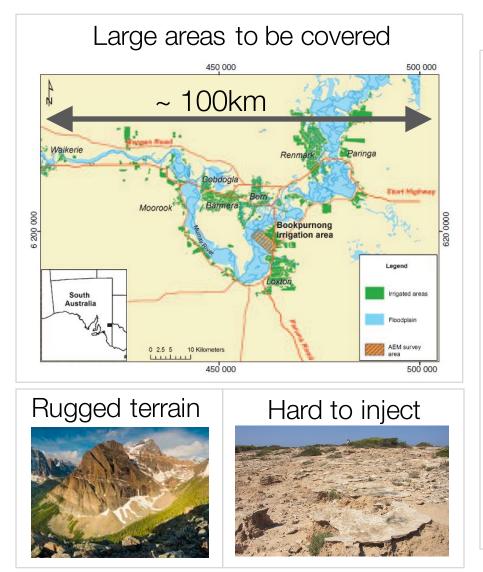
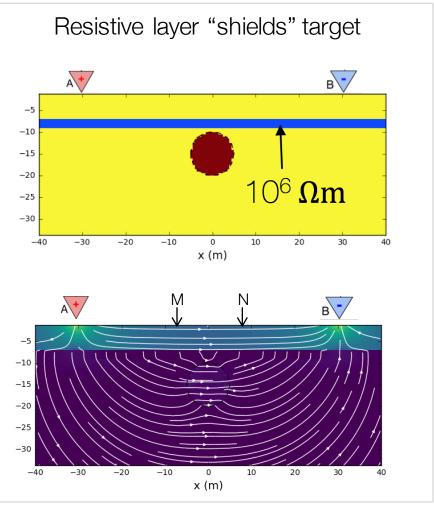
EM Fundamentals





Motivation: applications difficult for DC



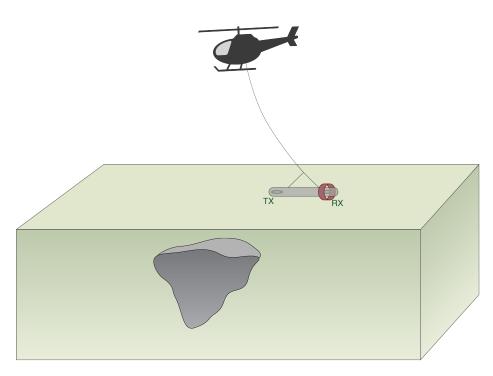


Outline

- Basic Survey
- Ampere's and Faraday's Laws (2-coil App)
- Circuit model for EM induction
- Frequency and time domain data
- Sphere in homogeneous earth
- Cyl code
- Energy losses in the ground

• Setup:

transmitter and receiver are in a towed bird

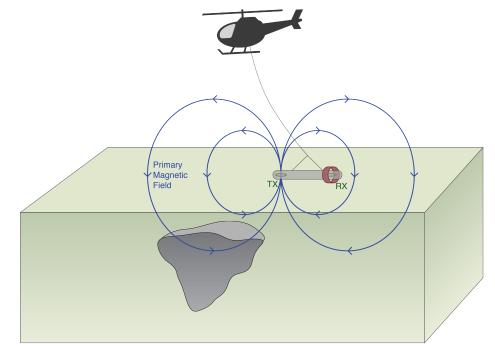


• Setup:

 transmitter and receiver are in a towed bird

• Primary:

 Transmitter produces a primary magnetic field

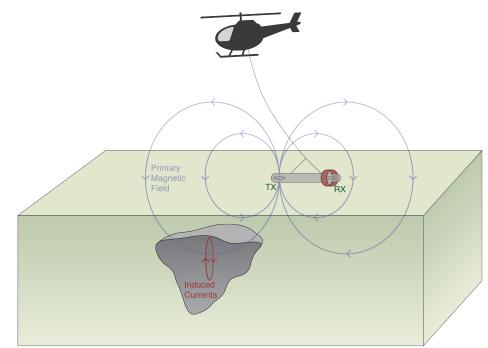


• Setup:

- transmitter and receiver are in a towed bird
- Primary:
 - Transmitter produces a primary magnetic field

• Induced Currents:

 Time varying magnetic fields generate electric fields everywhere and currents in conductors



• Setup:

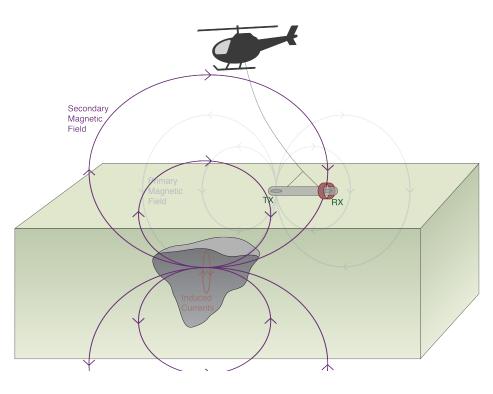
- transmitter and receiver are in a towed bird
- Primary:
 - Transmitter produces a primary magnetic field

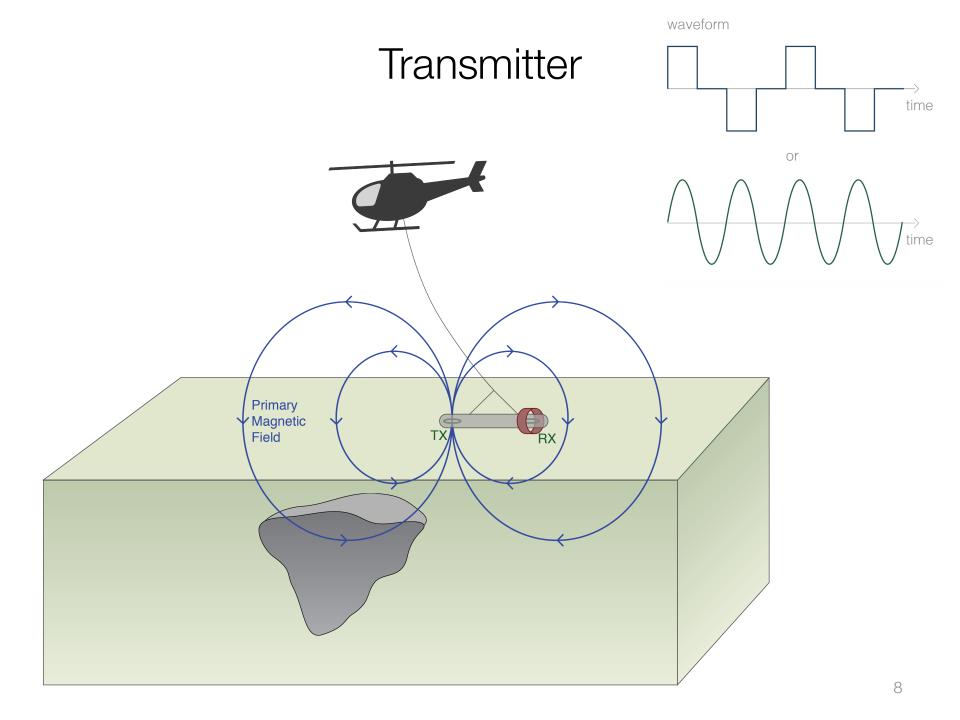
• Induced Currents:

 Time varying magnetic fields generate electric fields everywhere and currents in conductors

Secondary Fields:

 The induced currents produce a secondary magnetic field.



