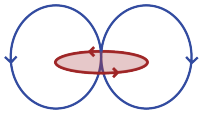
EM: Inductive Sources

DISC

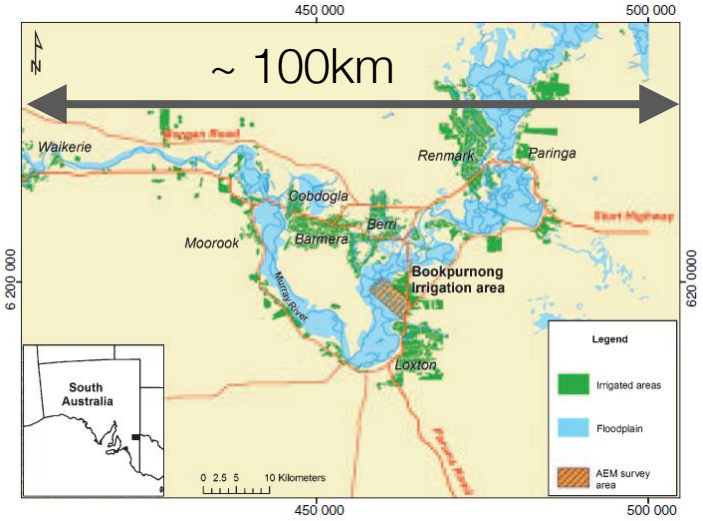
2017

Electromagnetics
Fundamentals and Applications

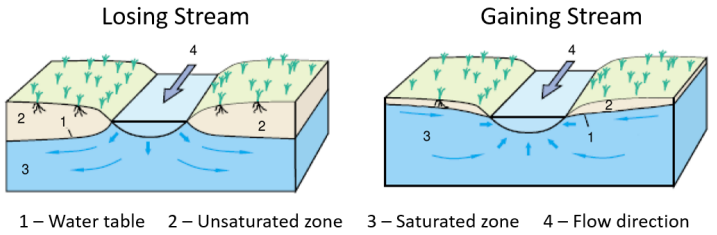


Motivation

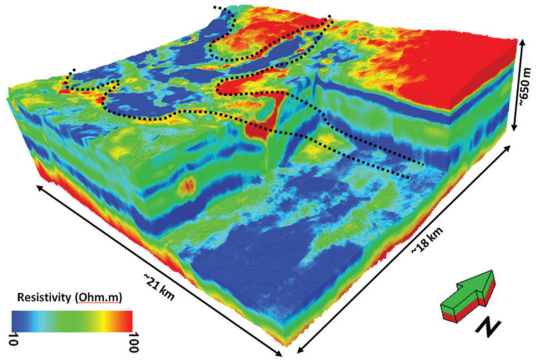
Large areas to be covered



Groundwater



High resolution near surface



Rugged terrain

Minerals

Outline

Setup

- Basic experiment
- Transmitters, Receivers

Frequency Domain EM

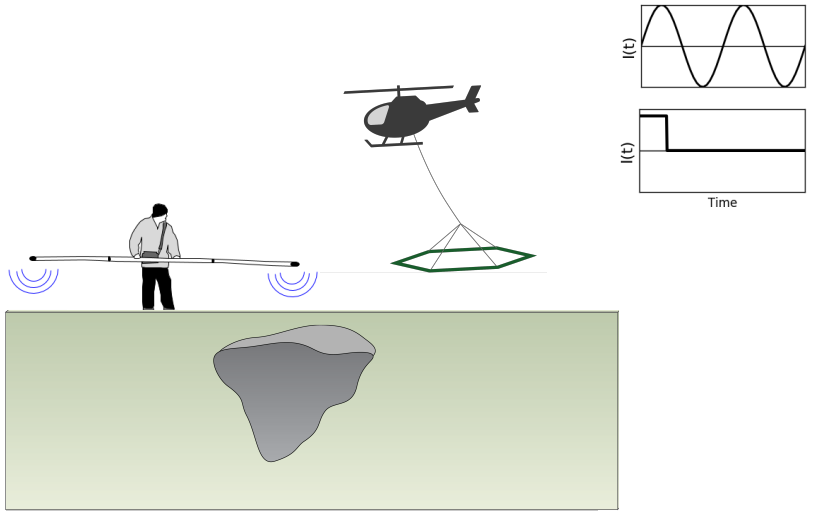
- Vertical Magnetic Dipole
- Effects of Frequency
- Case History – Groundwater

Time Domain EM

- Vertical Magnetic Dipole
- Propagation with Time
- Case History – Near surface geology

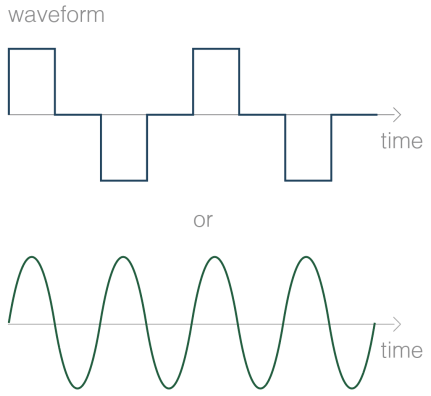
Important questions

- What is the target?
  - at the surface? At depth?. 1D, 2D, 3D?
- Transmitter
  - Location: surface? in the air?
  - Waveform: frequency or time?
  - "Size" and orientation?
- Exciting the target
  - Conductivity of the target and host
  - Geometry of the target (Coupling)
- Receiver and data
  - What fields to measure?
  - What instrument?



- Where to collect data? How many? How accurate?
- What is depth of investigation?
- What is the "footprint" of the transmitter"
  - These are questions of SURVEY DESIGN

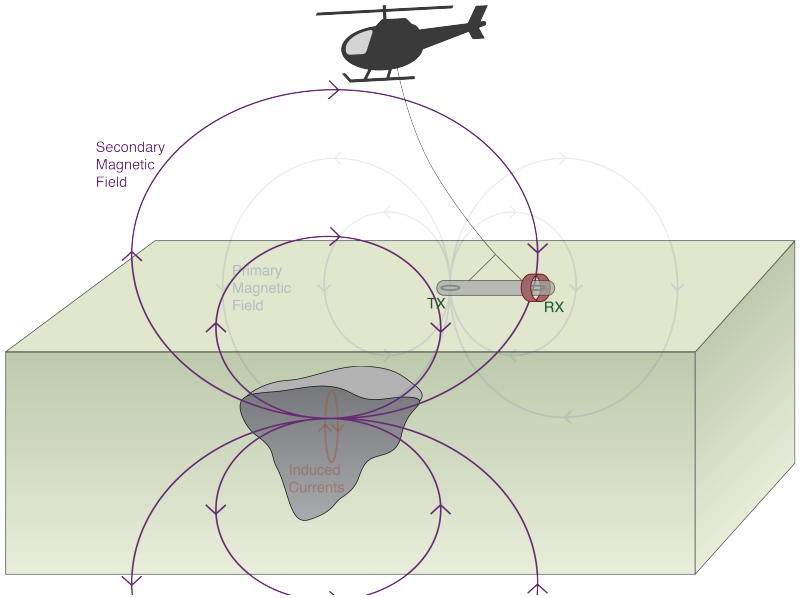
Basic Experiment



- **Transmitter:**
  - Produces a primary magnetic field

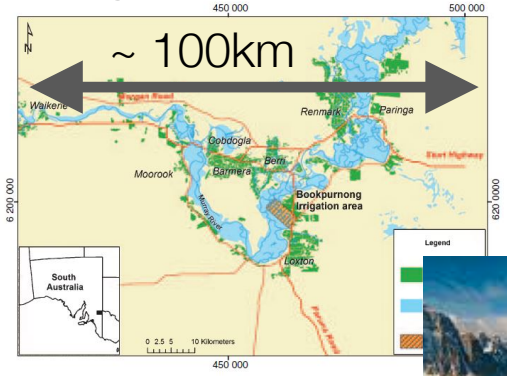
- **Exciting the target:**
  - Time varying magnetic fields generate electric fields everywhere
  - Producing currents in conductors

- **Receiver:**
  - Induced currents produce secondary magnetic fields



Transmitter

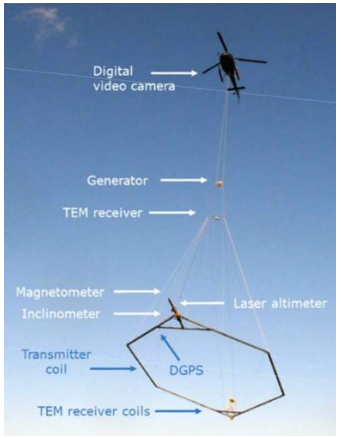
Large areas



Rugged terrain

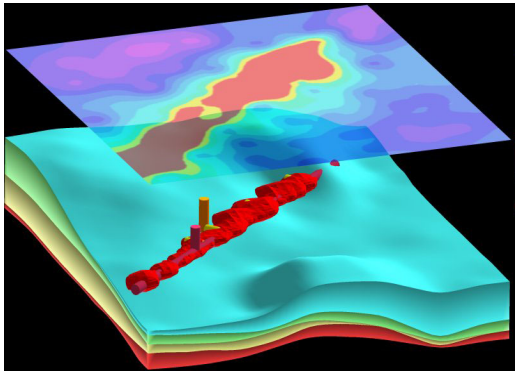
Airborne Survey

Resolve

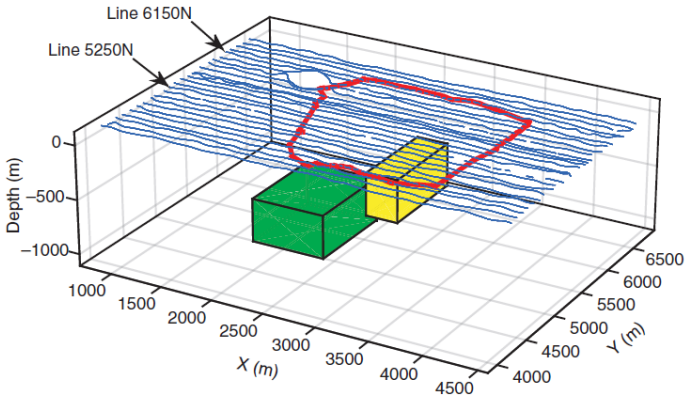


SkyTEM

Deep Targets

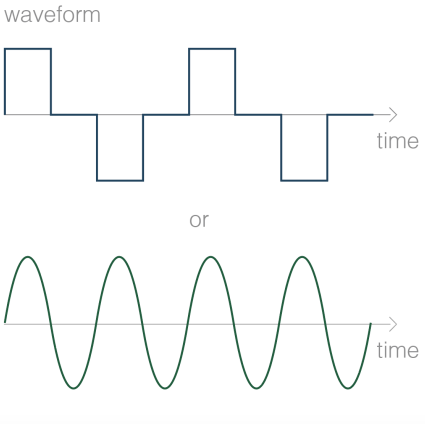


Large Loop



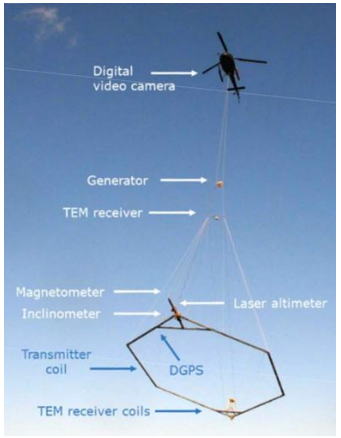
Transmitter

- Frequency or Time?



Airborne Survey

Resolve

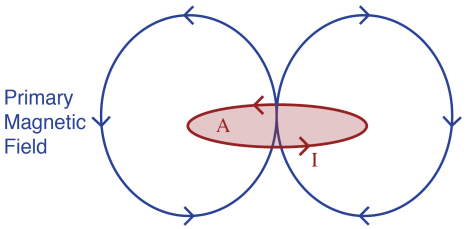


SkyTEM

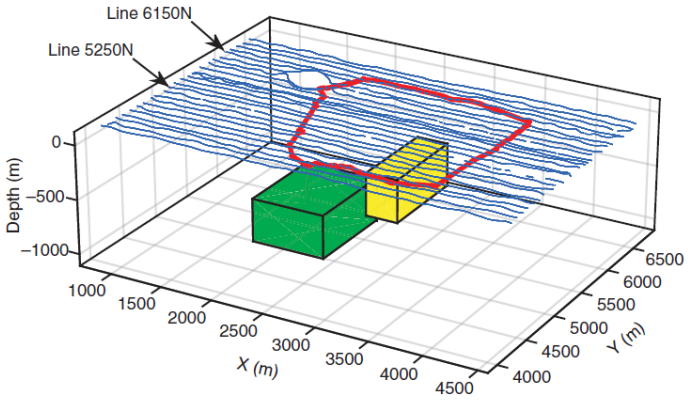
- Key factor is moment

$$m = I\ (\text{current})\ A\ (\text{area})\ N\ (\#\ \text{of turns})$$

$$\mathbf{B}(\mathbf{r}) = \frac{\mu_0}{4\pi}\left(\frac{3\mathbf{r}(\mathbf{m}\cdot\mathbf{r})}{|\mathbf{r}|^5} - \frac{\mathbf{m}}{|\mathbf{r}|^3}\right)$$



Large Loop

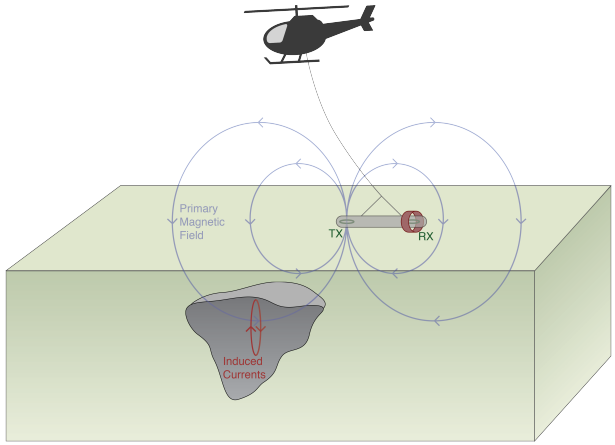


Exciting the target

- Primary field from a loop

$$\mathbf{B}(\mathbf{r}) = \frac{\mu_0}{4\pi}\left(\frac{3\mathbf{r}(\mathbf{m}\cdot\mathbf{r})}{|\mathbf{r}|^5} - \frac{\mathbf{m}}{|\mathbf{r}|^3}\right)$$

- Fields fall off
  - $1/r^3$ geometric decay
  - Attenuation
- Want to be as close as possible to target
  - Ground based systems
  - Helicopter
  - Fixed wing aircraft
- Always concerned about coupling

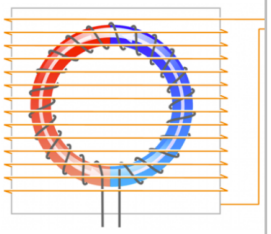


Receiver and Data

Magnetometer

- Measures:
  - Magnetic field
  - 3 components
- eg. 3-component fluxgate

$$\mathbf{b}(t)$$

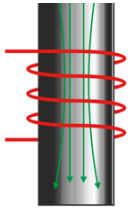


Fluxgate

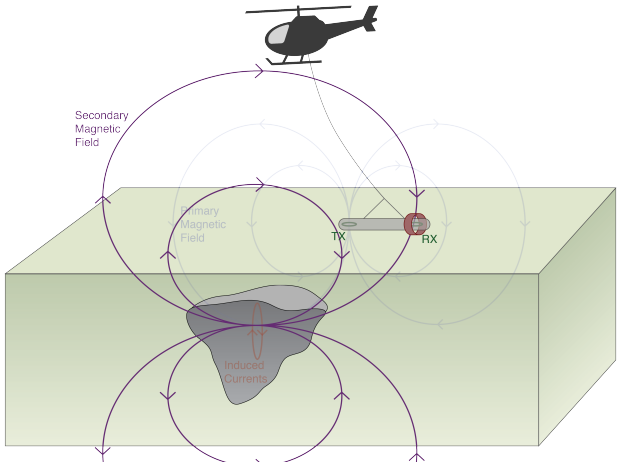
Coil

- Measures:
  - Voltage
  - Single component that depends on coil orientation
    - Coupling matters
- eg. airborne frequency domain.
  - ratio of Hs/Hp is the same as Vs/Vp

$$\frac{\partial b}{\partial t}$$

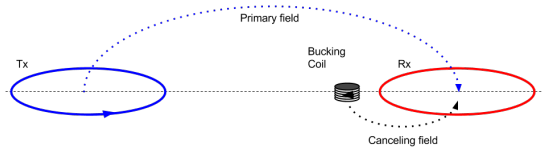


Coil

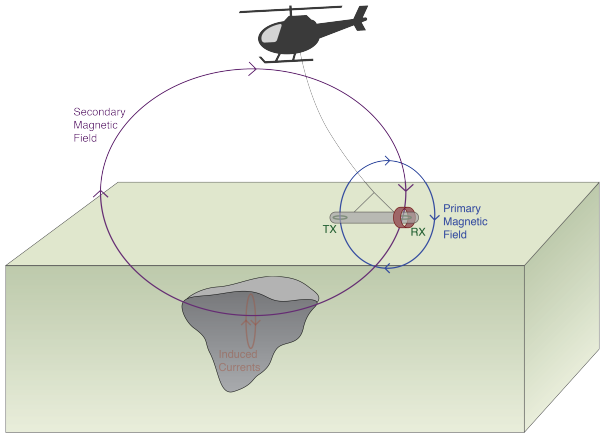


Receiver: Frequency Domain

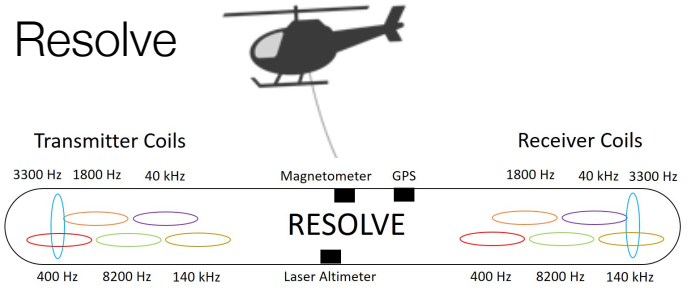
- Primary field
  - always “on”
  - large compared to secondary fields
- Primary removal
  - Compute and subtract
  - Bucking coil



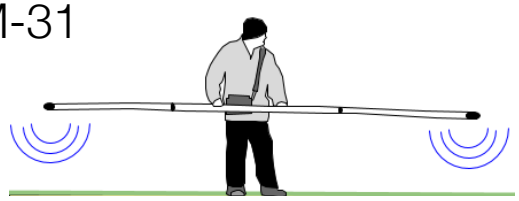
- Main requirement:
  - Know positions of Tx and Rx
  - Keep them in one unit



Resolve

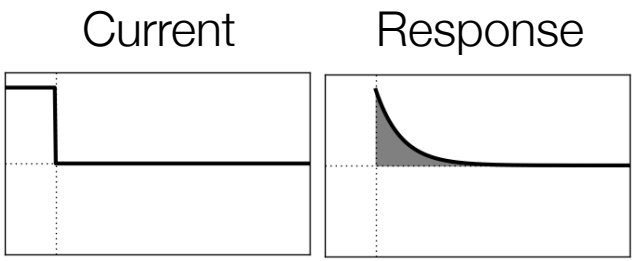


EM-31

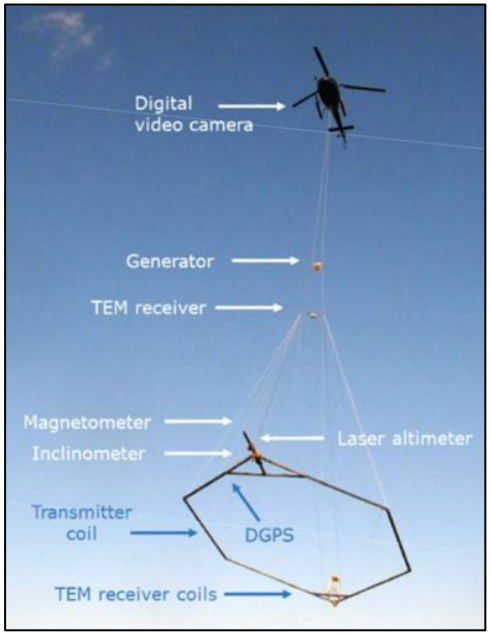


Receiver: Time Domain

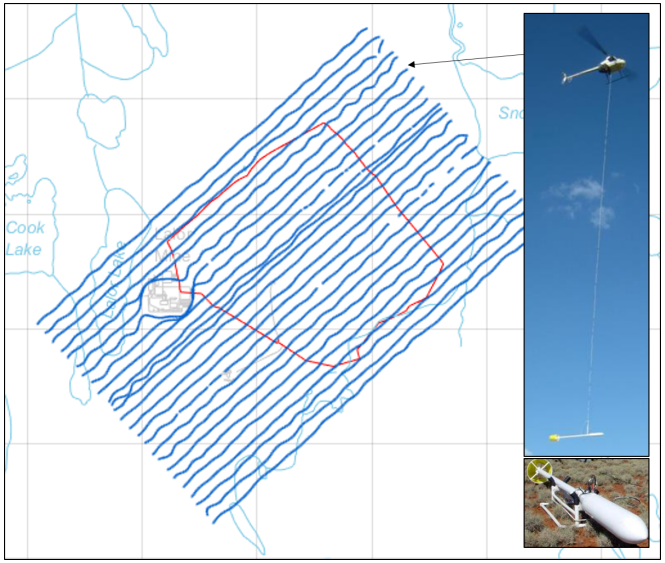
- Primary field has off-time
- Measure secondary fields
- Receivers can be mounted on transmitter loop or above it



SkyTEM



HeliSAM



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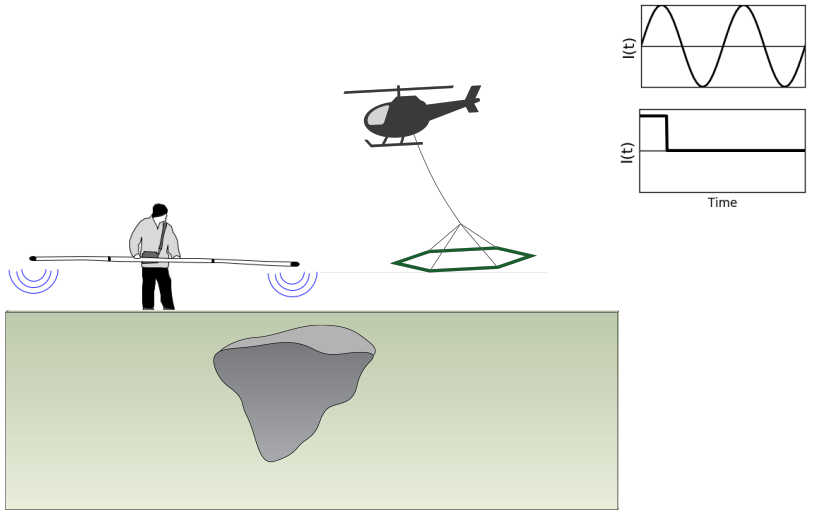


