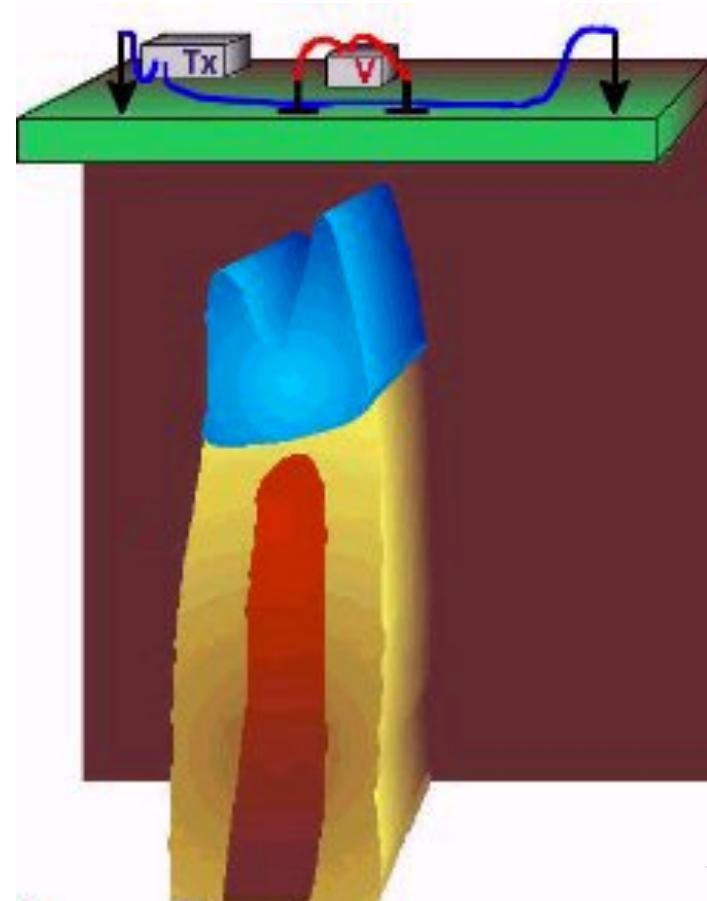
Rock Type	Ohm-m
Overburden	12
Host rocks	200
Gossan	420
Mineralization (pyritic)	0.6
Mineralization (pyrrhotite)	0.6



# Basic Experiment

- **Target:**
  - Ore body. Mineralized regions less resistive than host
- **Setup:**
  - Tx: Current electrodes
  - Rx: Potential electrodes

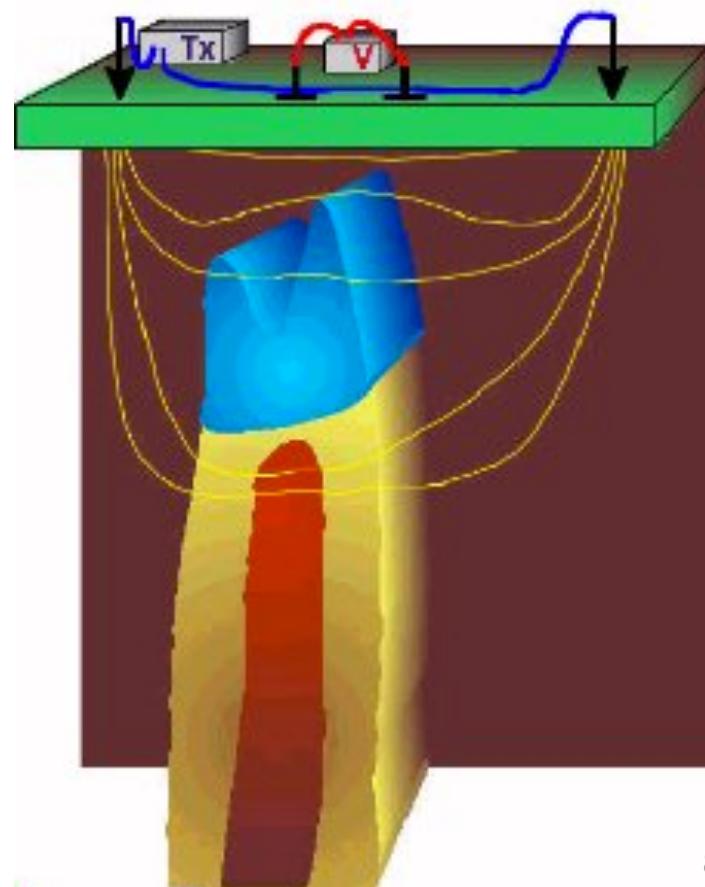
Elura Orebody Electrical resistivities	
Rock Type	Ohm-m
Overburden	12
Host rocks	200
Gossan	420
Mineralization (pyritic)	0.6
Mineralization (pyrrhotite)	0.6



# Basic Experiment

- **Target:**
  - Ore body. Mineralized regions less resistive than host
- **Setup:**
  - Tx: Current electrodes
  - Rx: Potential electrodes
- **Currents:**
  - Preferentially flow through conductors

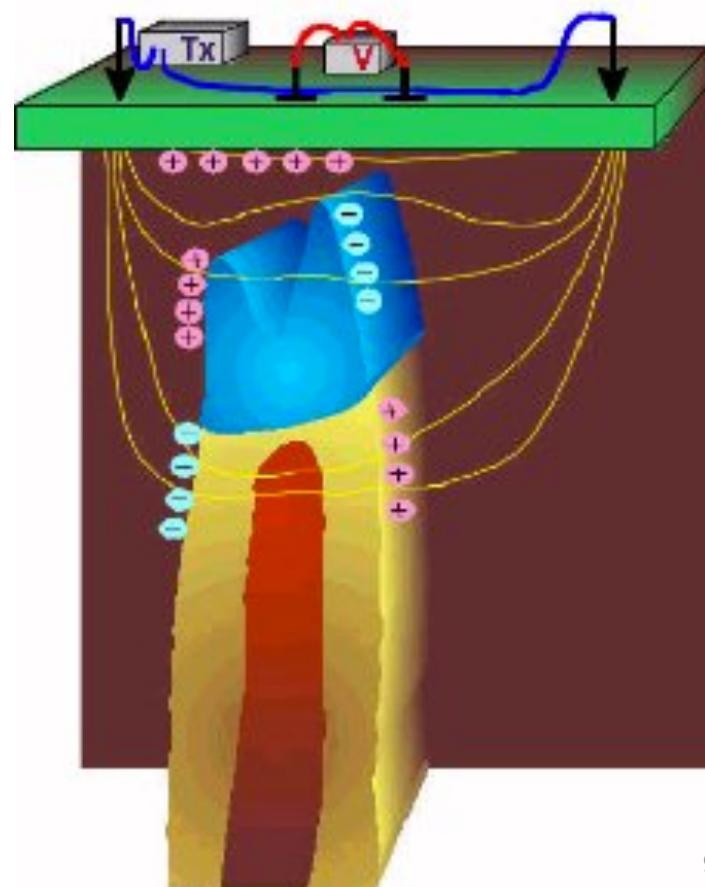
Elura Orebody Electrical resistivities	
Rock Type	Ohm-m
Overburden	12
Host rocks	200
Gossan	420
Mineralization (pyritic)	0.6
Mineralization (pyrrhotite)	0.6



# Basic Experiment

- **Target:**
  - Ore body. Mineralized regions less resistive than host
- **Setup:**
  - Tx: Current electrodes
  - Rx: Potential electrodes
- **Currents:**
  - Preferentially flow through conductors
- **Charges:**
  - Build up at interfaces

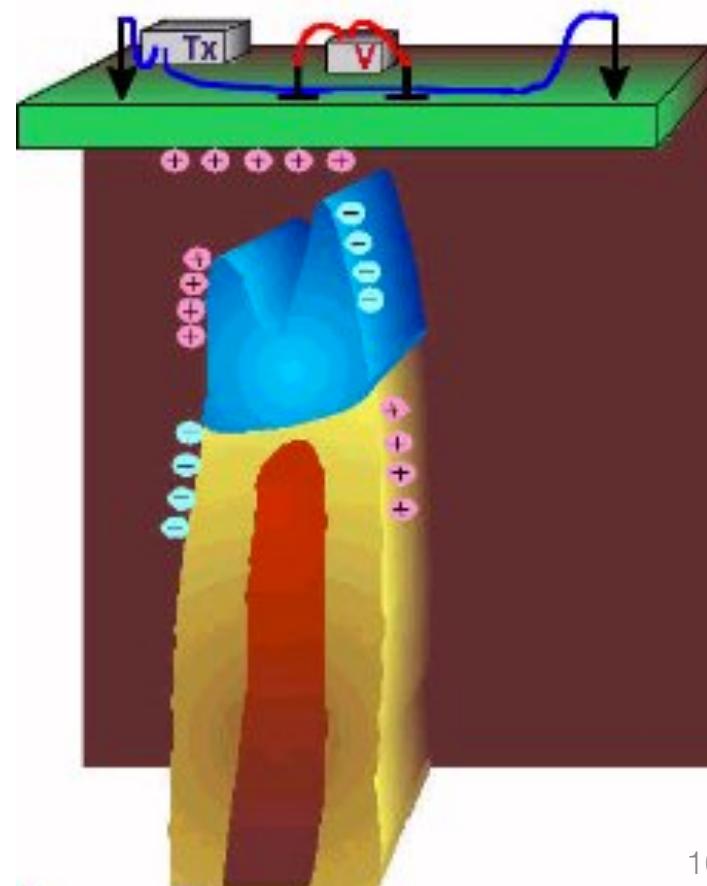
Elura Orebody Electrical resistivities	
Rock Type	Ohm-m
Overburden	12
Host rocks	200
Gossan	420
Mineralization (pyritic)	0.6
Mineralization (pyrrhotite)	0.6



# Basic Experiment

- **Target:**
  - Ore body. Mineralized regions less resistive than host
- **Setup:**
  - Tx: Current electrodes
  - Rx: Potential electrodes
- **Currents:**
  - Preferentially flow through conductors
- **Charges:**
  - Build up at interfaces
- **Potentials:**
  - Associated with the charges are measured at the surface

Elura Orebody Electrical resistivities	
Rock Type	Ohm-m
Overburden	12
Host rocks	200
Gossan	420
Mineralization (pyritic)	0.6
Mineralization (pyrrhotite)	0.6



How do we obtain resistivity?

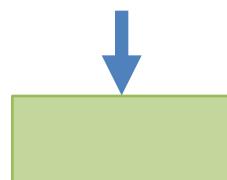
# Steady State Maxwell equations

	Full	Steady State
Faraday	$\nabla \times \vec{e} = -\frac{\partial \vec{b}}{\partial t}$	$\nabla \times \vec{e} = 0 \quad \vec{e} = -\nabla V$
Ampere	$\nabla \times \vec{h} = \vec{j} + \frac{\partial \vec{d}}{\partial t} + \vec{j}_s$	$\nabla \cdot \vec{j} = -\nabla \cdot \vec{j}_s$
Ohm's Law	$\vec{j} = \sigma \vec{e}$	

Put it together

$$\nabla \cdot \sigma \nabla V = I \delta(r)$$

Potential in a  
homogeneous halfspace



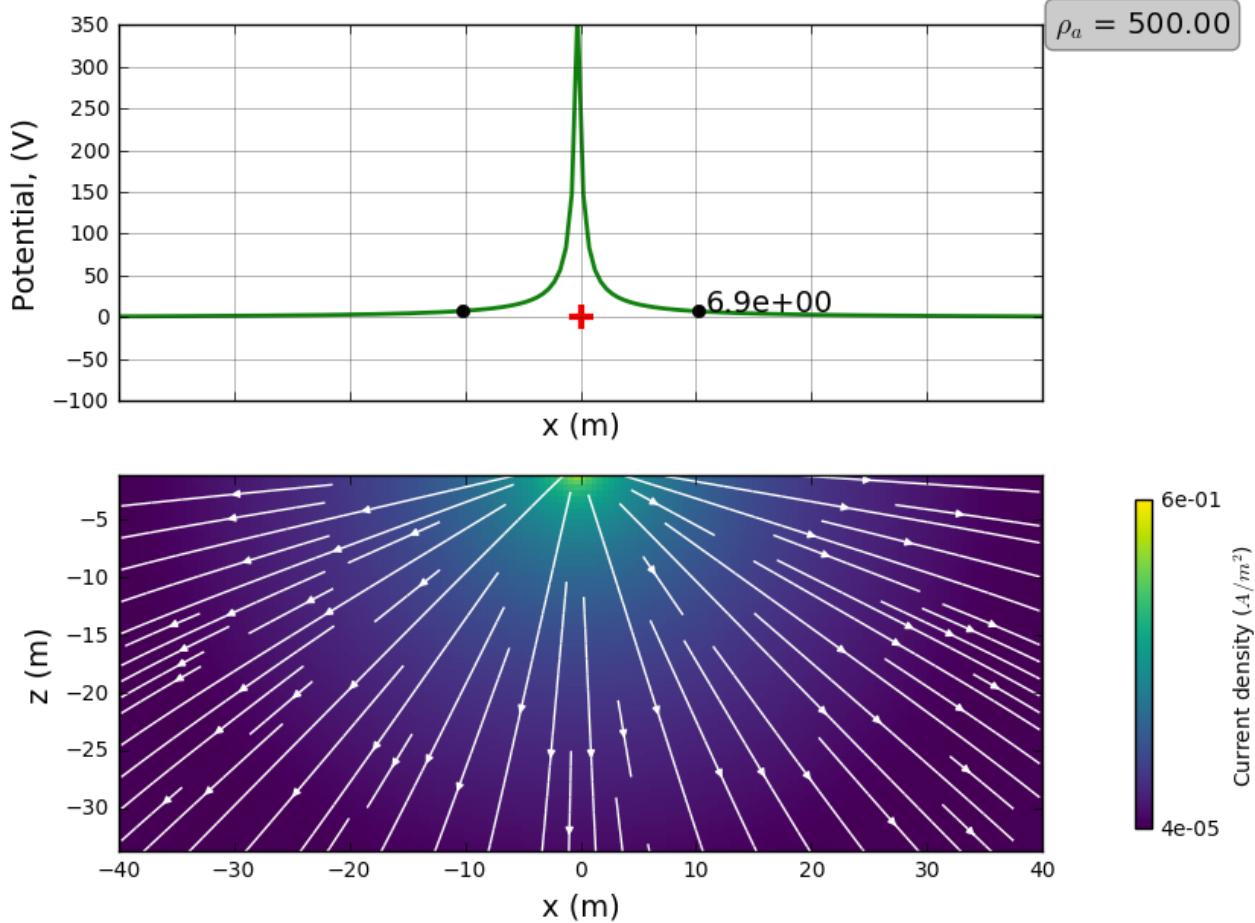
$$V = \frac{I}{2\pi\sigma} \frac{1}{r}$$

$$V = \frac{\rho I}{2\pi r}$$

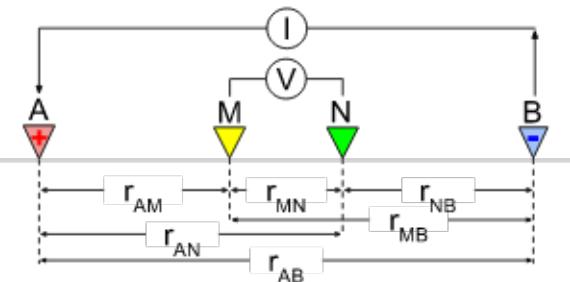
# Currents and potentials: halfspace

$$V = \frac{\rho I}{2\pi r}$$

$$\rho = \frac{2\pi r V}{I}$$



# Currents and potentials: 4-electrode array

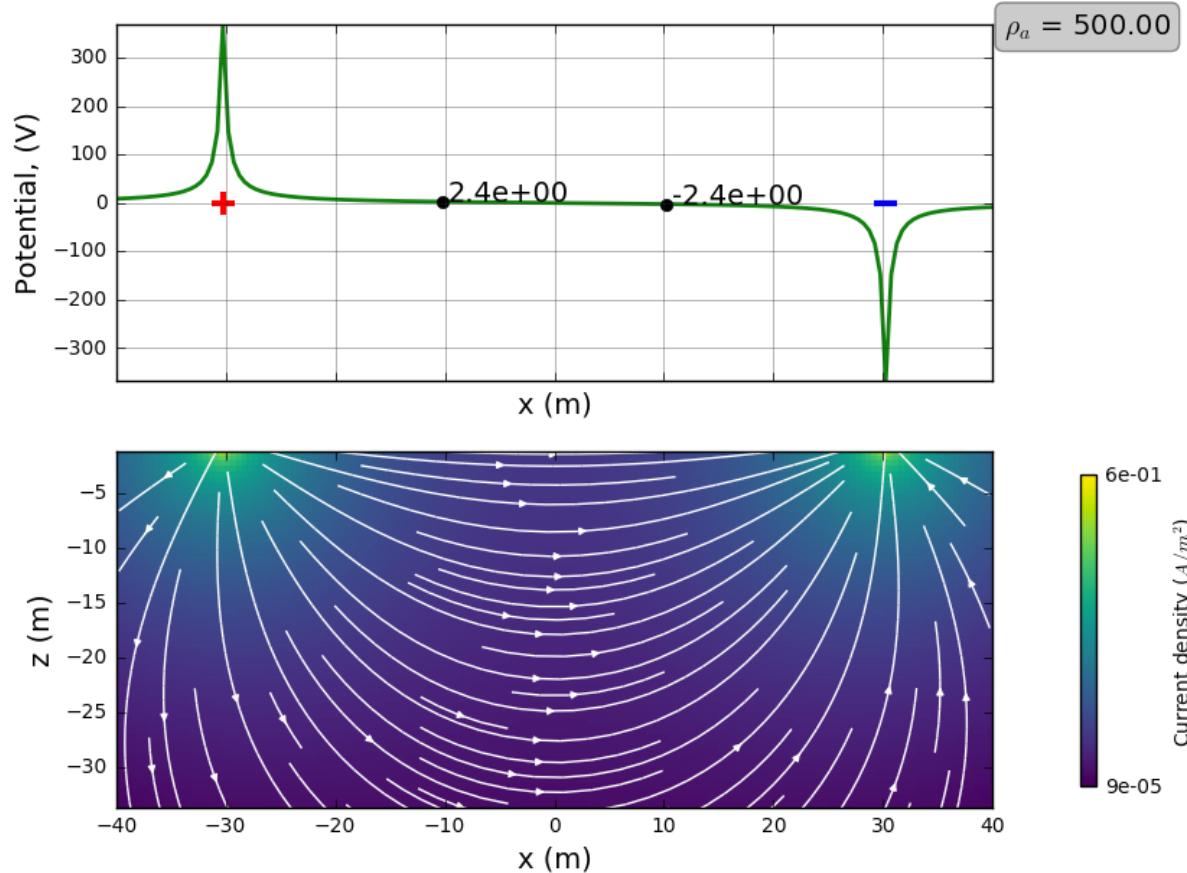


$$\Delta V_{MN} = \rho I \underbrace{\frac{1}{2\pi} \left[ \frac{1}{AM} - \frac{1}{MB} - \frac{1}{AN} + \frac{1}{NB} \right]}_G$$

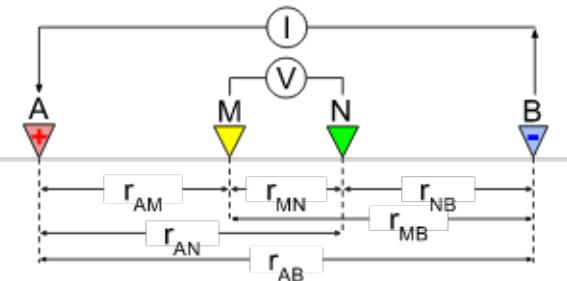
Resistivity

$$\rho = \frac{\Delta V_{MN}}{IG}$$

Halfspace ( $500 \Omega m$ )