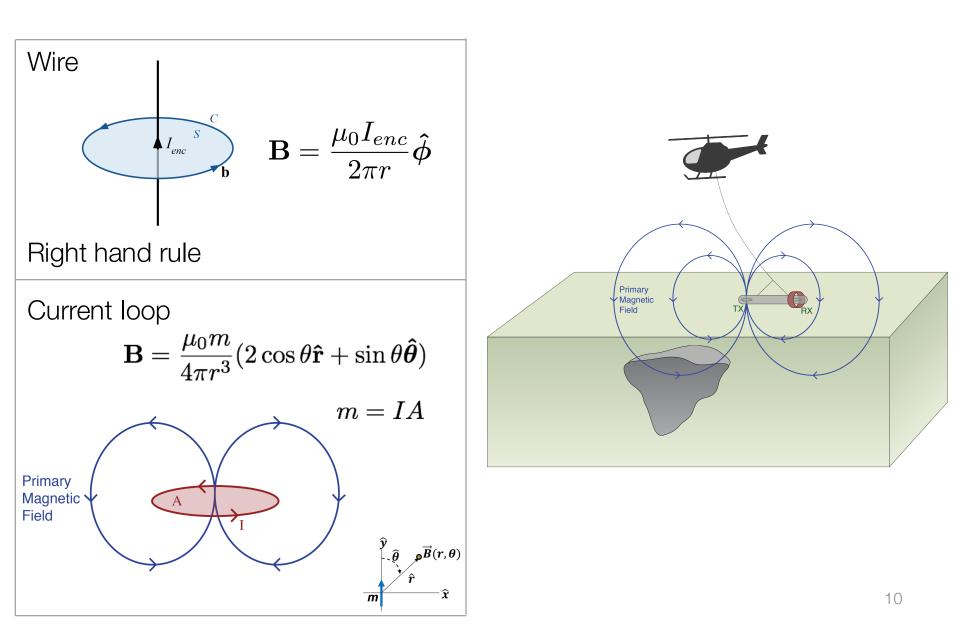


Basic Equations: Quasi-static

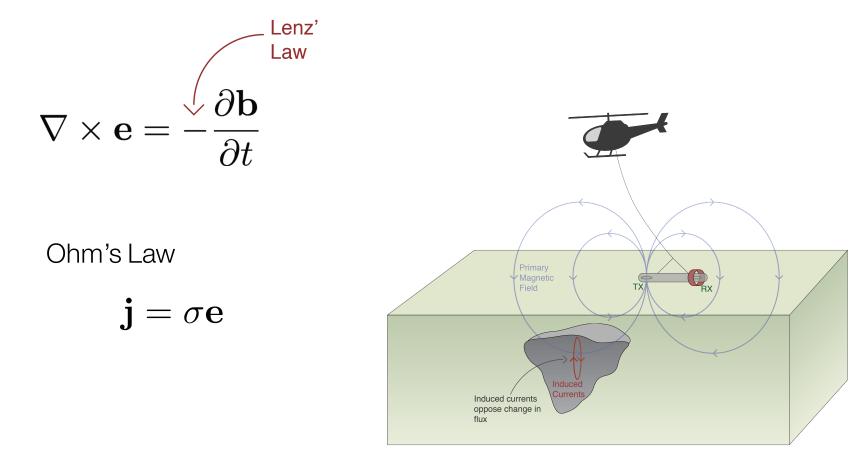
	Time	
Faraday's Law	$\nabla \times \mathbf{e} = -\frac{\partial \mathbf{b}}{\partial t}$	$ abla imes {f E} = -i\omega {f B}$
Ampere's Law	$ abla imes \mathbf{h} = \mathbf{j} + \frac{\partial \mathbf{d}}{\partial t}$	$ abla imes \mathbf{H} = \mathbf{J} + i\omega \mathbf{D}$
No Magnetic Monopoles	$\nabla \cdot \mathbf{b} = 0$	$\nabla \cdot \mathbf{B} = 0$
Constitutive Relationships (non-dispersive)	$\mathbf{j} = \sigma \mathbf{e}$ $\mathbf{b} = \mu \mathbf{h}$ $\mathbf{d} = \varepsilon \mathbf{e}$	$J = \sigma \mathbf{E}$ $\mathbf{B} = \mu \mathbf{H}$ $\mathbf{D} = \varepsilon \mathbf{E}$

* Solve with sources and boundary conditions

Ampere's Law $\nabla \times \mathbf{H} = \mathbf{J}$



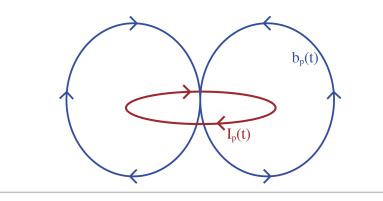
Faraday's Law and Induced Currents



Two Coil Example: Harmonic

Source (red loop)

Time varying current → Time varying magnetic flux



Faraday's Law

$$abla imes \mathbf{e} = -\frac{\partial \mathbf{b}}{\partial t}$$

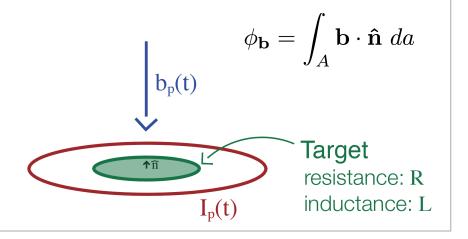
าโ

Ohm's Law

$$\mathbf{j} = \sigma \mathbf{e}$$

Target (green loop)

• Time varying magnetic flux



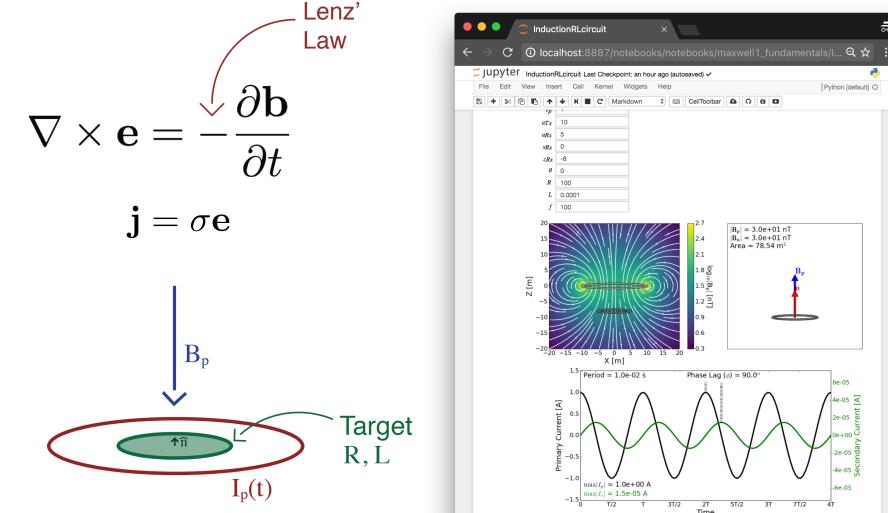
EMF (voltage) is related to time rate of change in flux.

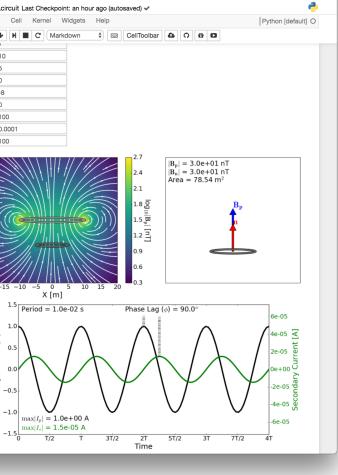
V

$$V = EMF = -\frac{d\phi_{\mathbf{b}}}{dt}$$

R

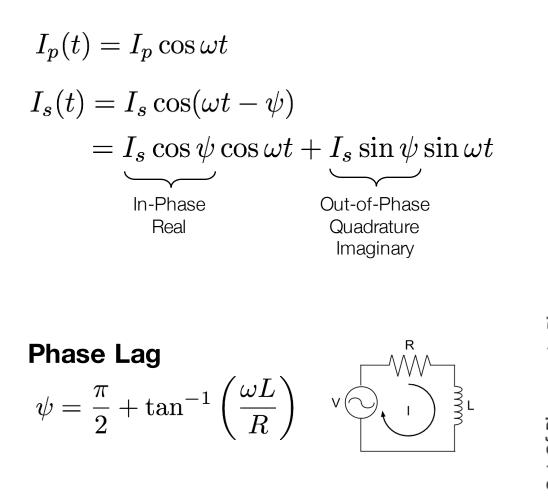
App for Faraday's Law

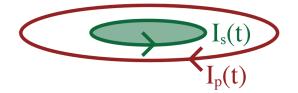


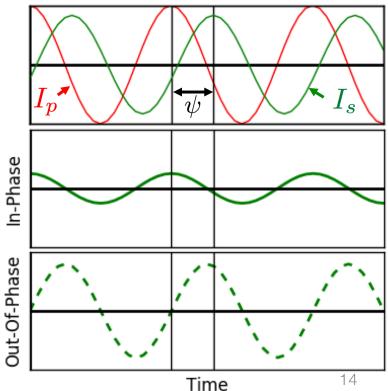


Two Coil Example: Harmonic

Induced Currents

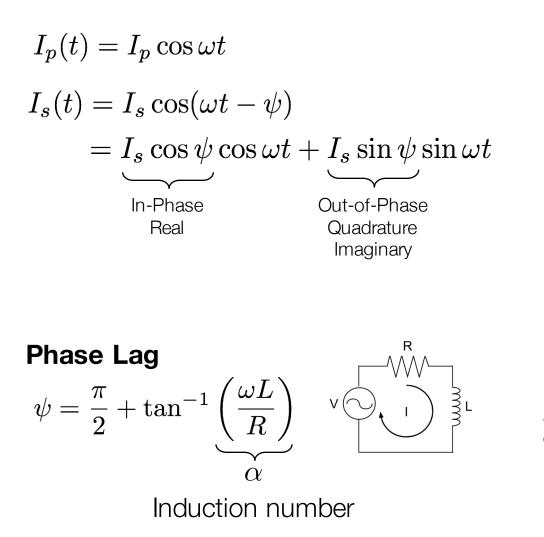


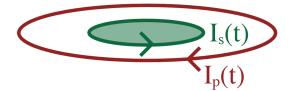


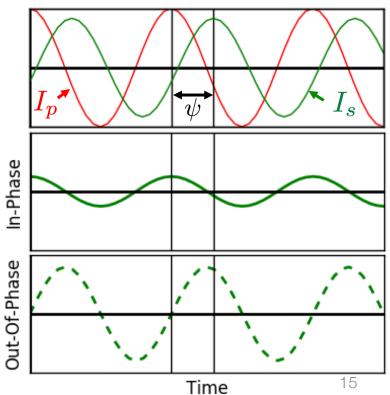


Two Coil Example: Harmonic

Induced Currents







Response Function

- Quantifies how a target responds to a time varying magnetic field
- Partitions real and imaginary parts