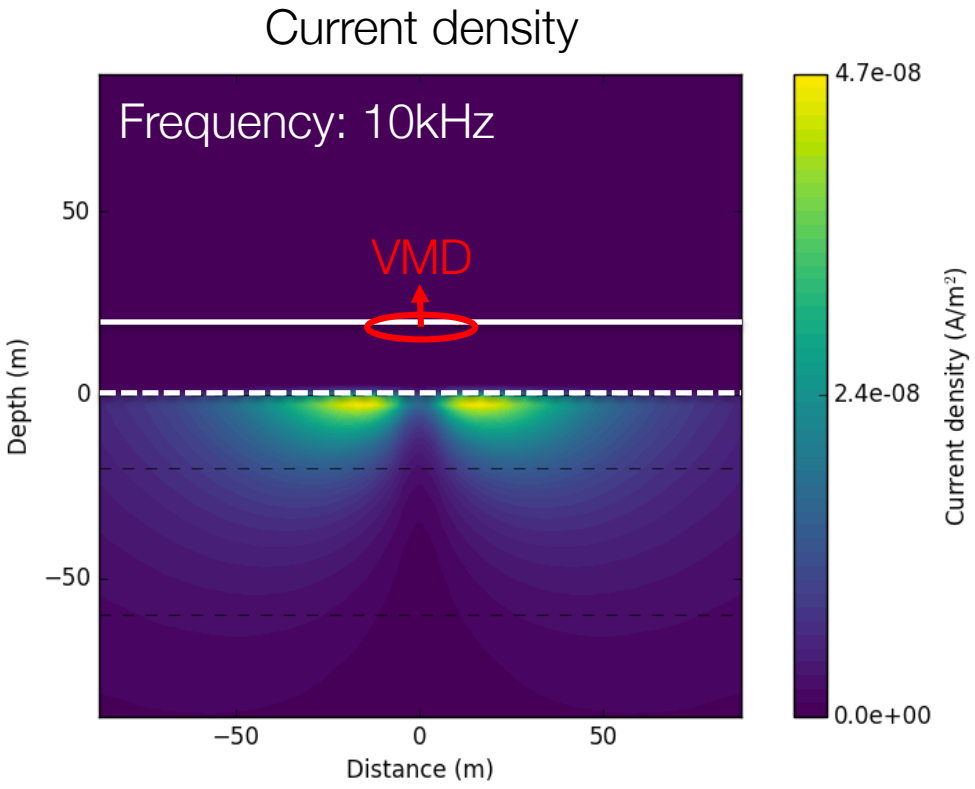
- Where to collect data? How many? How accurate?
- What is depth of investigation?
- What is the "footprint" of the transmitter"
  - These are questions of SURVEY DESIGN

Footprint of Airborne EM system

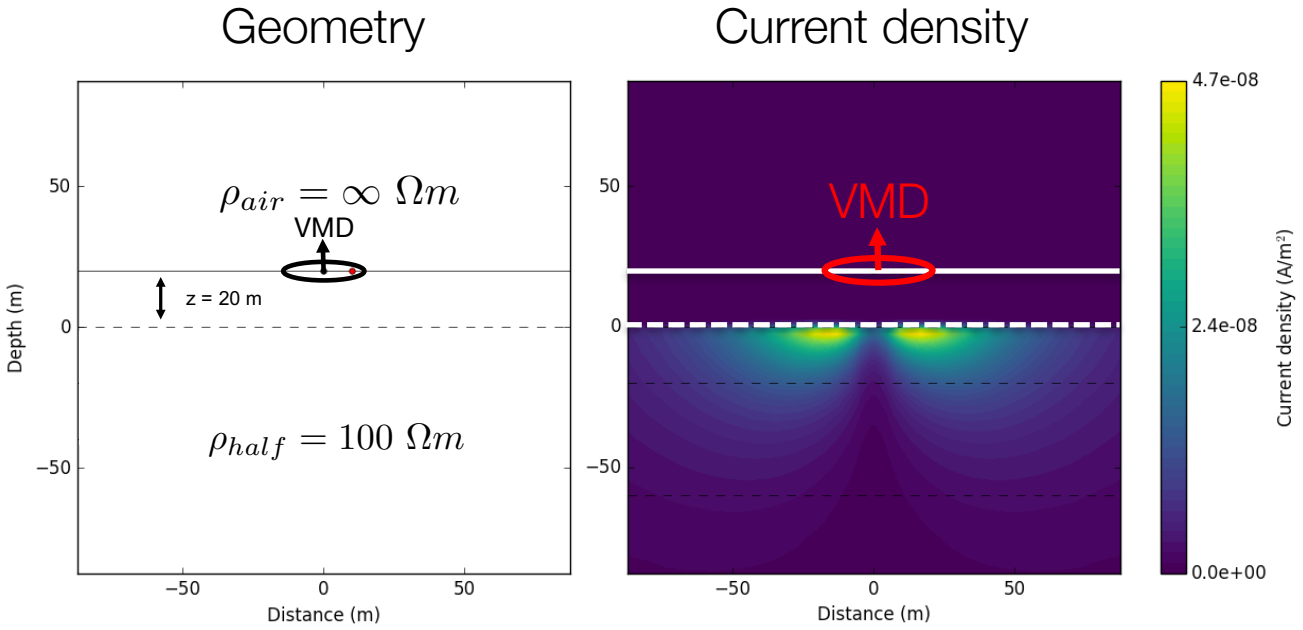
- What volume of earth is “seen” by the airborne system?
  - Where are the currents?

- Currents depend on
  - Transmitter
  - Waveform: frequency or time
  - Background conductivity

- Simple case: loop source over homogeneous earth

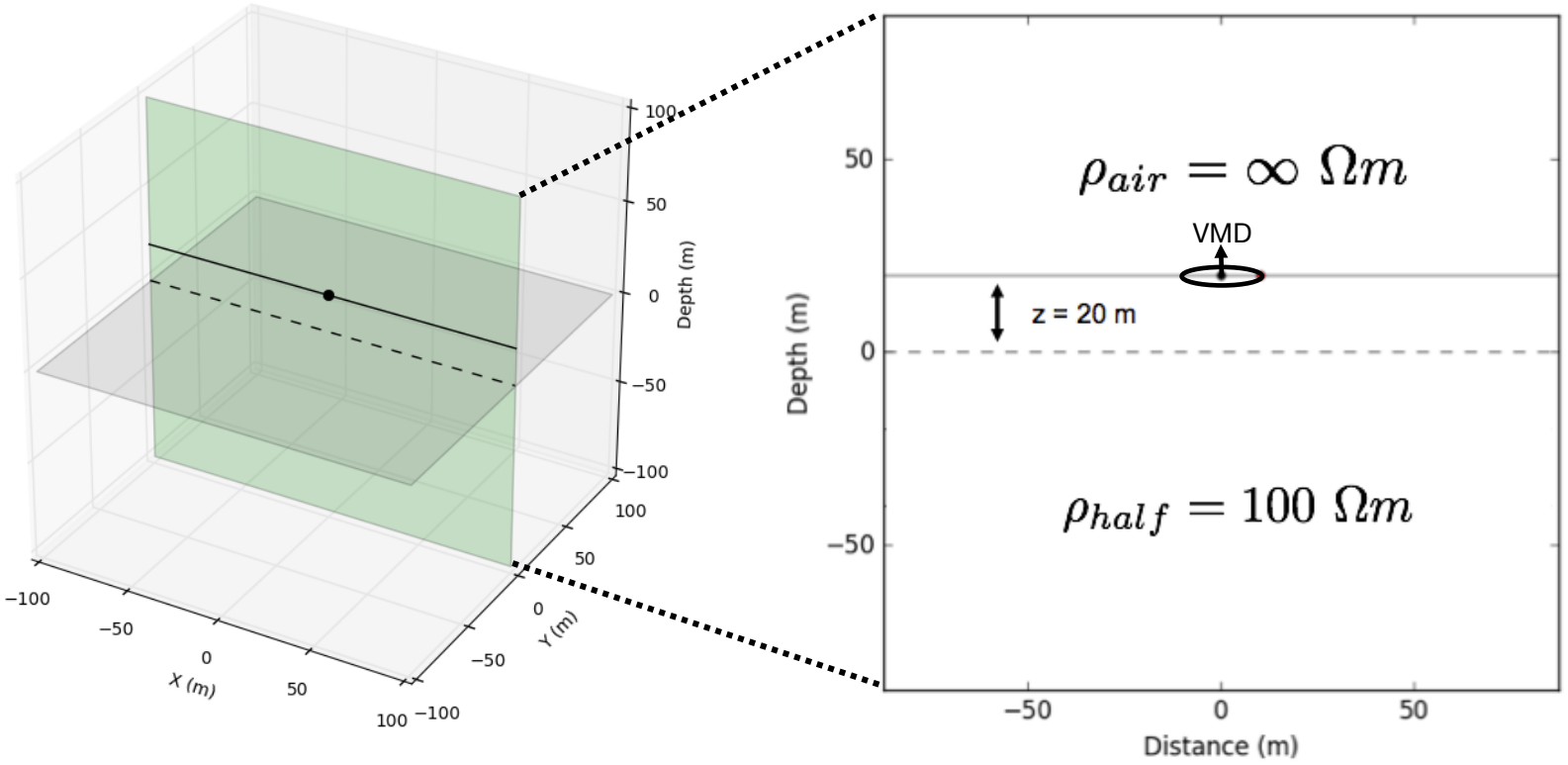


Vertical Magnetic Dipole (VMD)



- Some questions
  - Where, and how strong, are the currents?
  - How do they change with transmitter frequency?
  - How do they depend upon the conductivity?
  - What do the resulting magnetic fields look like?

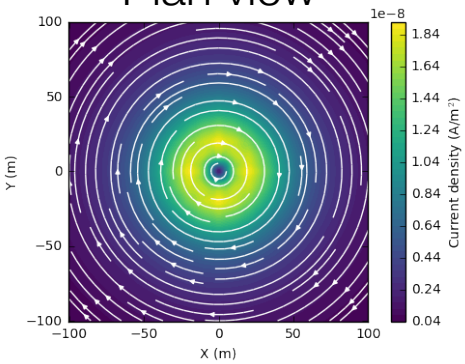
Vertical Magnetic Dipole over a halfspace (FDEM)



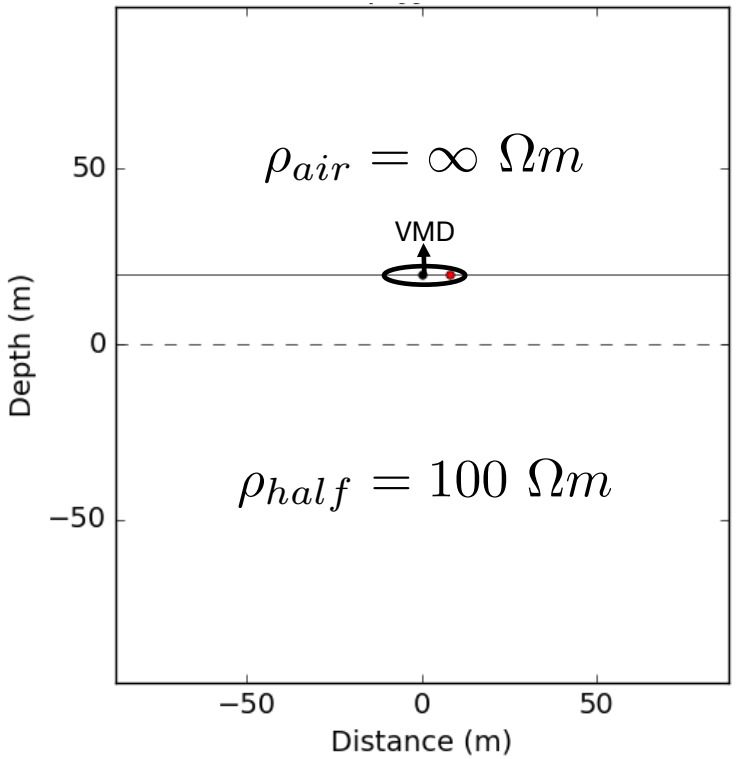
Current Density

- Frequency = 10 kHz
- Currents in the earth flow in planes parallel to the Tx

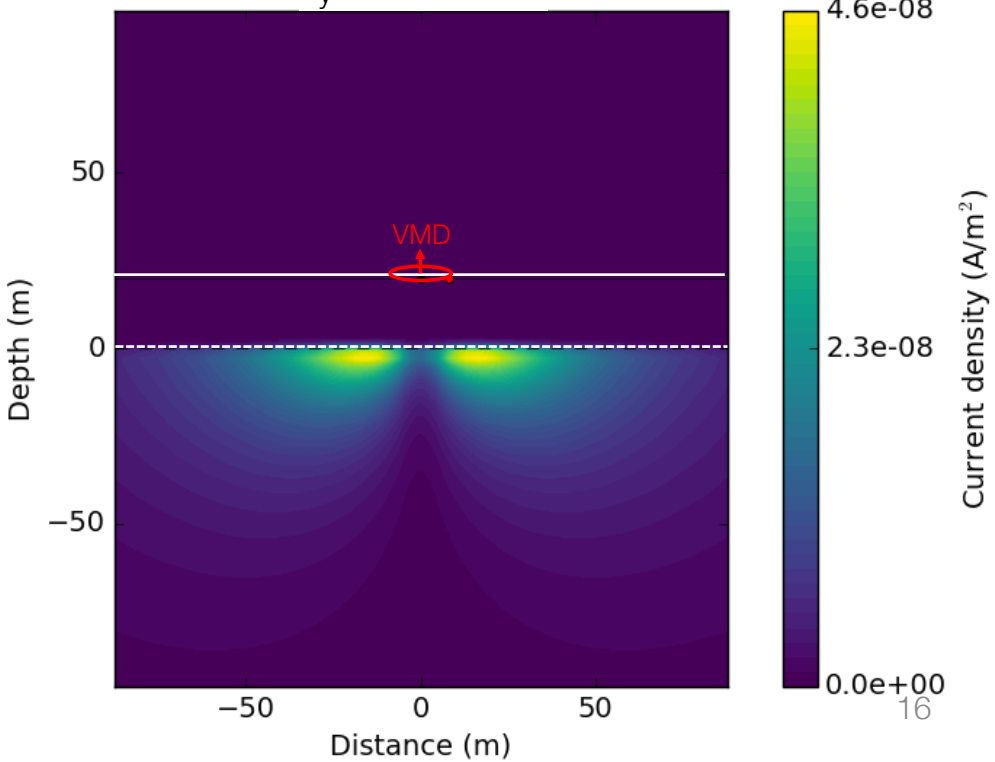
Plan view



Geometry

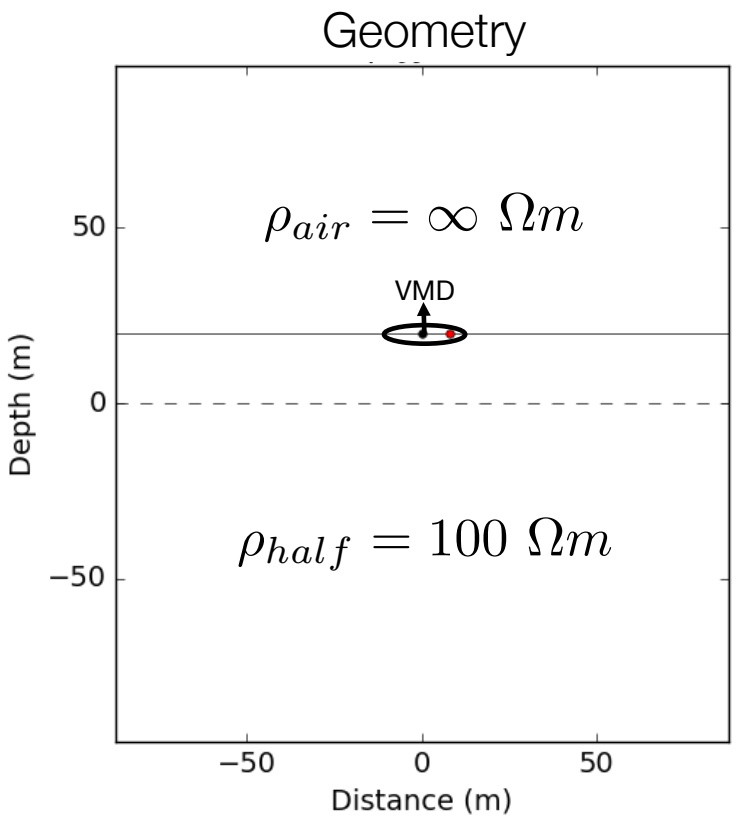


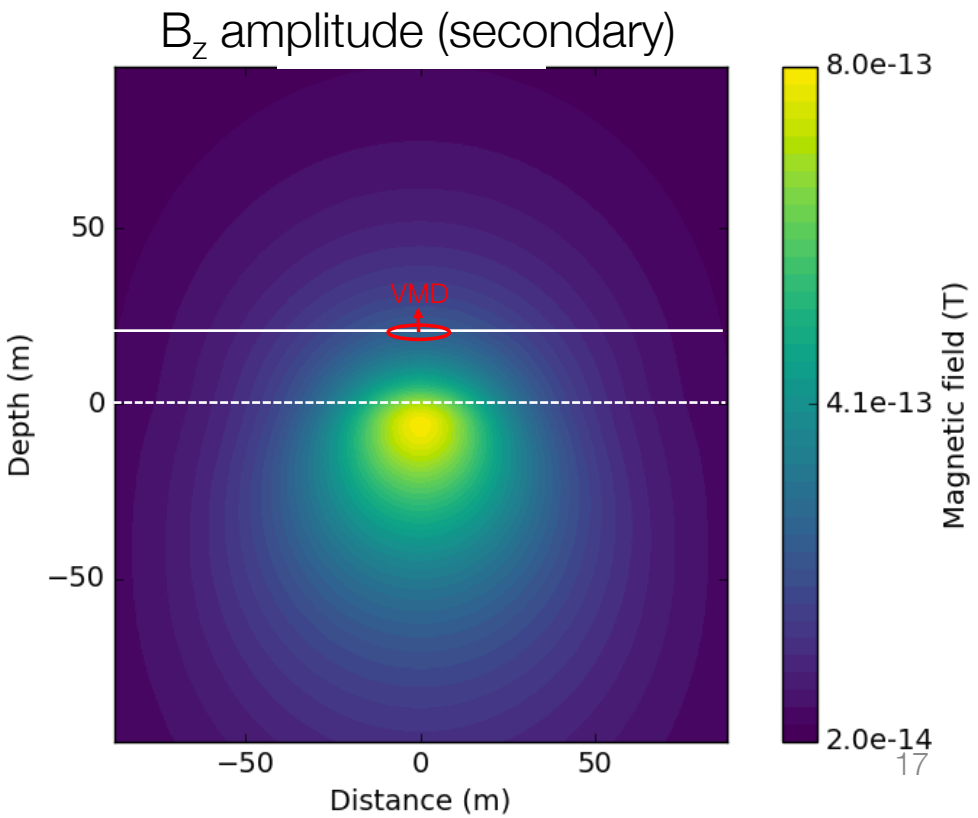
J_y amplitude



Secondary Magnetic Flux Density

- Frequency = 10 kHz

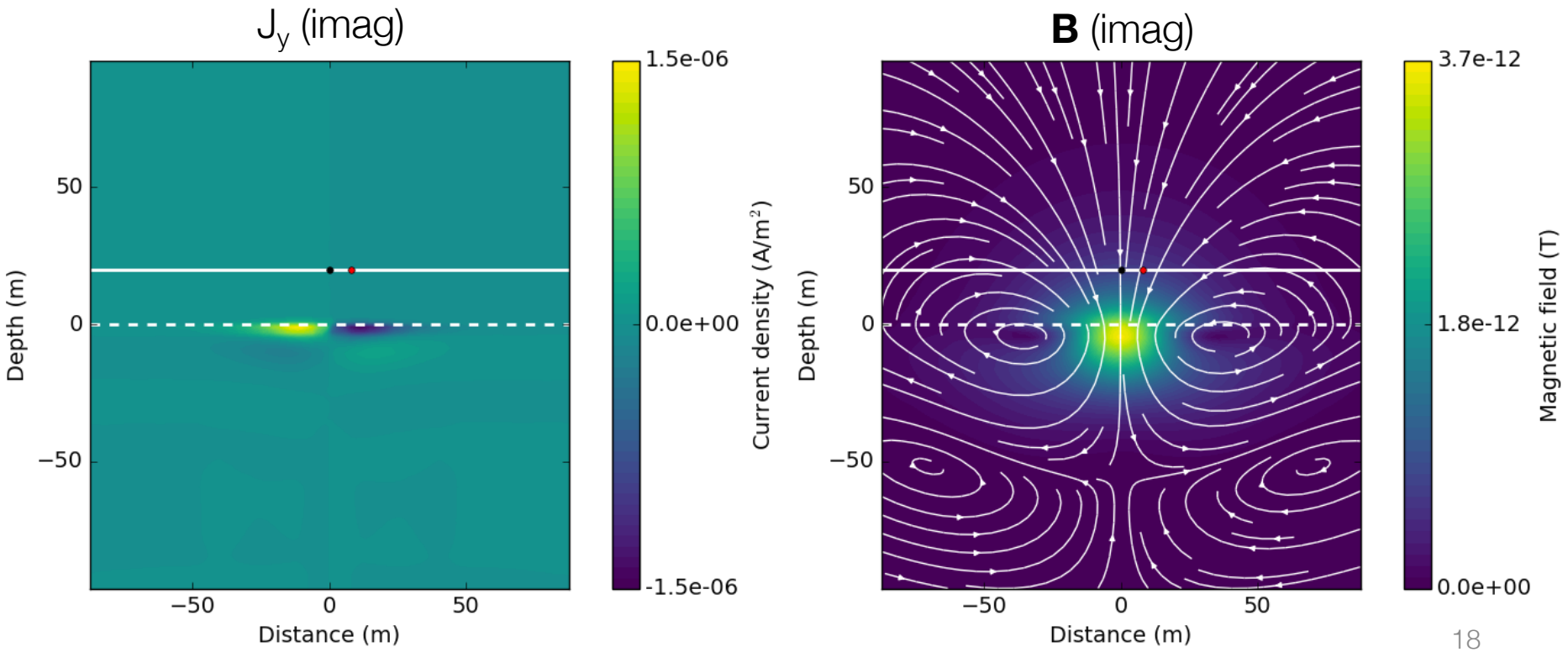




Effects of Frequency

- Frequency at 100 kHz
- Skin depth = 16 m
- Currents are concentrated at surface