# Currents and Apparent Resistivity

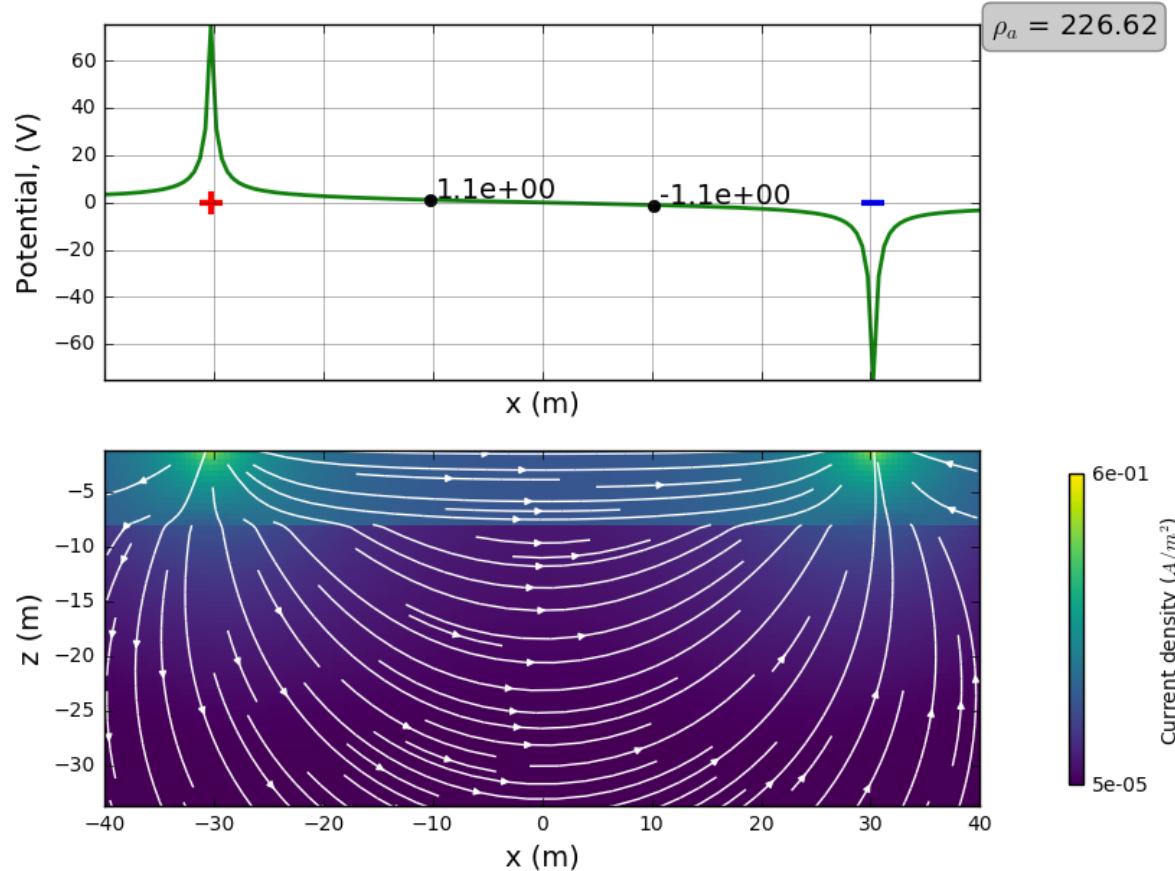


$$\Delta V_{MN} = \rho I \underbrace{\frac{1}{2\pi} \left[ \frac{1}{AM} - \frac{1}{MB} - \frac{1}{AN} + \frac{1}{NB} \right]}_G$$

Apparent resistivity

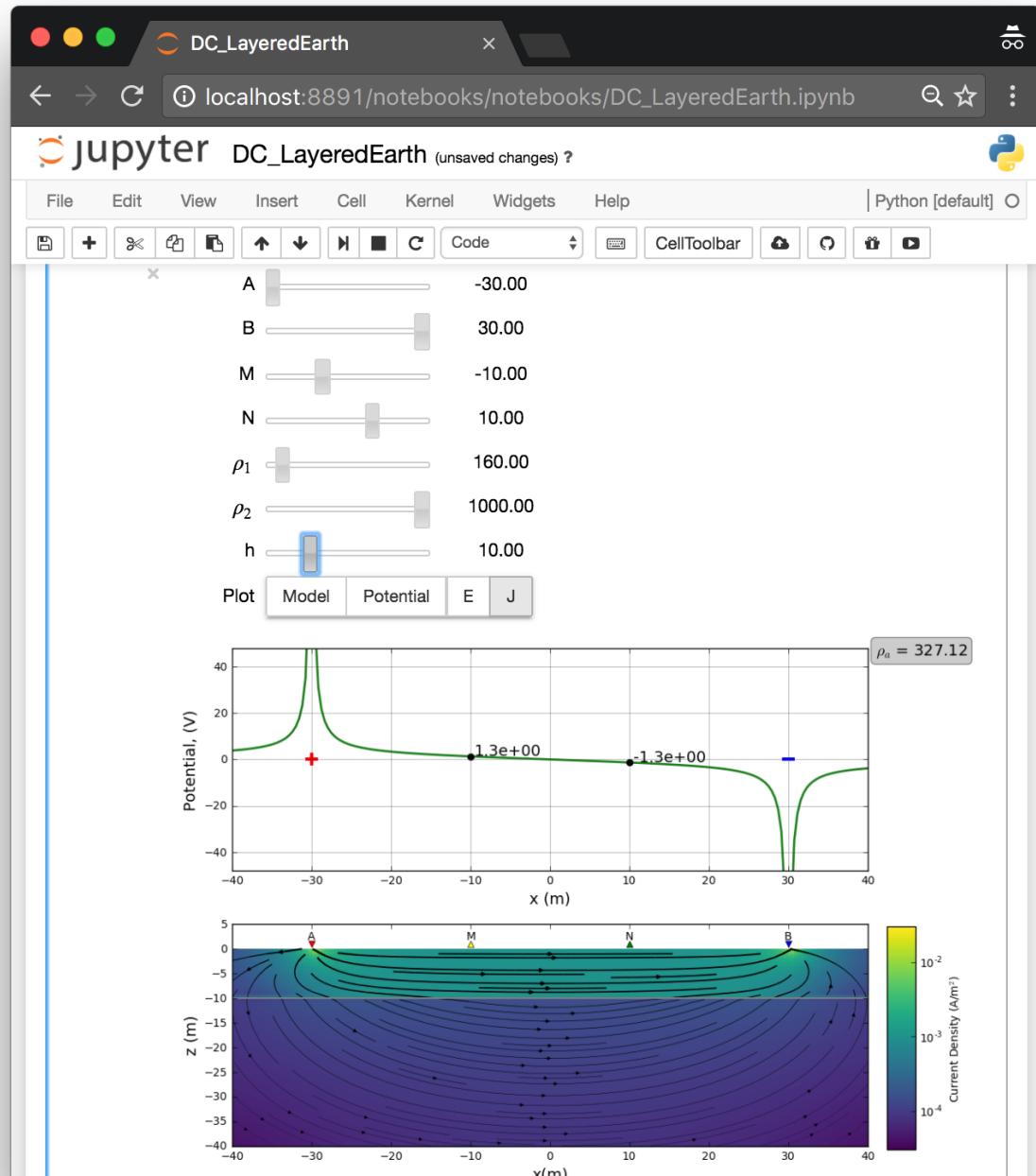
$$\rho_a = \frac{\Delta V_{MN}}{IG}$$

Conductive overburden ( $100 \Omega m$ )



# Why interactive apps?

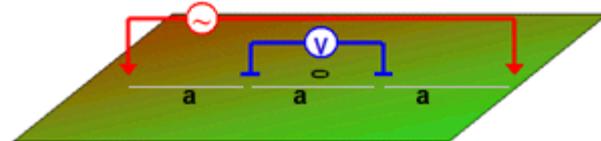
- Visualization aids understanding
- Learn through interaction
  - ask questions and investigate
- Open source:
  - Free to use
  - Welcome contributions!



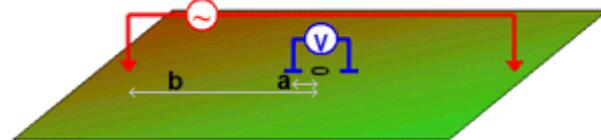
# Soundings and Arrays

Geometry

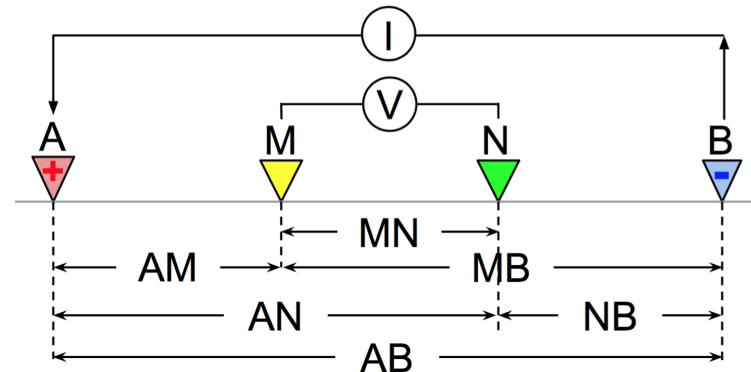
Wenner



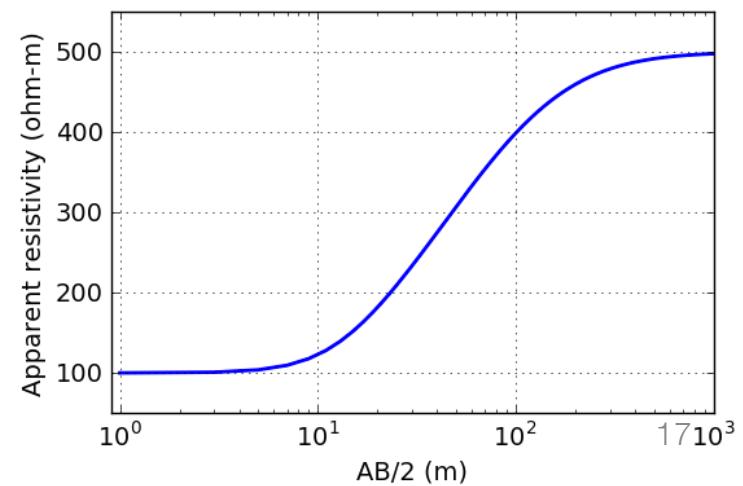
Schlumberger



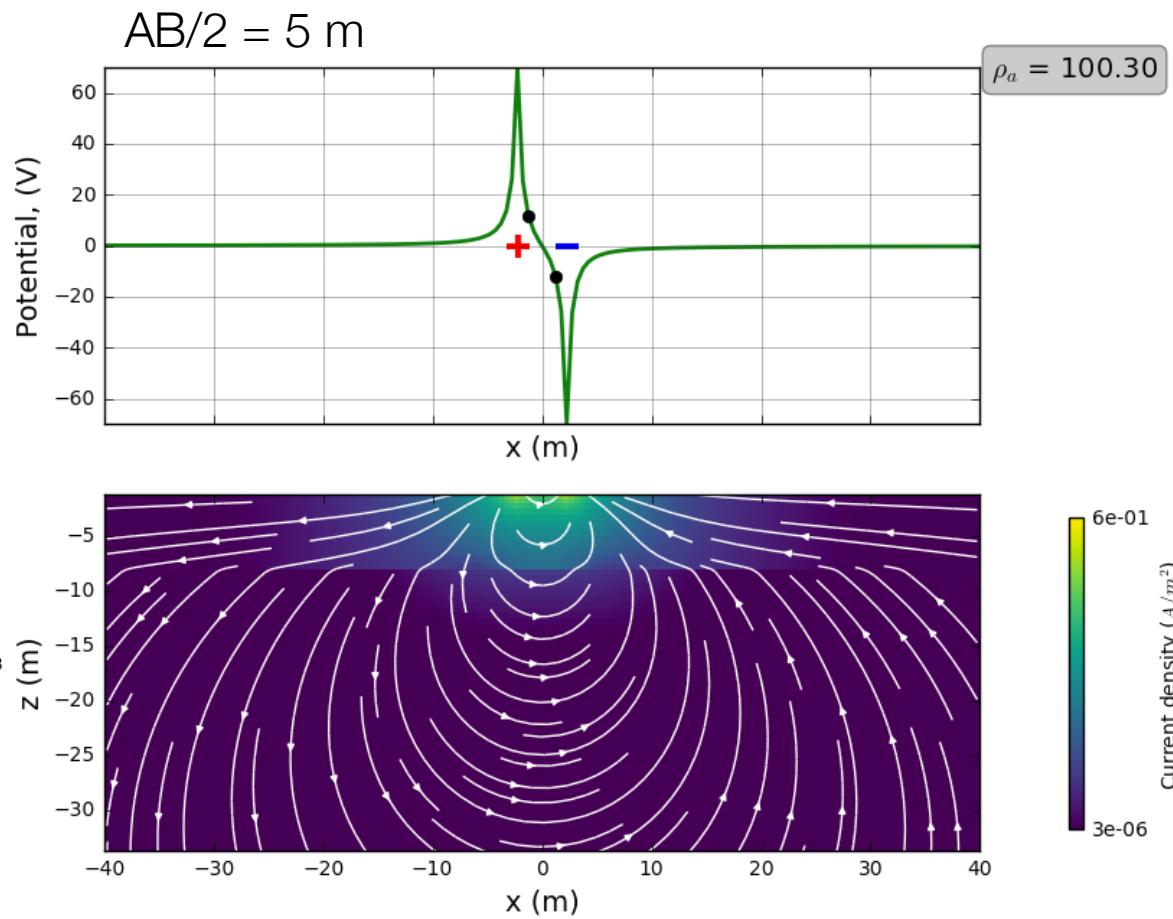
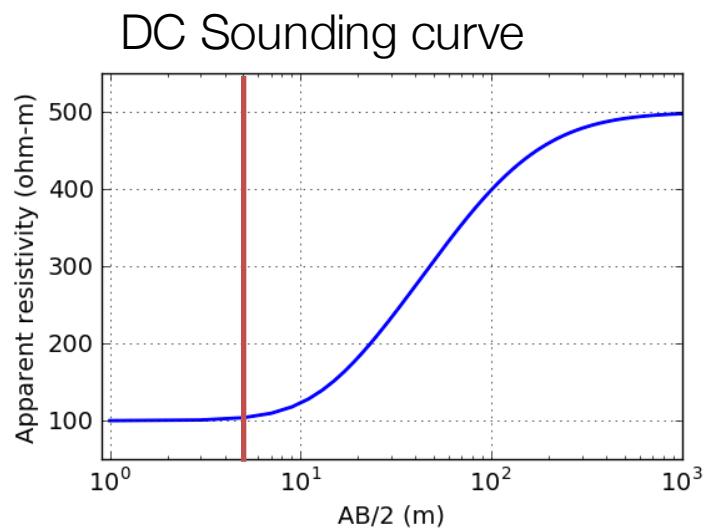
4 electrode Array



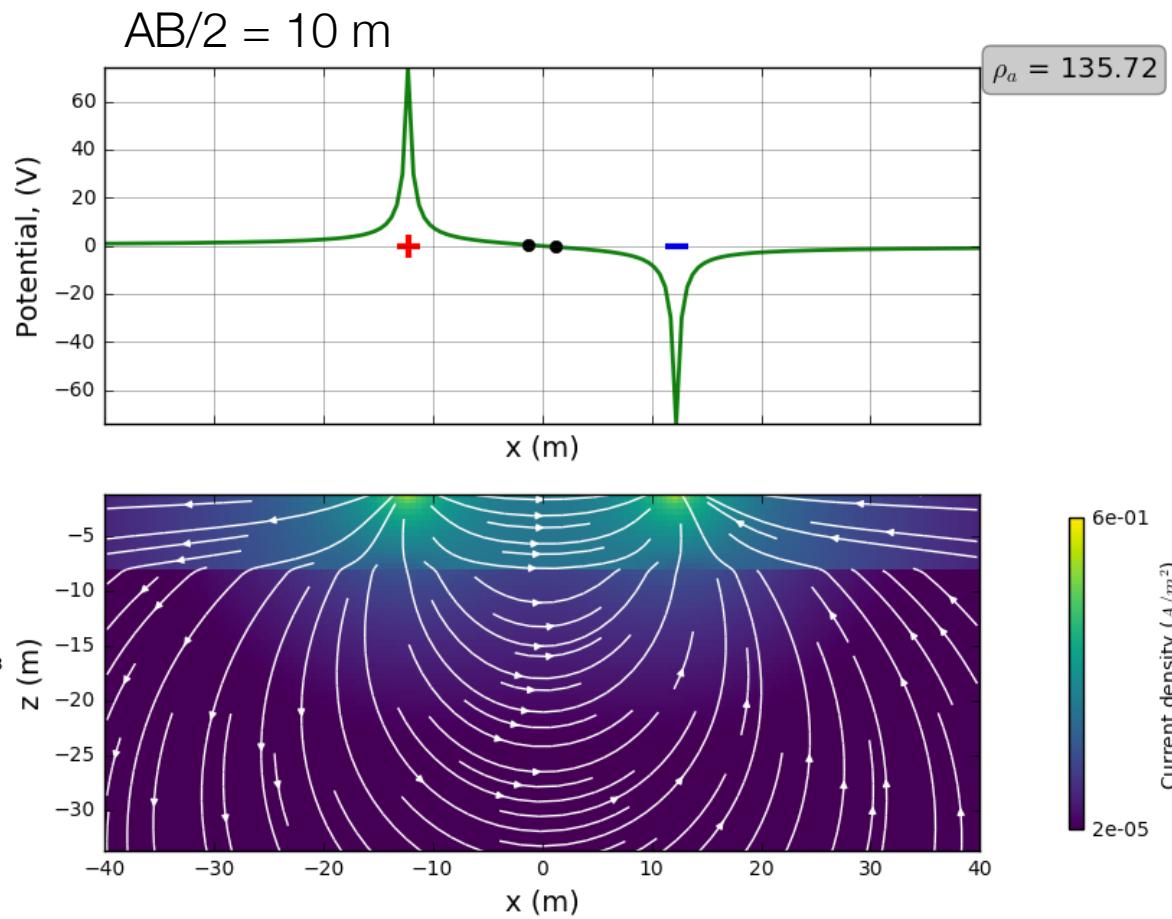
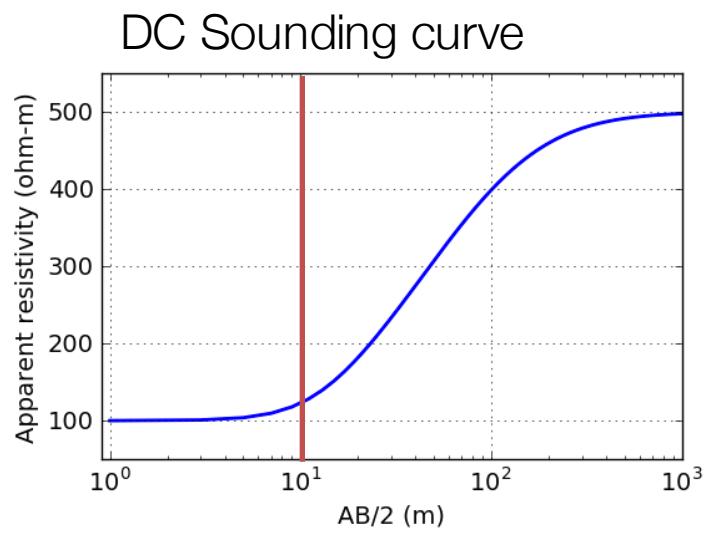
Sounding



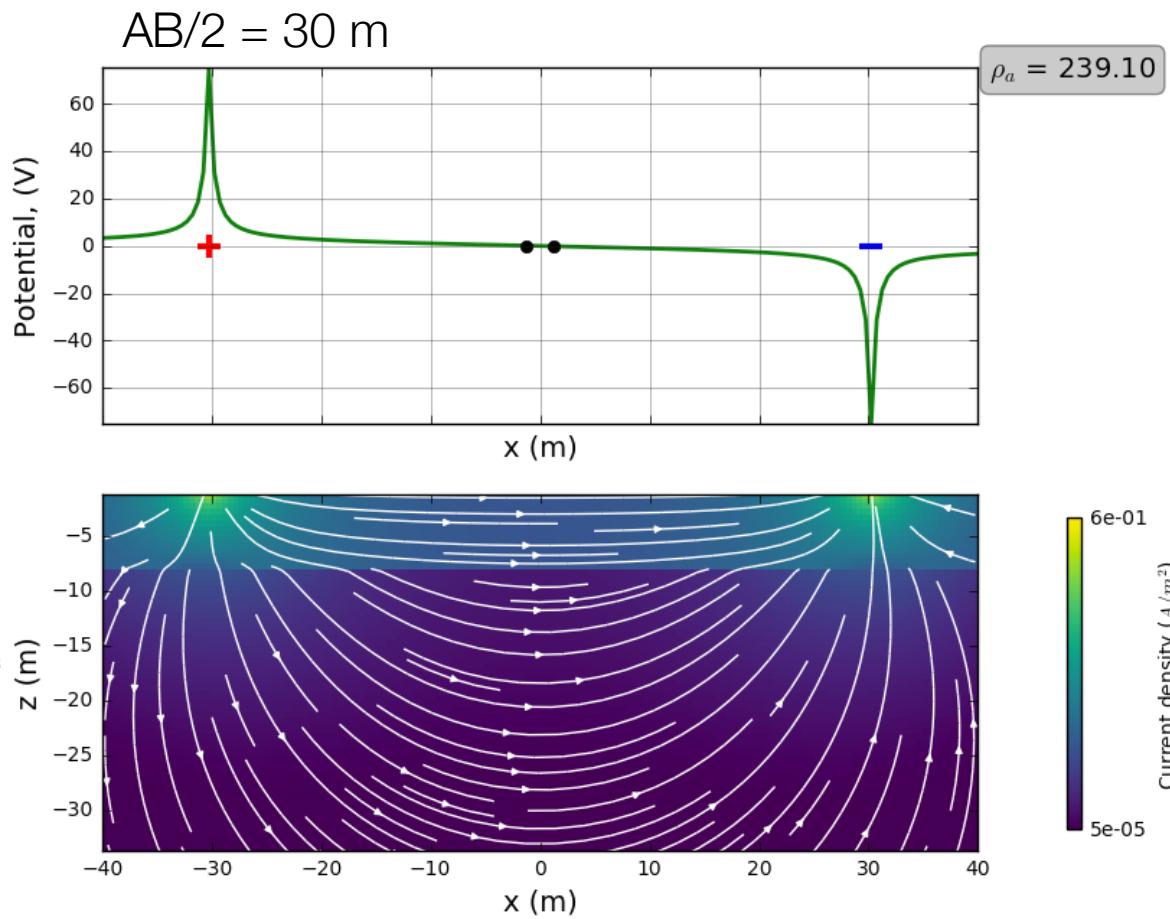
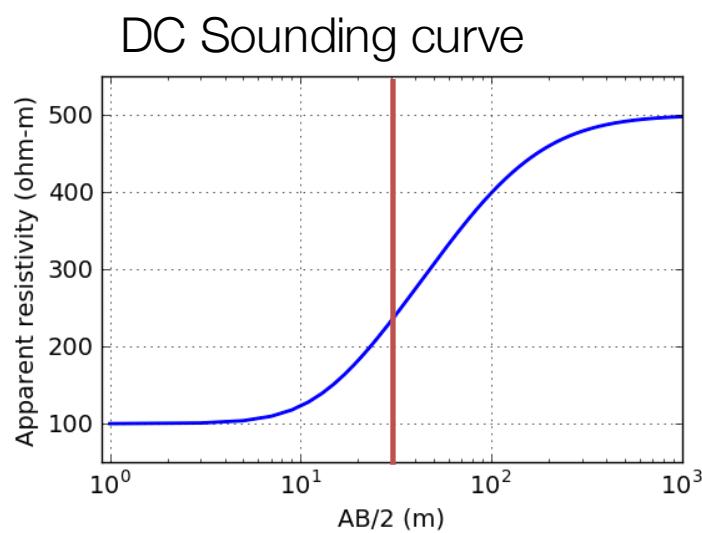
# Soundings