 ωL

R

 $\alpha =$

1.0

0.8

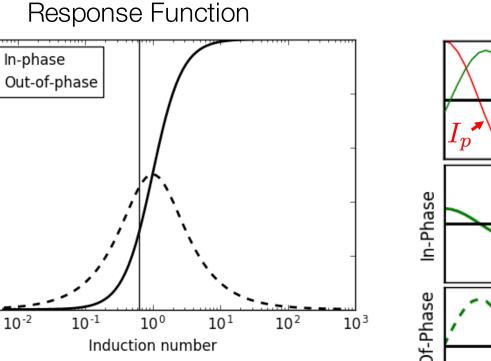
0.6

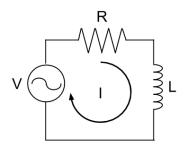
0.4

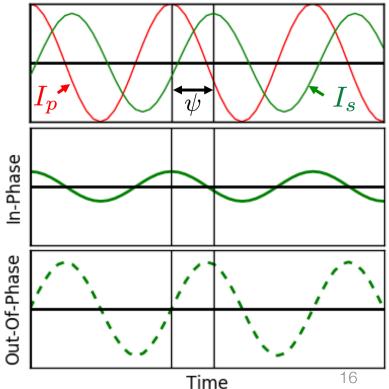
0.2

0.0 L 10⁻³

Harmonic response

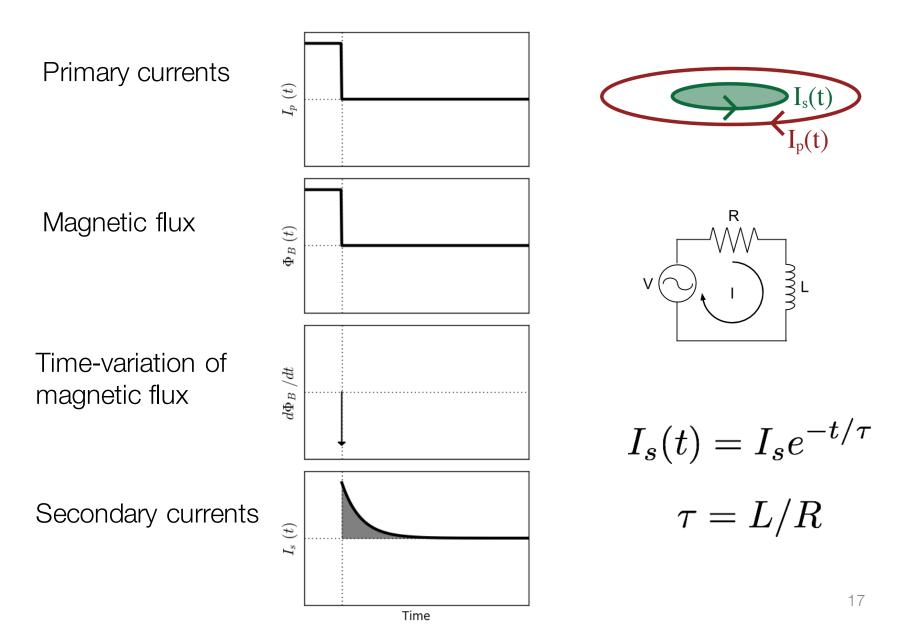






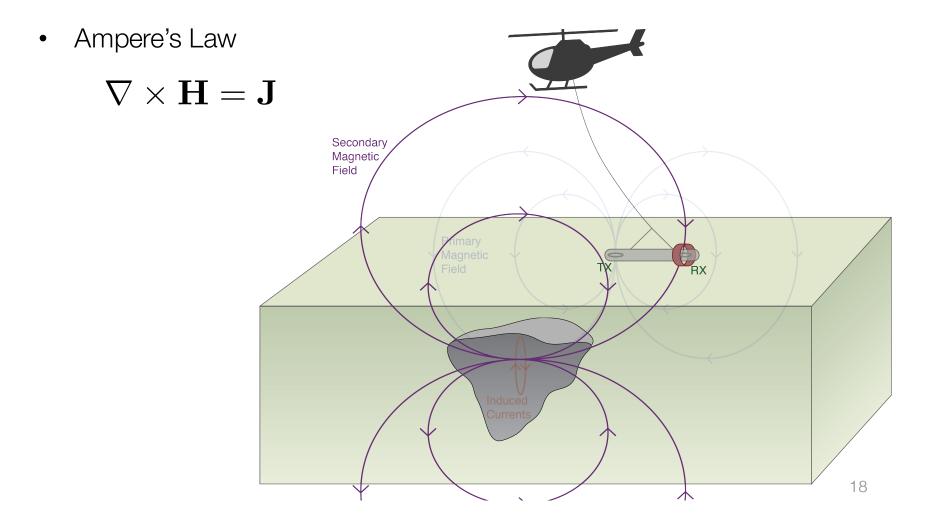
Two Coil Example: Transient

TDEM

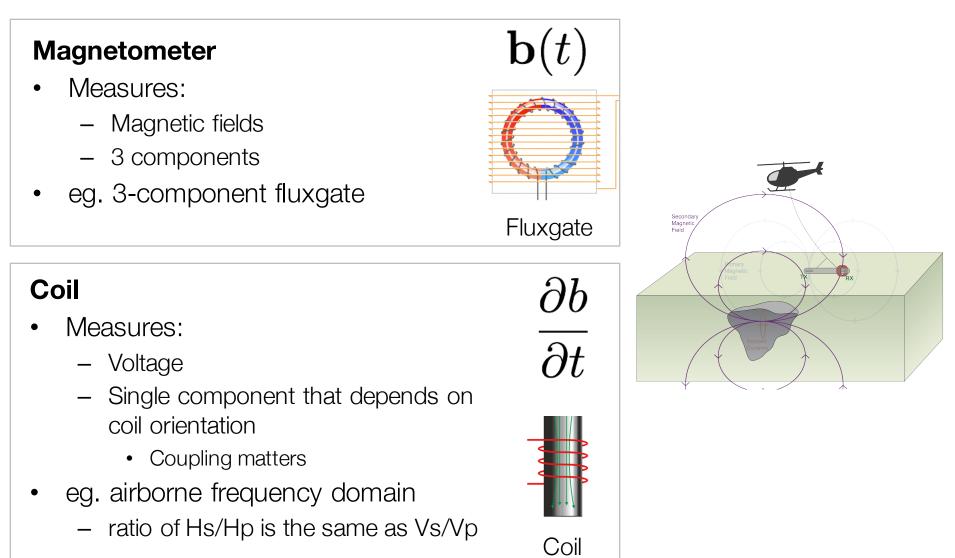


Secondary magnetic fields

Induced currents generate magnetic fields



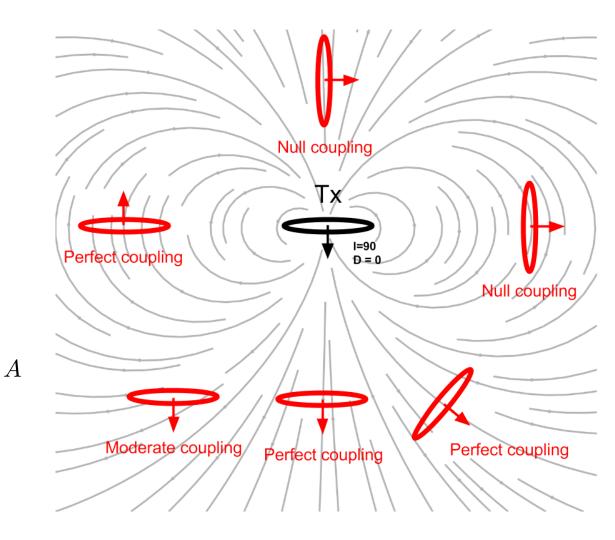
Receiver and Data



Coupling

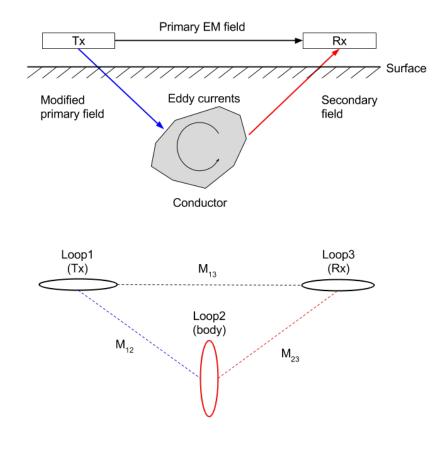
- Transmitter: Primary $I_p(t) = I_p \cos(\omega t)$ $\mathbf{B}_p(t) \sim I_p \cos(\omega t)$
- Target: Secondary

$$EMF = -\frac{\partial \phi_{\mathbf{B}}}{\partial t}$$
$$= -\frac{\partial}{\partial t} \left(\mathbf{B}_{p} \cdot \hat{\mathbf{n}} \right)$$