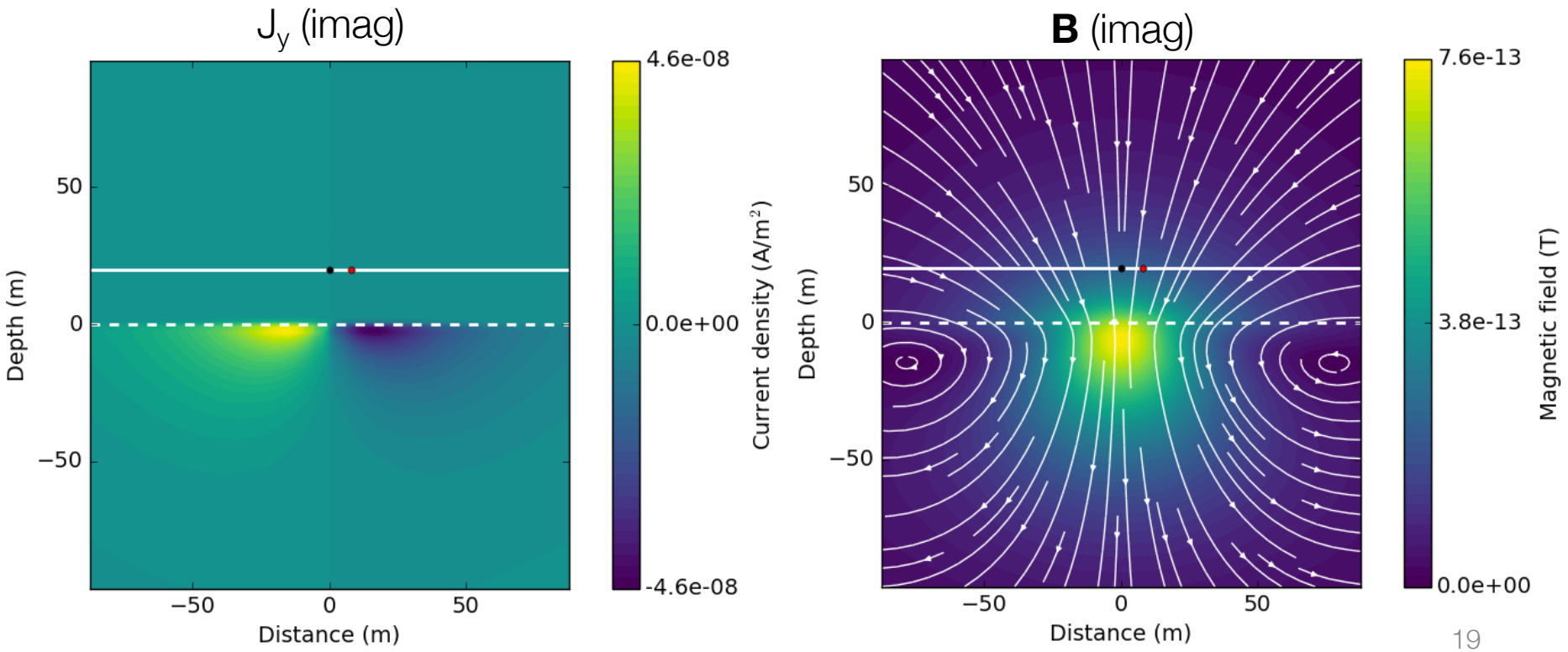
$$\delta = 503\sqrt{\frac{\rho}{f}}$$



Effects of Frequency

- Frequency at 10 kHz
- Skin depth = 50 m
- Currents diffusing downward and outward

$$\delta = 503\sqrt{\frac{\rho}{f}}$$



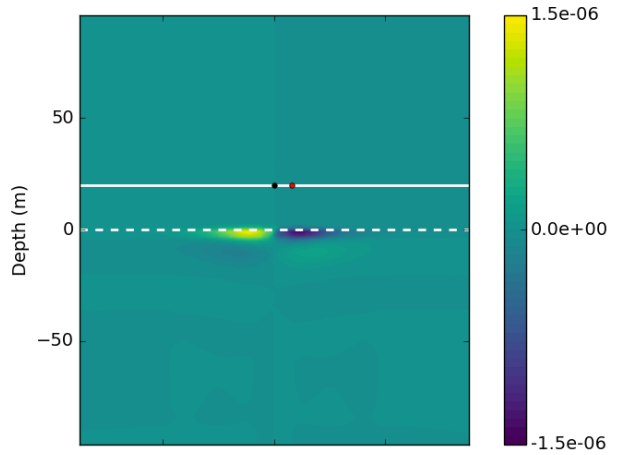
$$\delta = 503\sqrt{\frac{\rho}{f}}$$

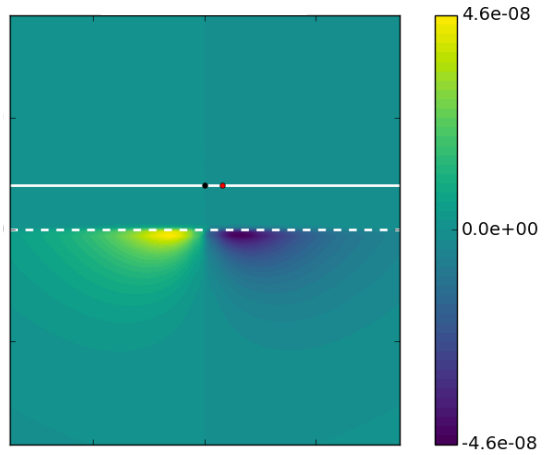
Summary: Effects of Frequency

100 kHz

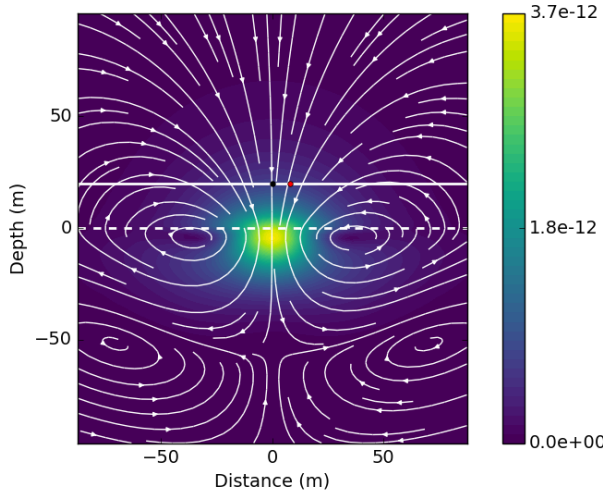
10 kHz

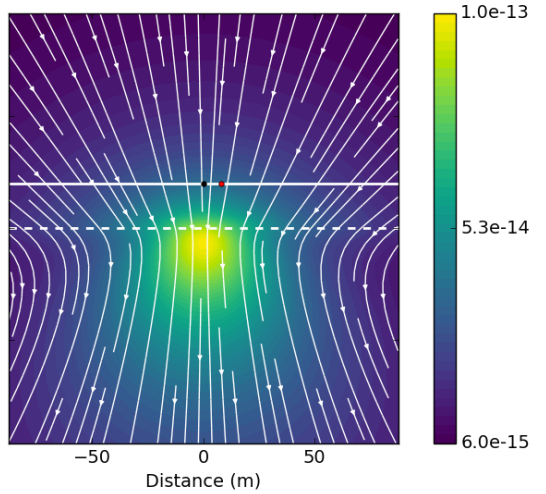
J_y imag.





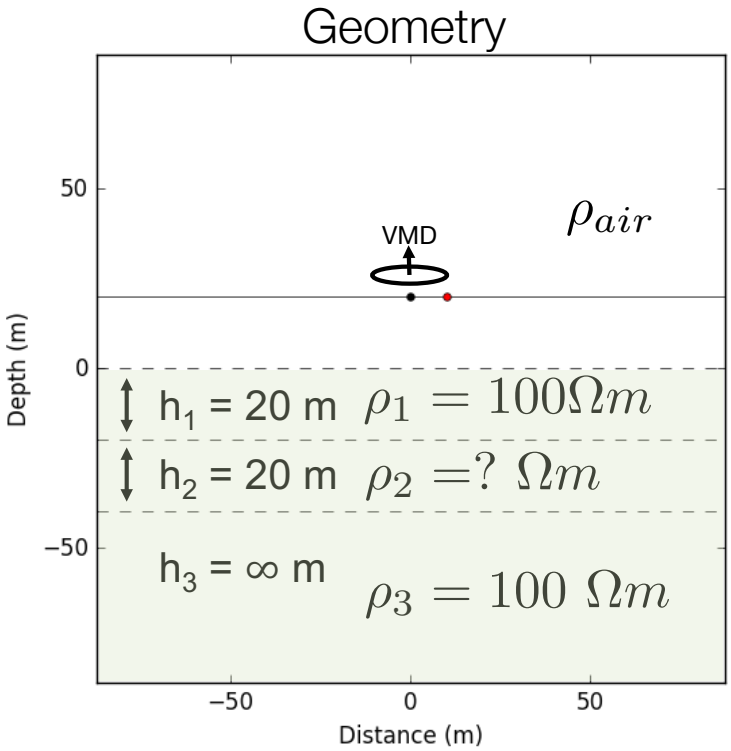
B imag.





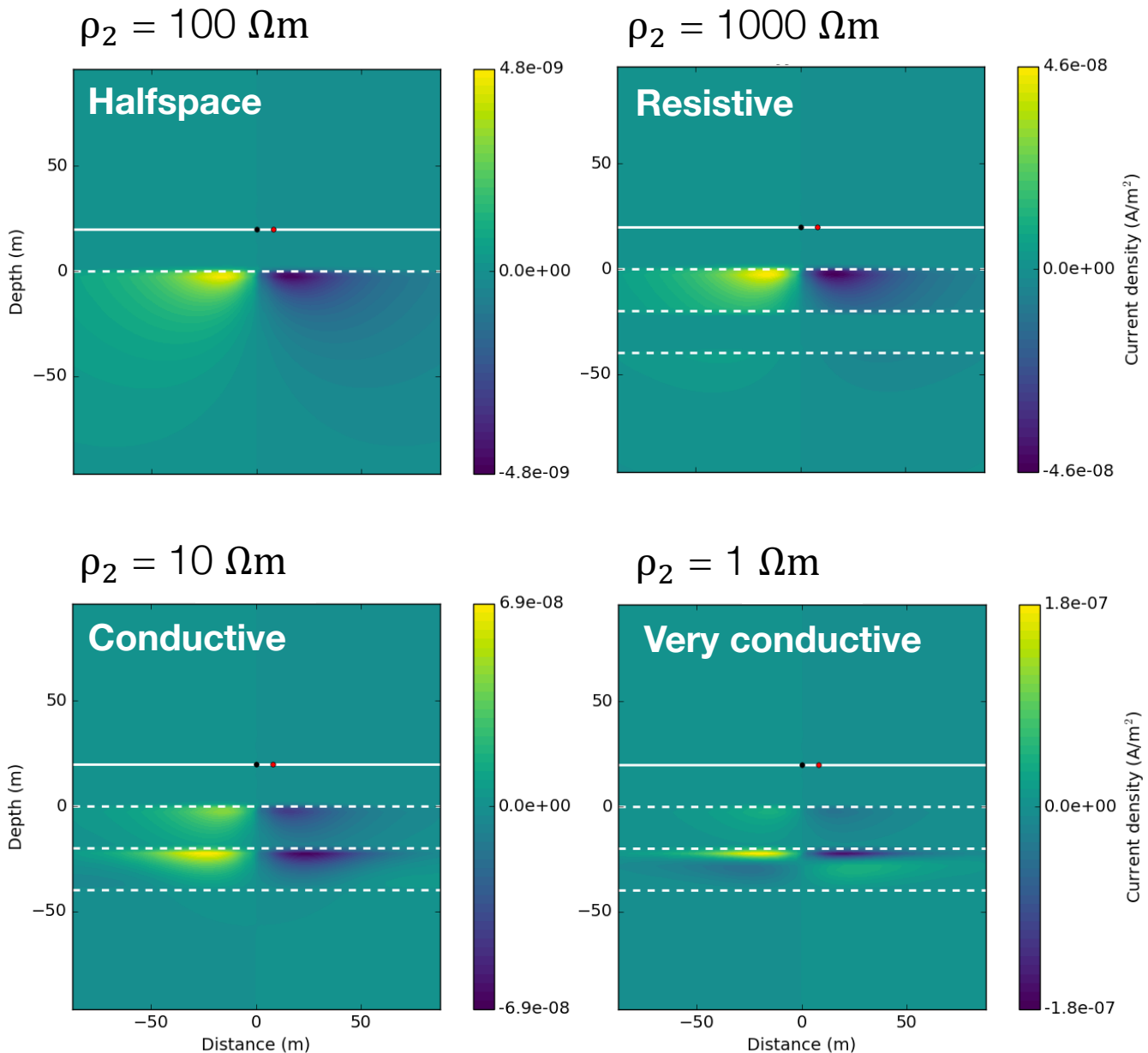
Layered earth

- 3 layers + air,
- ρ_2 varies



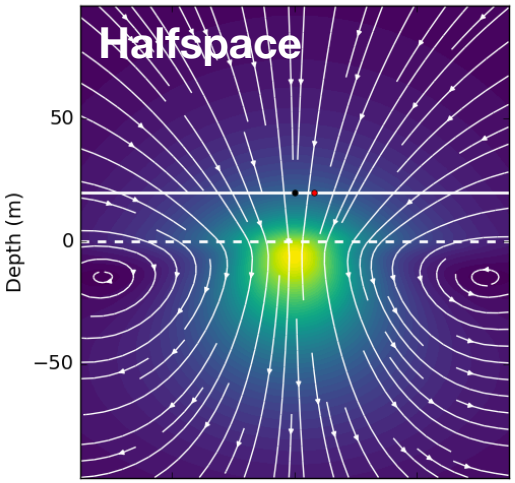
- Four different cases:
  - Halfspace
    $\rho_2 = 100\ \Omega m$
  - Resistive
    $\rho_2 = 1000\ \Omega m$
  - Conductive
    $\rho_2 = 10\ \Omega m$
  - Very conductive
    $\rho_2 = 1\ \Omega m$
- Fields
  - J_y imag
  - Secondary **B** imag

Current density (J_y imag)

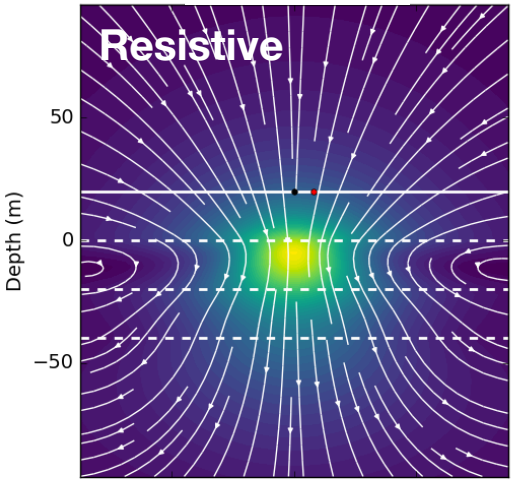


Magnetic flux density (**B** imag)