# Soundings

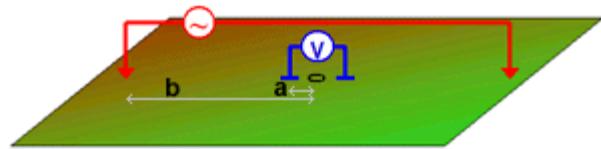


# Soundings

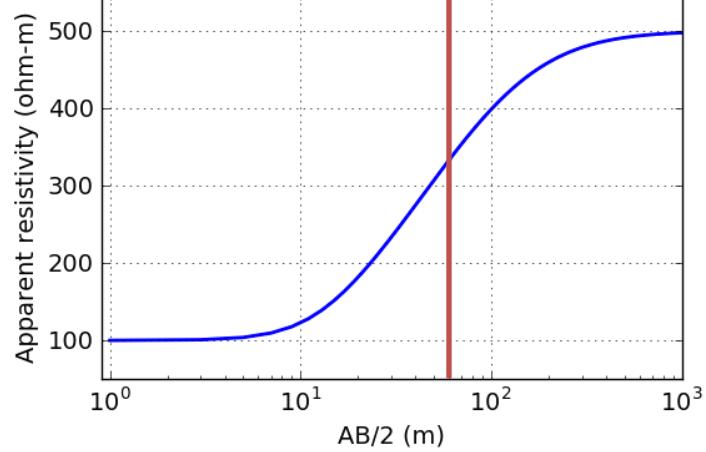


# Summary: soundings

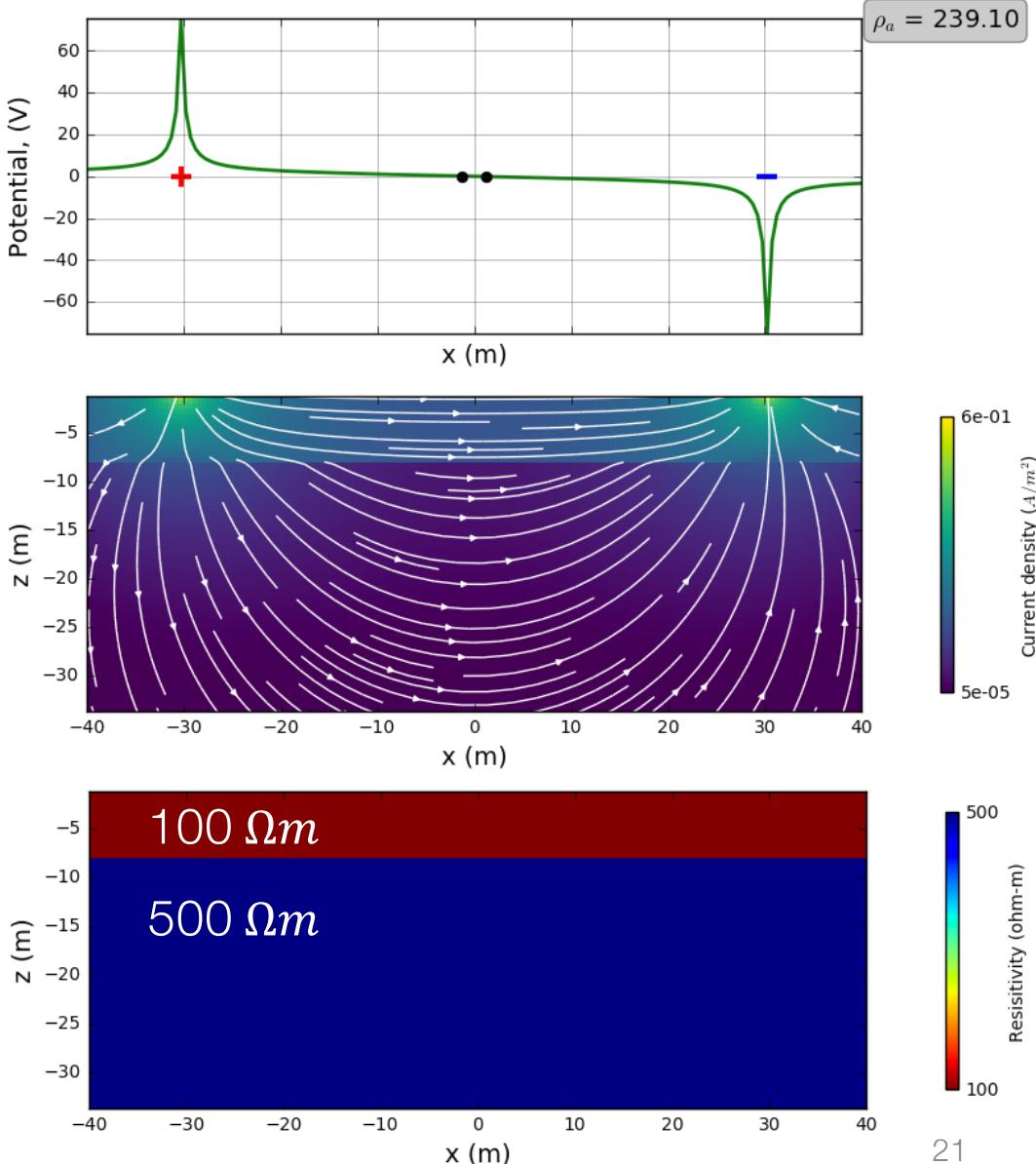
Schlumberger array



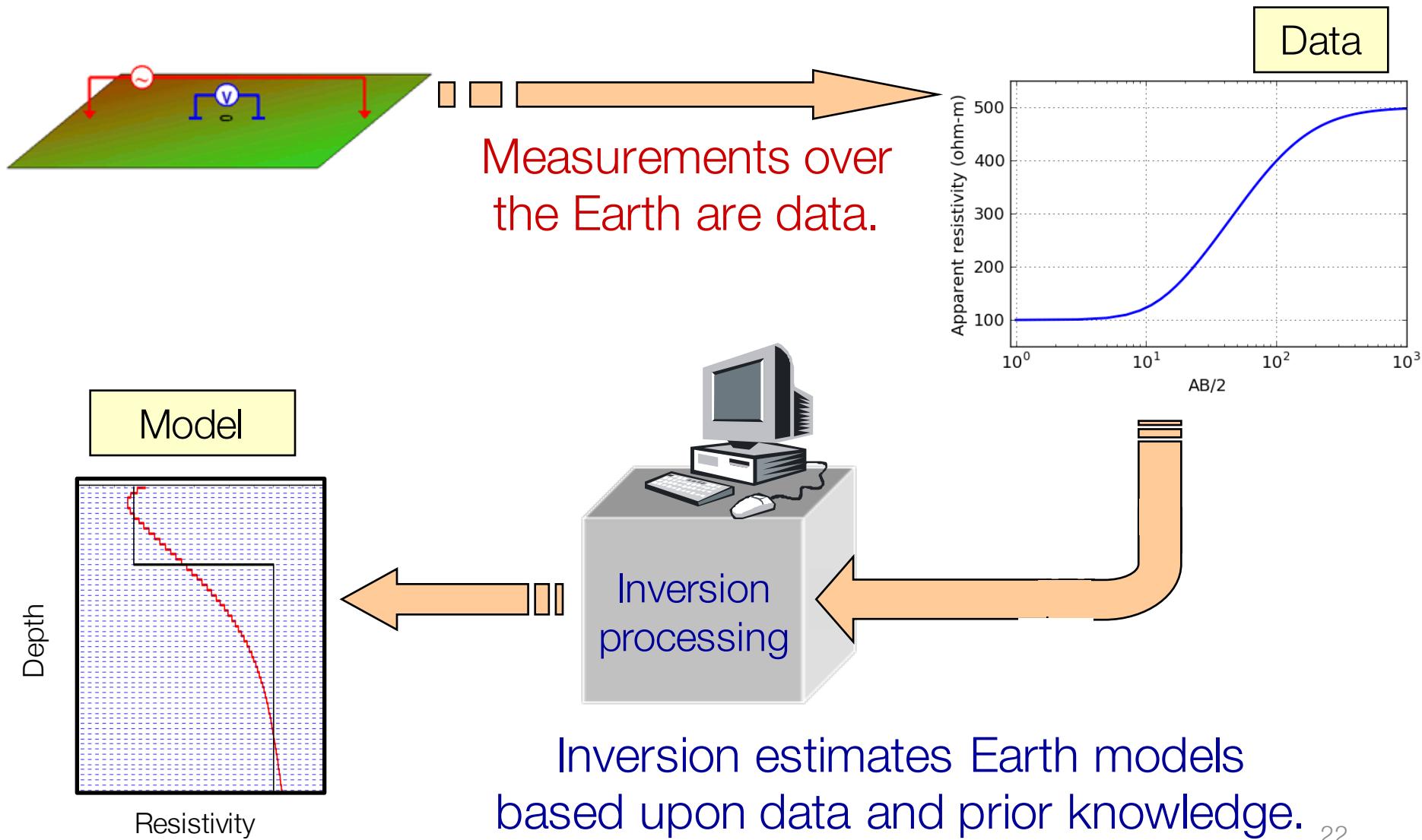
DC Sounding curve



Scale length of array must be large to see deep



# Inversion



# DCR for a confined body

- Useful to formally bring in the concept of charges

Normal component of current density is continuous

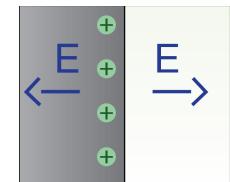
$$J_{1n} = J_{2n}$$

$$\sigma_1 E_{1n} = \sigma_2 E_{2n}$$

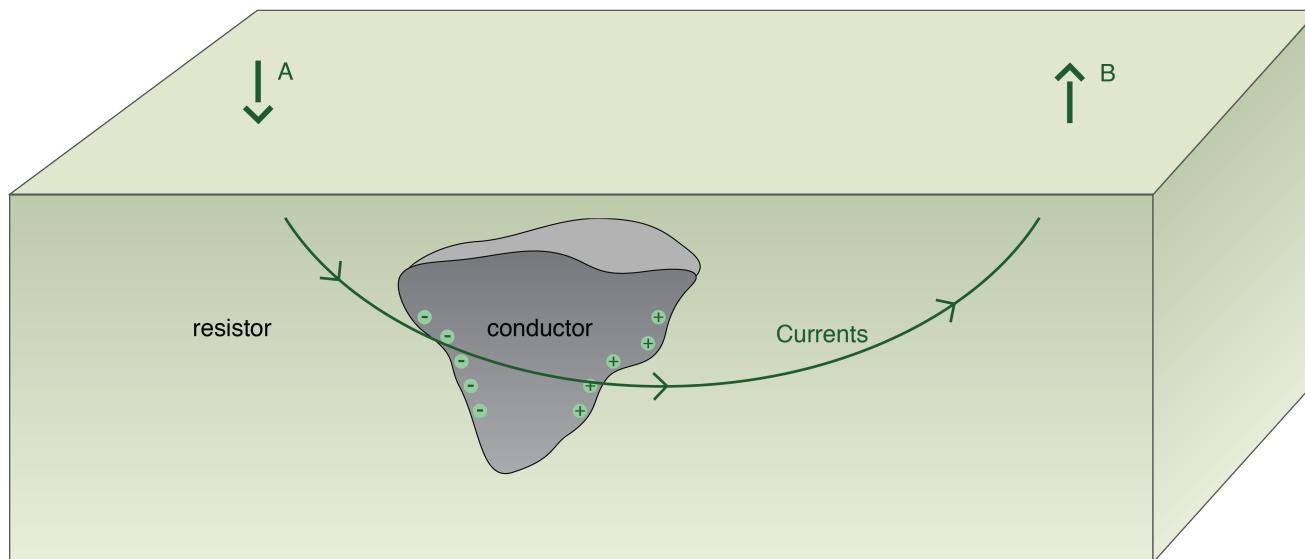
Conductivity contrast

$$\sigma_1 \neq \sigma_2$$

- Electric field discontinuous
- Charge build-up

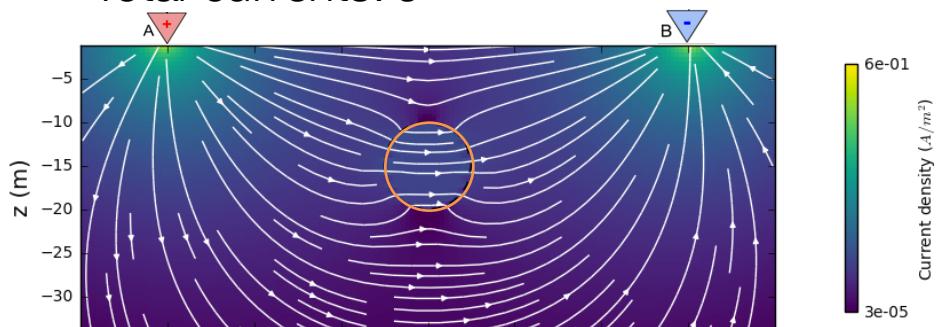


$$\mathbf{E} = \frac{Q}{4\pi\epsilon_0|\mathbf{r} - \mathbf{r}'|^2}\hat{\mathbf{r}}$$

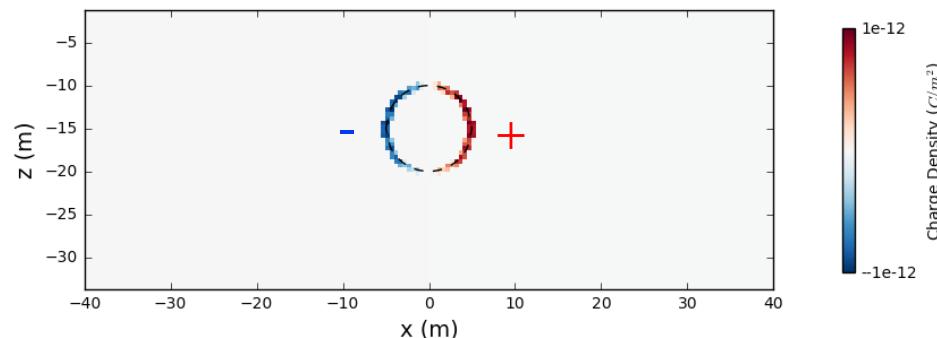
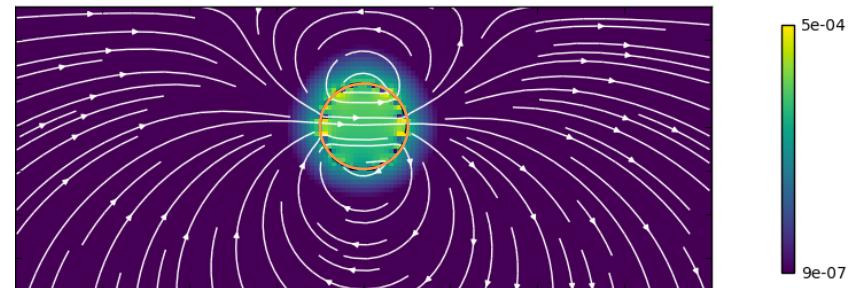