Circuit model of EM induction



Coupling coefficient

• Depends on geometry

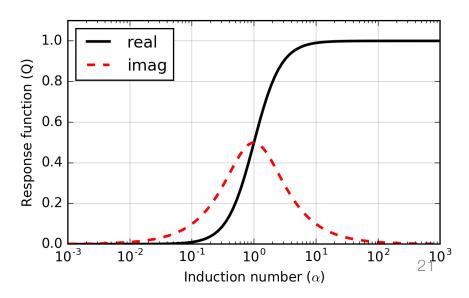
$$M_{12} = \frac{\mu_0}{4\pi} \oint \oint \frac{dl_1 \cdot dl_2}{|\mathbf{r} - \mathbf{r}'|^2}.$$

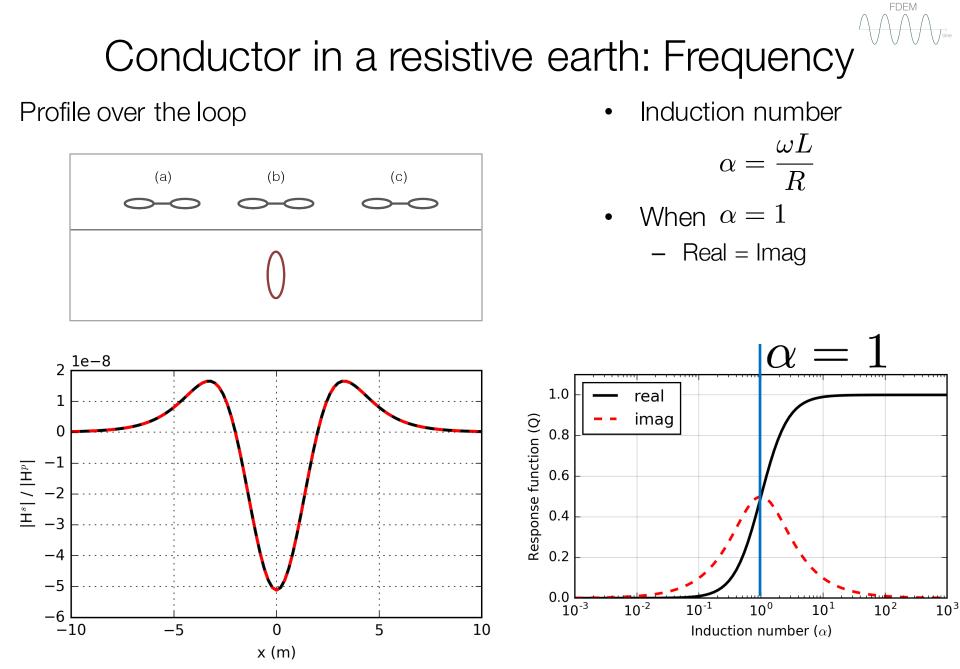
Magnetic field at the receiver

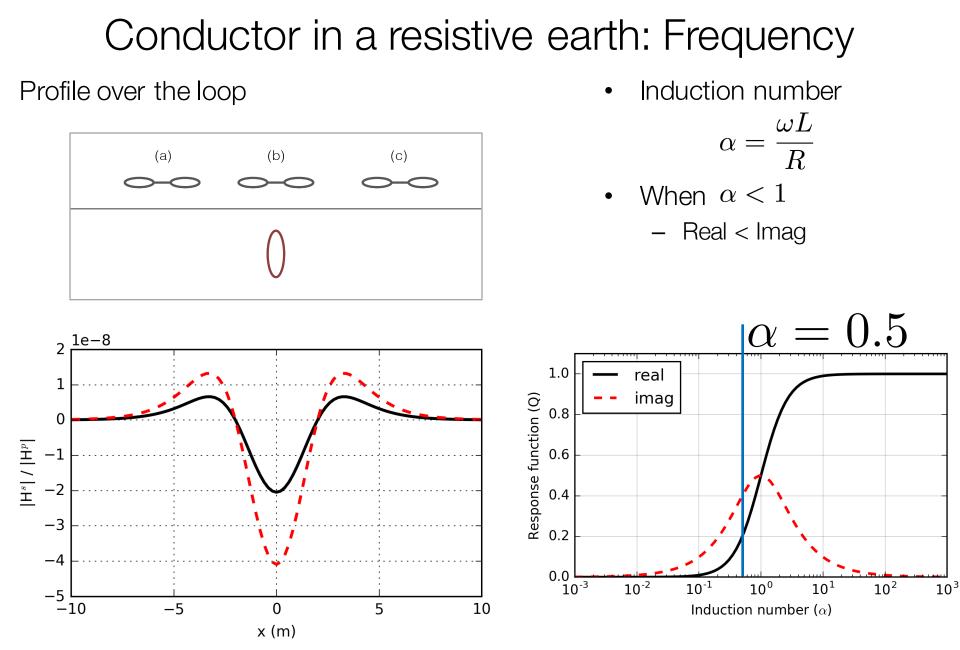
$$\frac{H^s}{H^p} = -\frac{M_{12}M_{23}}{M_{13}L} \underbrace{\left[\frac{\alpha^2 + i\alpha}{1 + \alpha^2}\right]}_Q$$

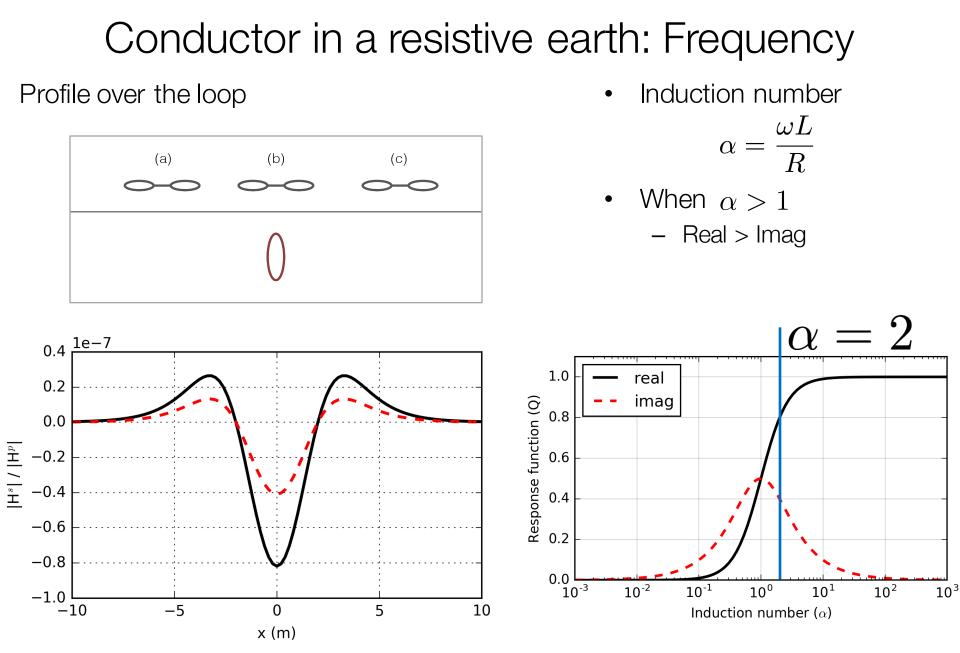
Induction Number

• Depends on properties $\alpha = \frac{\omega L}{R}$ of target







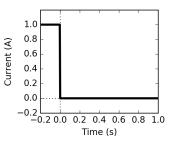


Conductor in a resistive earth: Transient

(b) (a) (C) 0.4 <u>le-6</u> 0.2 0.0 -0.2db/dt (V) ι_2 -0.4-0.6-0.8-1.0 \mathcal{T} ()-1.2∟ -10 -5 5 10 0 x (m)