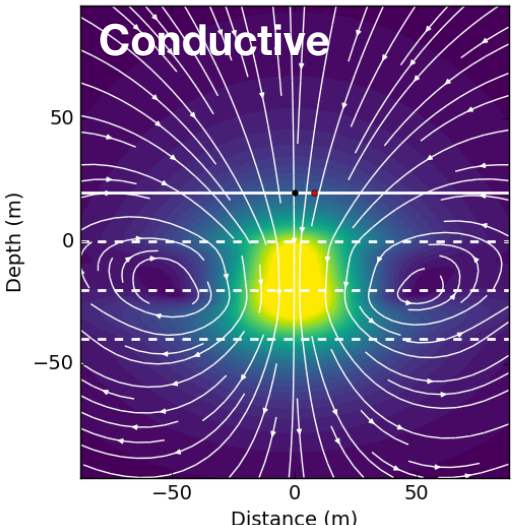
$\rho_2 = 100\ \Omega m$



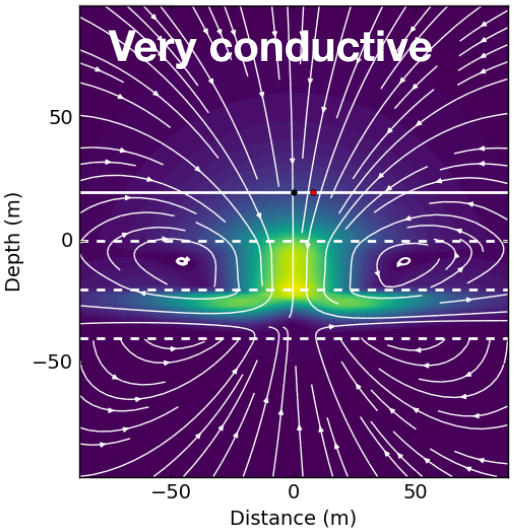
$\rho_2 = 1000\ \Omega m$

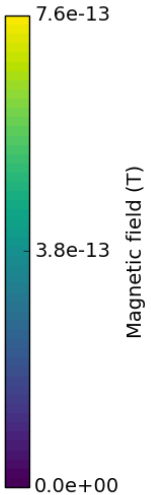


$\rho_2 = 10\ \Omega m$



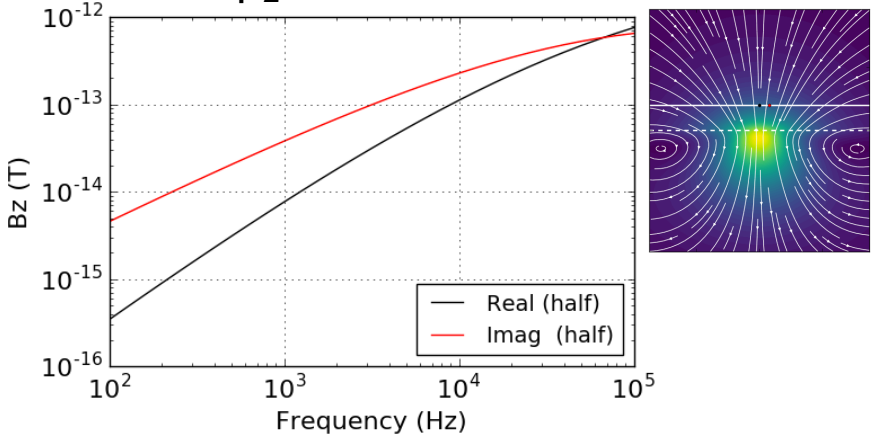
$\rho_2 = 1\ \Omega m$



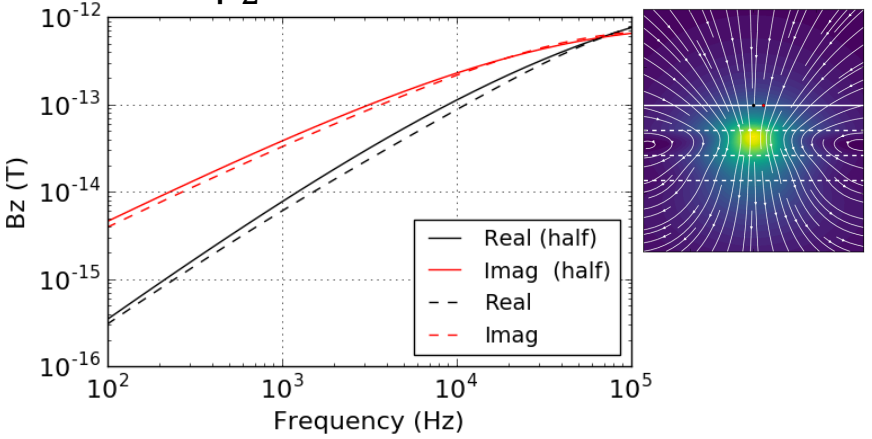


B_z sounding curves

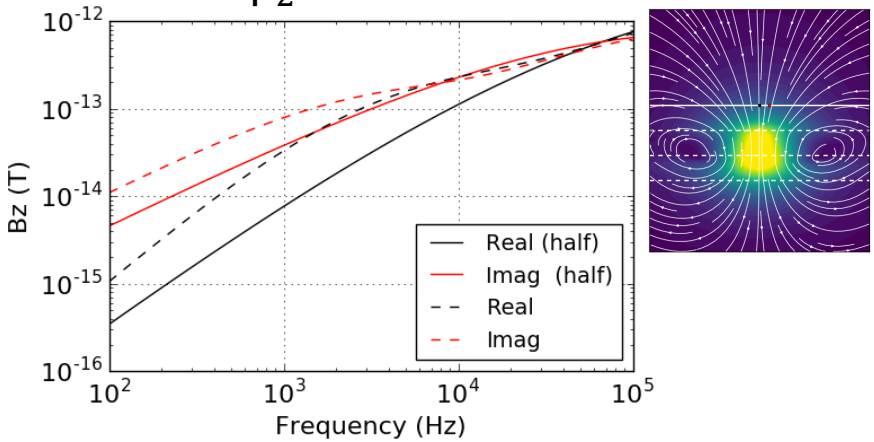
$\rho_2 = 100\ \Omega m$



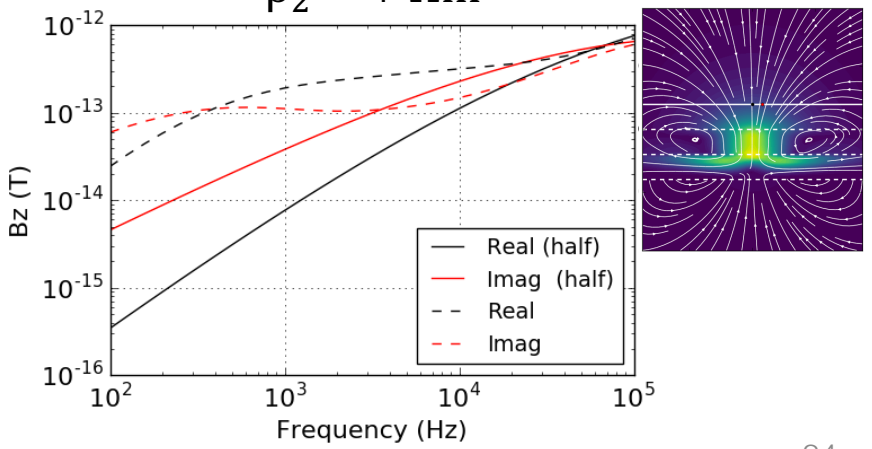
$\rho_2 = 1000\ \Omega m$



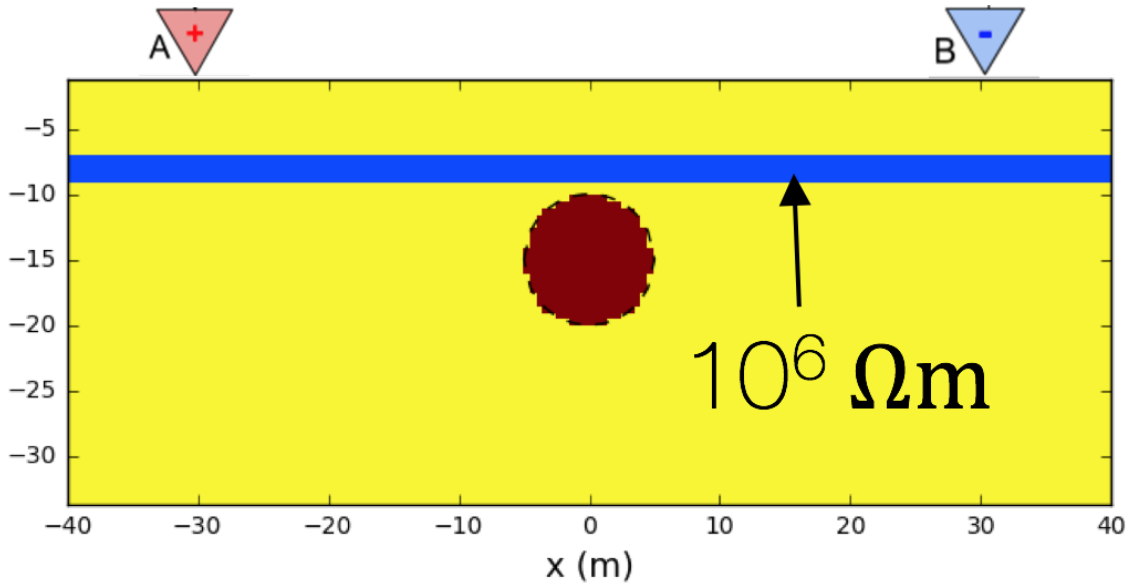
$\rho_2 = 10\ \Omega m$



$\rho_2 = 1\ \Omega m$

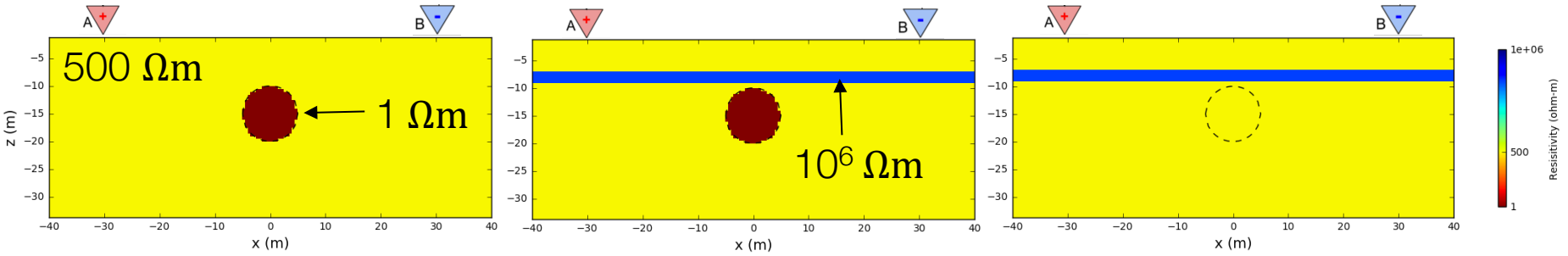


Back to the “shielding” problem

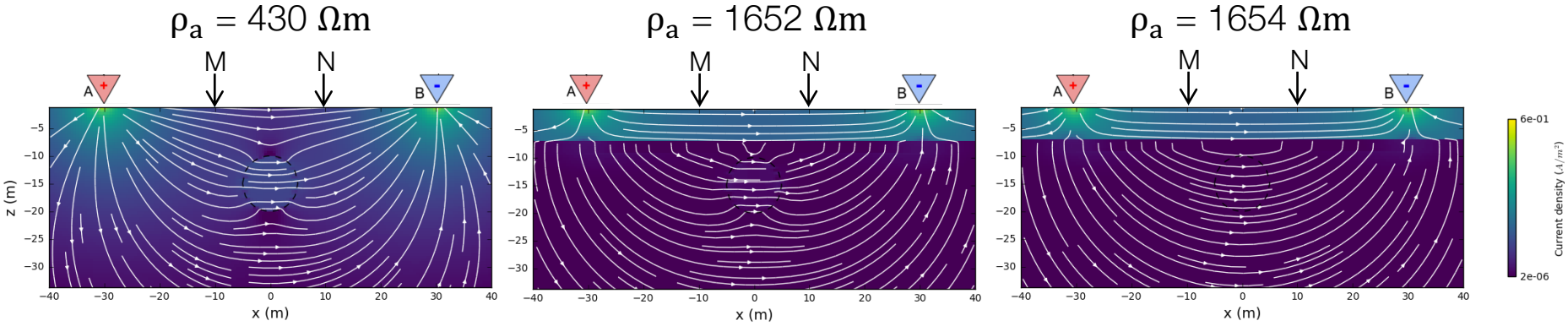


Shielding: DC with resistive layer

Resistivity models (thin **resistive** layer)

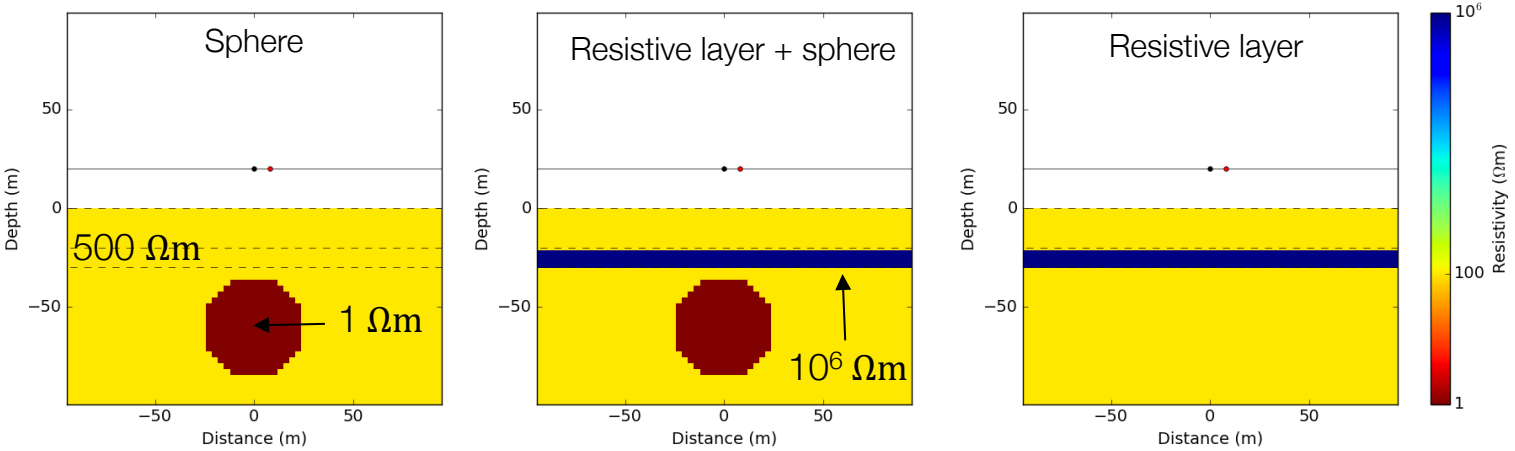


Currents and measured data at MN

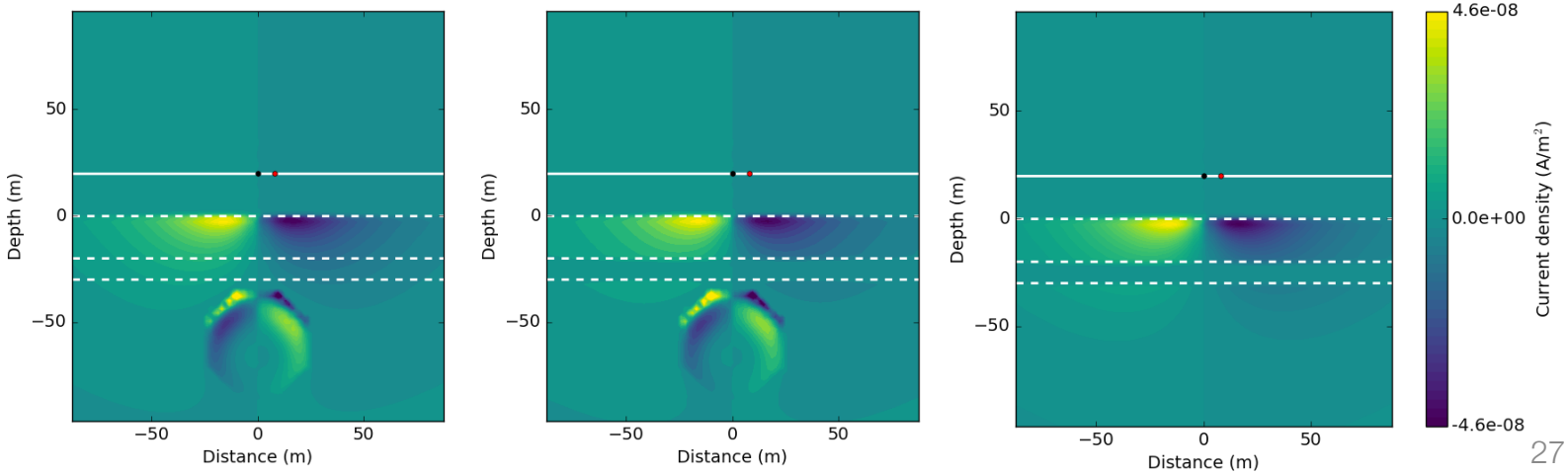


Shielding: EM with resistive layer

Resistivity models (thin **resistive** layer)

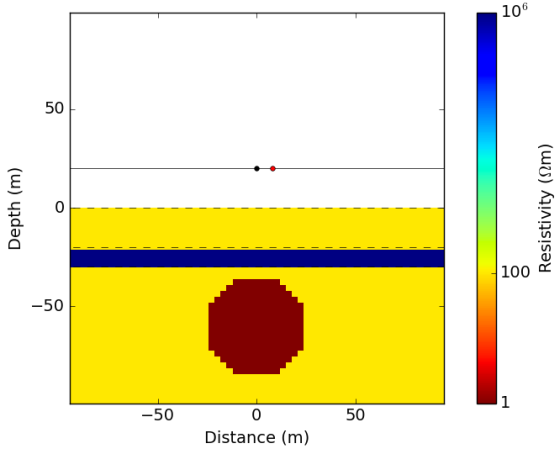


Currents (J_y imag)

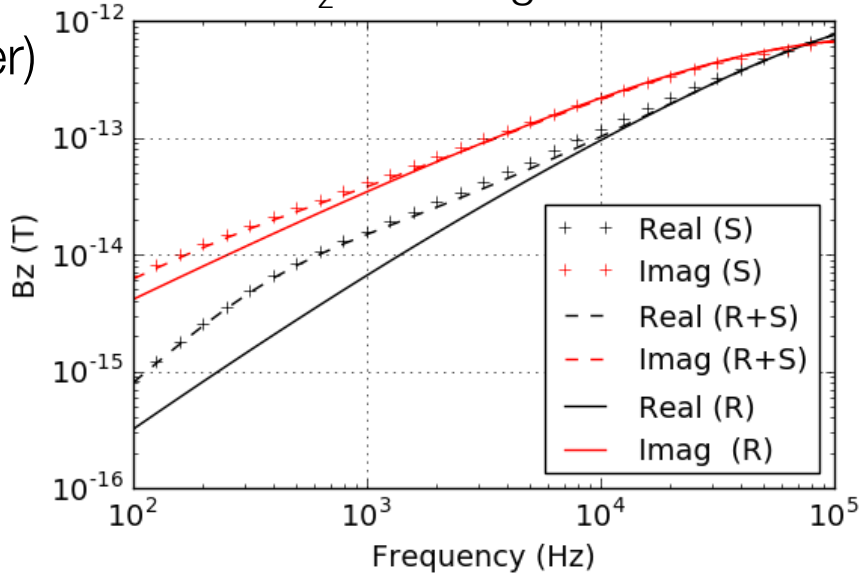


Shielding: EM with resistive layer

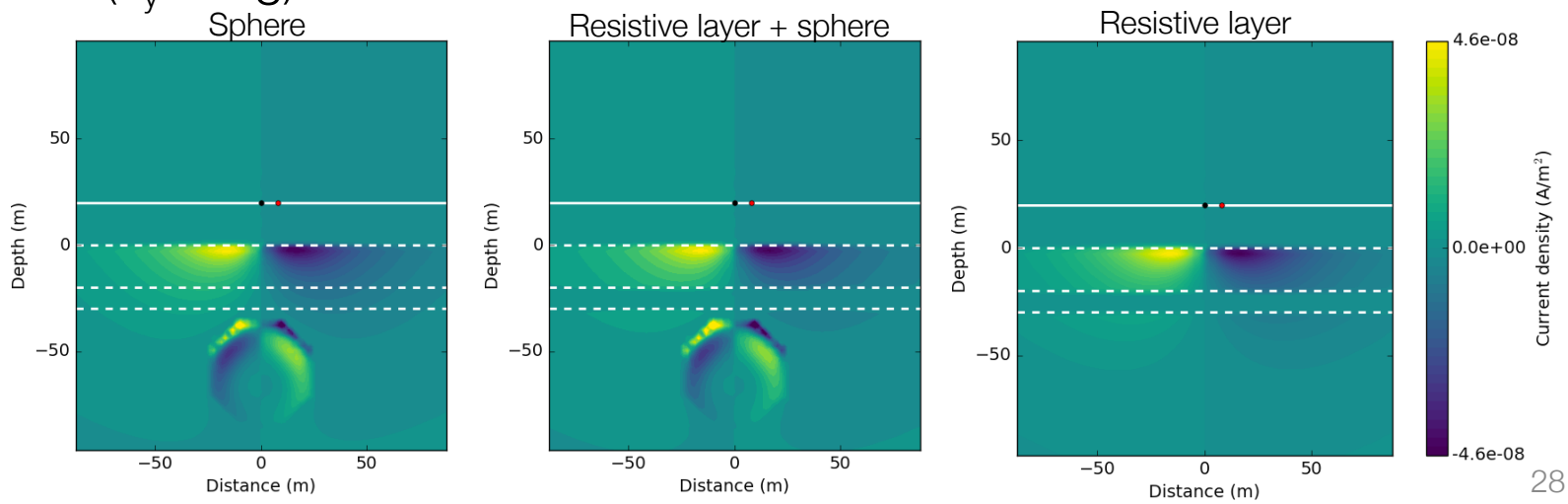
Resistivity models (thin **resistive** layer)



B_z sounding curves

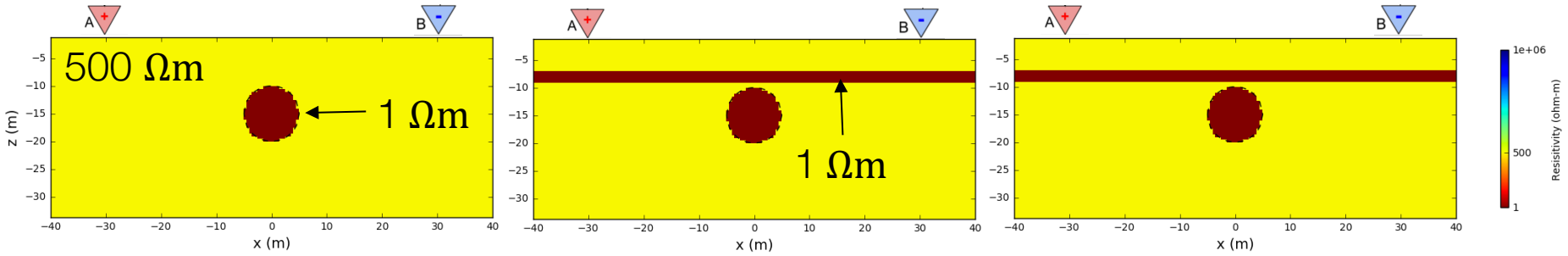


Currents (J_y imag)

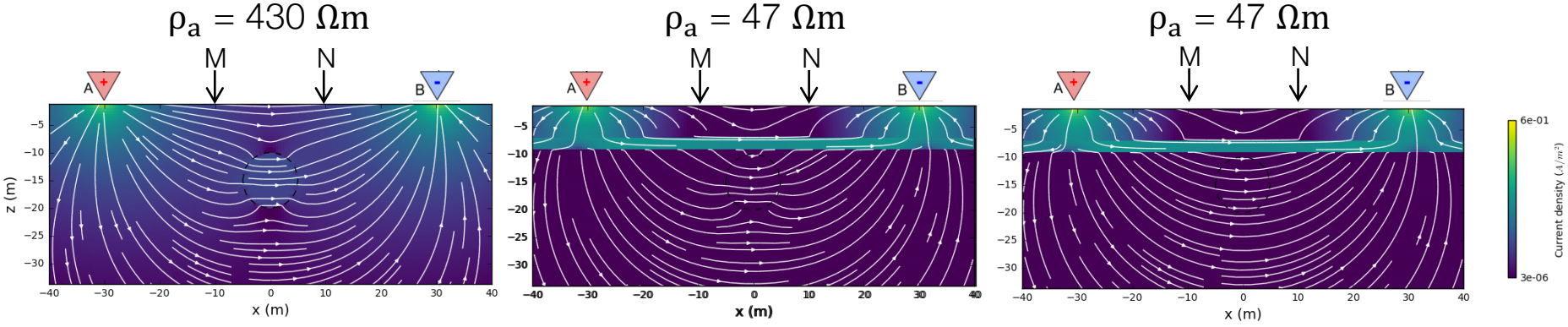


Shielding: DC with conductive layer

Resistivity models (thin **conductive** layer)

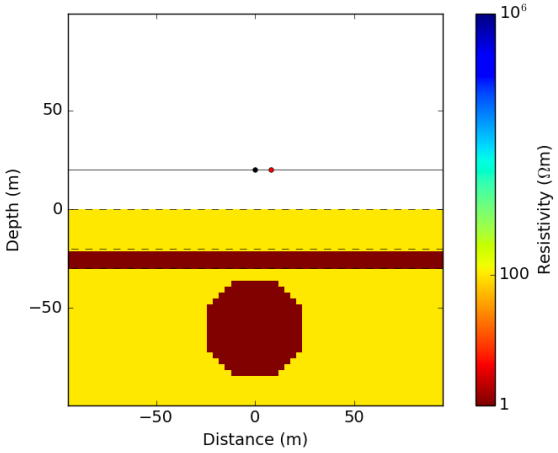


Currents and measured data at MN

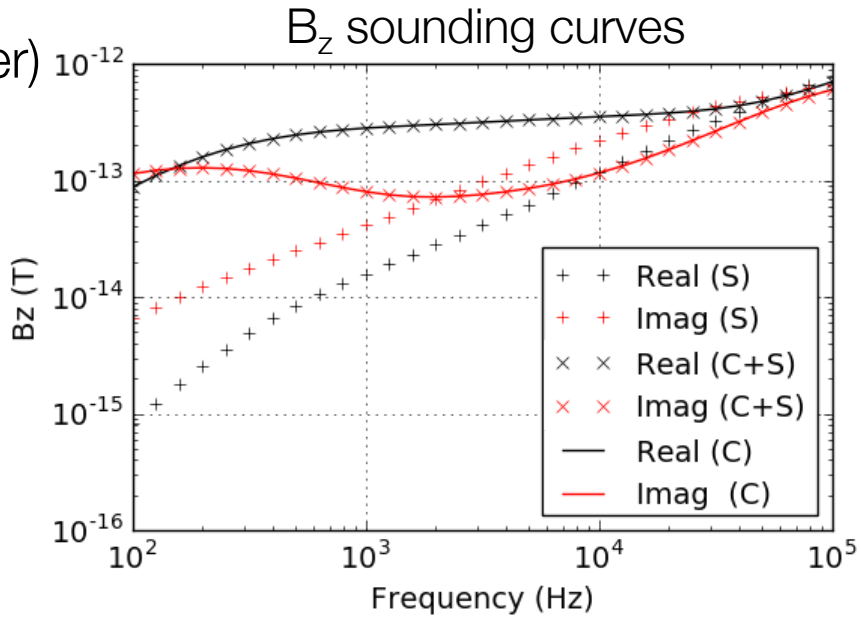


Shielding: EM with conductive layer

Conductivity models (thin **resistive** layer)

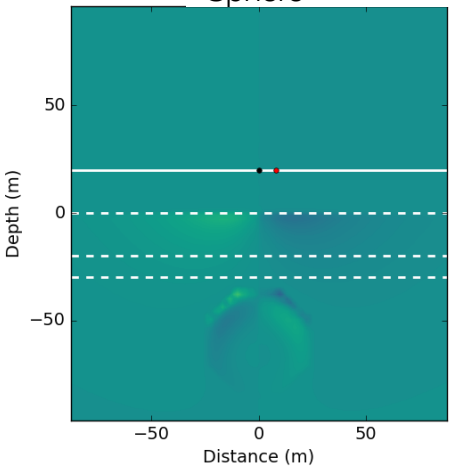


B_z sounding curves

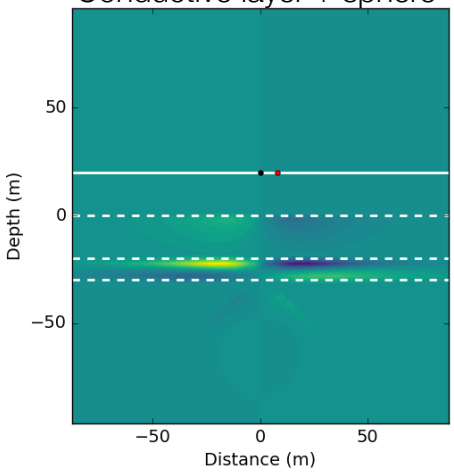


Currents (J_y imag)

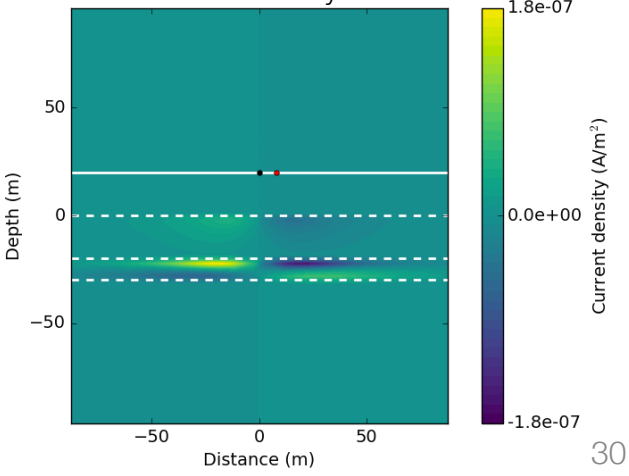
Sphere



Conductive layer + sphere



Conductive layer



Outline

Setup

- Basic experiment
- Transmitters, Receivers

Frequency Domain EM

- Vertical Magnetic Dipole
- Effects of Frequency

- Questions

- Case History – Groundwater

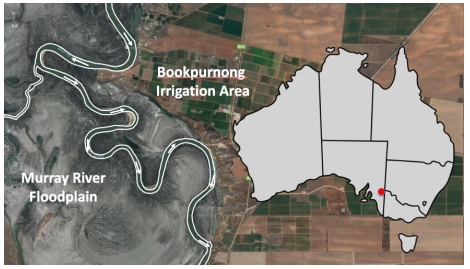
Time Domain EM

- Vertical Magnetic Dipole
- Propagation with Time
- Case History – Near surface geology

Case History: Bookpurnong

Viezzoli et al., 2009

Setup



Geoscience Australia project

- Characterizing river salination

?