# Currents, charges, and potentials

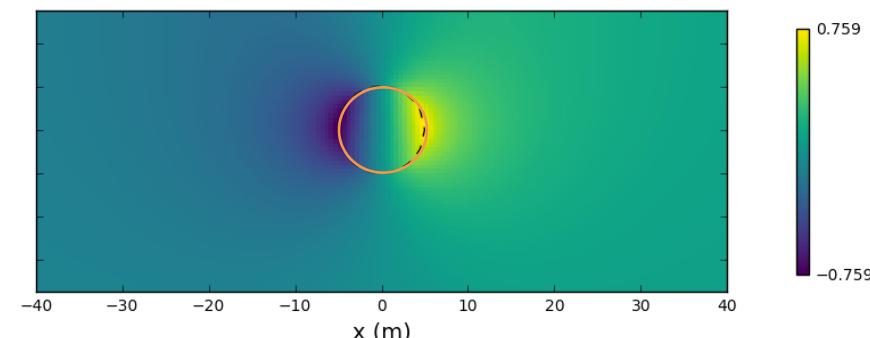
Total currents:  $\mathbf{J}$



Secondary currents:  $\mathbf{J}_s$



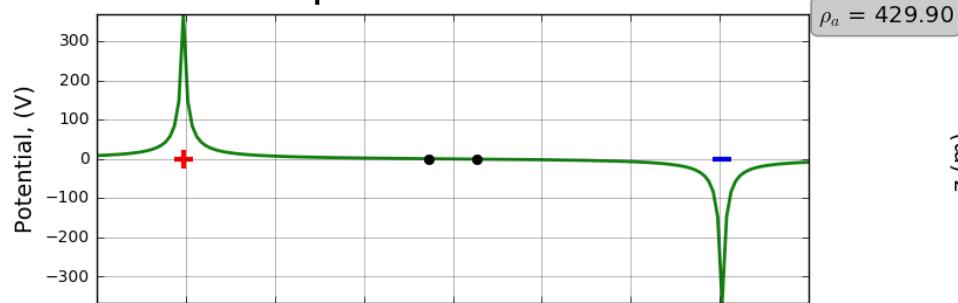
Secondary charges:  $Q_s$



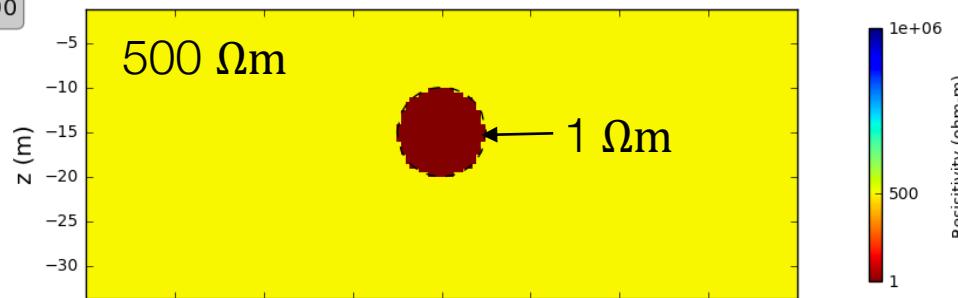
Secondary potential:  $\phi_s$

# Measurements of DC data: gradient array

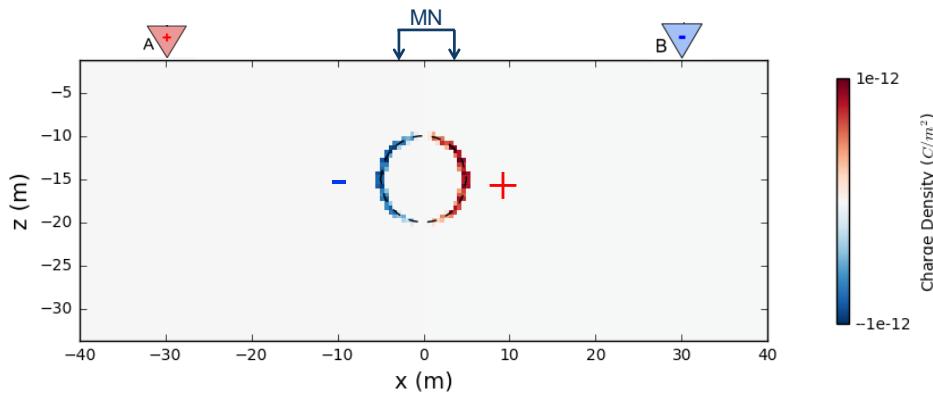
Potential profile



Resistivity model

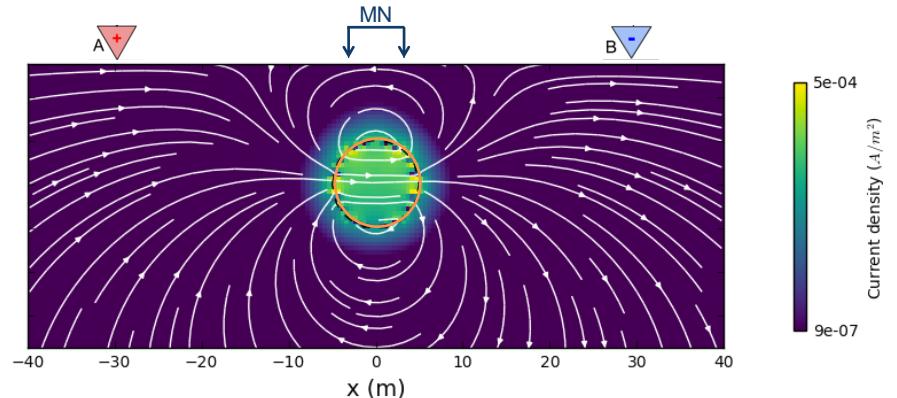


$\rho_a = 430$



Secondary charges:  $Q_s$

$\rho_a = 430$



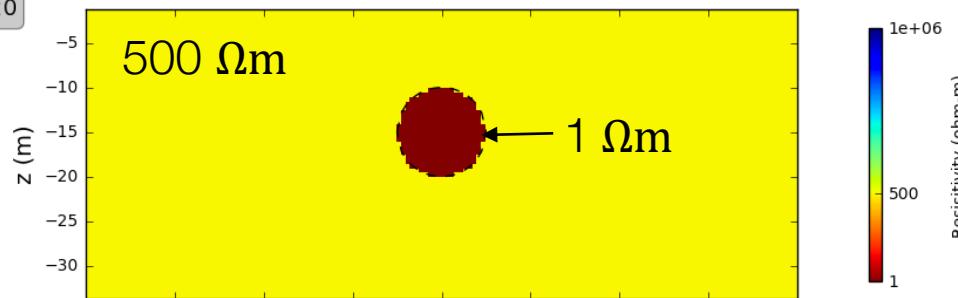
Secondary currents:  $J_s$

# Measurements of DC data: gradient array

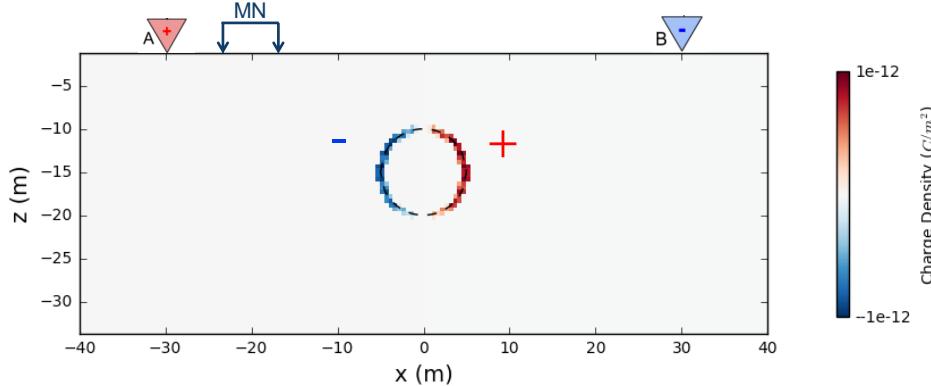
Potential profile



Resistivity model

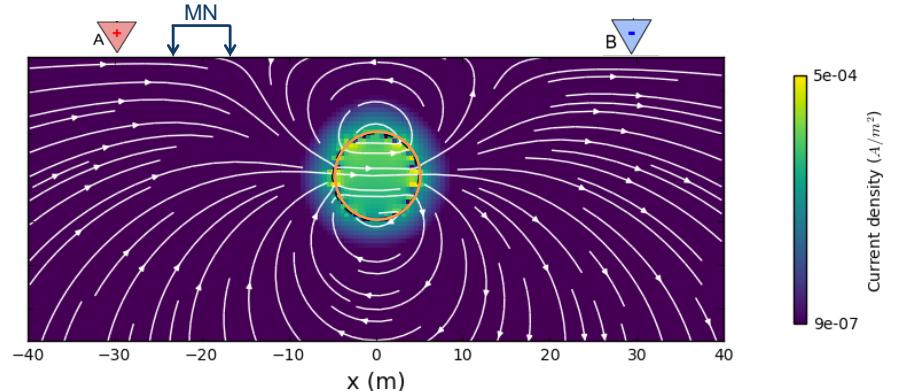


$\rho_a = 502$



Secondary charges:  $Q_s$

$\rho_a = 502$



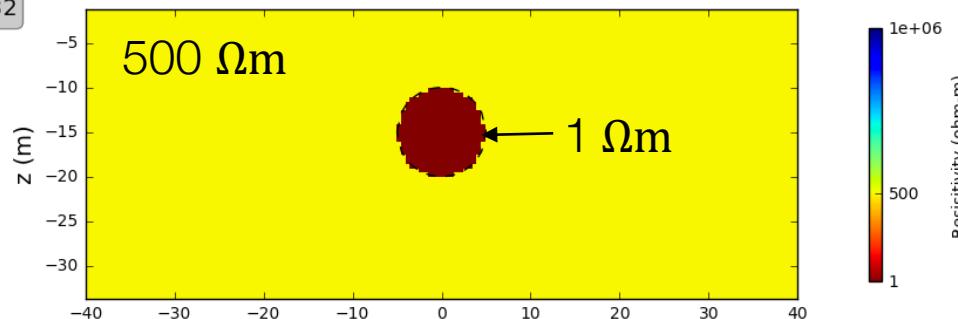
Secondary currents:  $J_s$

# Measurements of DC data: gradient array

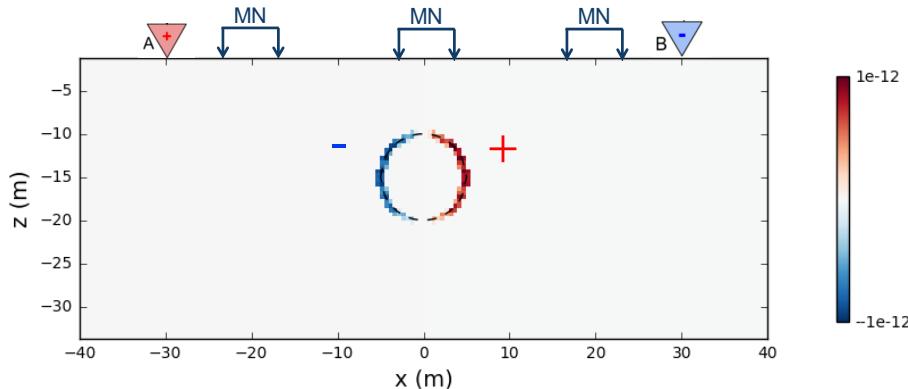
Potential profile



Resistivity model

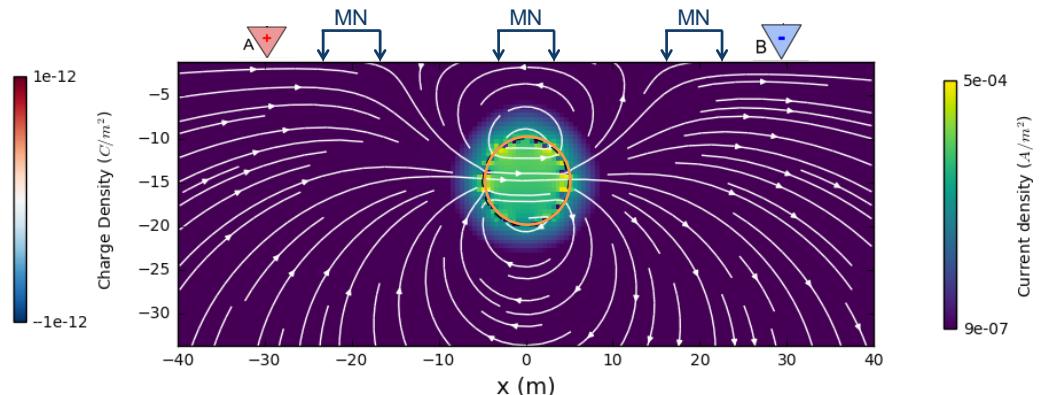


$$\rho_a = 502 \quad \rho_a = 430 \quad \rho_a = 502$$



Secondary charges:  $Q_s$

$$\rho_a = 502 \quad \rho_a = 430 \quad \rho_a = 502$$



Secondary currents:  $J_s$

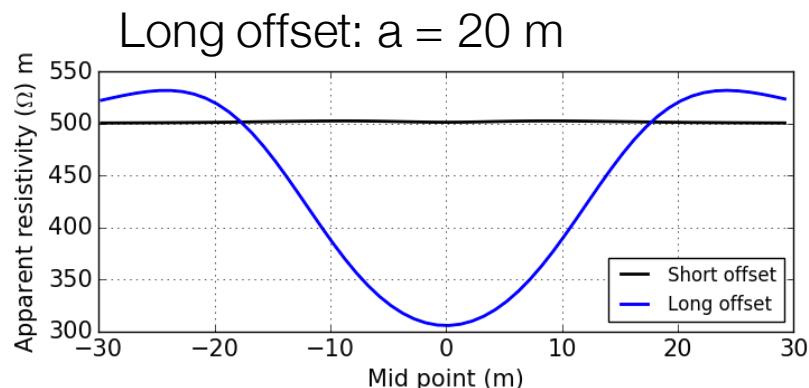
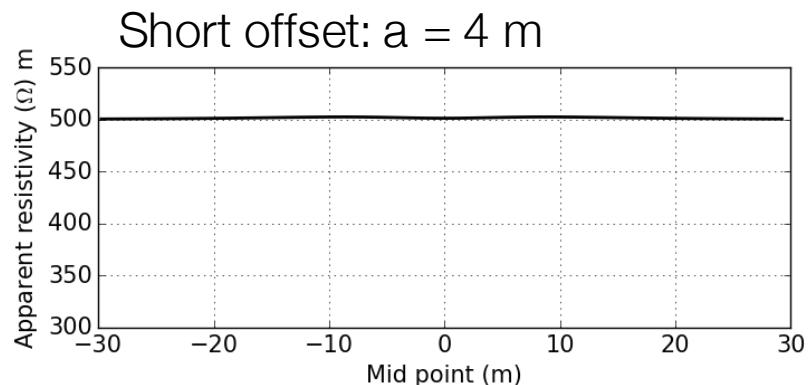
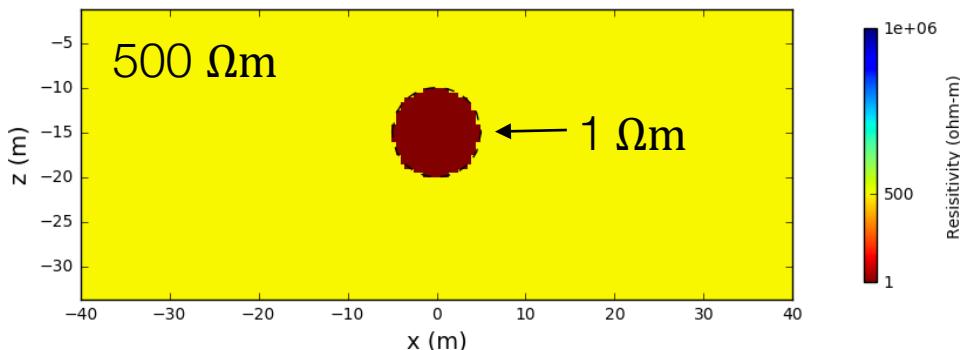
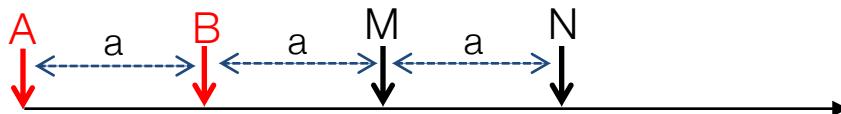
# Profiling

Fixed geometry: Move laterally

Short offset,  $a=4\text{m}$



Long offset,  $a=20\text{m}$

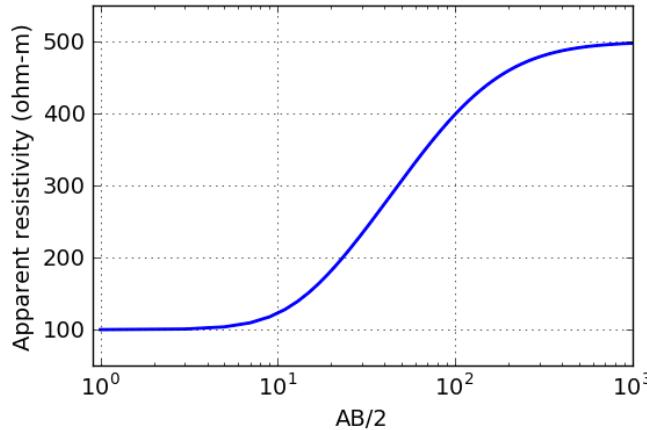


Depth of investigation depends upon offset or array length

# Summary: Soundings and Profiles

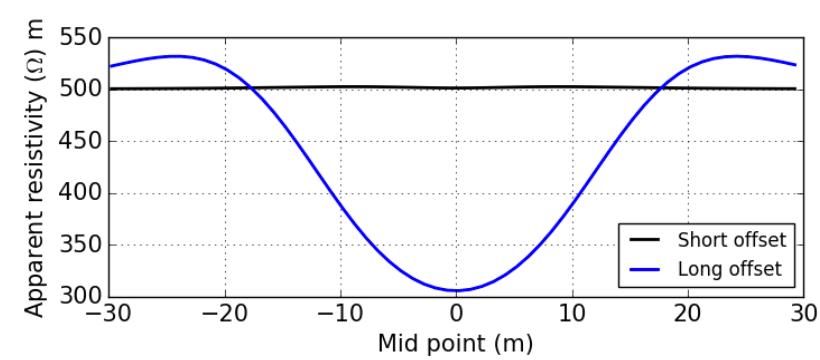
## Sounding

Expand



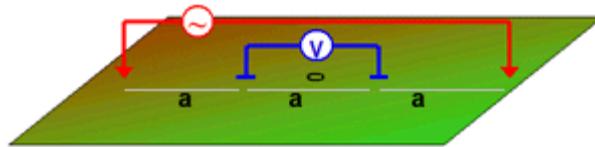
## Profiling

Translate

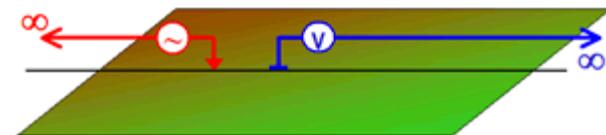


# Basic Survey Setups

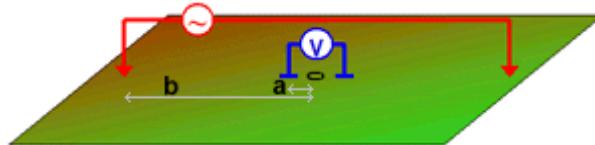
Wenner



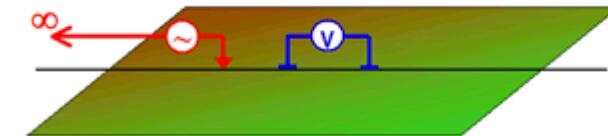
Pole-Pole



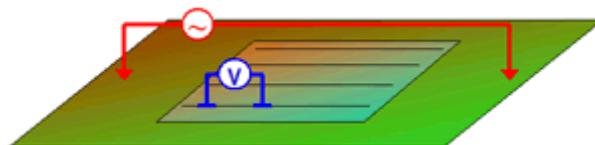
Schulmberger



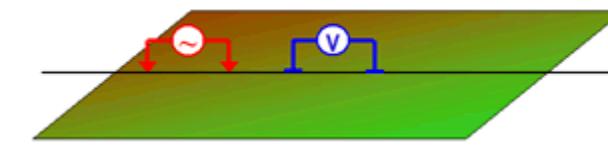
Pole-Dipole



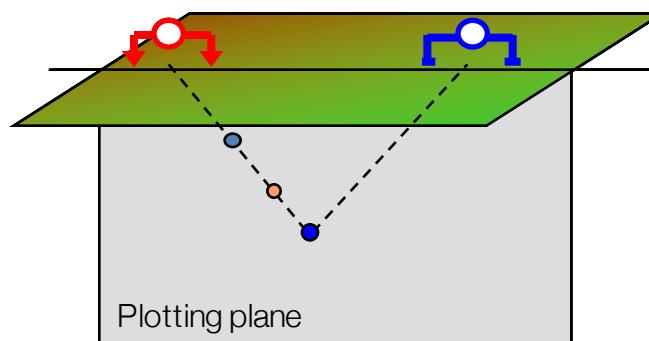
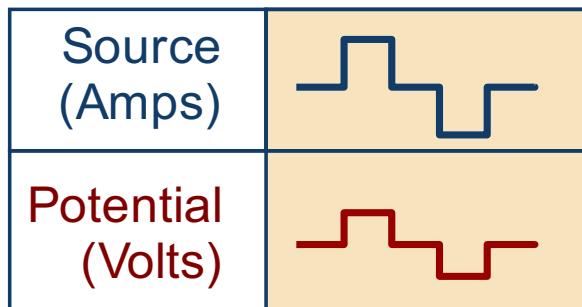
Gradient



Dipole-Dipole

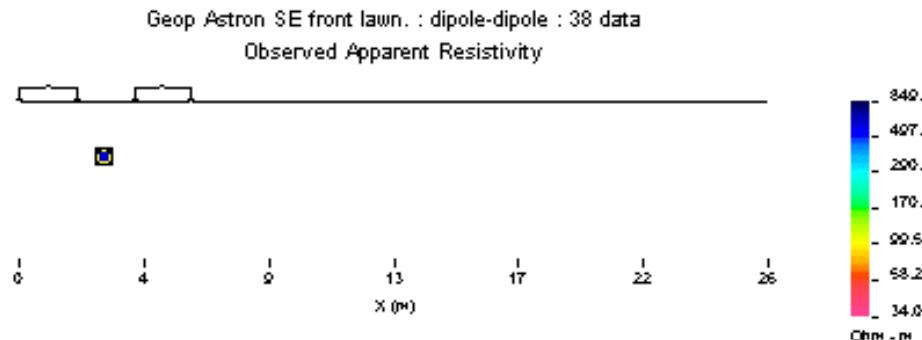


# DC resistivity data



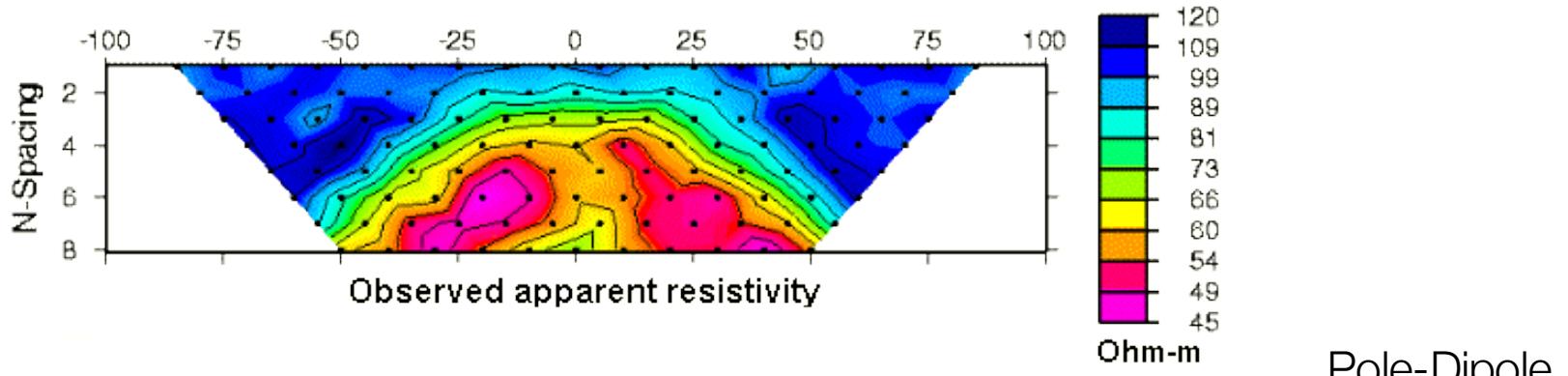
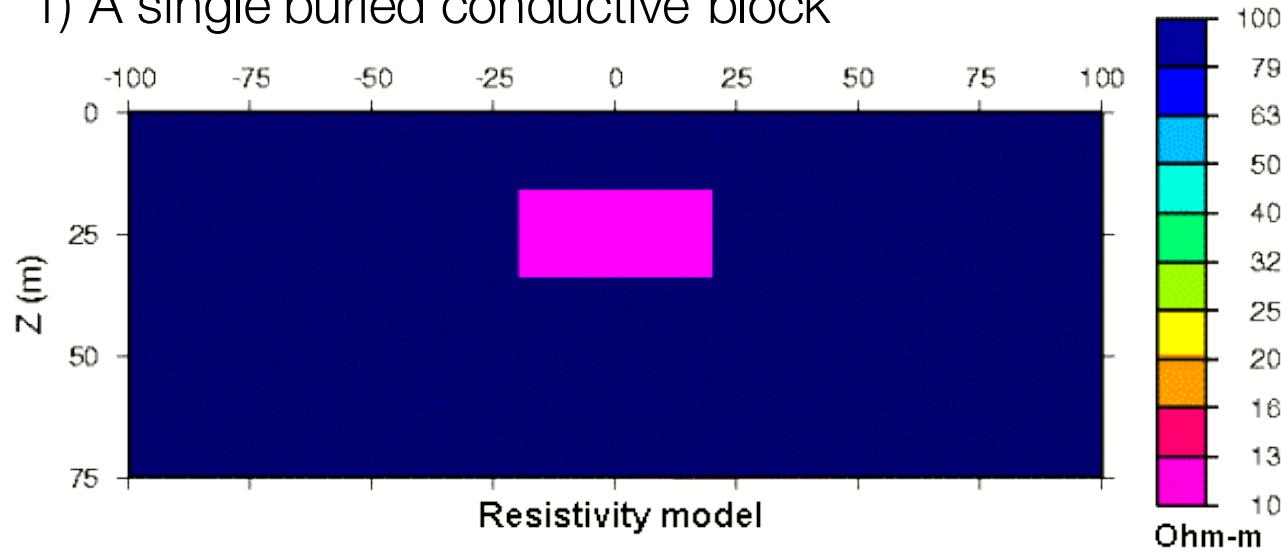
Each data point is an apparent resistivity:

