# **EM** Fundamentals





# Motivation: applications difficult for DC





# Outline

- Basic Survey
- Ampere's and Faraday's Laws (2-coil App)
- Circuit model for EM induction
- Frequency and time domain data
- Sphere in homogeneous earth
- Cyl code
- Energy losses in the ground

#### • Setup:

 transmitter and receiver are in a towed bird



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 Transmitter produces a primary magnetic field



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### Induced Currents:

 Time varying magnetic fields generate electric fields everywhere and currents in conductors



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### • Induced Currents:

 Time varying magnetic fields generate electric fields everywhere and currents in conductors

### Secondary Fields:

 The induced currents produce a secondary magnetic field.





# Basic Equations: Quasi-static

	Time	Frequency
Faraday's Law	$\nabla \times \mathbf{e} = -\frac{\partial \mathbf{b}}{\partial t}$	$ abla  imes \mathbf{E} = -i\omega \mathbf{B}$
Ampere's Law	$ abla  imes \mathbf{h} = \mathbf{j} + rac{\partial \mathbf{d}}{\partial t}$	$ abla  imes \mathbf{H} = \mathbf{J} + i\omega \mathbf{D}$
No Magnetic Monopoles	$\nabla \cdot \mathbf{b} = 0$	$\nabla \cdot \mathbf{B} = 0$
Constitutive Relationships (non-dispersive)	$\mathbf{j} = \sigma \mathbf{e}$	$\mathbf{J}=\sigma\mathbf{E}$
	$\mathbf{b}=\mu\mathbf{h}$	${f B}=\mu {f H}$
	$\mathbf{d} = \varepsilon \mathbf{e}$	$\mathbf{D} = \varepsilon \mathbf{E}$

\* Solve with sources and boundary conditions

### Ampere's Law $\nabla \times \mathbf{H} = \mathbf{J}$



### Faraday's Law



# Faraday's Law





Magnetic Flux

$$\phi_{\mathbf{b}} = \int_{A} \mathbf{b} \cdot \hat{\mathbf{n}} \, da$$

Induced EMF

$$V = EMF = -\frac{d\phi_{\mathbf{b}}}{dt} = \mathbf{0}$$



# $\phi_b$ : constant







# App for Faraday's Law

### 2 Apps:

- Harmonic
- Transient





http://em.geosci.xyz/apps.html

### Two Coil Example: Transient

TDEM



# **Response Function: Transient**



### Transient and Harmonic Signals

We have seen a transient pulse...

What happens when he have a harmonic?





# Two Coil Example: Harmonic

#### **Induced Currents**







# Two Coil Example: Harmonic

#### **Induced Currents**







# **Response Function**

- Quantifies how a target responds to a time varying magnetic field
- Partitions real and imaginary parts







# **Response Functions: Summary**



# Secondary magnetic fields

Induced currents generate magnetic fields



# Receiver and Data



# Coupling

- Transmitter: Primary  $I_p(t) = I_p \cos(\omega t)$  $\mathbf{B}_p(t) \sim I_p \cos(\omega t)$
- Target: Secondary

$$EMF = -\frac{\partial \phi_{\mathbf{B}}}{\partial t}$$
$$= -\frac{\partial}{\partial t} \left( \mathbf{B}_{p} \cdot \hat{\mathbf{n}} \right)$$





# Circuit model of EM induction



Coupling coefficient

Depends on geometry

$$M_{12} = \frac{\mu_0}{4\pi} \oint \oint \frac{dl_1 \cdot dl_2}{|\mathbf{r} - \mathbf{r}'|^2}.$$

Magnetic field at the receiver

$$\frac{H^s}{H^p} = -\frac{M_{12}M_{23}}{M_{13}L} \underbrace{\left[\frac{\alpha^2 + i\alpha}{1 + \alpha^2}\right]}_Q$$

Induction Number

• Depends on properties  $\alpha = \frac{\omega L}{R}$  of target









# Conductor in a resistive earth: Transient

### Profile over the loop



• Time constant

$$\tau = L/R$$

• Step-off current in Tx



• Response function depends on time, au

$$q(t) = e^{-t/\tau}$$



# Recap: what have we learned?

- Basics of EM induction
- Response functions
- Mutual coupling
- Data for frequency or time
   domain systems
- Circuit model provides
   representative results
  - Applicable to geologic targets?



# Sphere in a resistive background

How representative is a circuit model?



# Cyl Code



- Finite Volume EM
  - Frequency and Time



- Built on SimPEG
- Open source, available at: <u>http://em.geosci.xyz/apps.html</u>

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# Recap: what have we learned?

- Basics of EM induction
- Response functions
- Mutual coupling
- Data for frequency or time
   domain systems
- Circuit model is a good proxy

Major item not yet accounted for...

- Propagation of energy from
  - Transmitter to target
  - Target to receiver



# How do EM fields and fluxes behave in a conductive background?

### Revisit Maxwell's equations



### Plane waves in a homogeneous media



### Plane waves in a homogeneous media



# Plane Wave apps



http://em.geosci.xyz/apps.html



- Buried, conductive sphere
- Vary background conductivity
- Time: 10<sup>-5</sup> s





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10<sup>4</sup> Hz

# Recap: what have we learned?

- Basics of EM induction
- Response functions
- Mutual coupling
- Data for frequency or time
   domain systems
- Circuit model is a good proxy
- Need to account for energy losses
- Ready to look at some field examples



# Today's Case Histories



Mt. Isa, Australia: Mineral Exploration







Barents Sea, Norway: Hydrocarbon de-risking

# Today's Case Histories







Mt. Isa, Australia: Mineral Exploration

# End of EM Fundamentals