Losing Stream

Gaining Stream

1 – Water table 2 – Unsaturated zone 3 – Saturated zone 4 – Flow direction

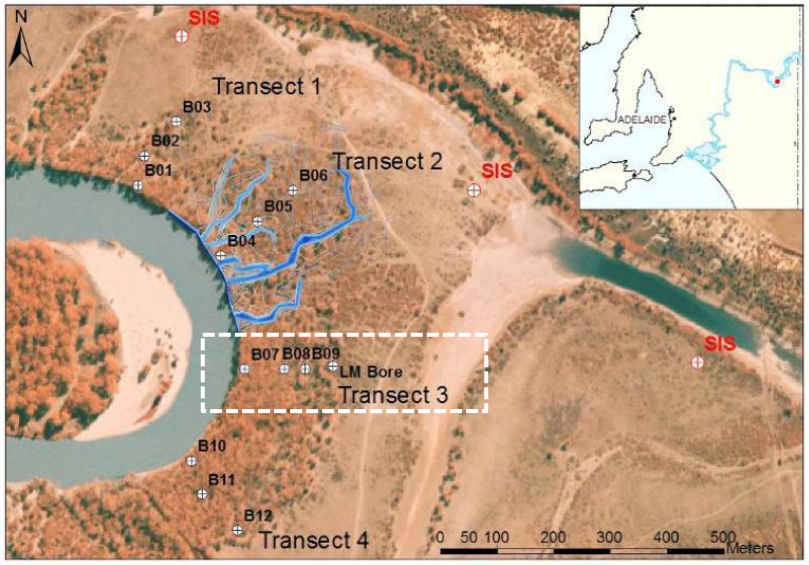
Saline water intrusion

Elevation (m)

55 50 45 40 35 30 25 20 15 10

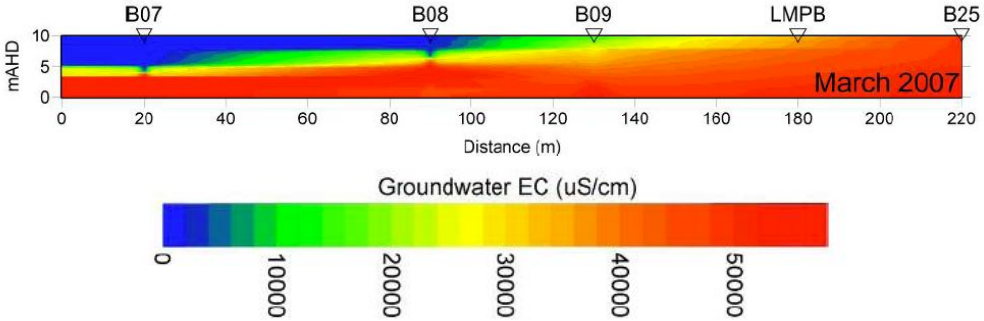
Properties

Location map for salinity measurements



Unit	Conductivity
Saline water	High, 3 - 5 S/m
Fresh water	Low, 0.01 S/m

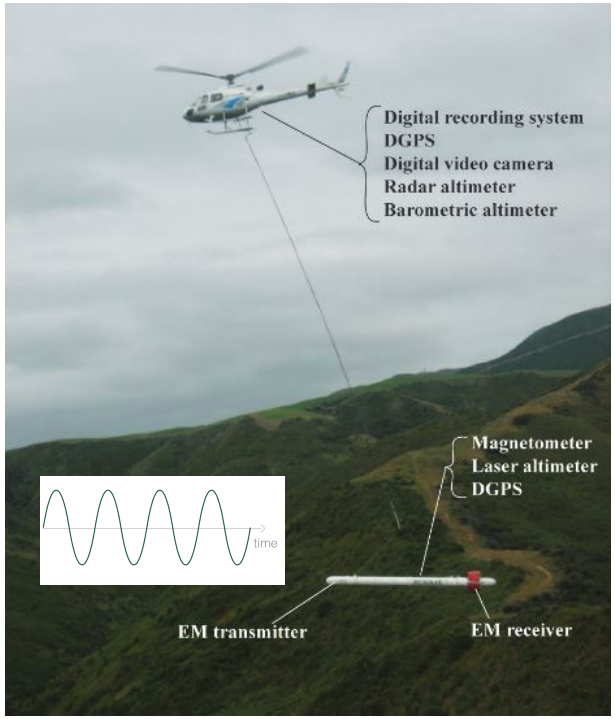
Conductivity from salinity measurements



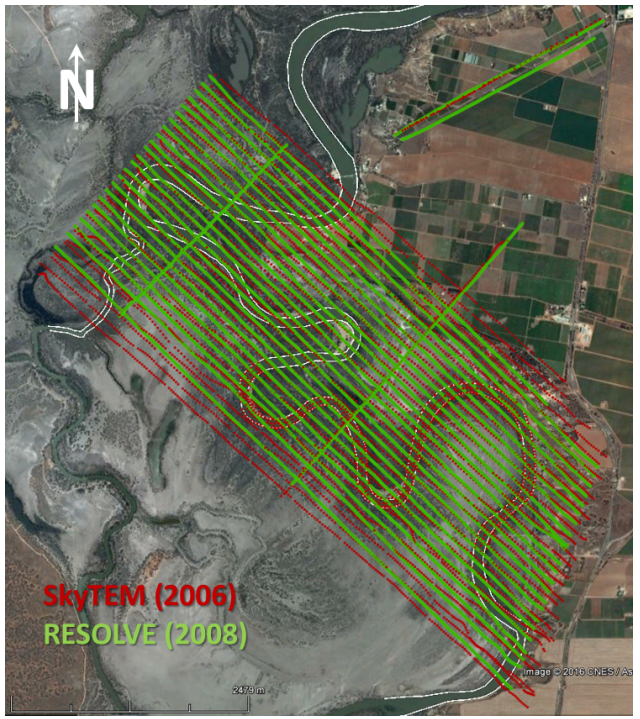
Holland et. al., 2008.

Survey

Resolve system (2008)



Flight lines

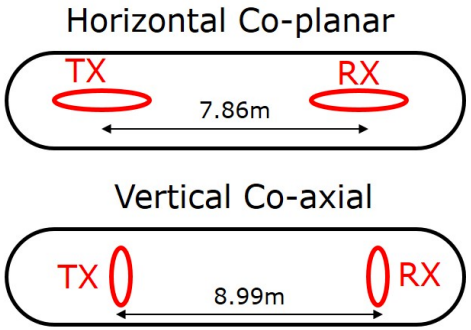


Horizontal Co-planar (HCP) frequencies:

- 382, 1822, 7970, 35920 and 130100 Hz

Vertical Co-axial (VCA) frequencies:

- 3258 Hz

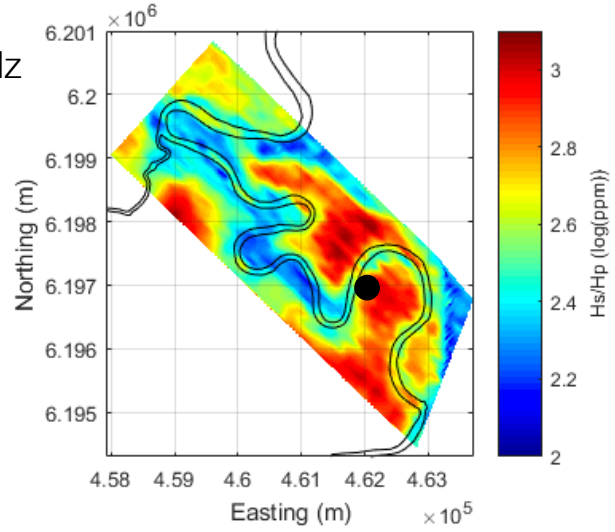


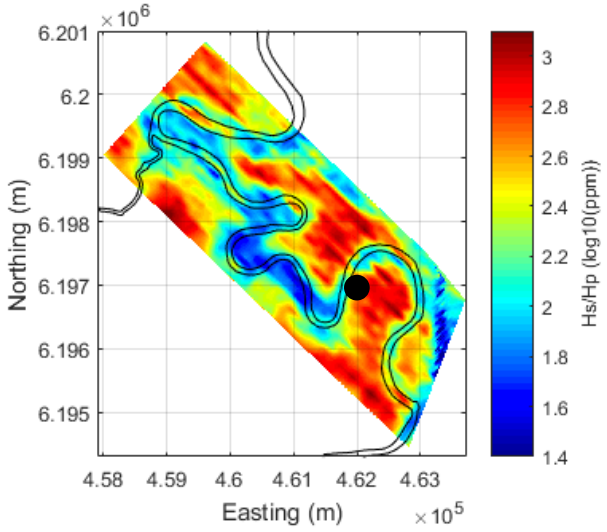
Horizontal Co-planar (HCP) data

In-Phase (Real)

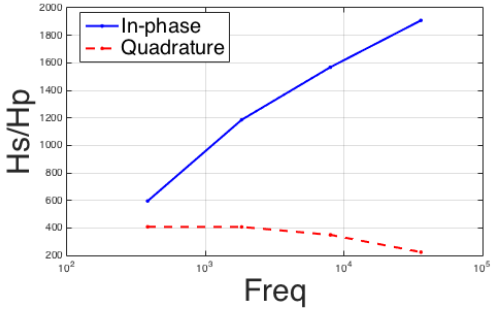
Quadrature (Imaginary)

382 Hz

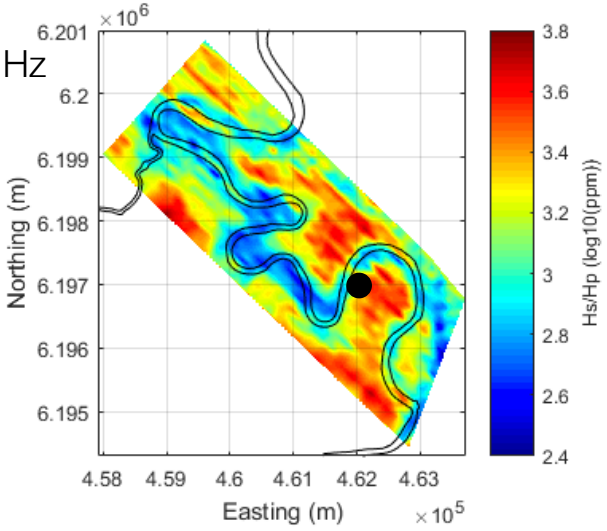


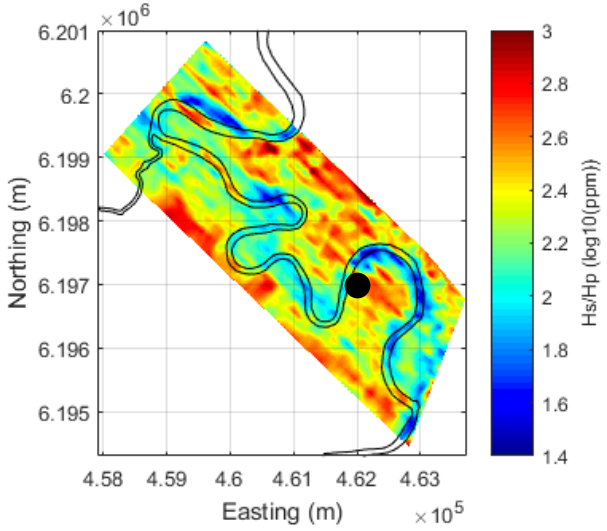


Sounding curve

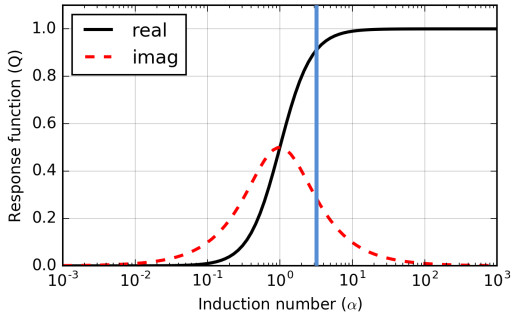


35920 Hz



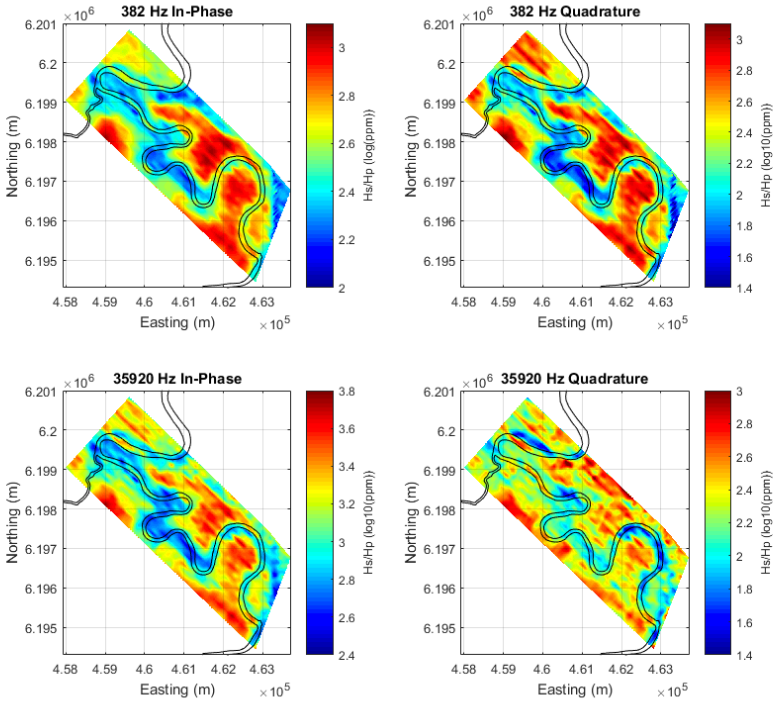


Response curve

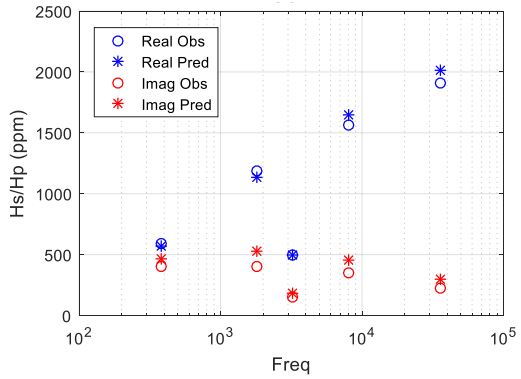


Processing: 1D inversion

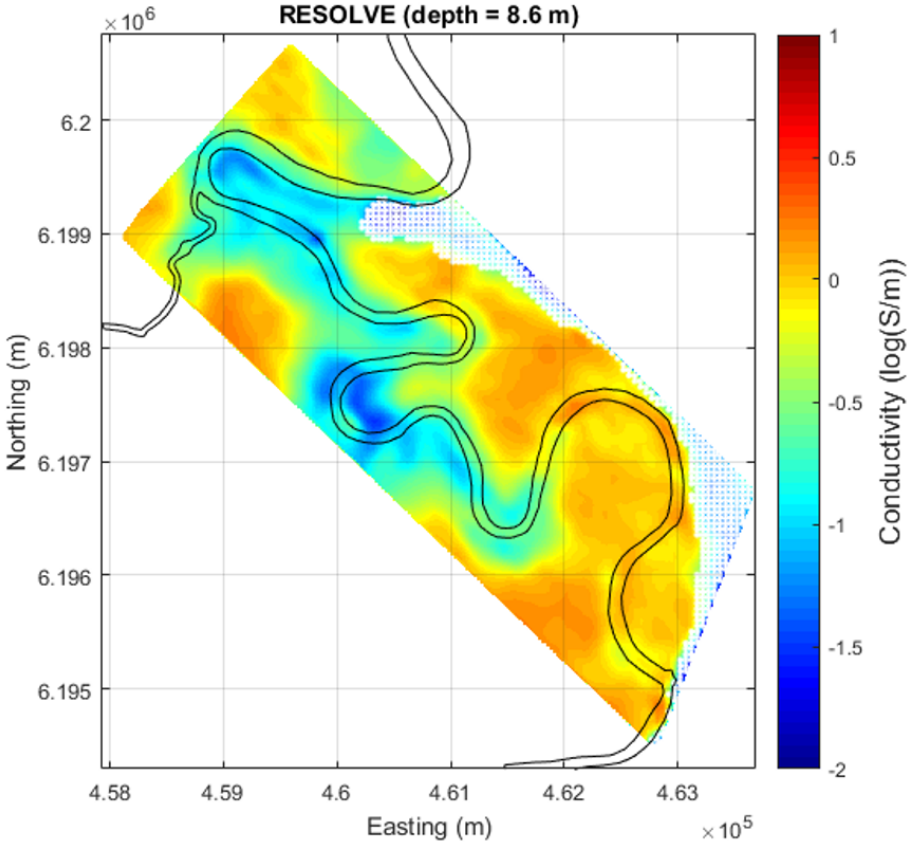
Data



Data fit

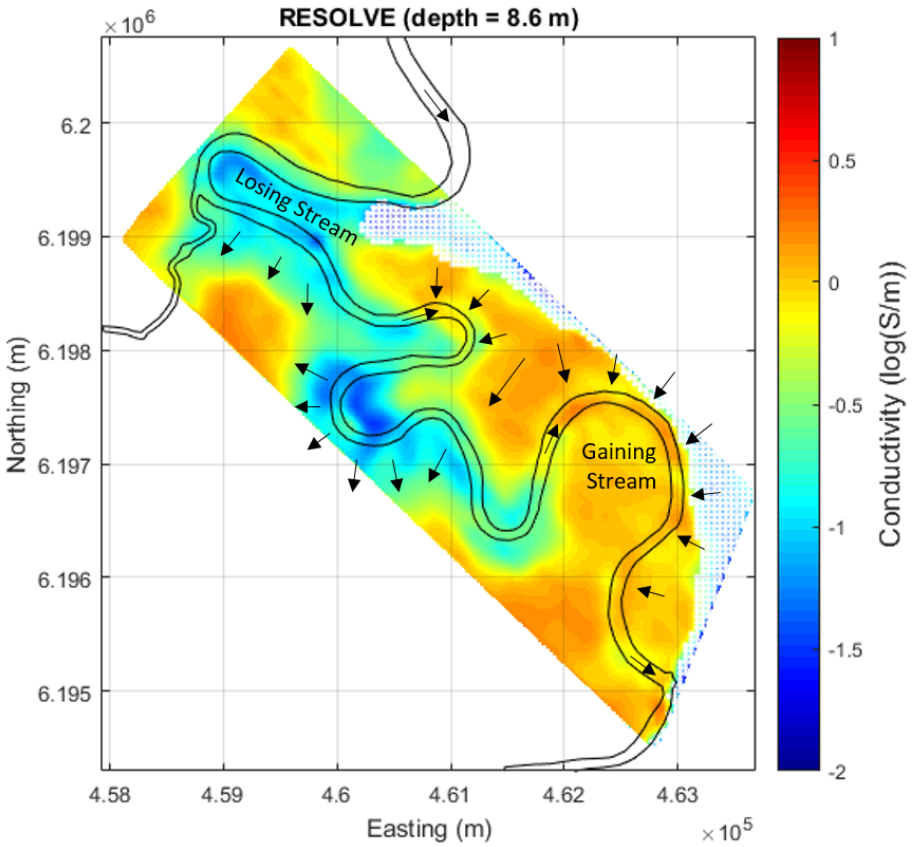


Conductivity model (stitched)

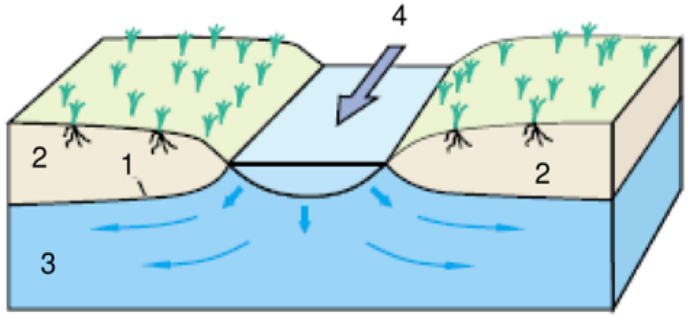


Interpretation

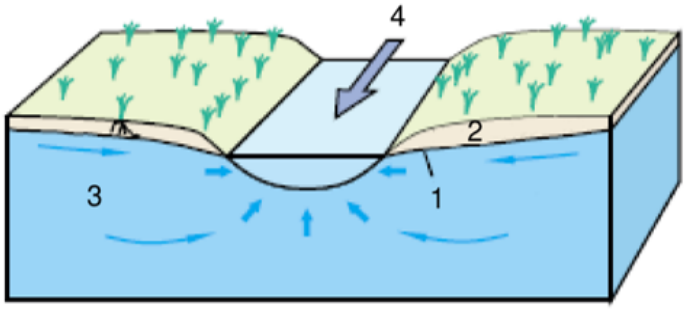
Conductivity model (stitched)