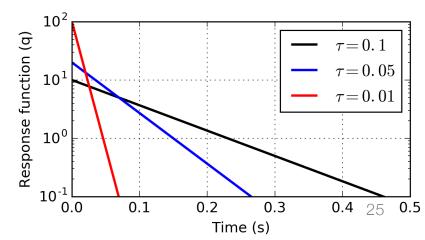
Profile over the loop

- Time constant $\tau = L/R$
- Step-off current in Tx



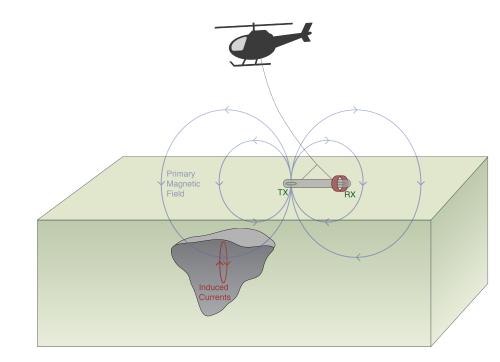
• Response function depends on time, au

$$q(t) = e^{-t/\tau}$$



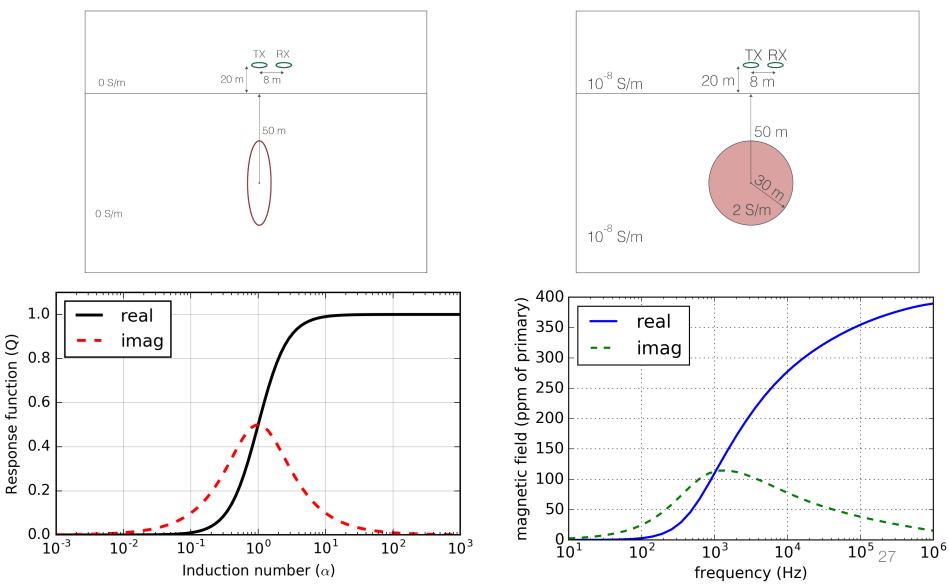
Recap: what have we learned?

- Basics of EM induction
- Response functions
- Mutual coupling
- Data for frequency or time
 domain systems
- Circuit model provides
 representative results
 - Applicable to geologic targets?



Sphere in a resistive background

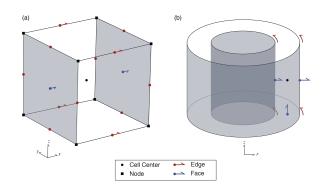
How representative is a circuit model?



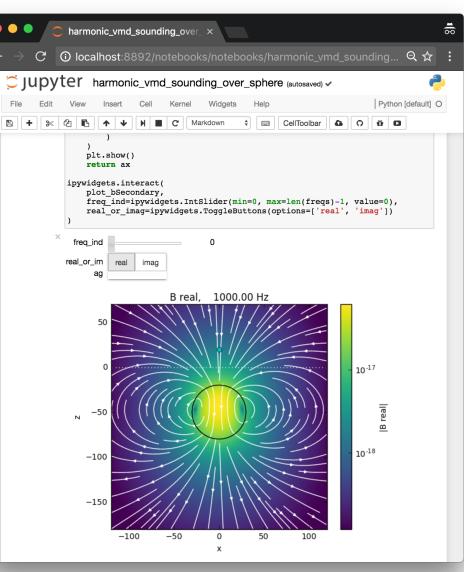
Cyl Code



- Finite Volume EM
 - Frequency and Time



- Built on SimPEG
- Open source, available at: <u>http://em.geosci.xyz/apps.html</u>

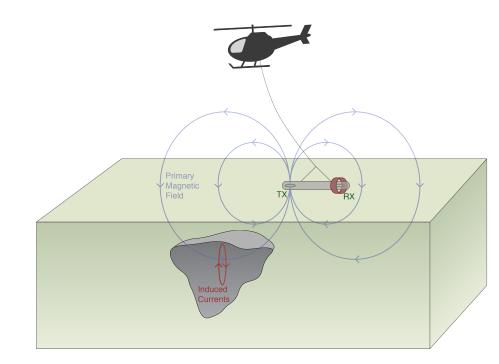


Recap: what have we learned?

- Basics of EM induction
- Response functions
- Mutual coupling
- Data for frequency or time
 domain systems
- Circuit model is a good proxy

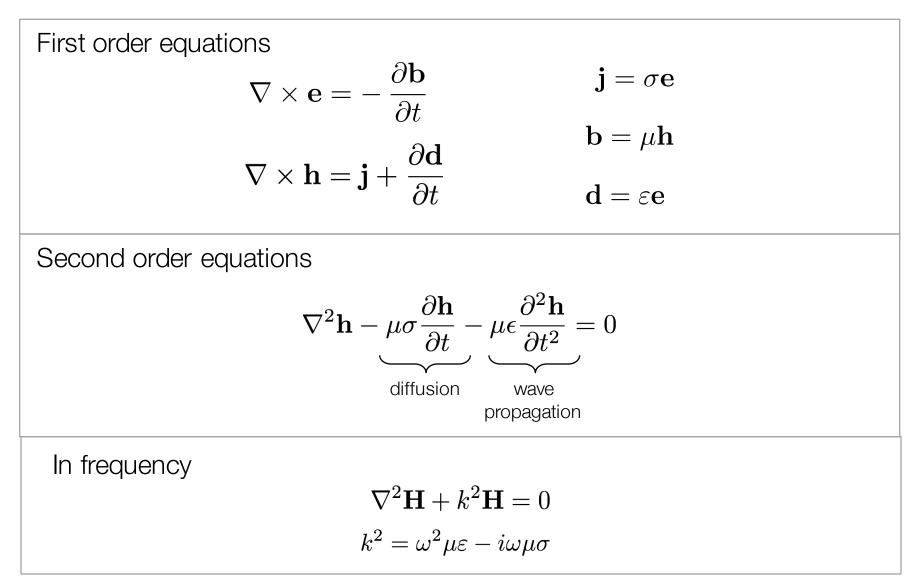
Major item not yet accounted for...

- Propagation of energy from
 - Transmitter to target
 - Target to receiver



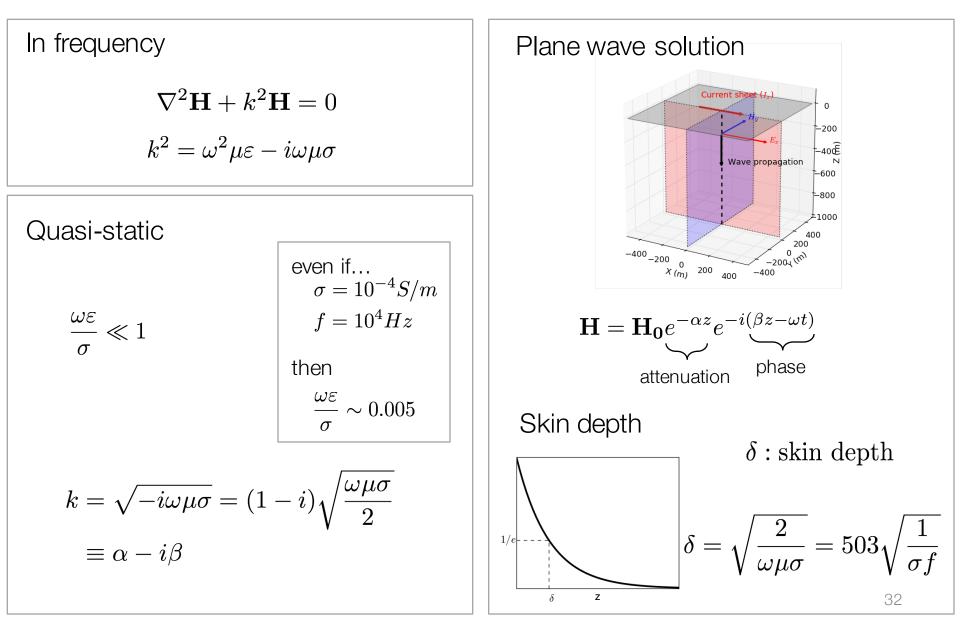
How do EM fields and fluxes behave in a conductive background?