$$\rho_a = \frac{2\pi\Delta V}{IG}$$

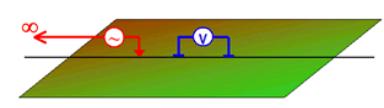


# Example pseudosections

1) A single buried conductive block

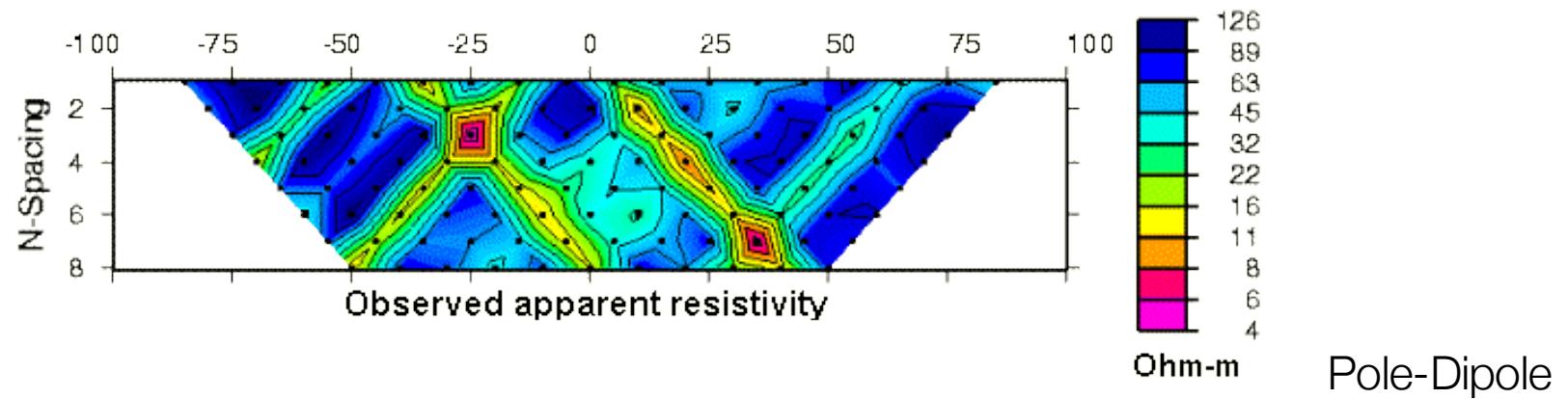
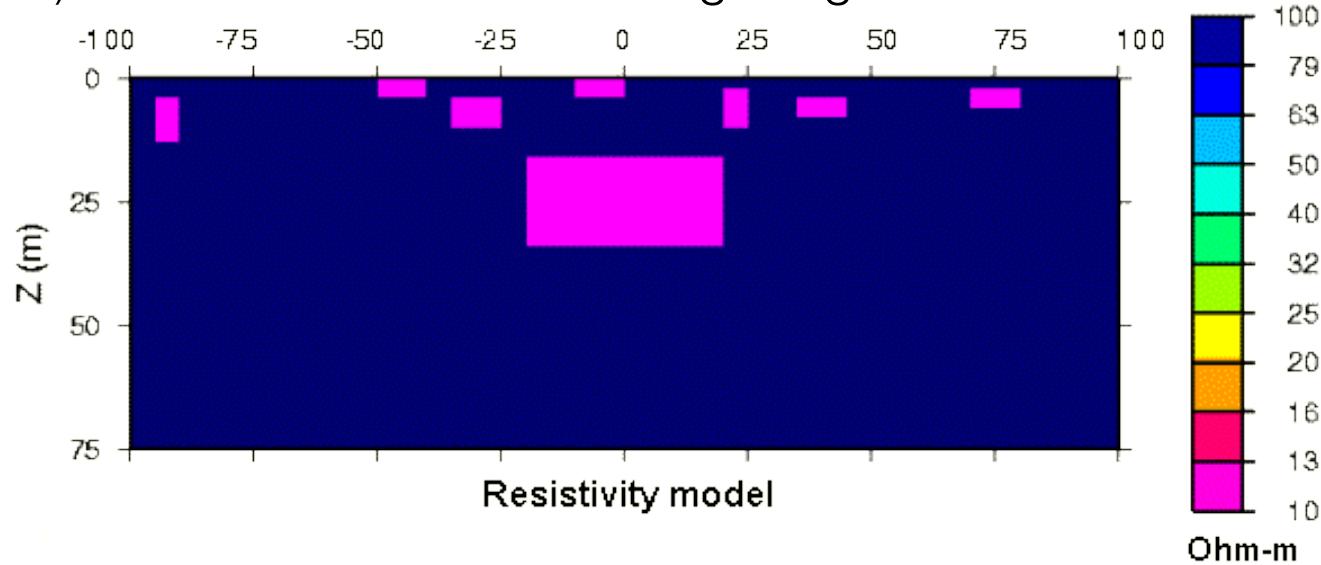


- Pole-dipole;  $n=1,8$ ;  $a=10\text{m}$ ;  $N=316$



# Example pseudosections

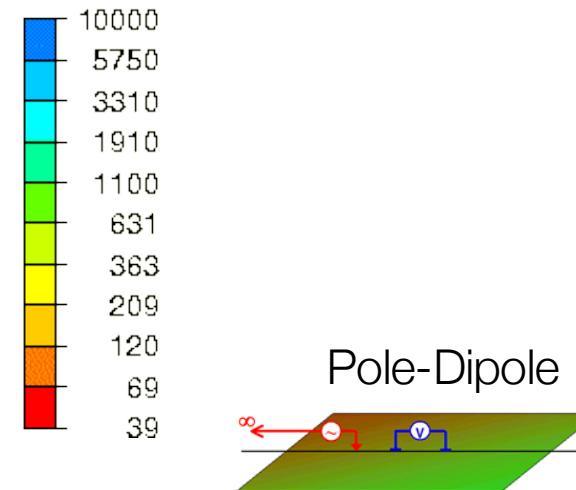
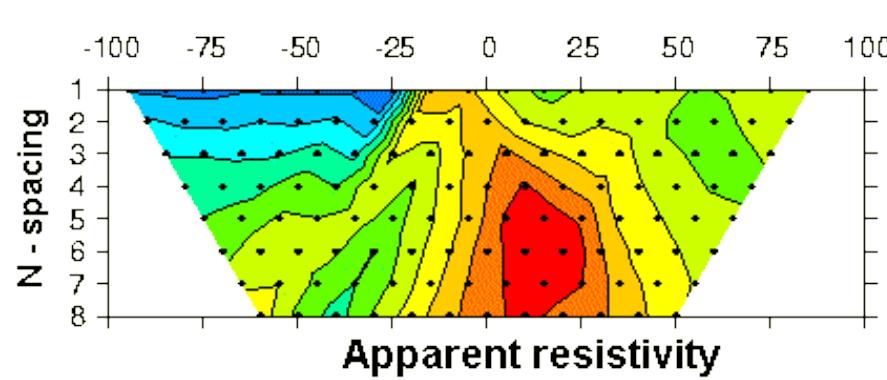
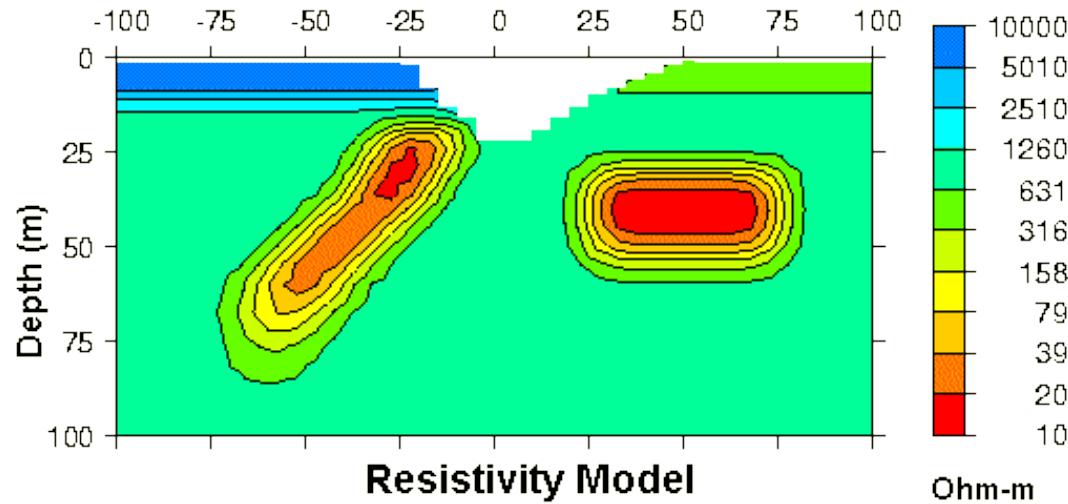
2) The conductive block with geologic noise.



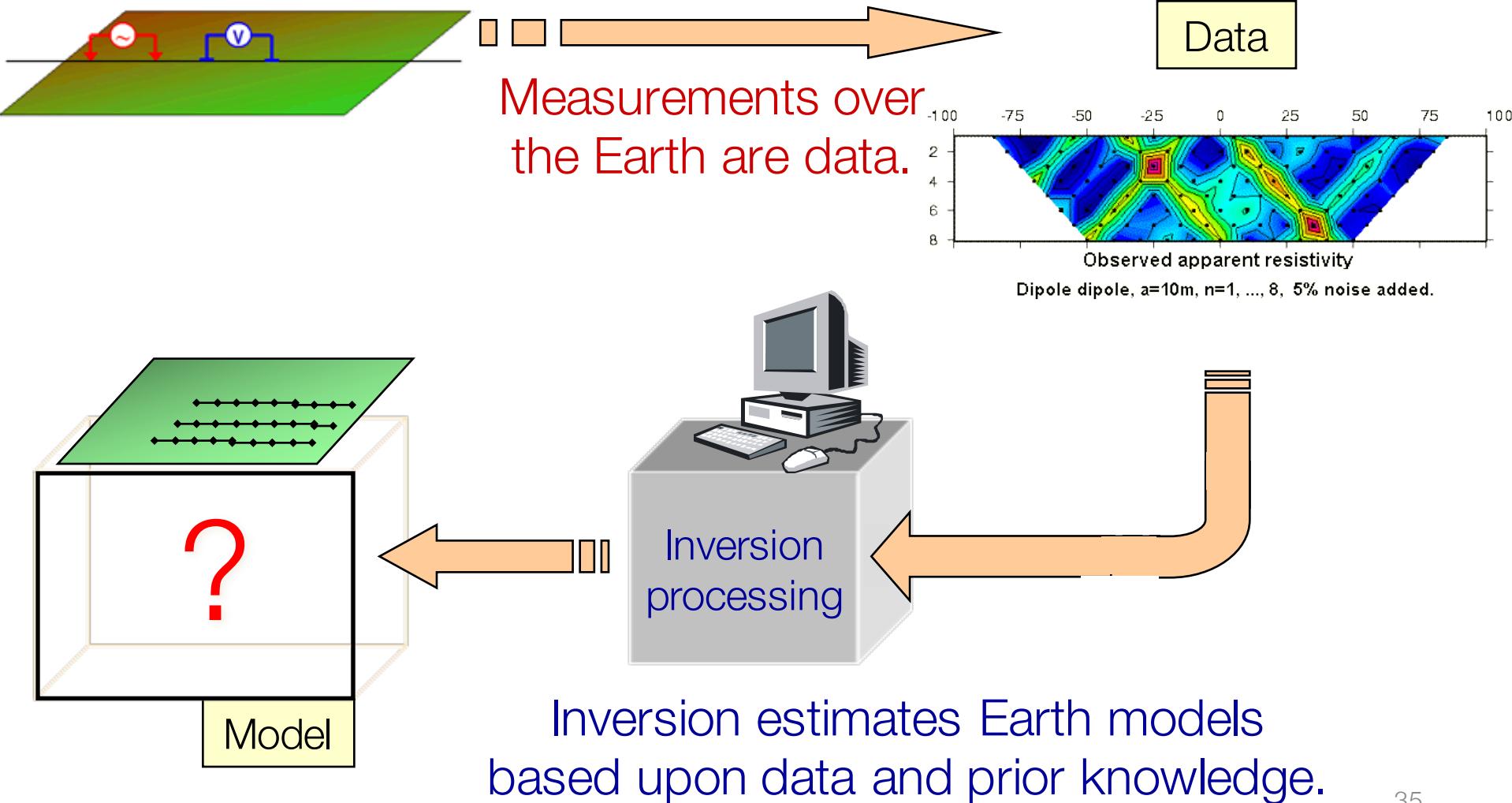
- Pole-dipole;  $n=1,8$ ;  $a=10\text{m}$ ;  $N=316$

# Example pseudosections

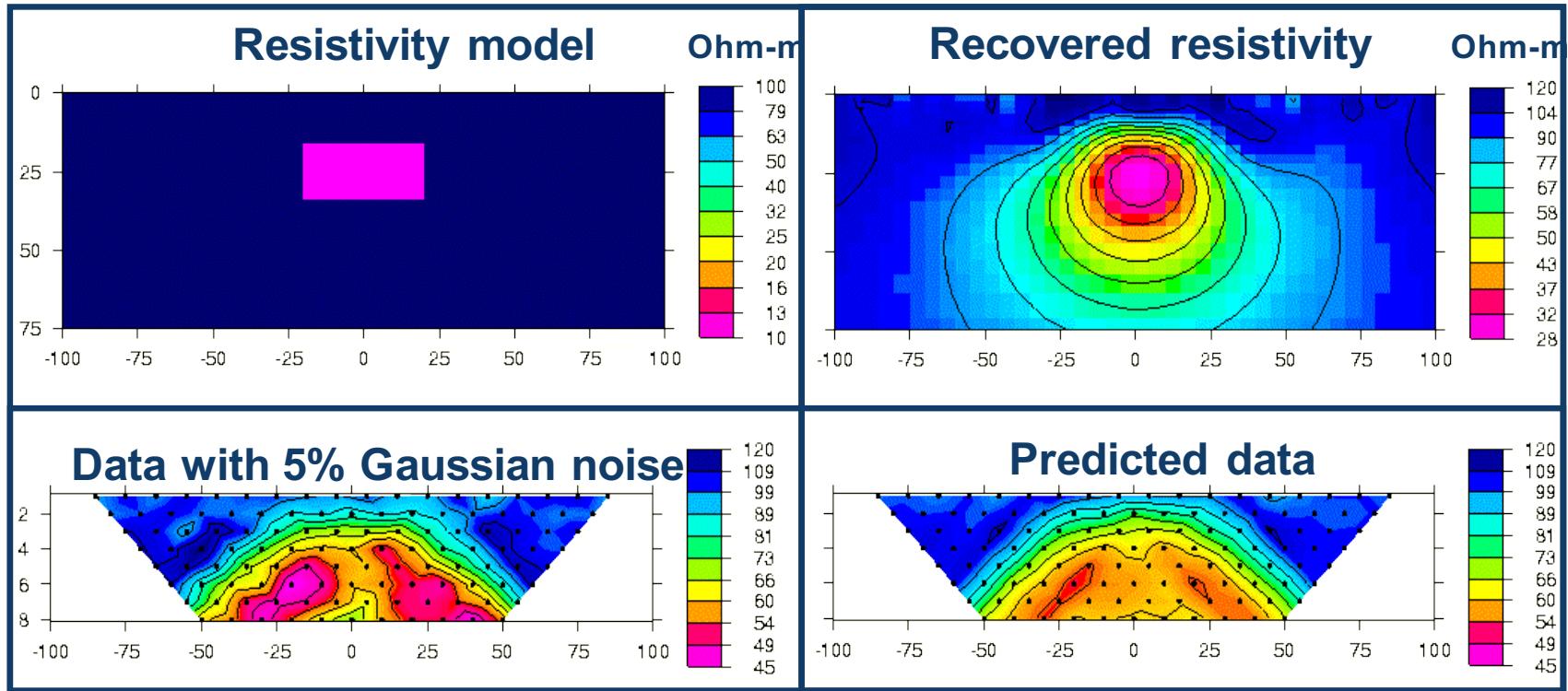
## 3) The “UBC-GIF model”