Losing Stream



Gaining Stream

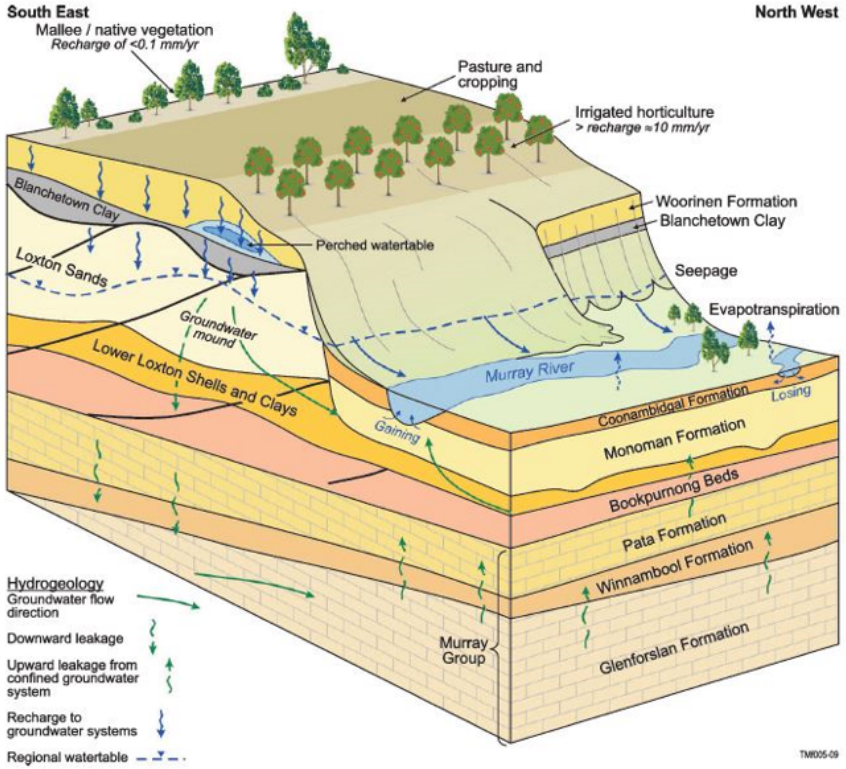


1 – Water table 2 – Unsaturated zone

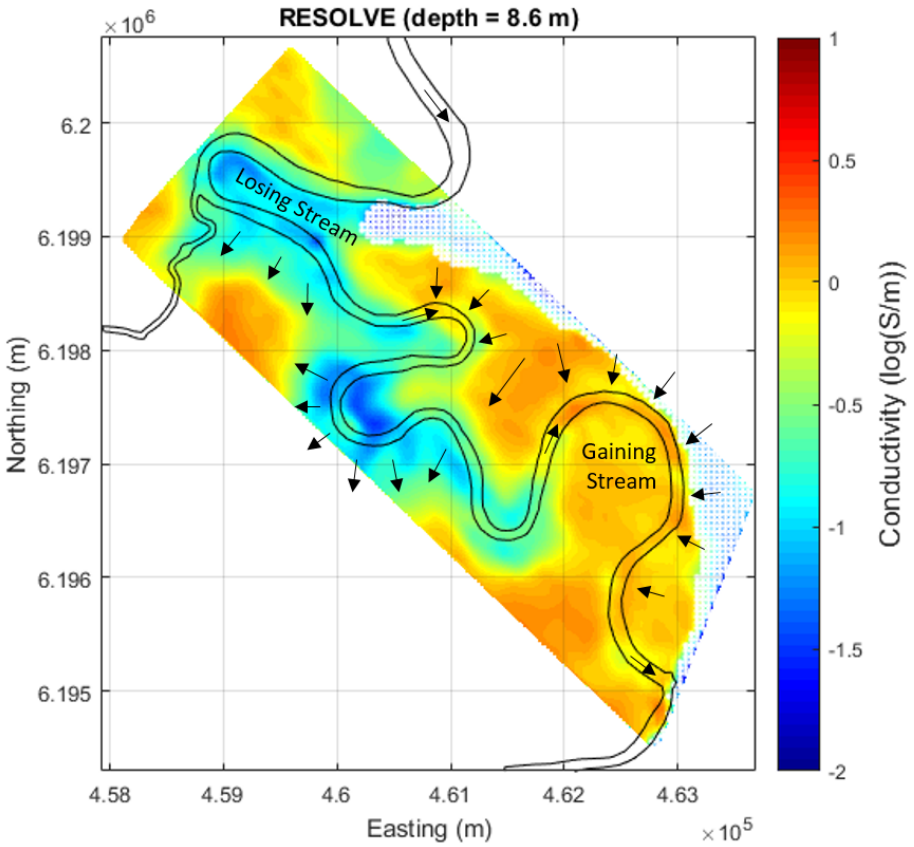
3 – Saturated zone 4 – Flow direction

Synthesis

Hydrological model



Conductivity model (stitched)



Outline

Setup

- Basic experiment
- Transmitters, Receivers

Frequency Domain EM

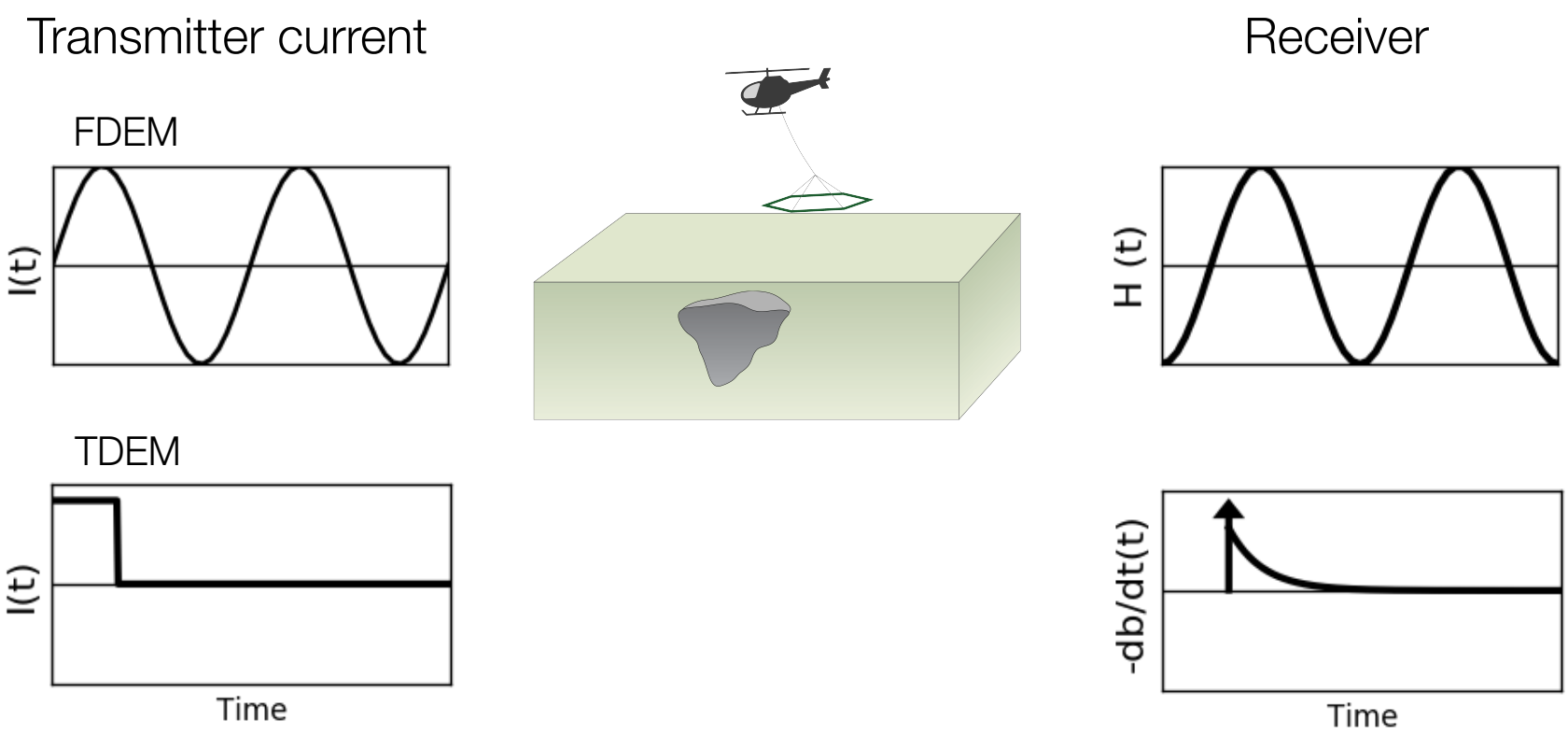
- Vertical Magnetic Dipole
- Effects of Frequency
- Case History – Ground water

Time Domain EM

- Vertical Magnetic Dipole
- Propagation with Time
- Case History – Near surface geology

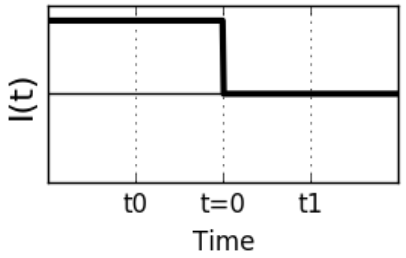
EM with Inductive Sources

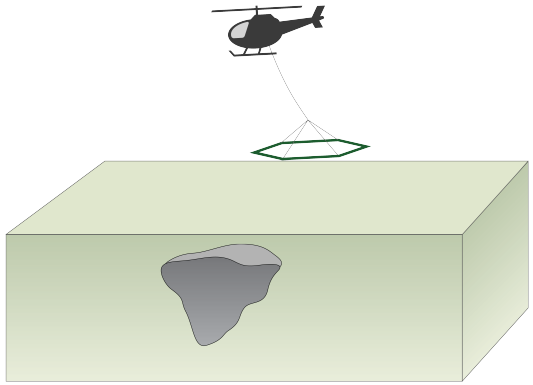
- Induction principles are the same for
  - FDEM: Frequency domain EM
  - TDEM: Time domain EM



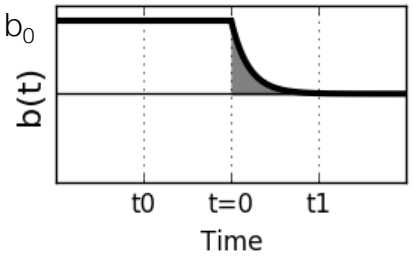
EM with Inductive Sources: Time Domain

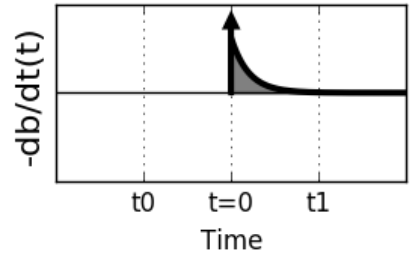
Transmitter current





Receiver

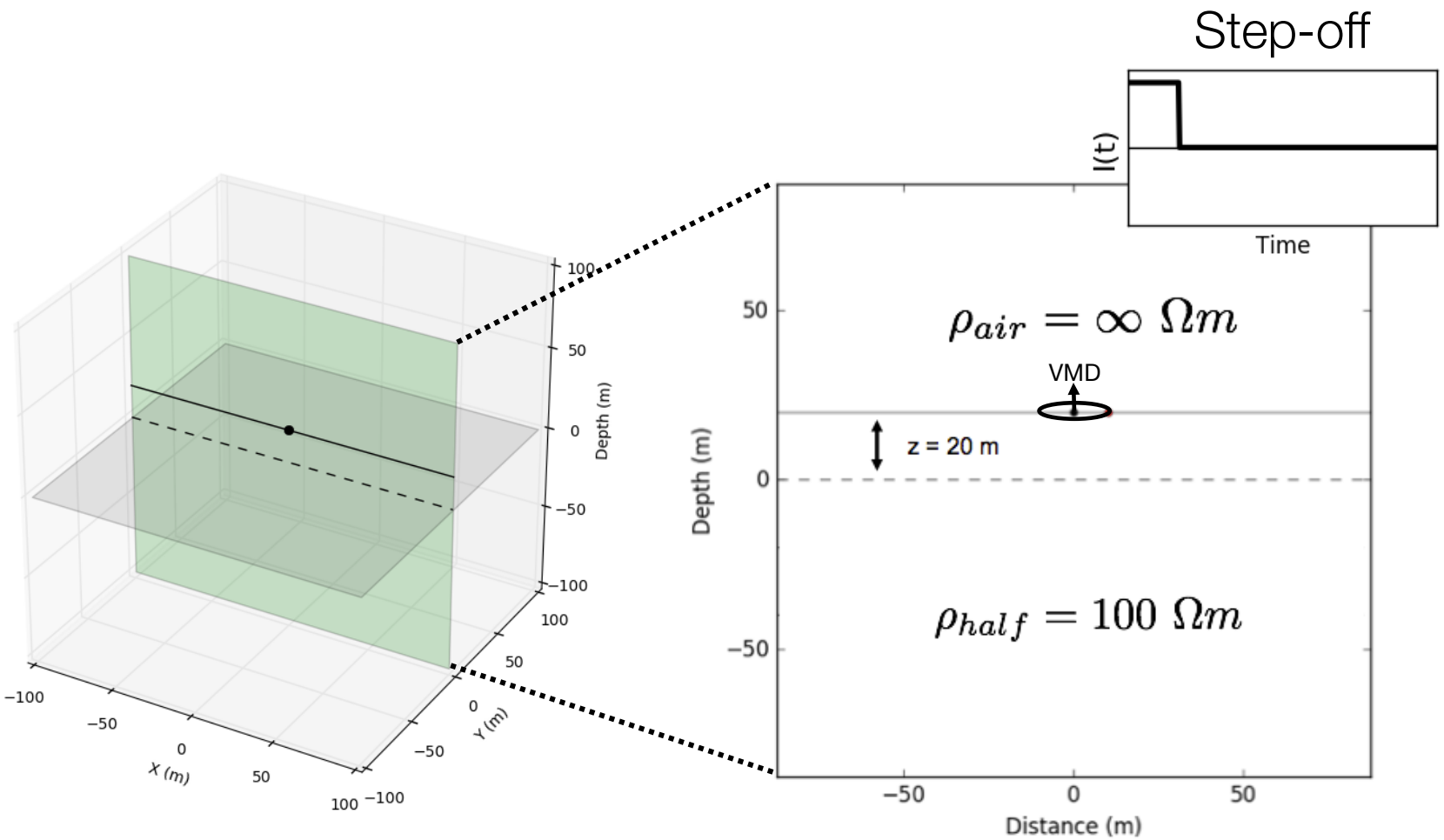




time	**b**	**db/dt**
$t < 0$	b_0	0
$t = 0$	b_0	$-b_0\delta(t)$
$t > 0$	secondary	secondary

$\delta(t)$: Dirac-delta function

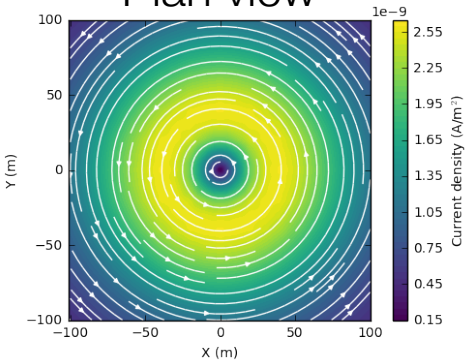
Vertical Magnetic Dipole over a halfspace (TDEM)



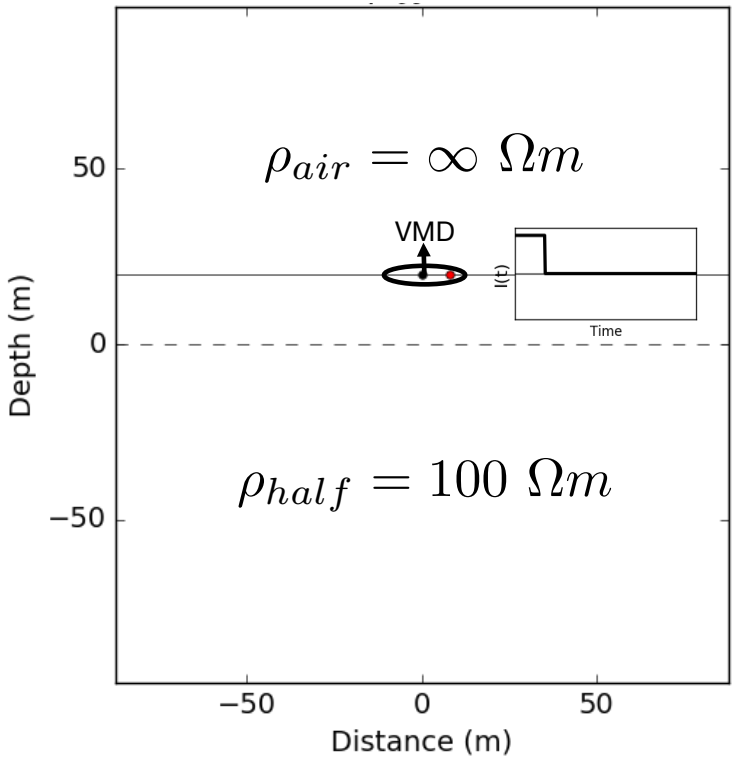
Current Density

- Time: 0.01ms

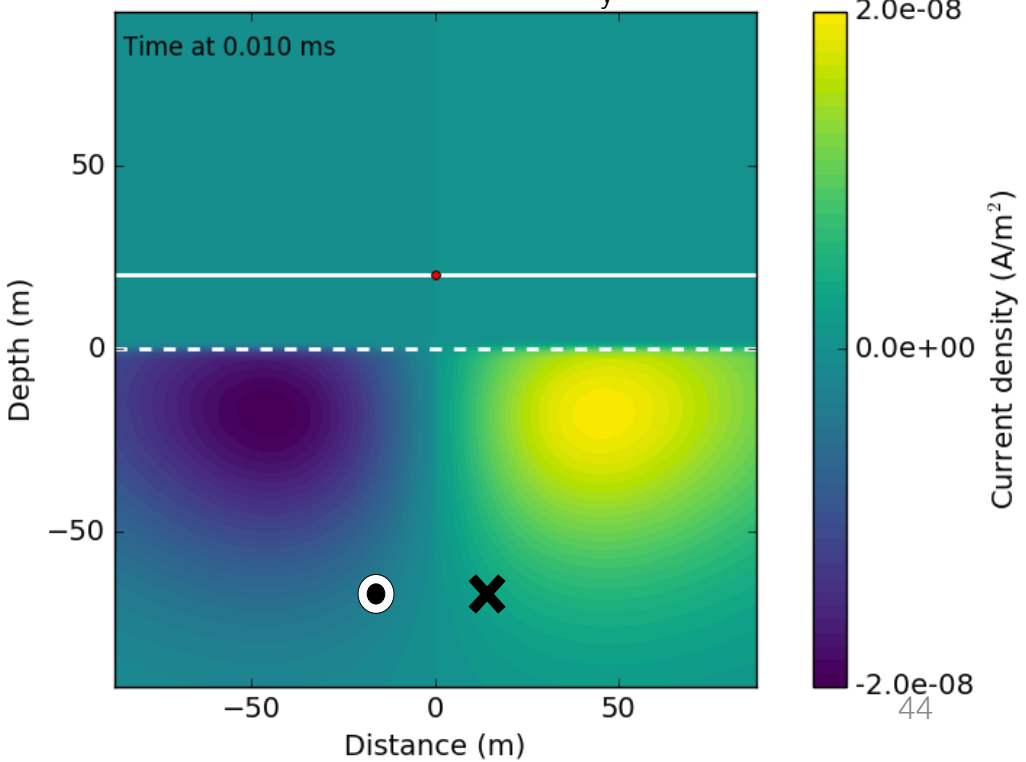
Plan view



Geometry

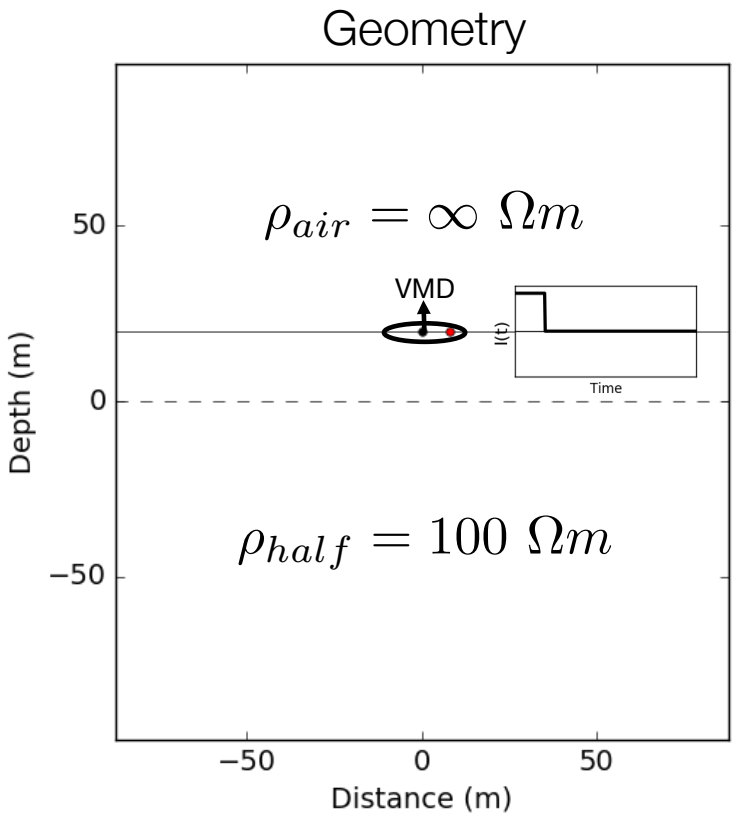


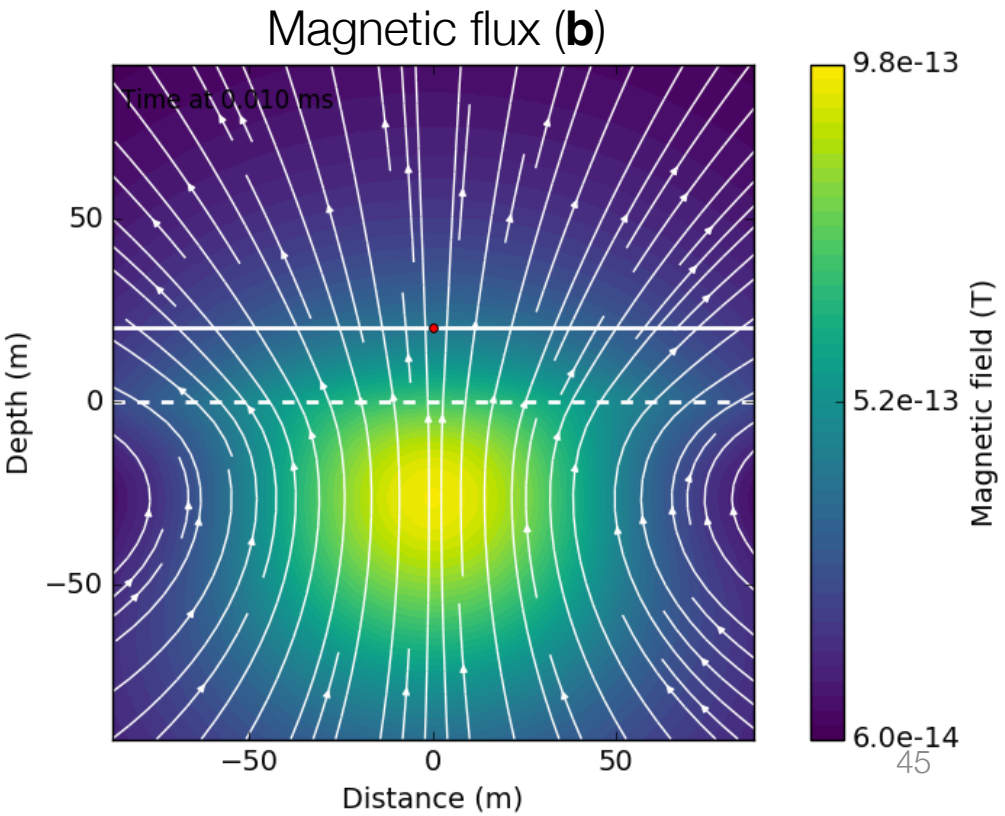
Current density (j_y)