Revisit Maxwell's equations

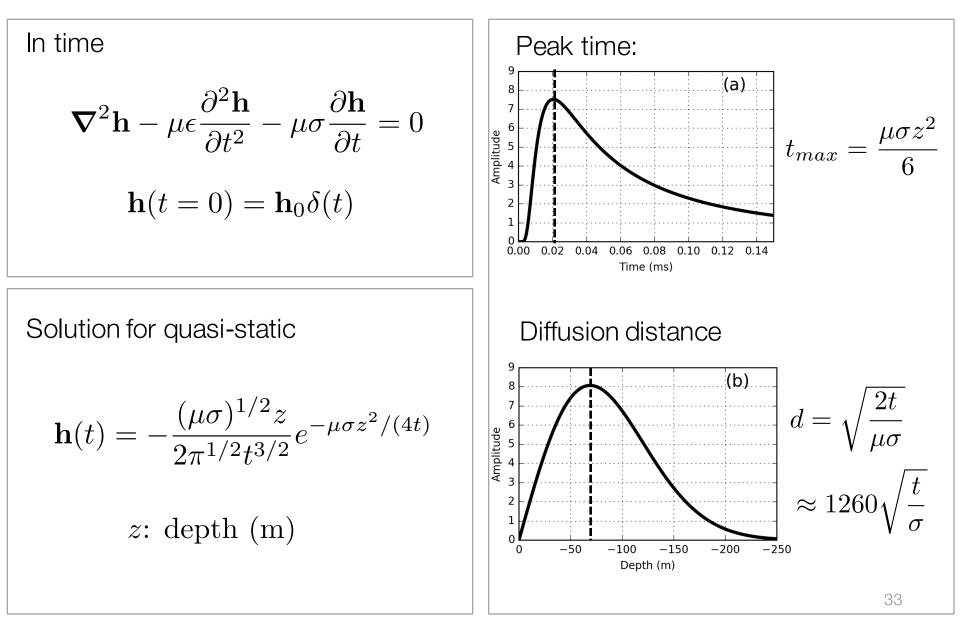


* Same equation holds for E

Plane waves in a homogeneous media

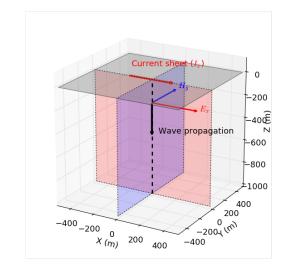


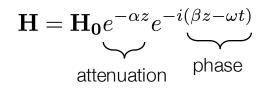
Plane waves in a homogeneous media

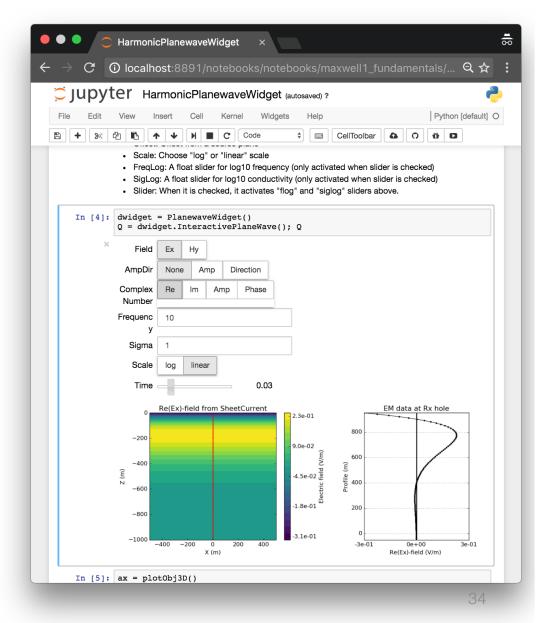


Frequency Domain App: Plane waves

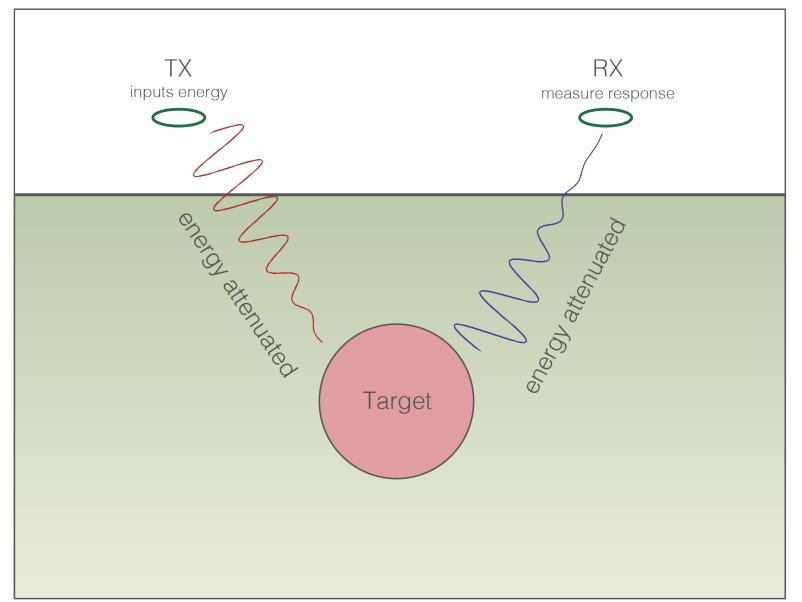
Plane wave







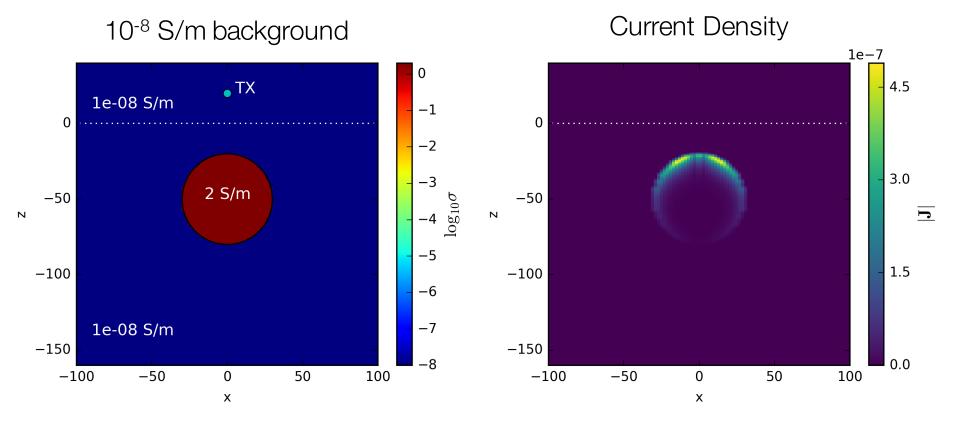
Effects of background resistivity



Effects of background resistivity: Frequency

- Buried, conductive sphere
- Vary background conductivity
- Frequency: 10⁴ Hz



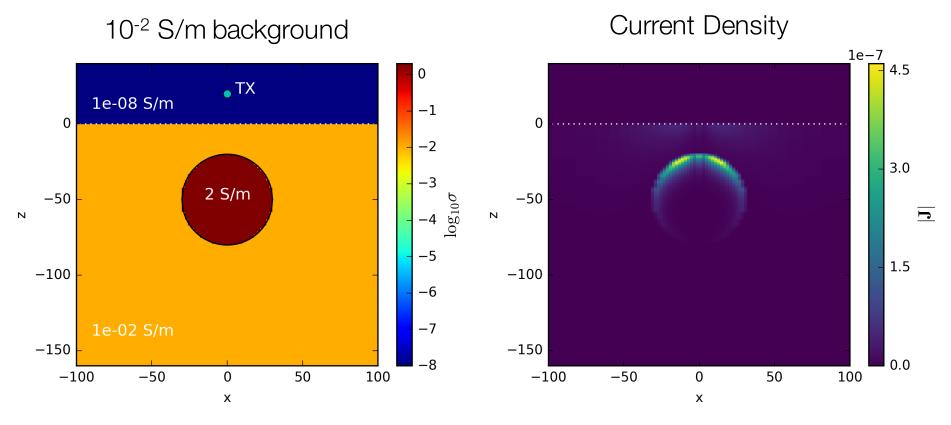


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- Buried, conductive sphere
- Vary background conductivity