# Inversion

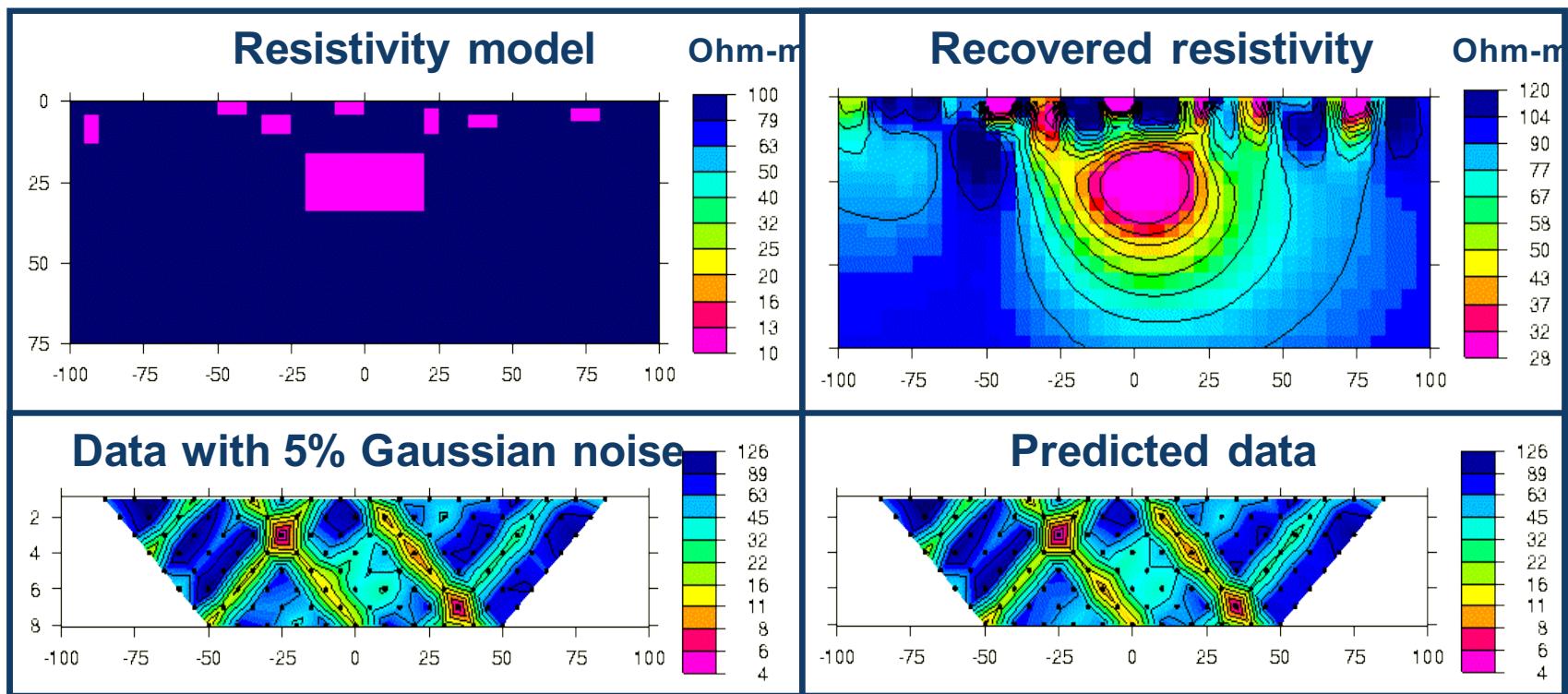


# Example 1: buried prism



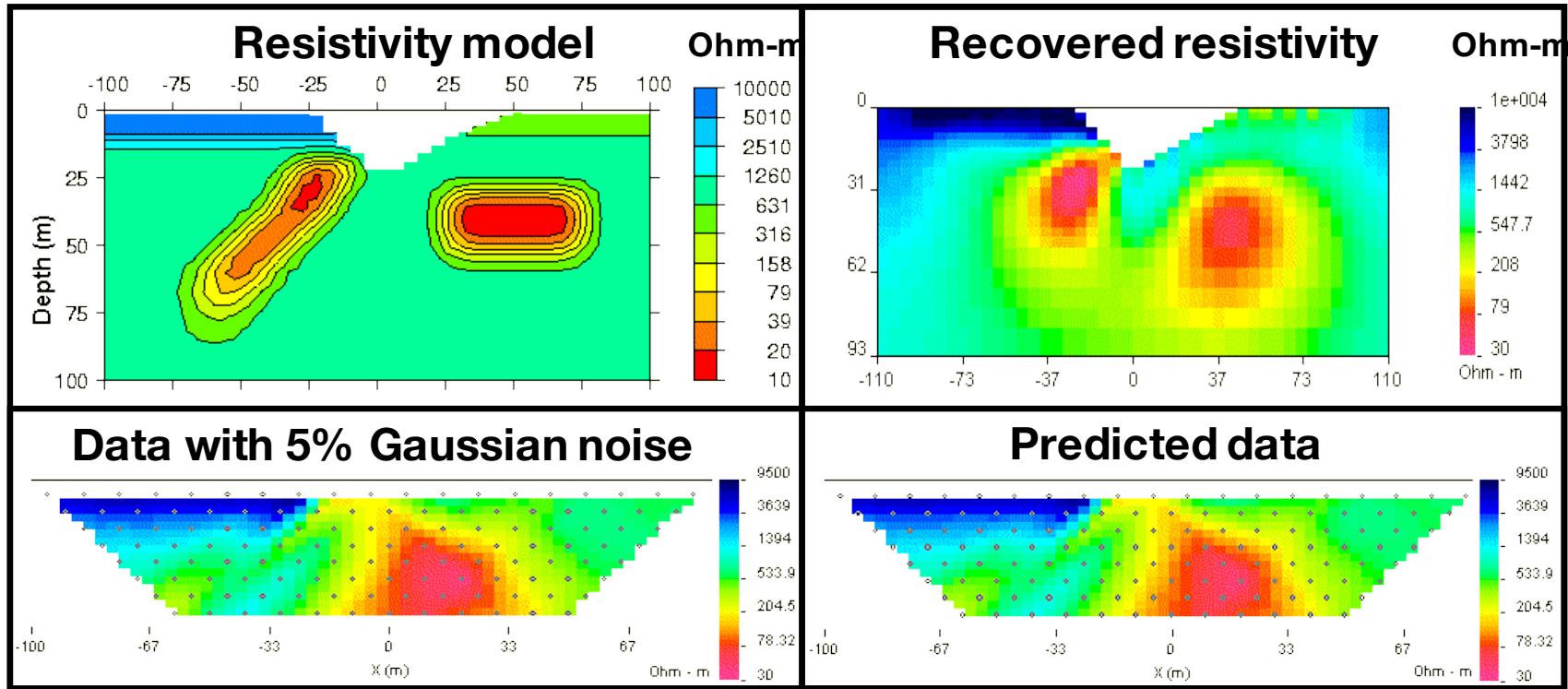
- Pole-dipole;  $n=1,8$ ;  $a=10\text{m}$ ;  $N=316$ ;  $(\alpha_s, \alpha_x, \alpha_z)=(.001, 1.0, 1.0)$

# Example 2: prism with geologic noise



- Pole-dipole;  $n=1,8$ ;  $a=10\text{m}$ ;  $N=316$ ;  $(\alpha_s, \alpha_x, \alpha_z)=(.001, 1.0, 1.0)$

# Example 3: UBC-GIF model



- Pole-dipole;  $n=1,8$ ;  $a=10\text{m}$

# The world is 3D

- Target
  - Size, shape, depth
- Background
  - Variable resistivity
- Questions
  - Where to put currents? 2D acquisition? 3D?
  - Where to make measurements?
  - Which measurements?
  - Effects of topography?
- These are survey design questions
- Crucial element is the **sensitivity**

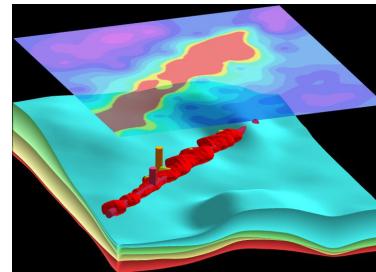
Host



Water underground



Ore body

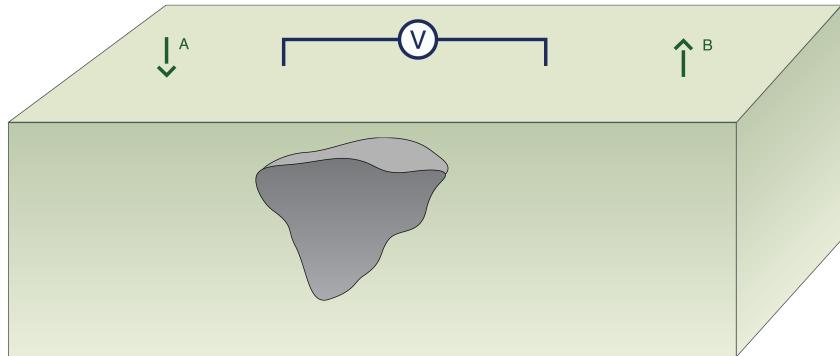


Topography



# Sensitivity

# Sensitivity Function

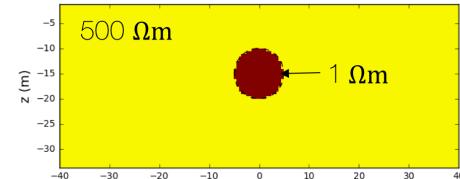


Is the measured potential *sensitive* to the target?

Quantified by the sensitivity

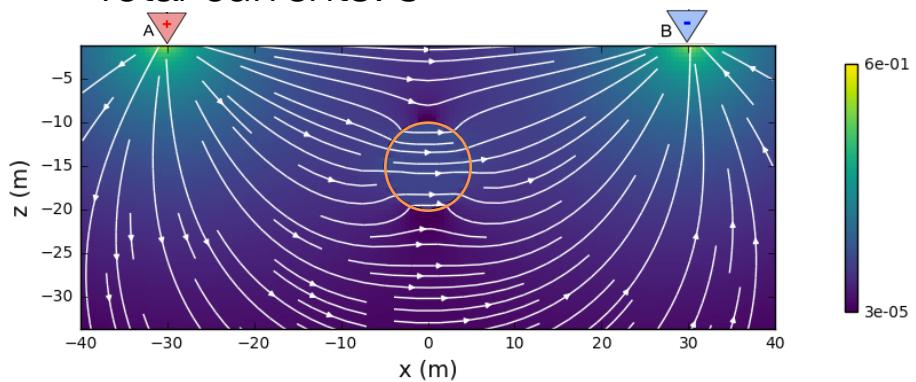
$$G = \frac{\Delta d}{\Delta p} = \frac{\text{change in data}}{\text{change in model}}$$

- Collect the data that are sensitive to the target
  - Need to **excite** the target
  - Need to have sensor **close** to the target

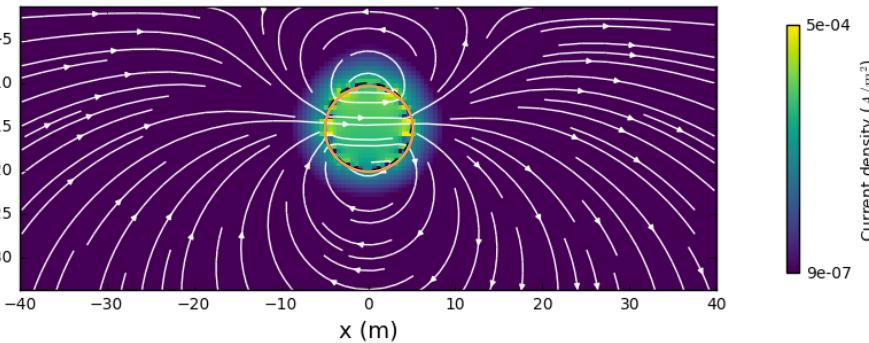


# Exciting the target

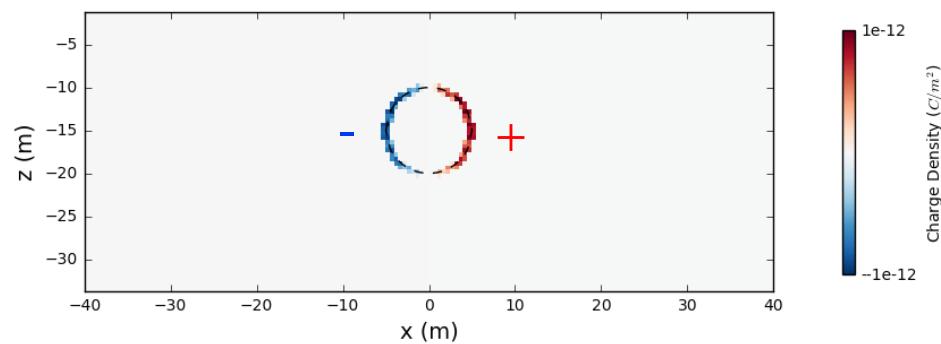
Total currents:  $\mathbf{J}$



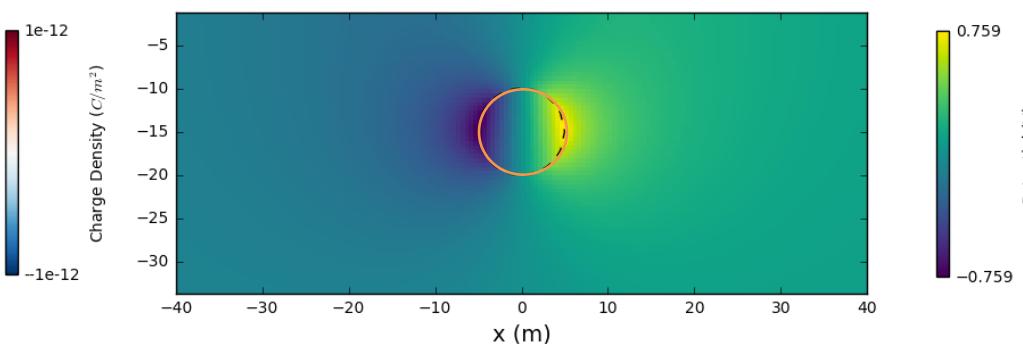
Secondary currents:  $\mathbf{J}_S$

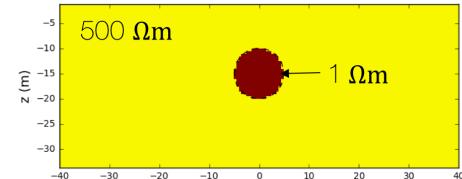


Secondary charges:  $Q_S$



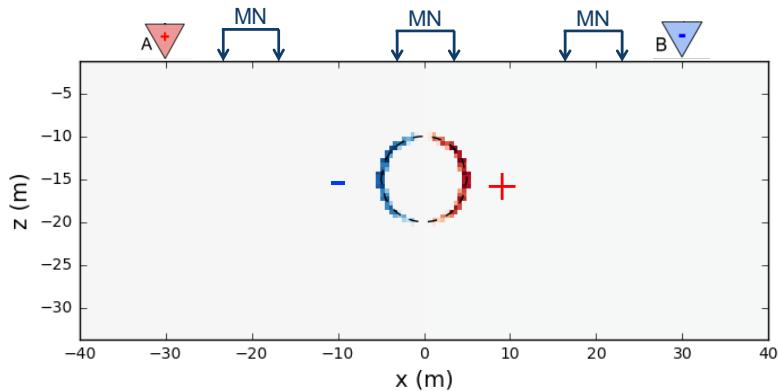
Secondary potential:  $\phi_S$



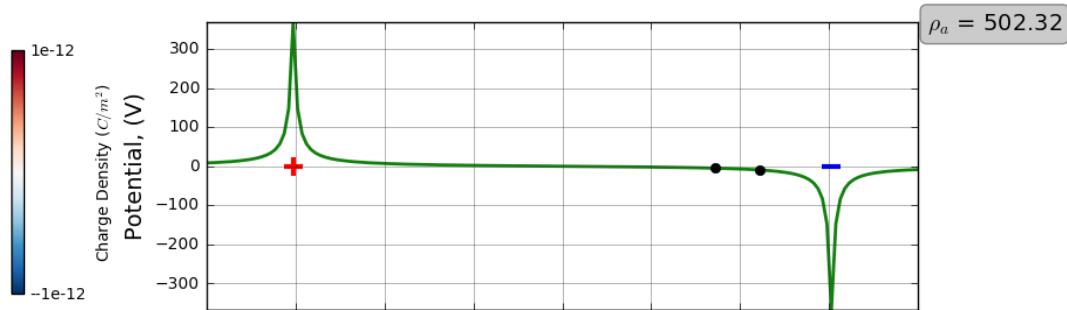


# Measurements

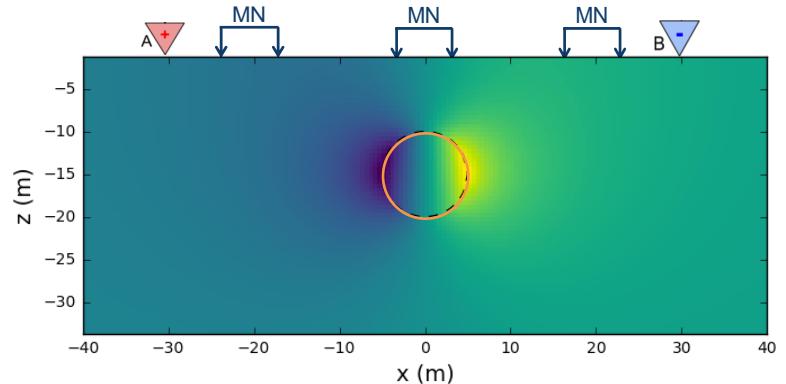
Secondary charges:  $Q_s$



Potential profile

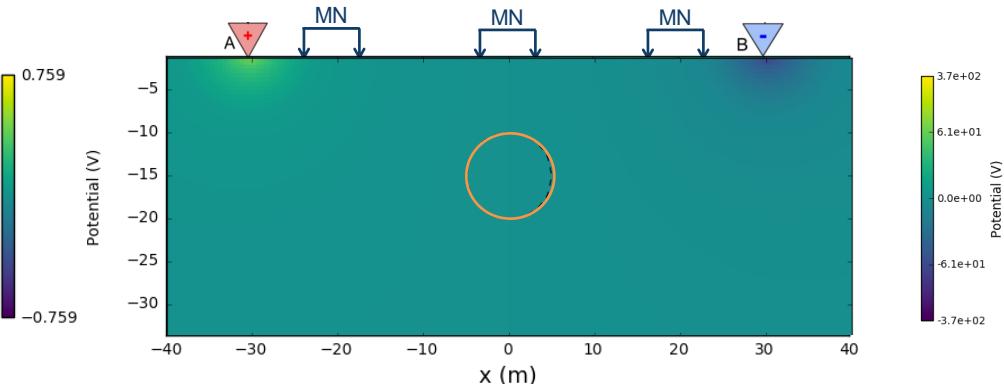


Secondary potential:  $\phi_s$



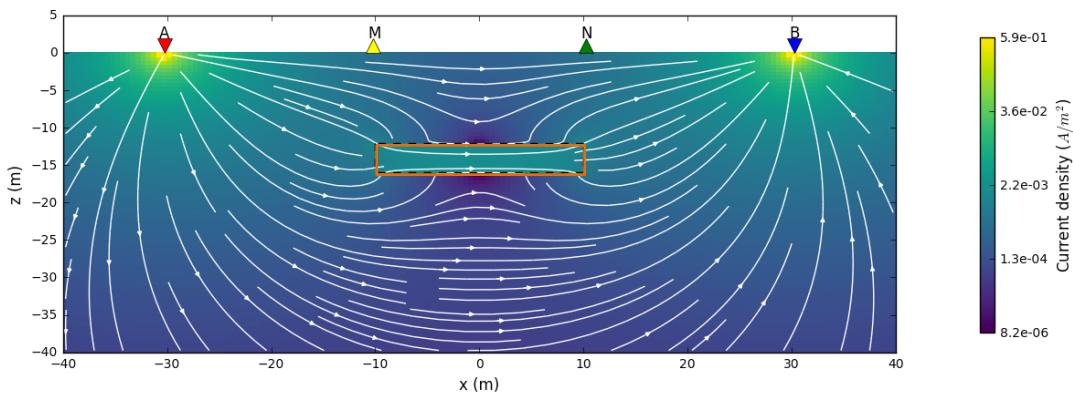
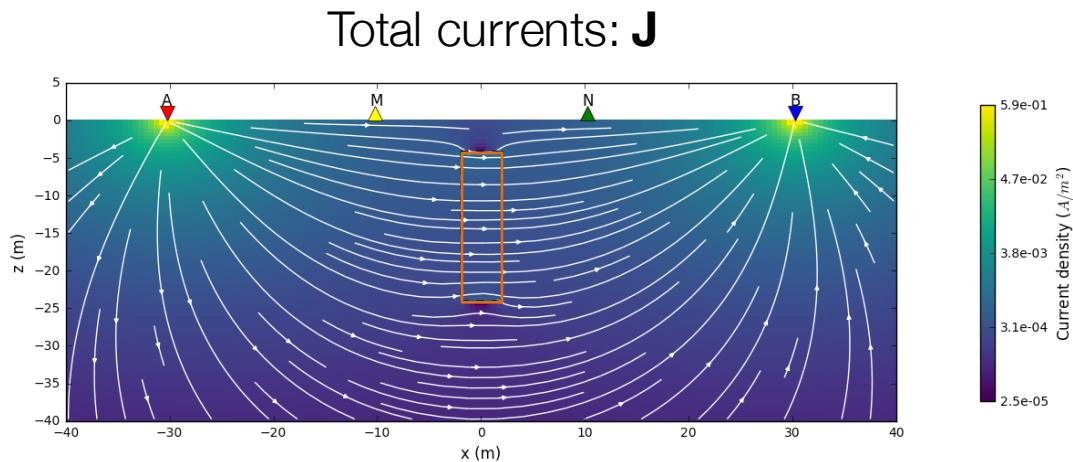
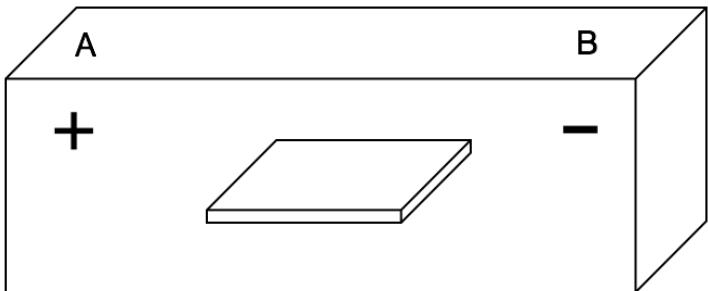
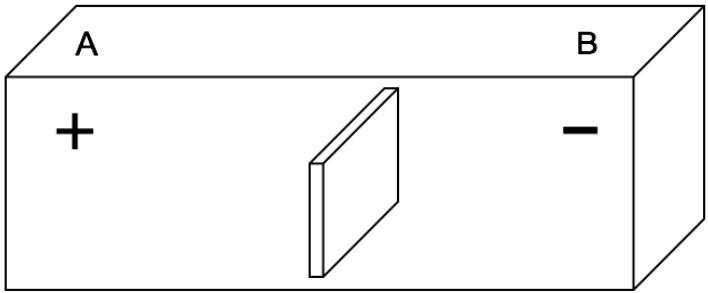
Total potential:  $\phi$

$$\rho_a = 502 \quad \rho_a = 430 \quad \rho_a = 502$$



# Coupling

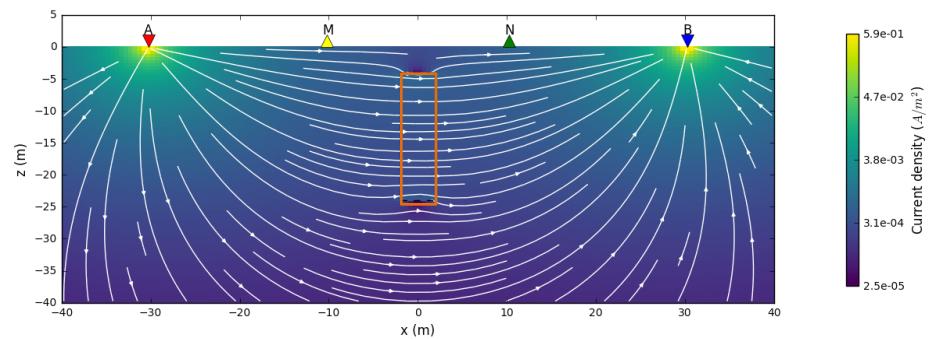
- Thin plate – different orientations  
→ different data