Magnetic flux density

- Time: 0.01ms

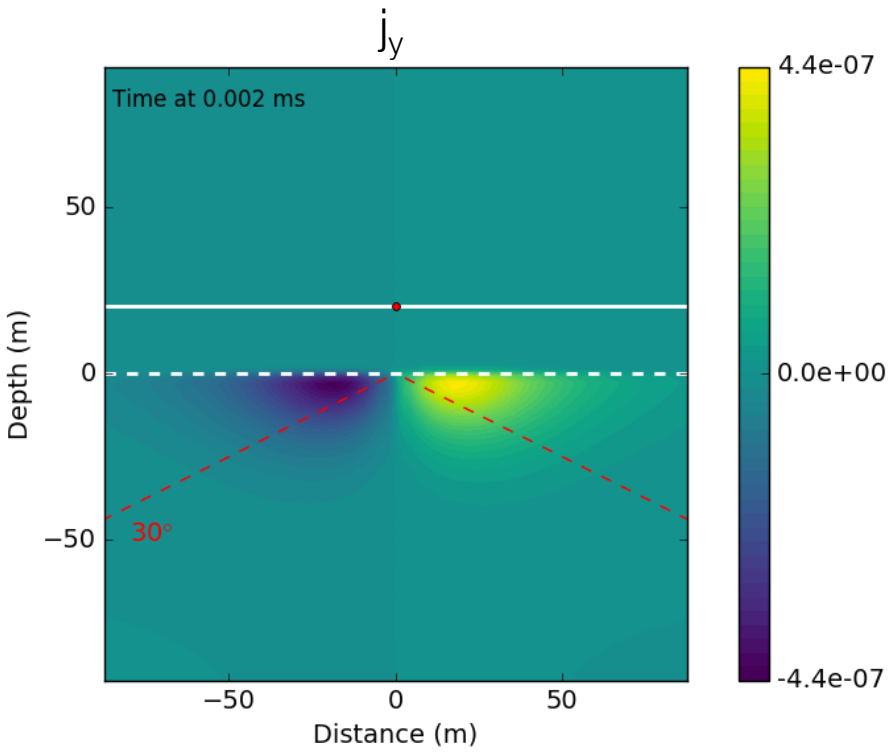


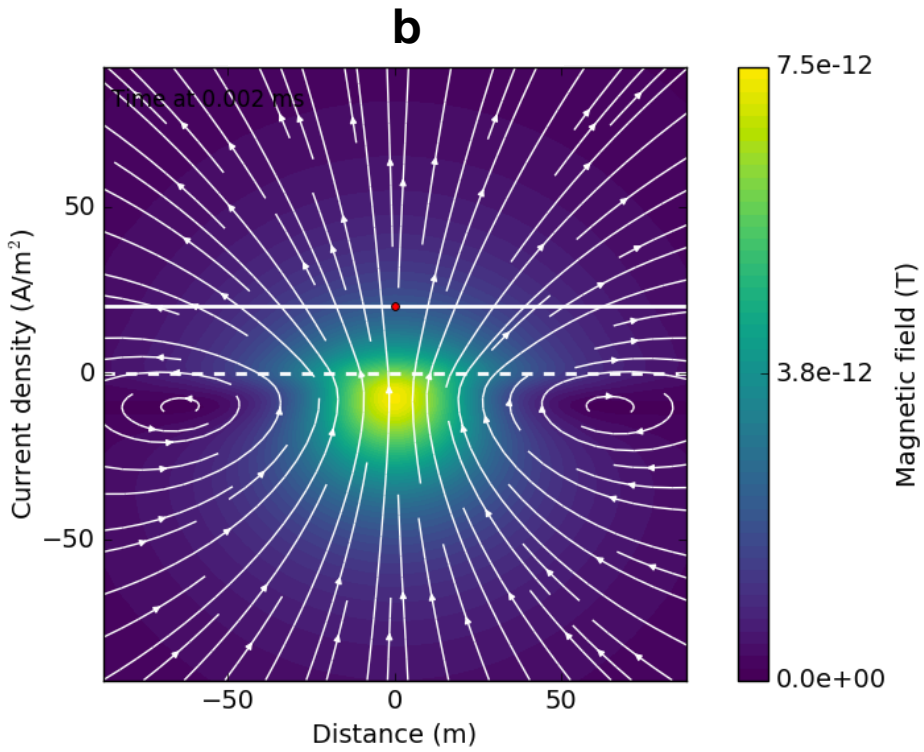


Propagation through time

- Time: 0.002ms
- diffusion distance = 18 m

$$d = 1260\sqrt{t\rho}$$

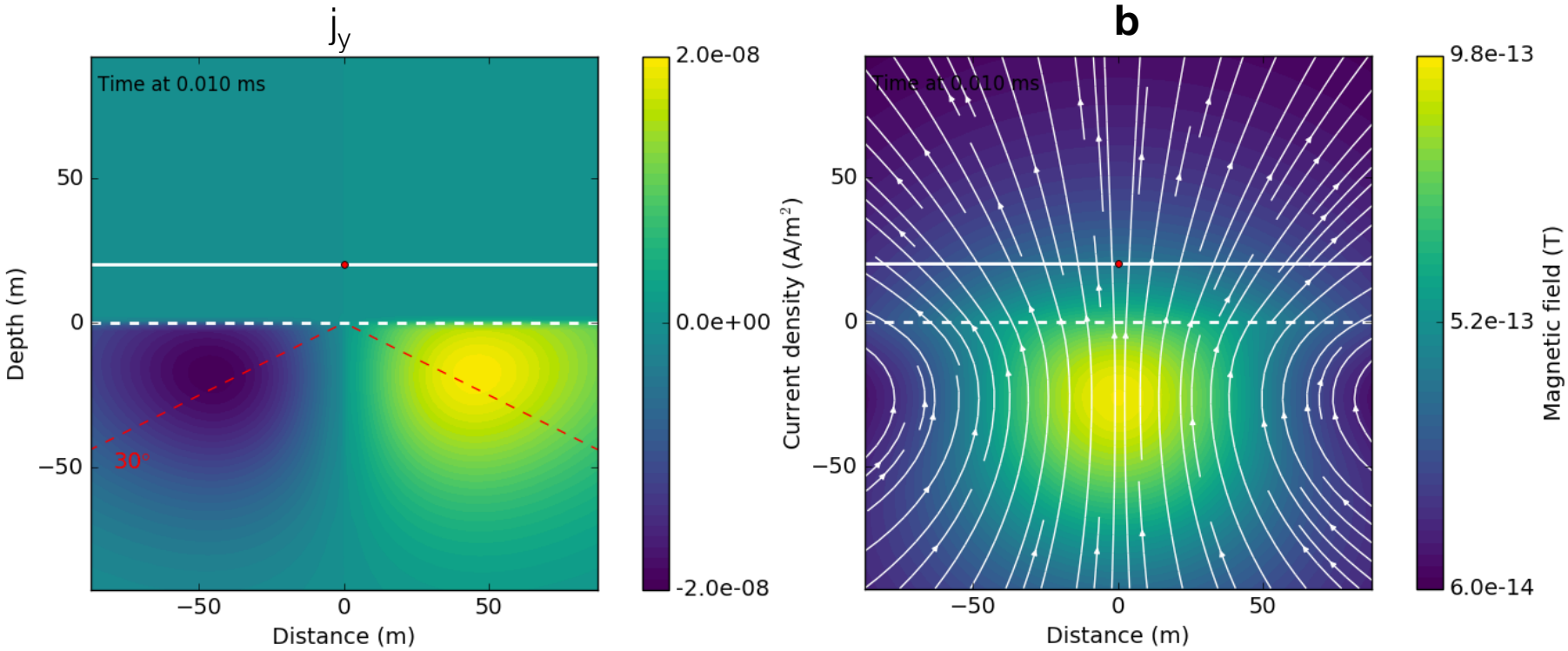




Propagation through time

- Time: 0.01ms
- diffusion distance = 38 m

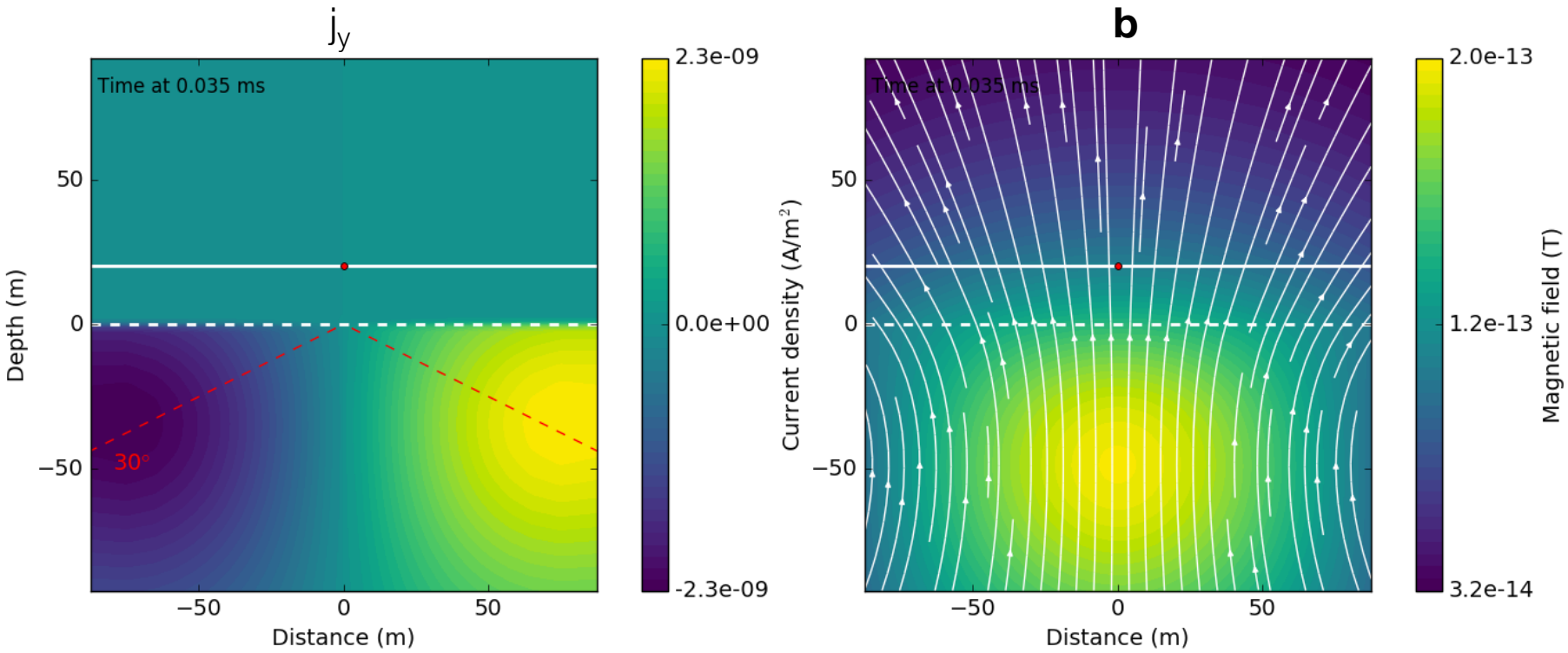
$$d = 1260\sqrt{t\rho}$$



Propagation through time

- Time: 0.035ms
- diffusion distance = 75 m

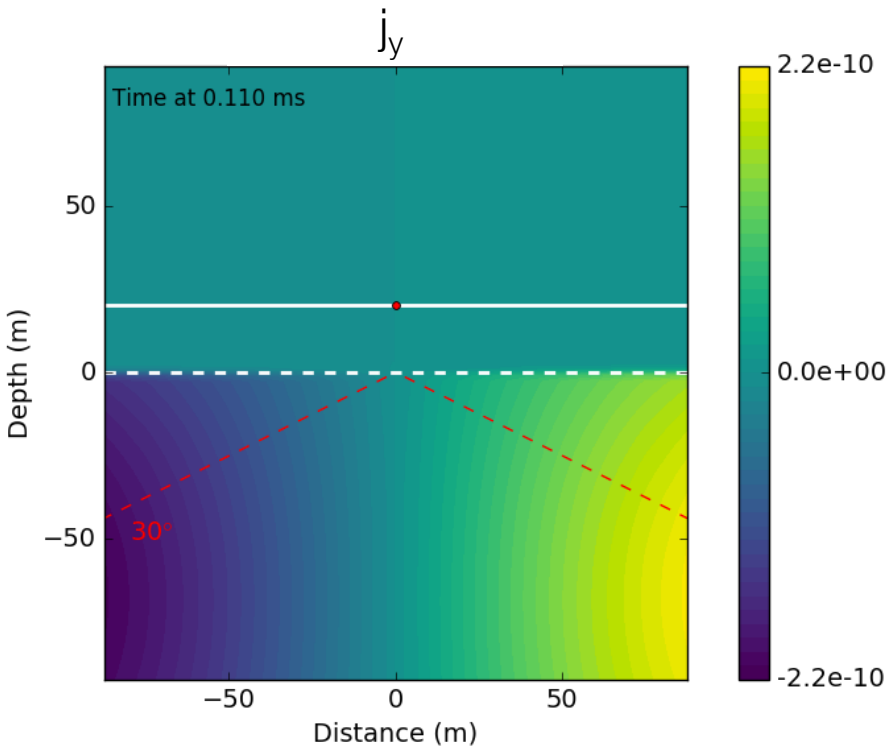
$$d = 1260\sqrt{t\rho}$$

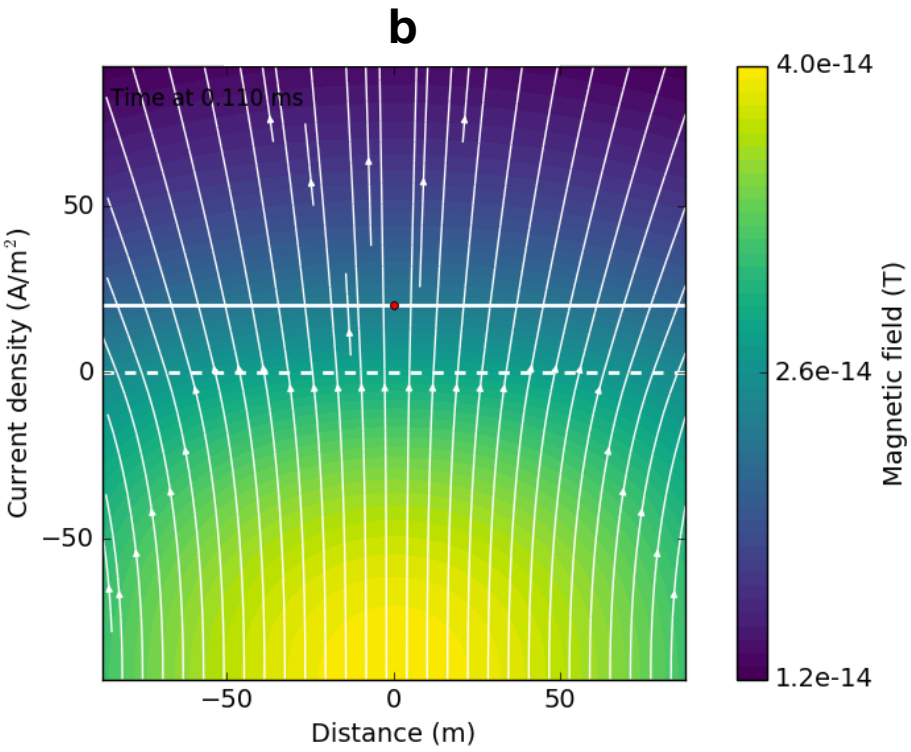


Propagation through time

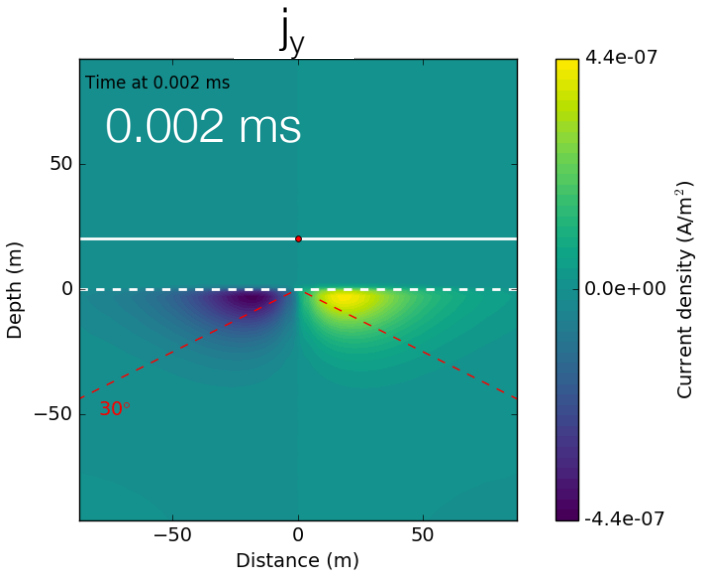
- Time: 0.110ms
- diffusion distance = 132 m

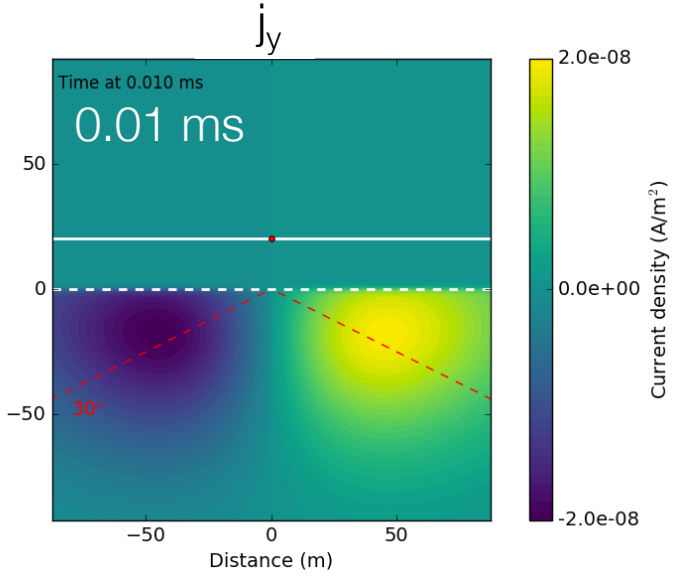
$$d = 1260\sqrt{t\rho}$$

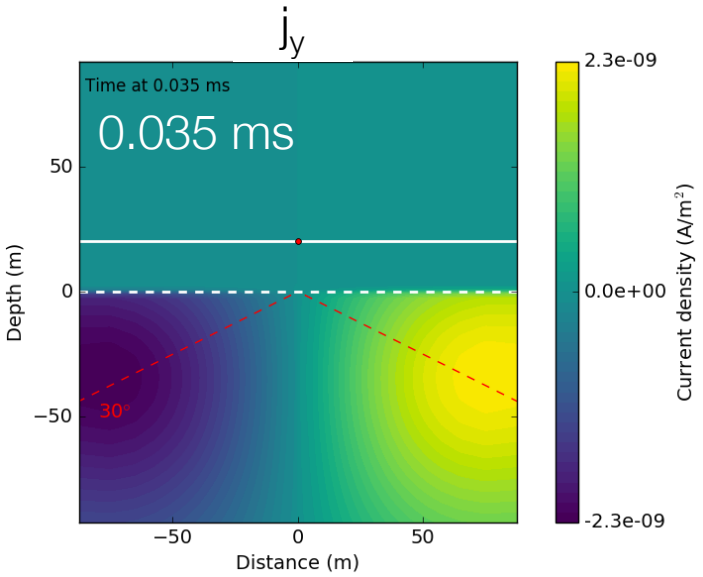




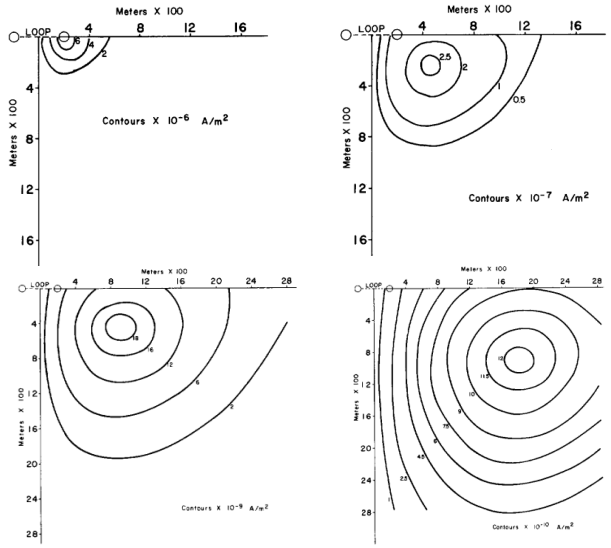
Summary: propagation through time





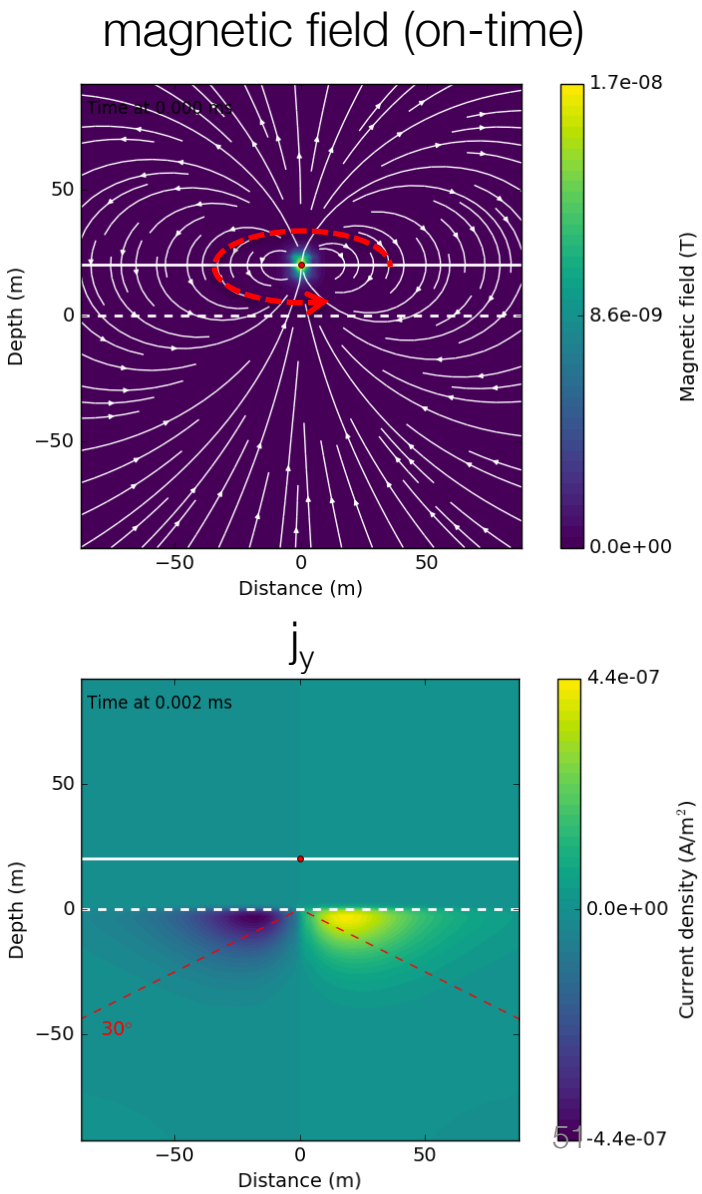


Nabighian (1979)



Important points

- Currents flow in same plane as transmitter currents
- Currents diffuse outward downward
- Each transmitter has a “footprint”
- Max resolution controlled by earliest time
- Depth of investigation controlled by latest time