Frequency: 10⁴ Hz

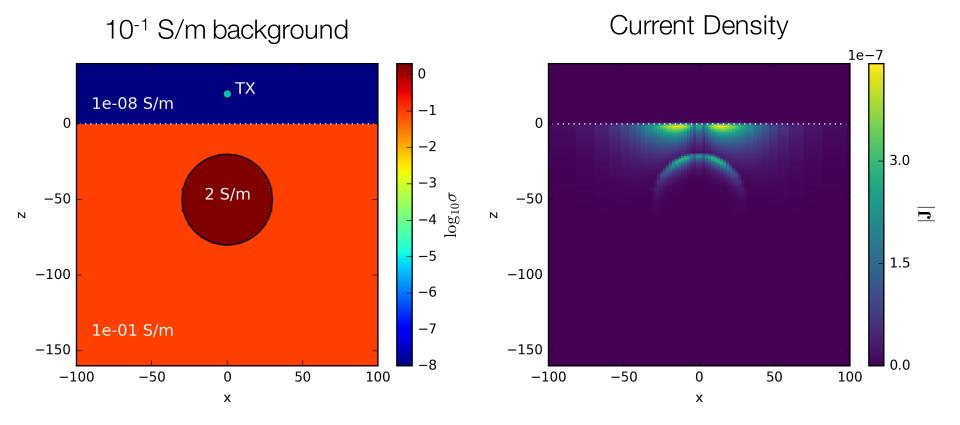




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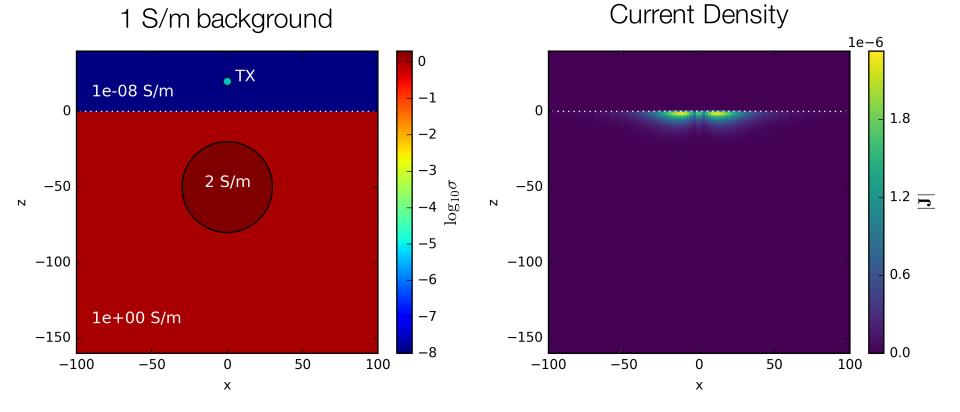
- Buried, conductive sphere
- Vary background conductivity
- Frequency: 10⁴ Hz

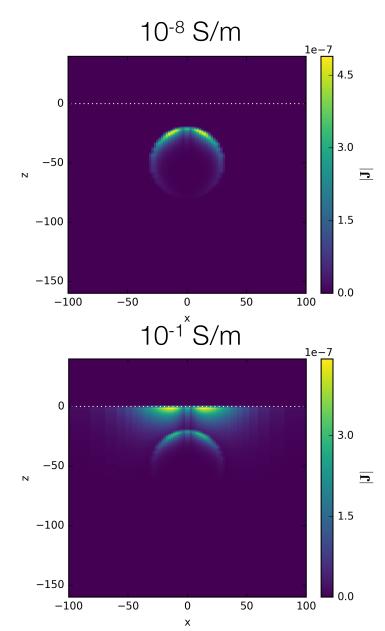


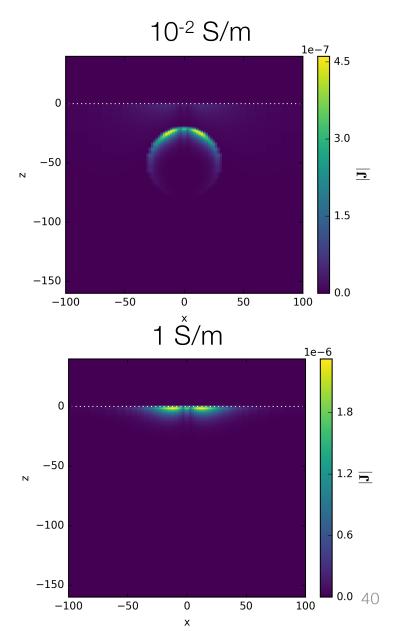


- Buried, conductive sphere
- Vary background conductivity
- Frequency: 10⁴ Hz





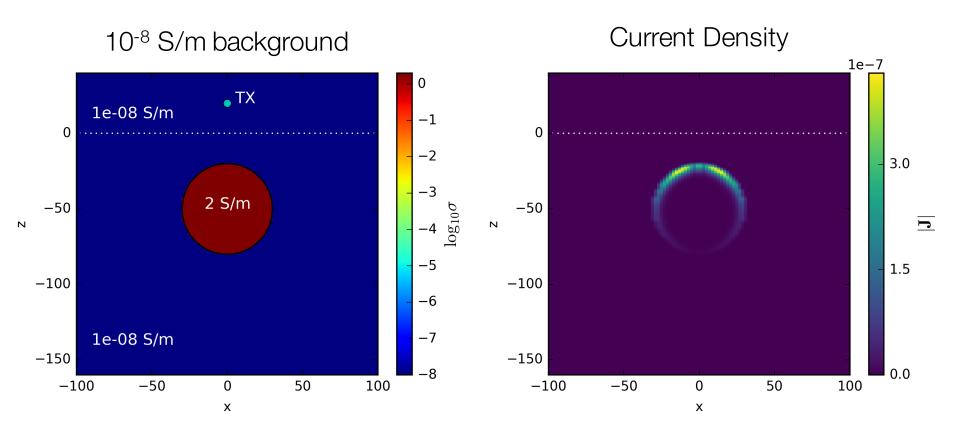




10⁴ Hz

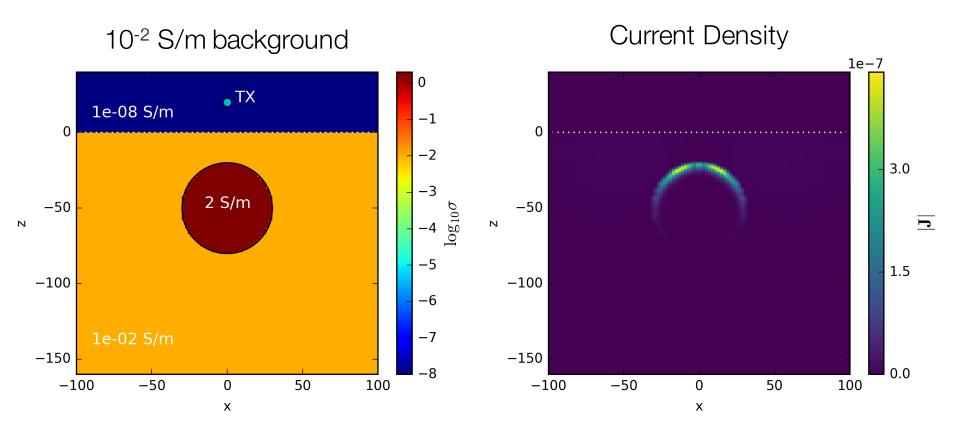
- Buried, conductive sphere
- Vary background conductivity
- Time: 10⁻⁵ s



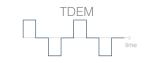


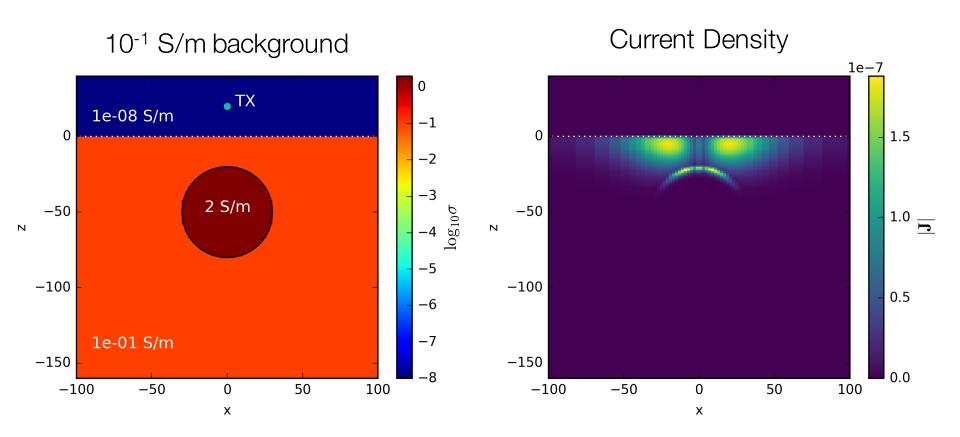
- Buried, conductive sphere
- Vary background conductivity
- Time: 10⁻⁵ s