# Conductive vs. Resistive Target

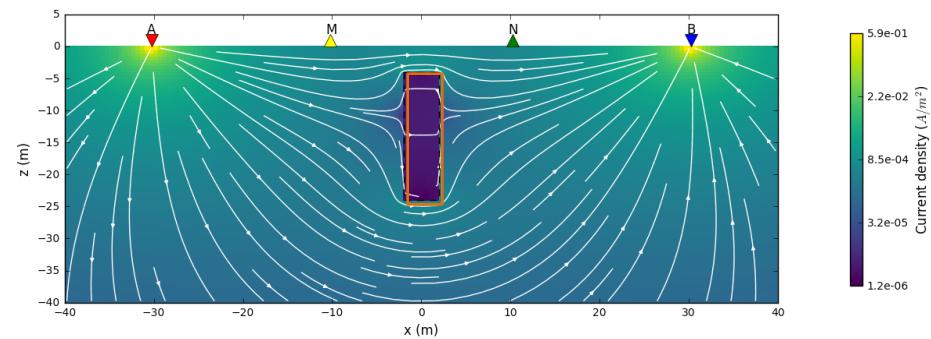
Conductive Target

Total currents:  $\mathbf{J}$

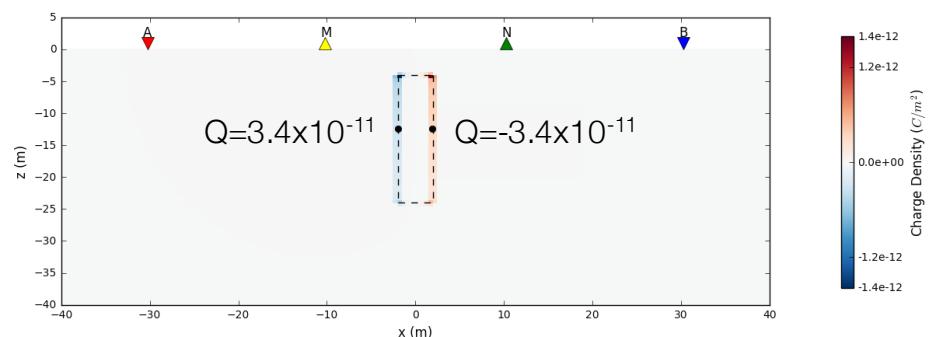


Resistive Target

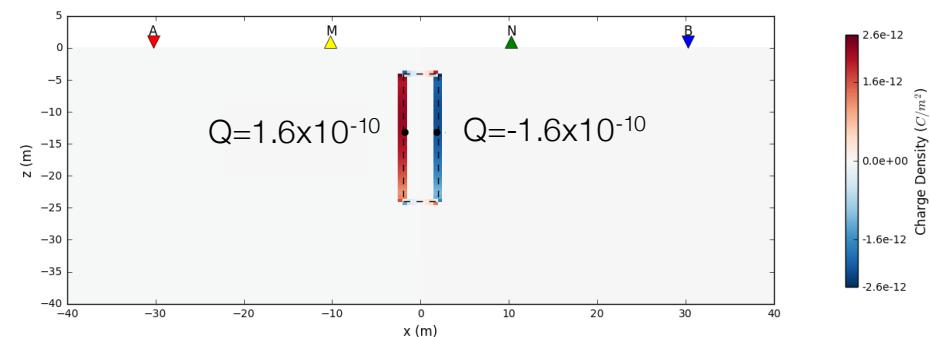
Total currents:  $\mathbf{J}$



Secondary charges:  $Q_s$



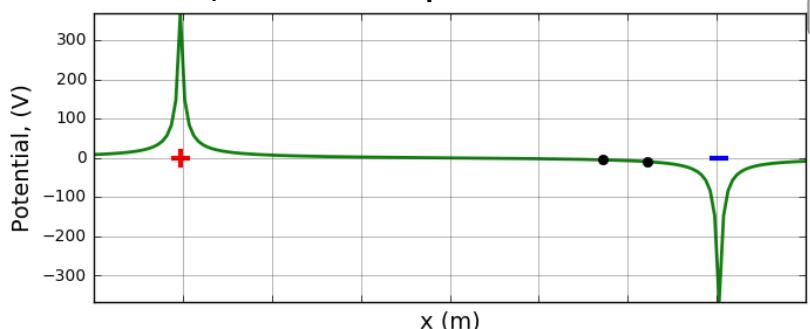
Secondary charges:  $Q_s$



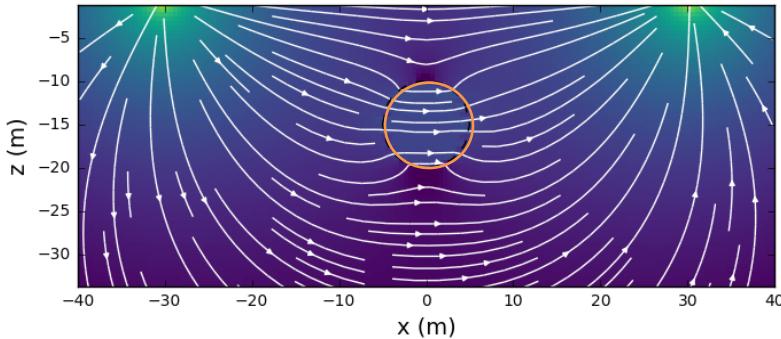
# Summary: Sensitivity

- “Excite” the target
  - Drive currents to target
  - Need good coupling with target
- Measuring a datum
  - Proximity to target
  - Electrode orientation and separation
- Background resistivity is important

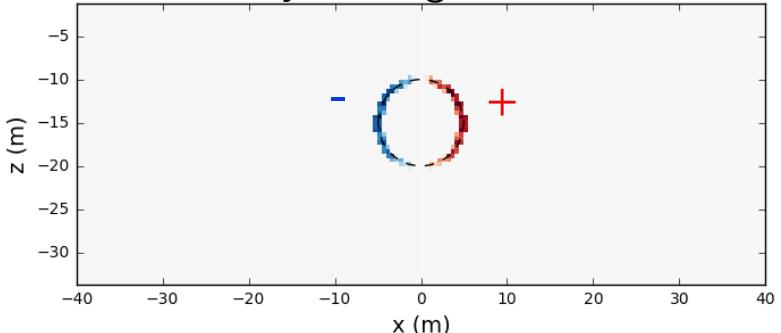
Total potential:  $\phi$



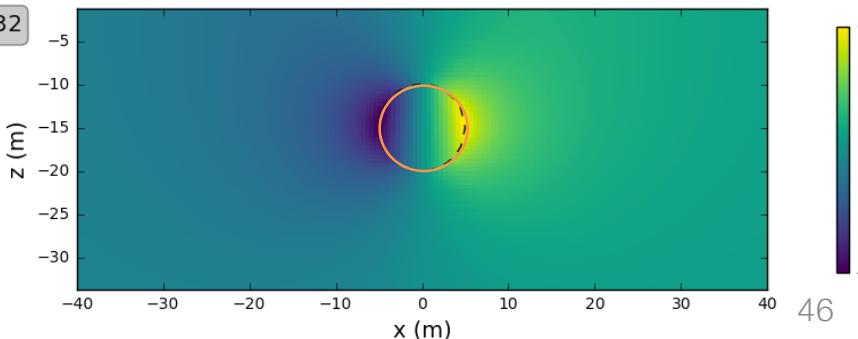
Total currents:  $\mathbf{J}$



Secondary Charges:  $Q$

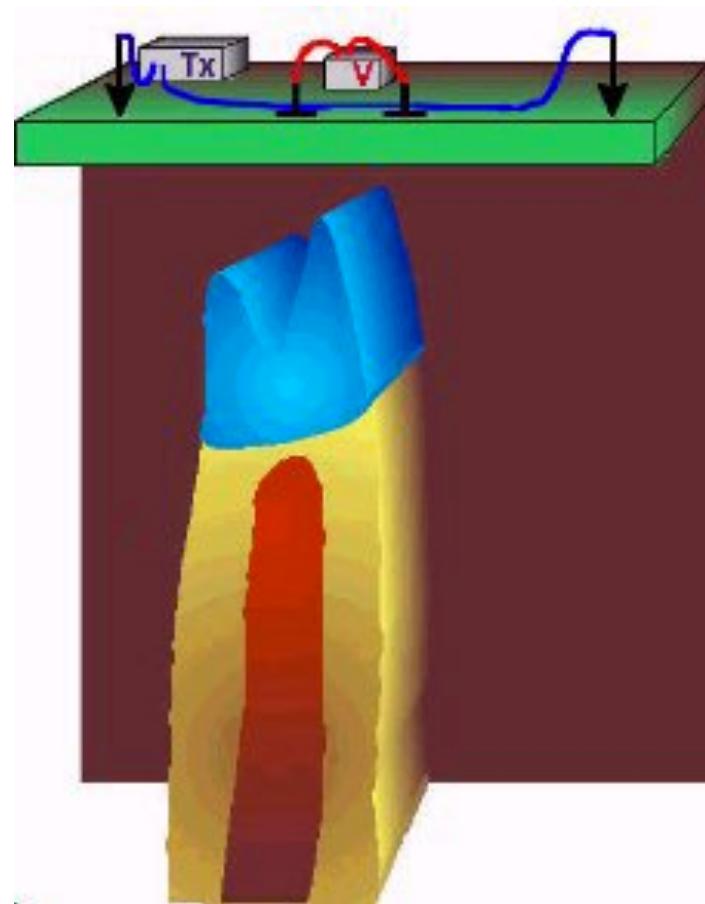


Secondary potential:  $\phi_s$

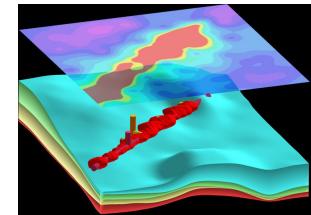


# Survey Design: Questions

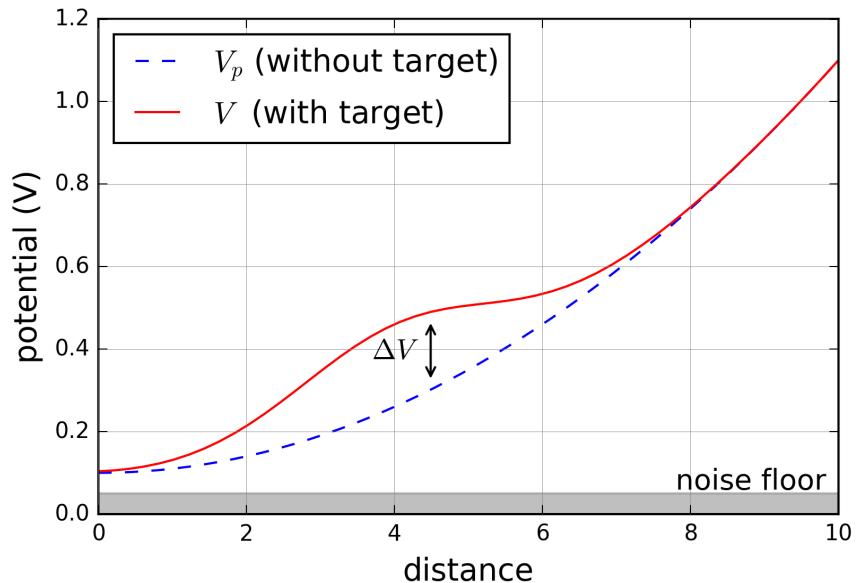
- What is objective?
  - Layered earth (1D)  
→ do a sounding
  - Target body (2D)  
→ profile, sounding  
perpendicular to geology
  - Target body (3d)  
→ need 3D coverage
- What is the background resistivity?
- What are the noise sources?  
fences, power lines, ...



# Survey Design: in general



- Numerical simulation – can we **see** the target?
- Steps:
  - Define a geologic model
  - Assign physical properties
  - Select a survey
  - Simulate with ( $V$ ) and without ( $V_p$ ) target
- Best practice
  - Assign uncertainties to simulated data
  - Invert with code you will use for the field data



Signal from target

$$\Delta V = V - V_p$$

Need

$$\Delta V > floor$$

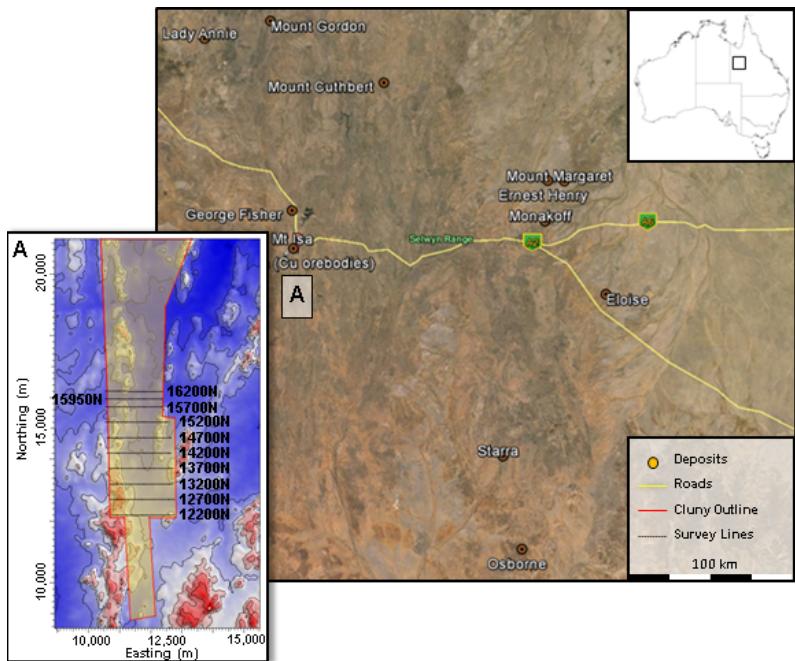
$$\frac{\Delta V}{V_p} > \%|V|$$

# Outline

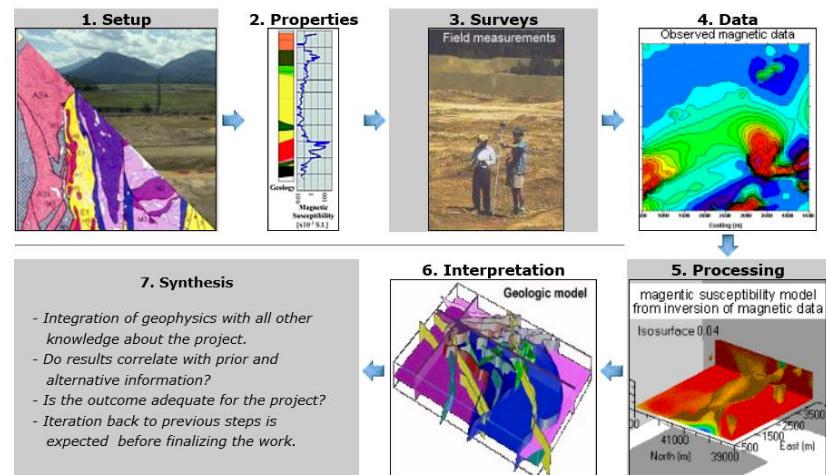
- Basic experiment
- Currents, charges, potentials and apparent resistivities
- Soundings, profiles and arrays
- Data, pseudosections and inversion
- Sensitivity
- Survey Design
- Questions
- Case History – Mt Isa
- Effects of background resistivity

# Mt. Isa

## Mt. Isa (Cluny prospect)

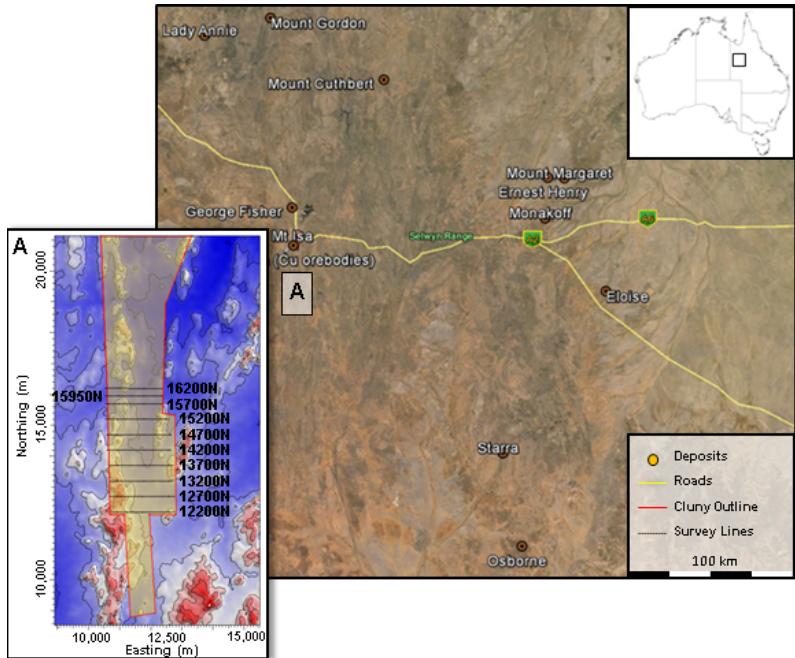


## Seven Steps

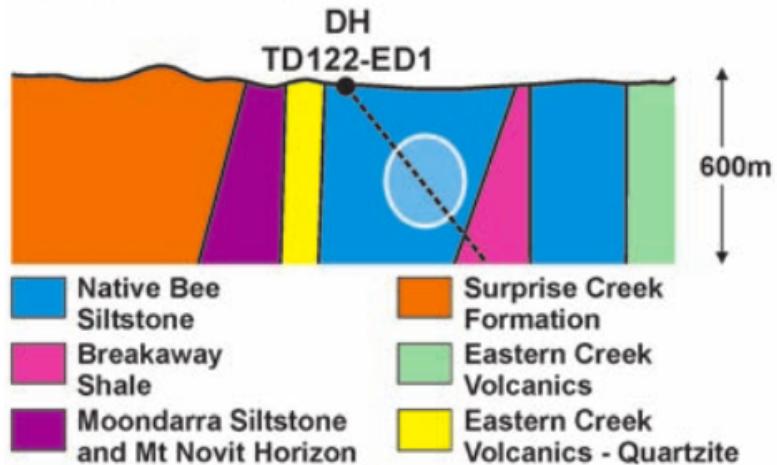


# Setup

## Mt. Isa (Cluny prospect)



## Geologic model

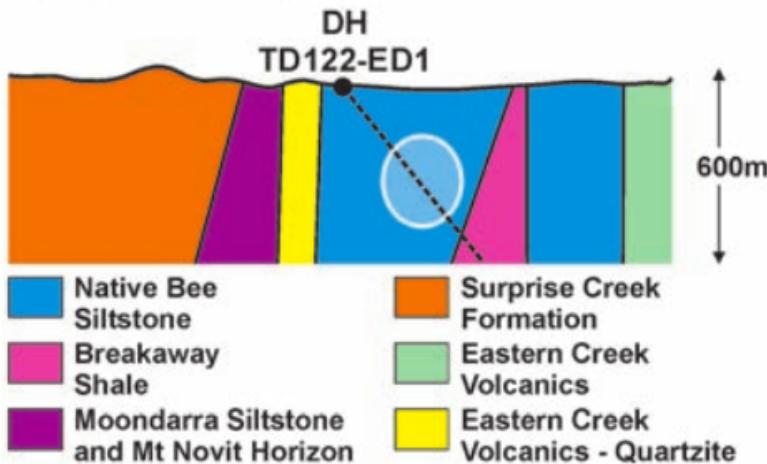


## Question

- Can conductive units, which would be potential targets within the siltstones, be identified with DC data?

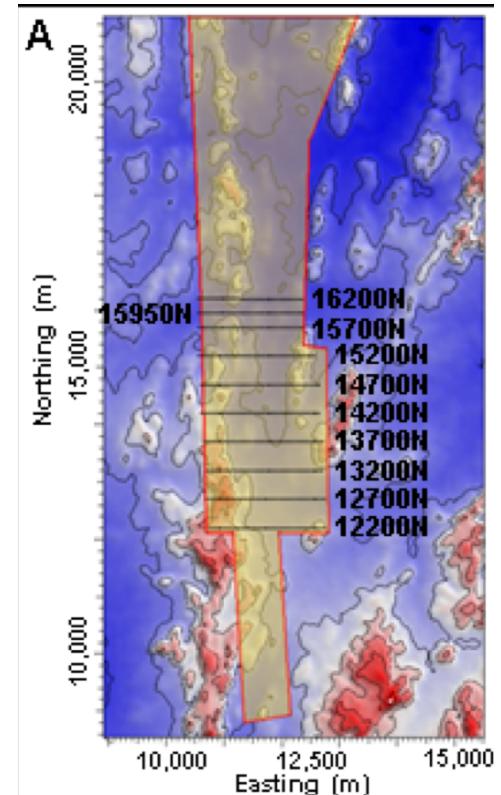
# Properties

## Geologic model



Rock Unit	Conductivity
Native Bee Siltstone	Moderate
Moondarra Siltstone	Moderate
Breakaway Shale	Very High
Mt Novit Horizon	High
Surprise Creek Formation	Low
Eastern Creek Volcanics	Low

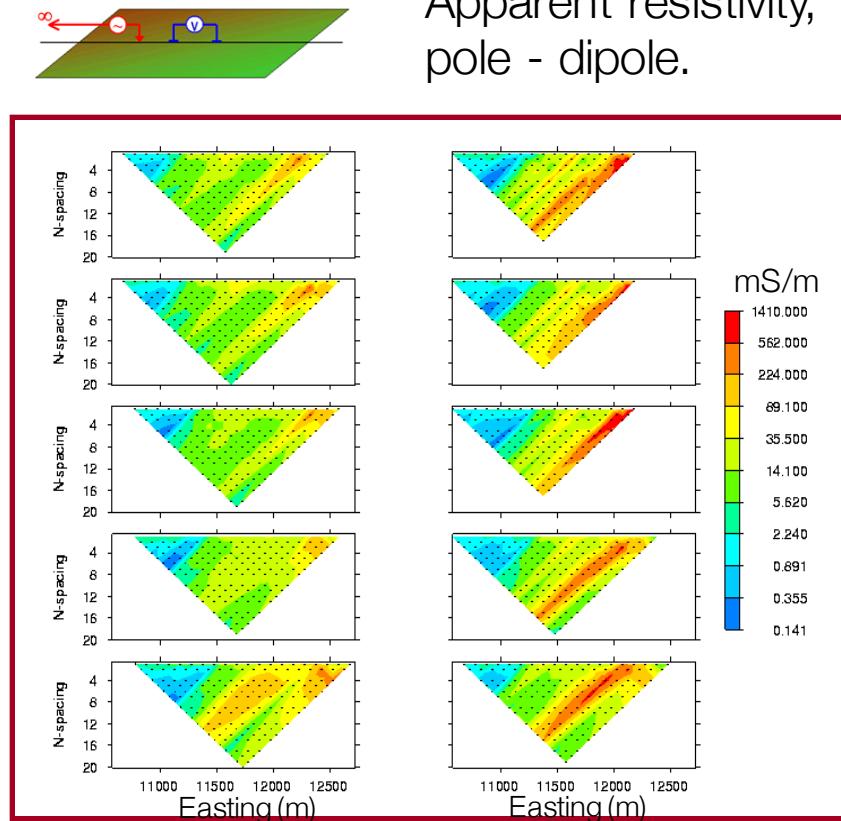
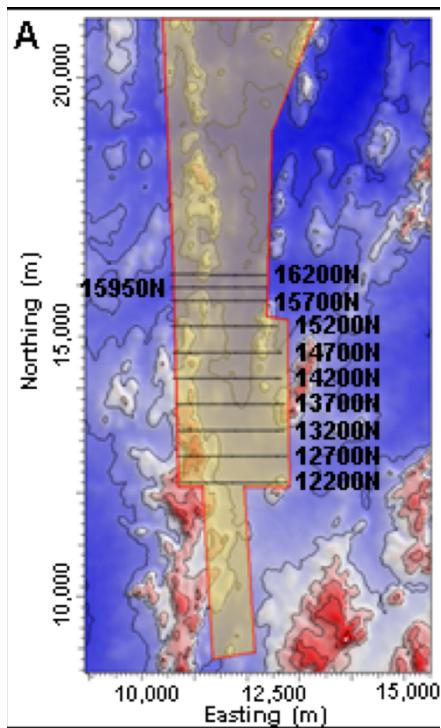
## Surface topography



# Survey and Data

- Eight survey lines
- Two survey configurations.

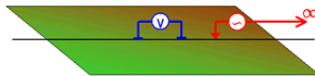
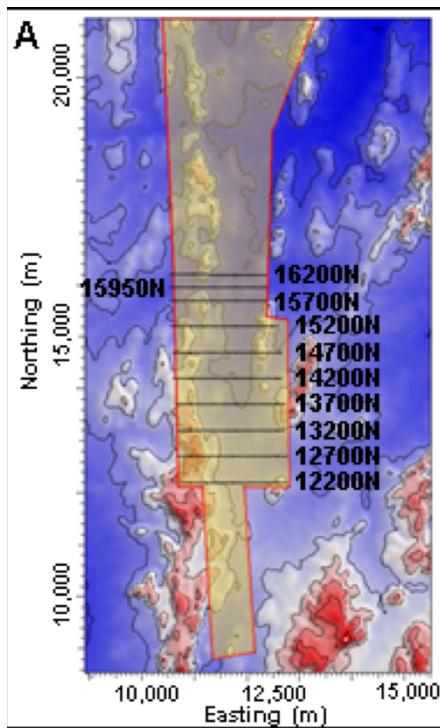
Surface topography



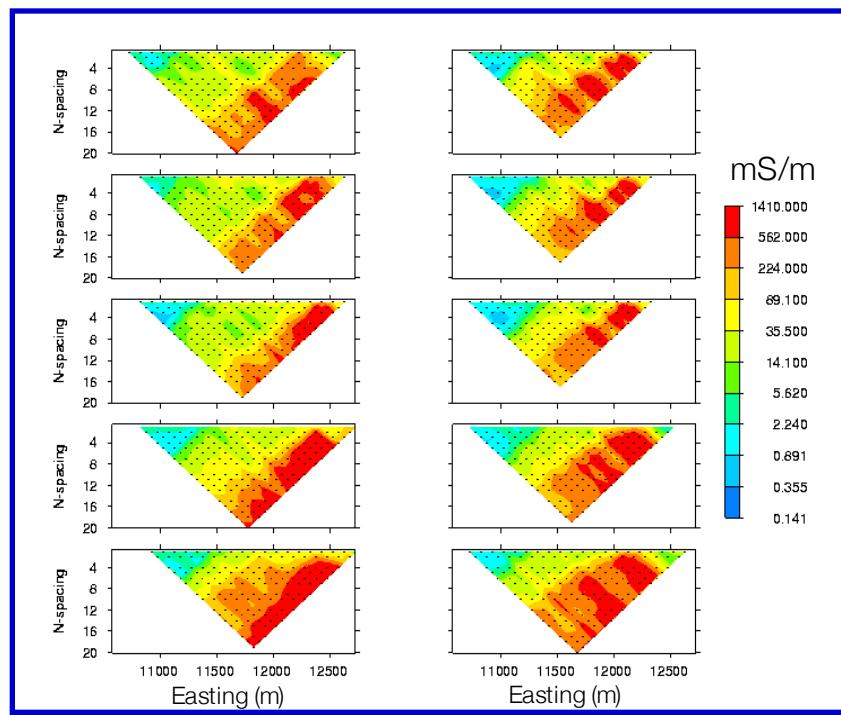
# Survey and Data

- Eight survey lines
- Two survey configurations.

Surface topography

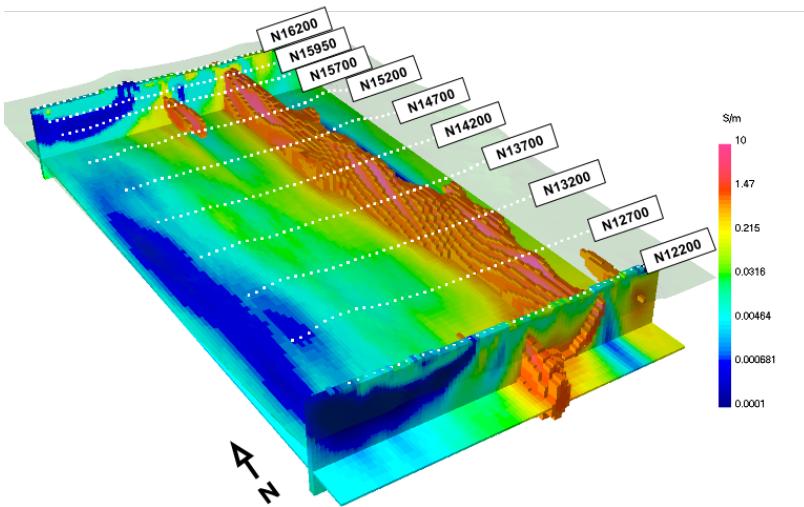


Data set #2:  
Apparent resistivity,  
dipole - pole

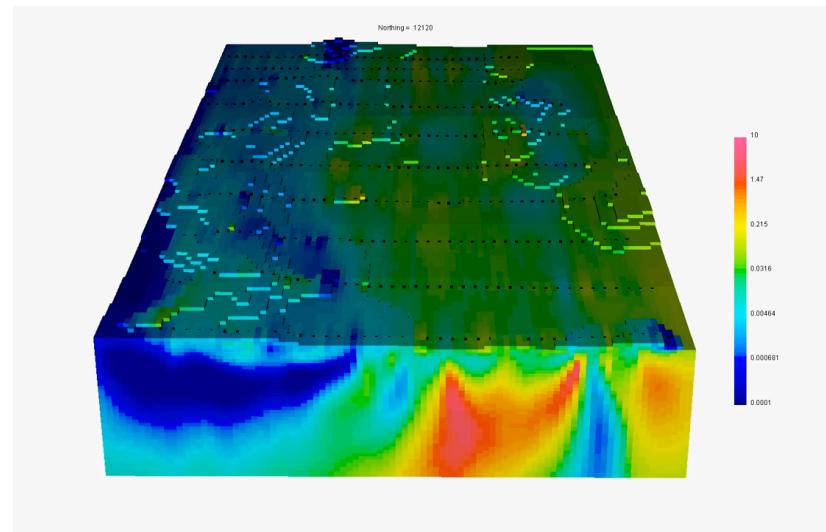


# Processing and interpretation

3D resistivity model



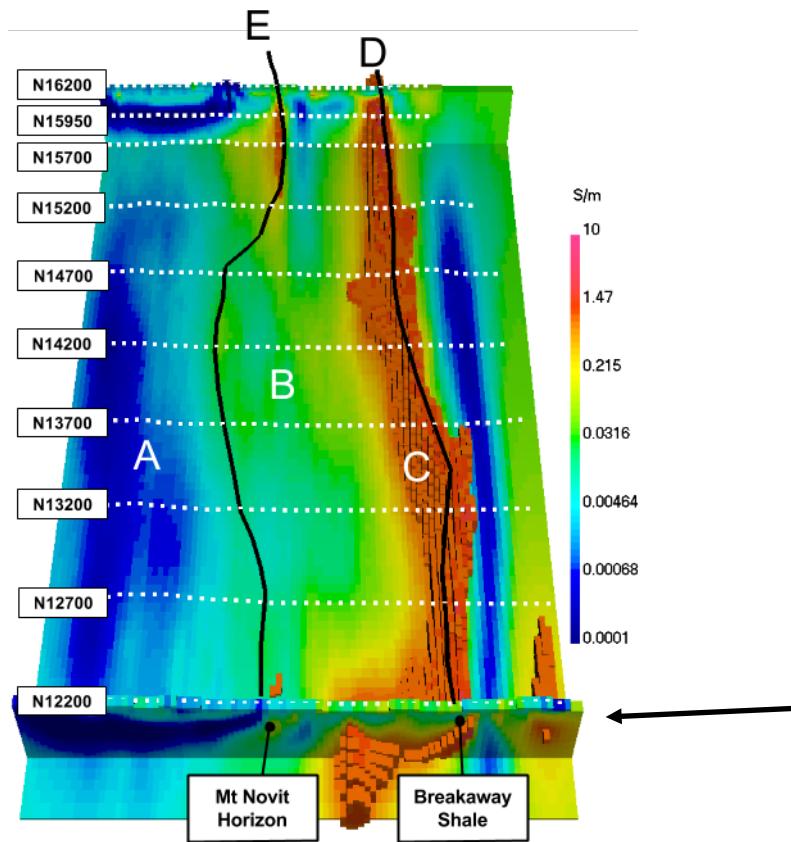
Animation



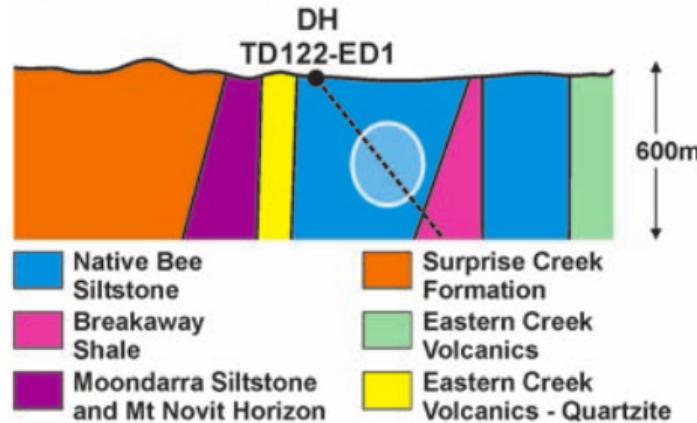
# Synthesis

- Identified a major conductor → black shale unit
- Some indication of a moderate conductor

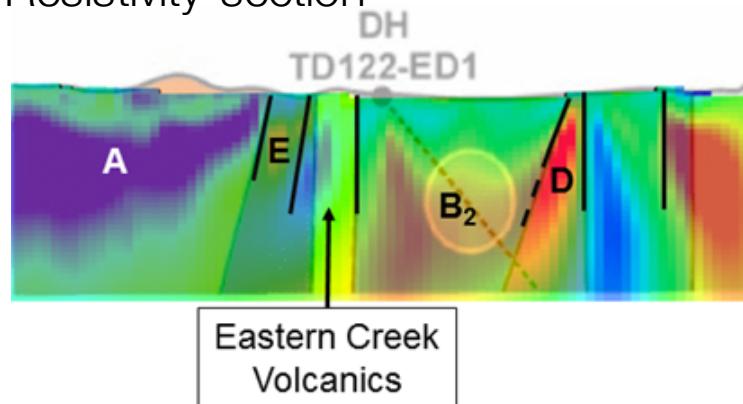
3D resistivity model



Geologic section



Resistivity section

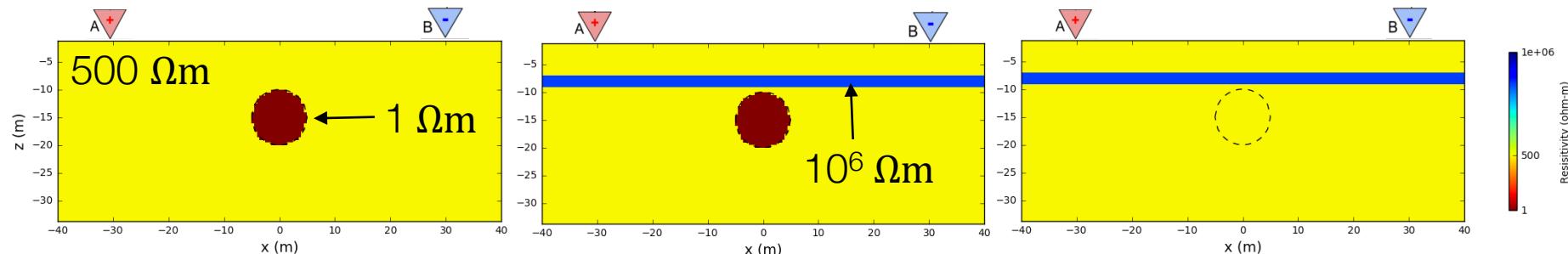


# Outline

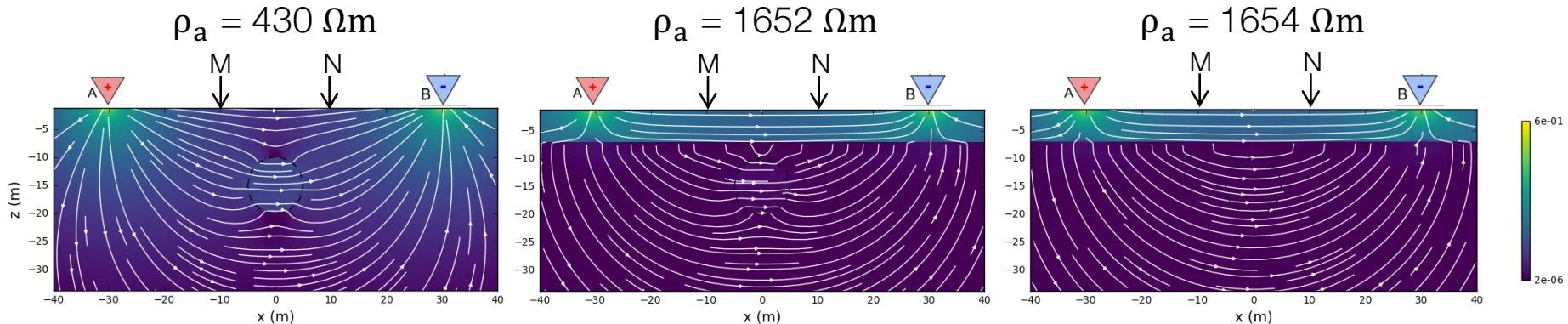
- Basic experiment
- Currents, charges, potentials and apparent resistivities
- Soundings, profiles and arrays
- Data, pseudosections and inversion
- Sensitivity
- Survey Design
- Case History – Mt Isa
  
- Effects of background resistivity

# Effects of background resistivity

Resistivity models (thin resistive layer)

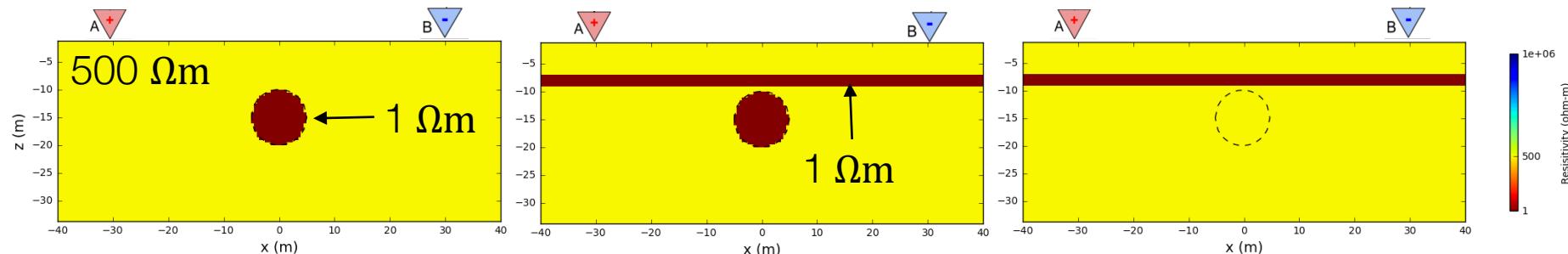


Currents and measured data at MN

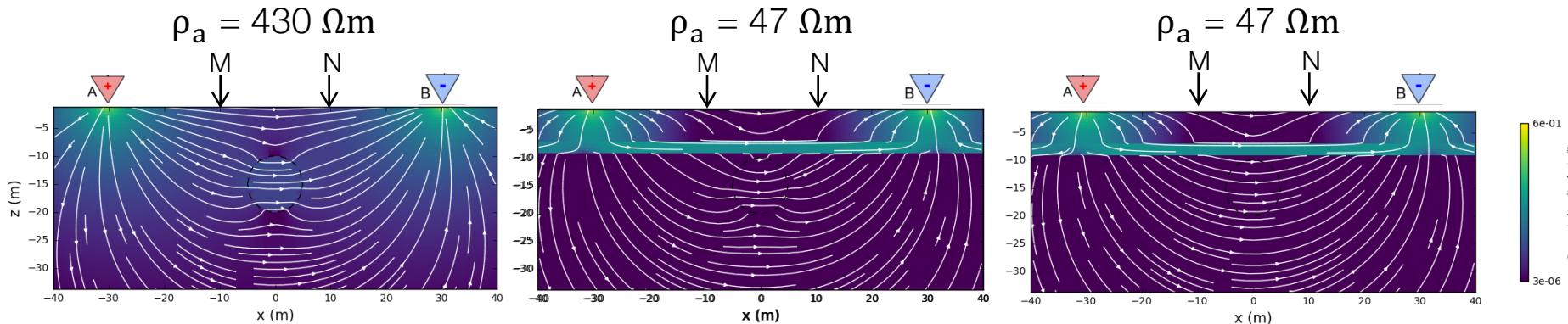


# Effects of background resistivity

Resistivity models (thin conductive layer)



Currents and measured data at MN



# End of DCR

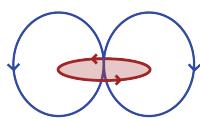
Next up



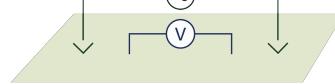
DC Resistivity



EM  
Fundamentals



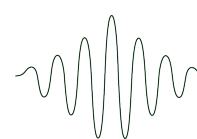
Inductive  
Sources



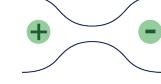
Grounded  
Sources



Natural  
Sources



GPR



Induced  
Polarization



The  
Future



Lunch: Play with apps