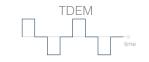


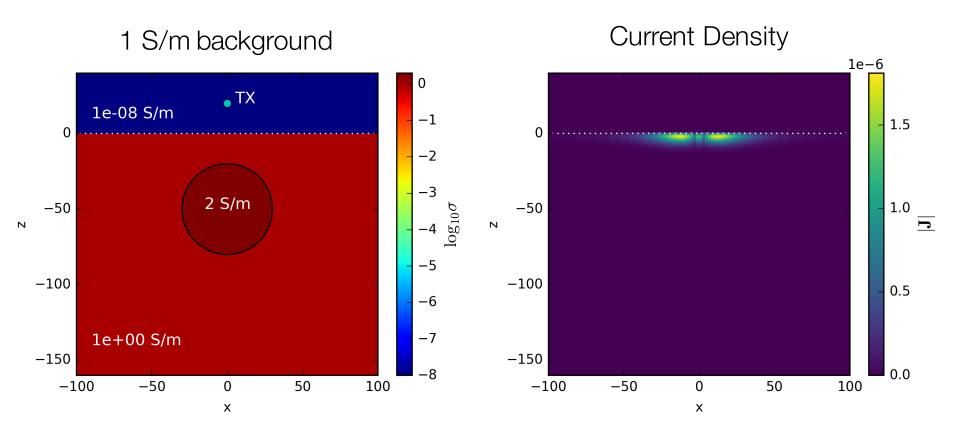
- Buried, conductive sphere
- Vary background conductivity
- Time: 10⁻⁵ s

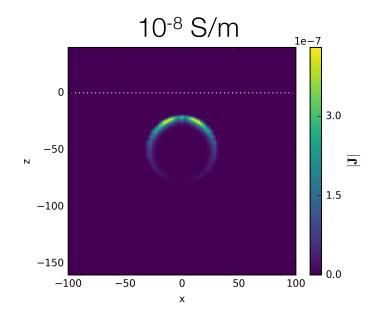




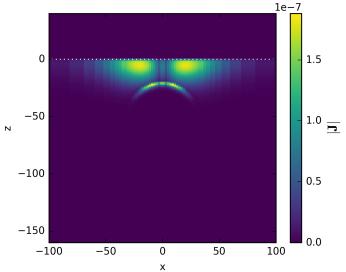
- Buried, conductive sphere
- Vary background conductivity
- Time: 10⁻⁵ s

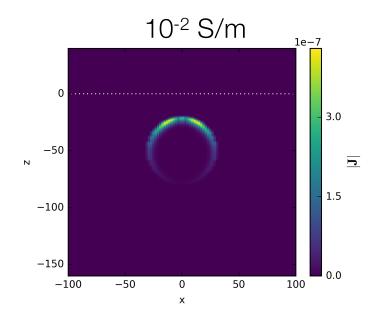




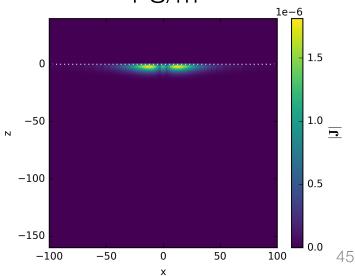






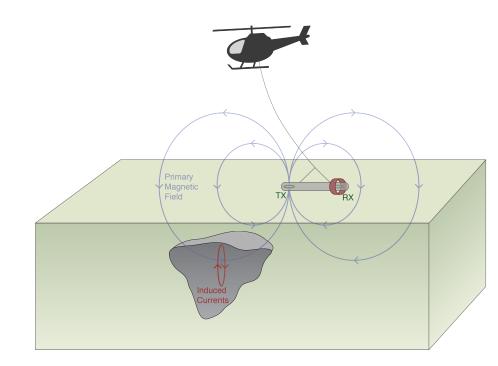




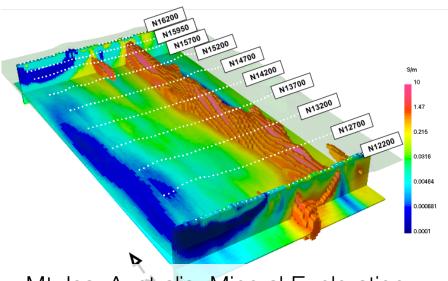


Recap: what have we learned?

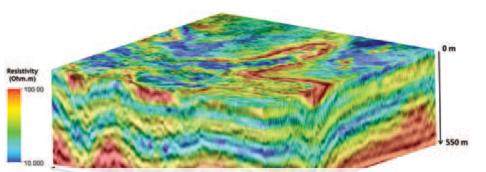
- Basics of EM induction
- Response functions
- Mutual coupling
- Data for frequency or time
 domain systems
- Circuit model is a good proxy
- Need to account for energy losses
- Ready to look at some field examples



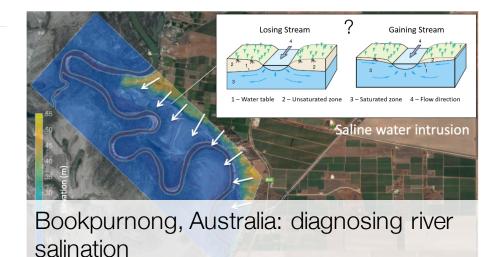
Today's Case Histories

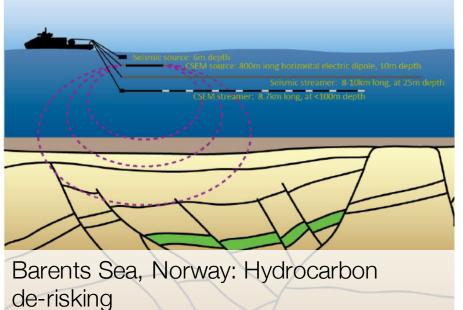


Mt. Isa, Australia: Mineral Exploration

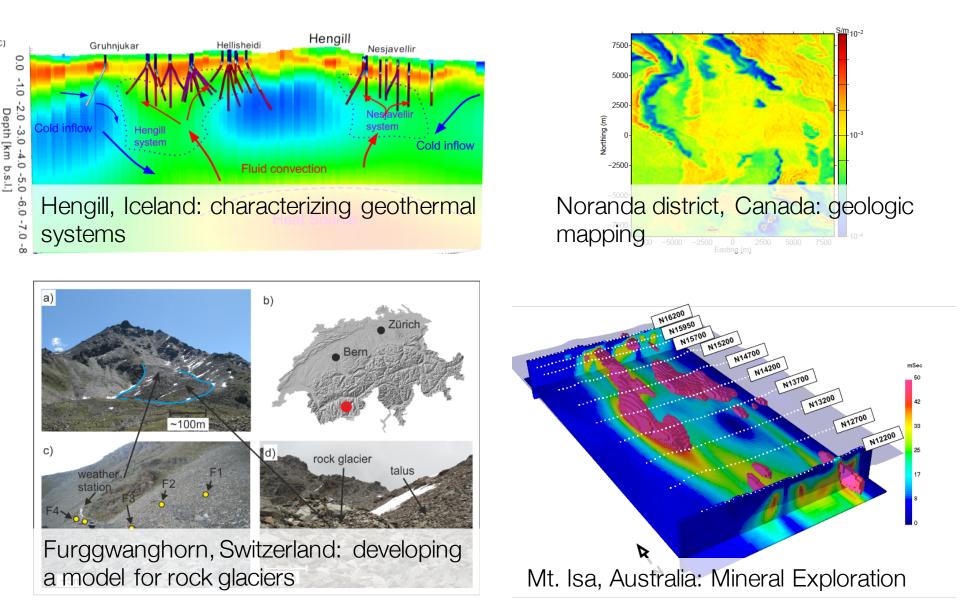


Wadi Sahba, Saudi Arabia: Improving seismic imaging using airborne EM

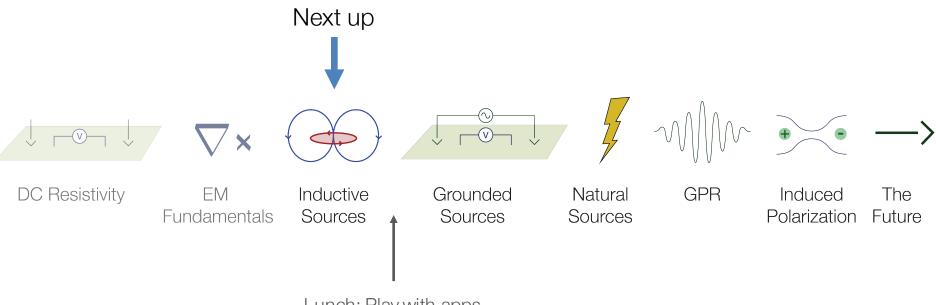




Today's Case Histories



End of EM Fundamentals



Lunch: Play with apps