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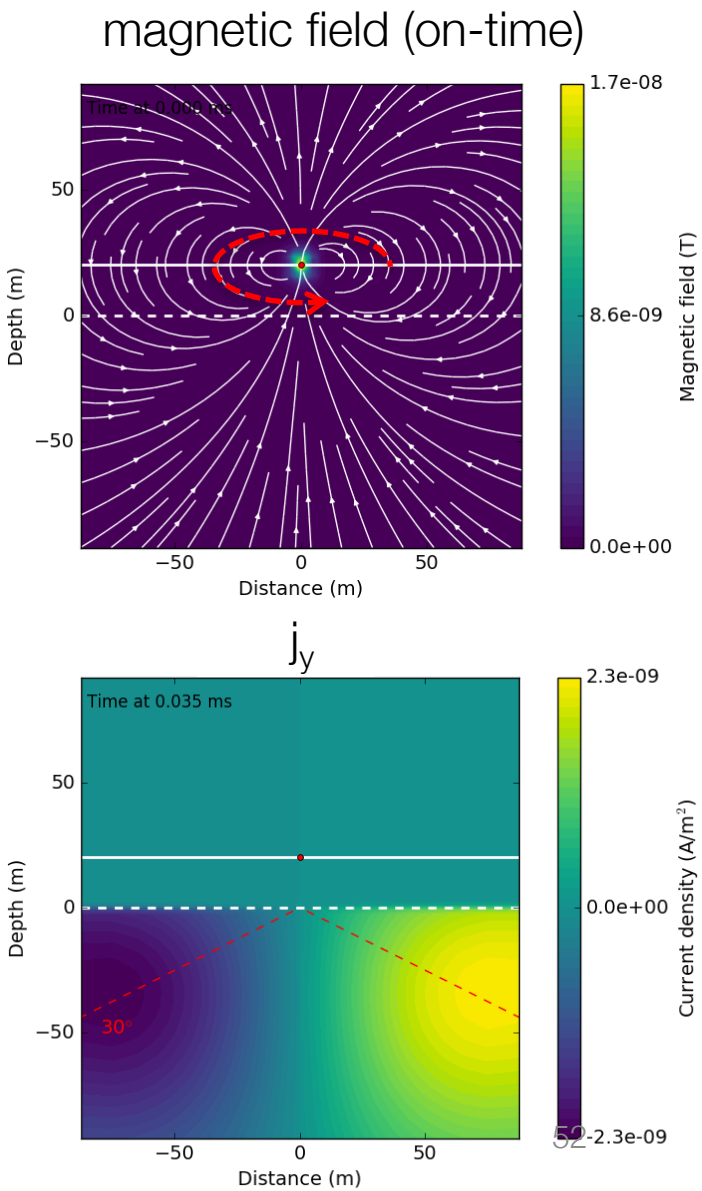
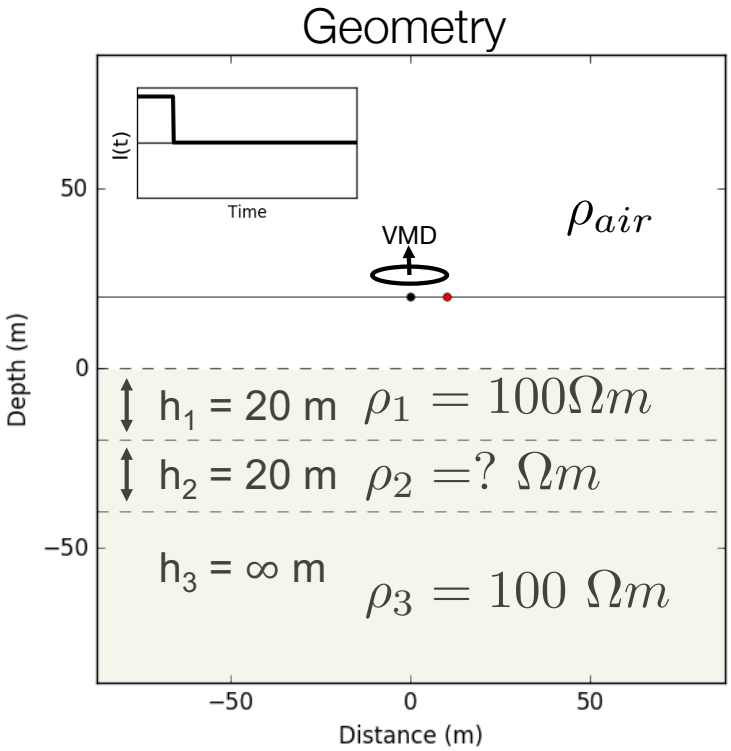


Layered earth

- 3 layers + air,
- ρ_2 varies

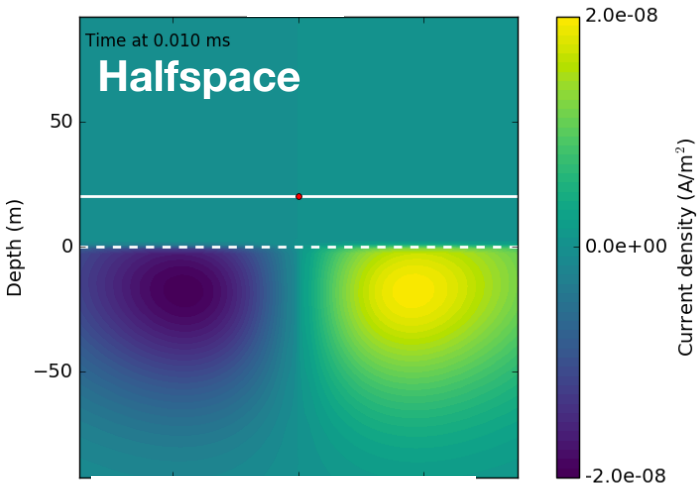


- Four different cases:
  - Halfspace
    $\rho_2 = 100\ \Omega m$
  - Resistive
    $\rho_2 = 1000\ \Omega m$
  - Conductive
    $\rho_2 = 10\ \Omega m$
  - Very conductive
    $\rho_2 = 1\ \Omega m$

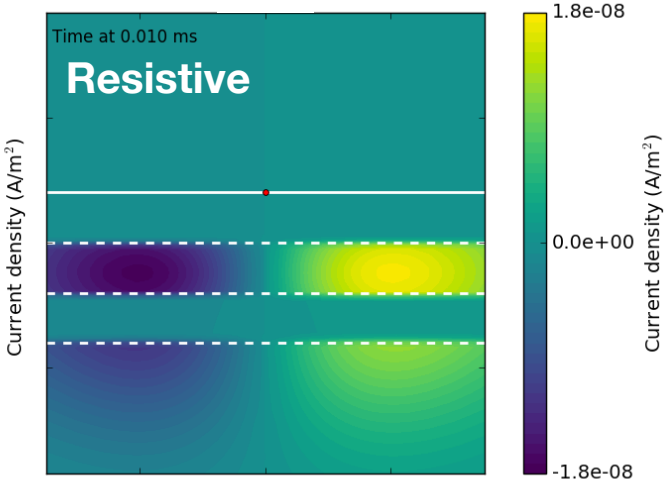
- Fields
  - j_y off-time
  - **b** off-time

Layered earth currents (j_y)

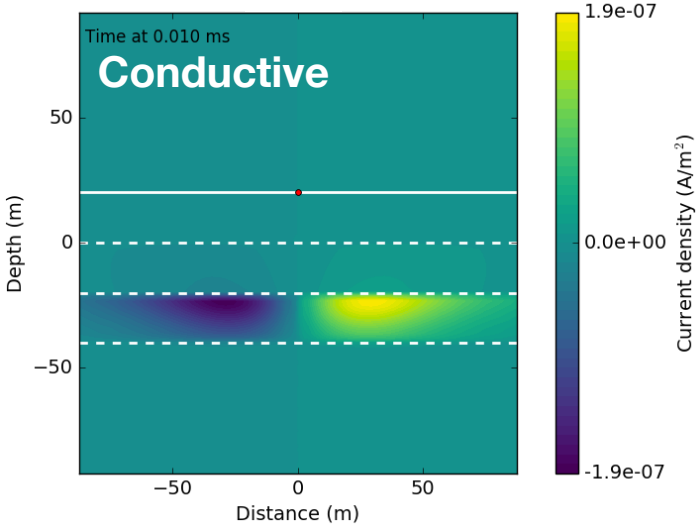
$\rho_2 = 100\ \Omega m$



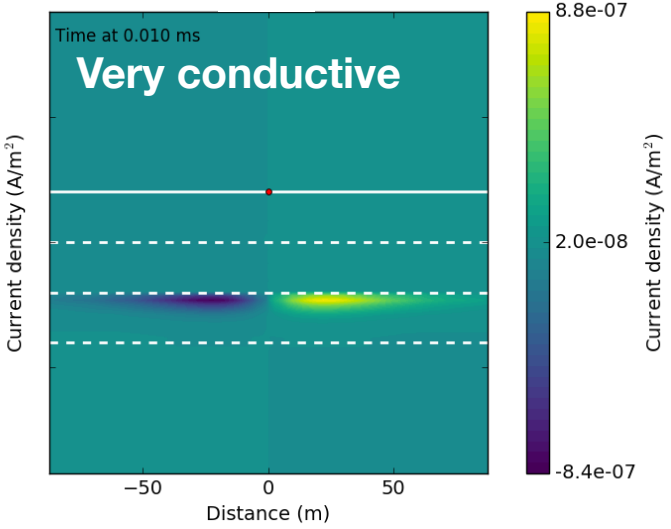
$\rho_2 = 1000\ \Omega m$



$\rho_2 = 10\ \Omega m$

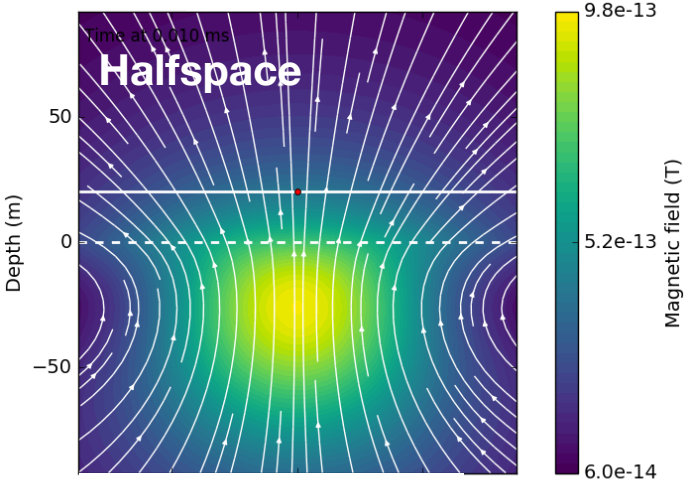


$\rho_2 = 1\ \Omega m$

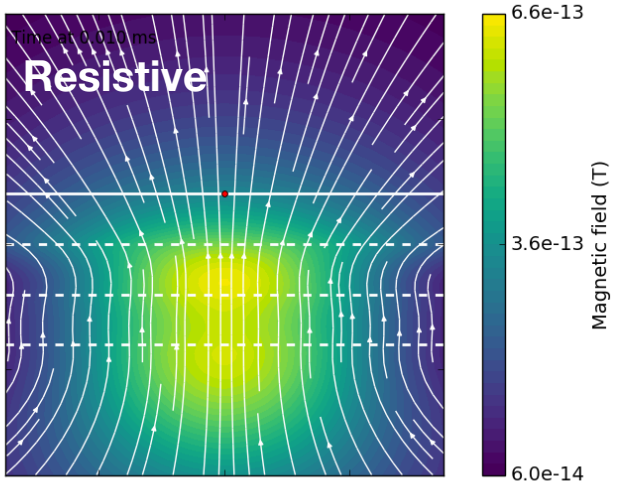


Layered earth mag. fields (**b**)

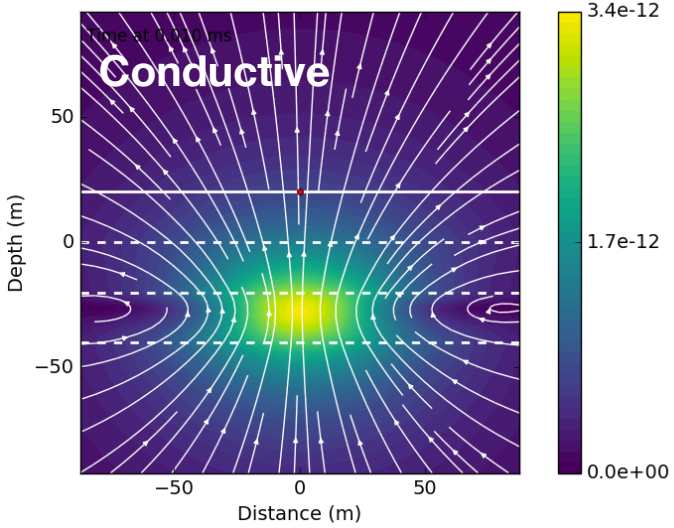
$\rho_2 = 100\ \Omega m$



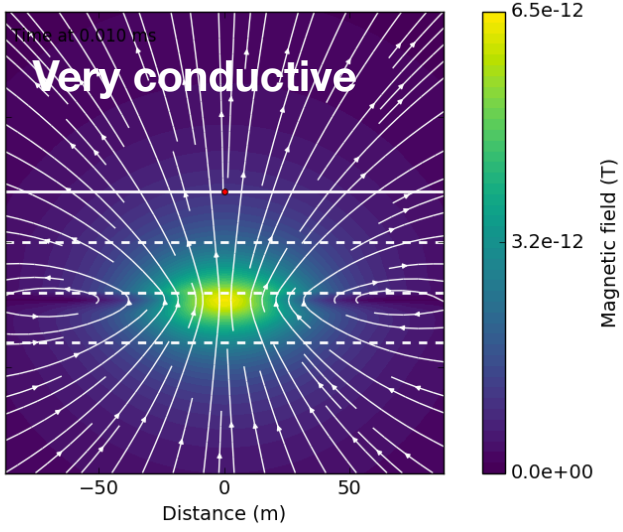
$\rho_2 = 1000\ \Omega m$



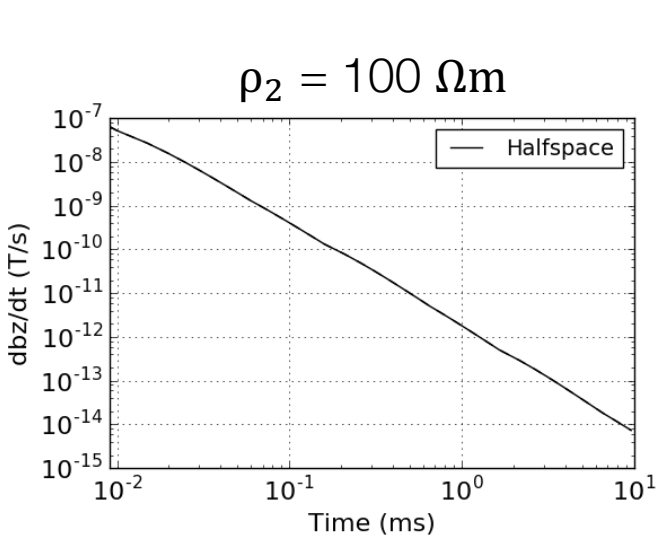
$\rho_2 = 10\ \Omega m$

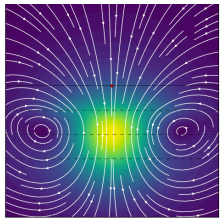


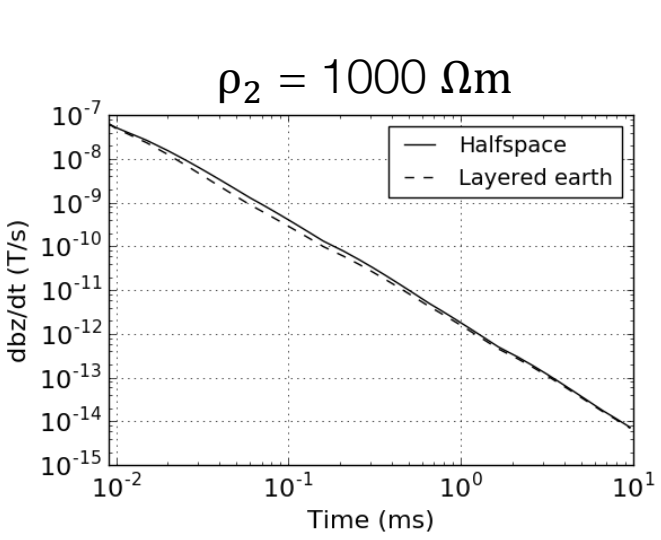
$\rho_2 = 1\ \Omega m$

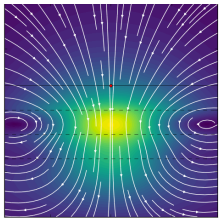


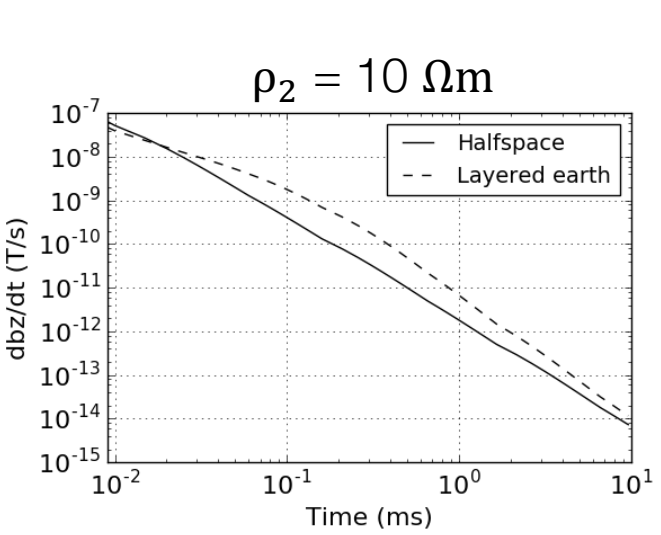
db_z/dt sounding curves

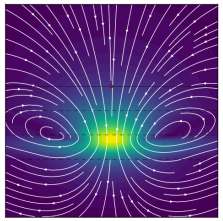


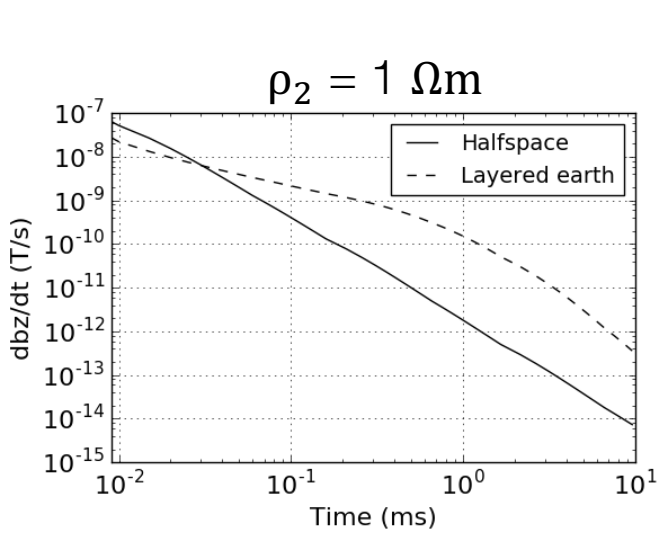


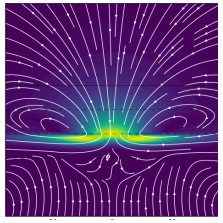






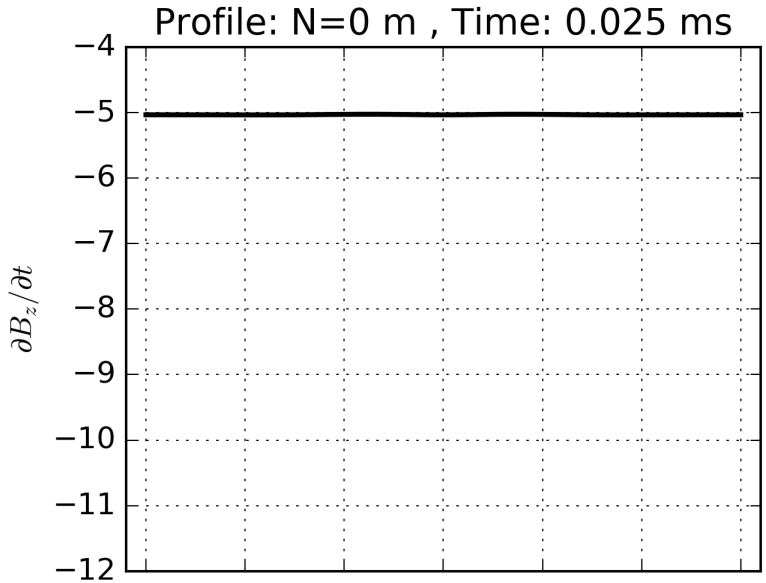




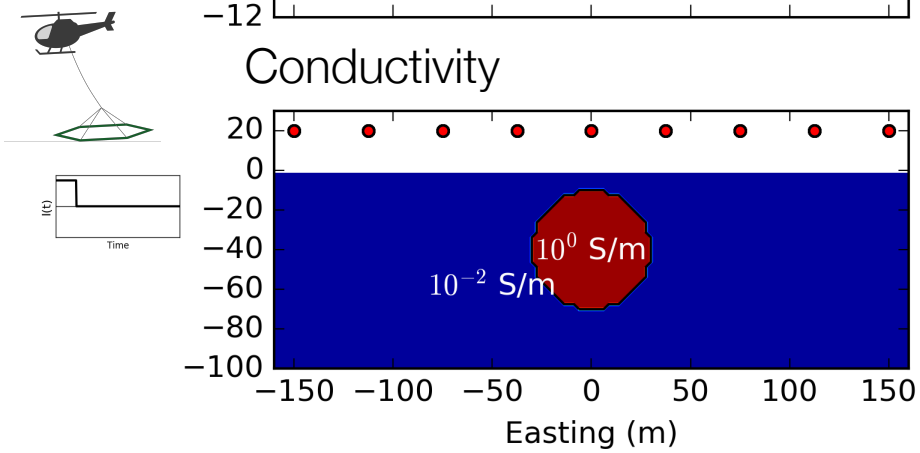


Airborne example: conductive sphere

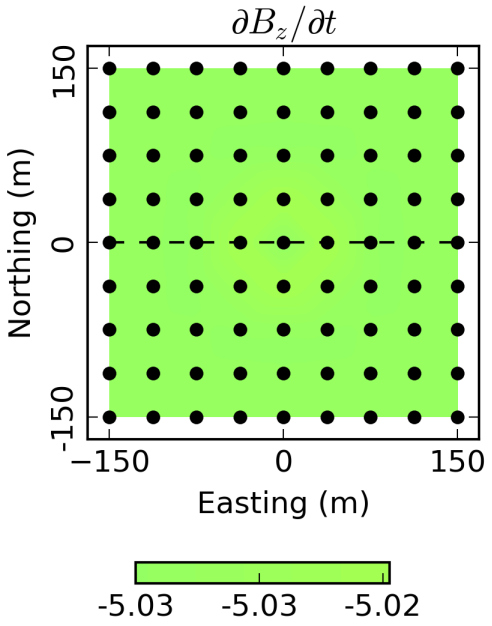
Data profile



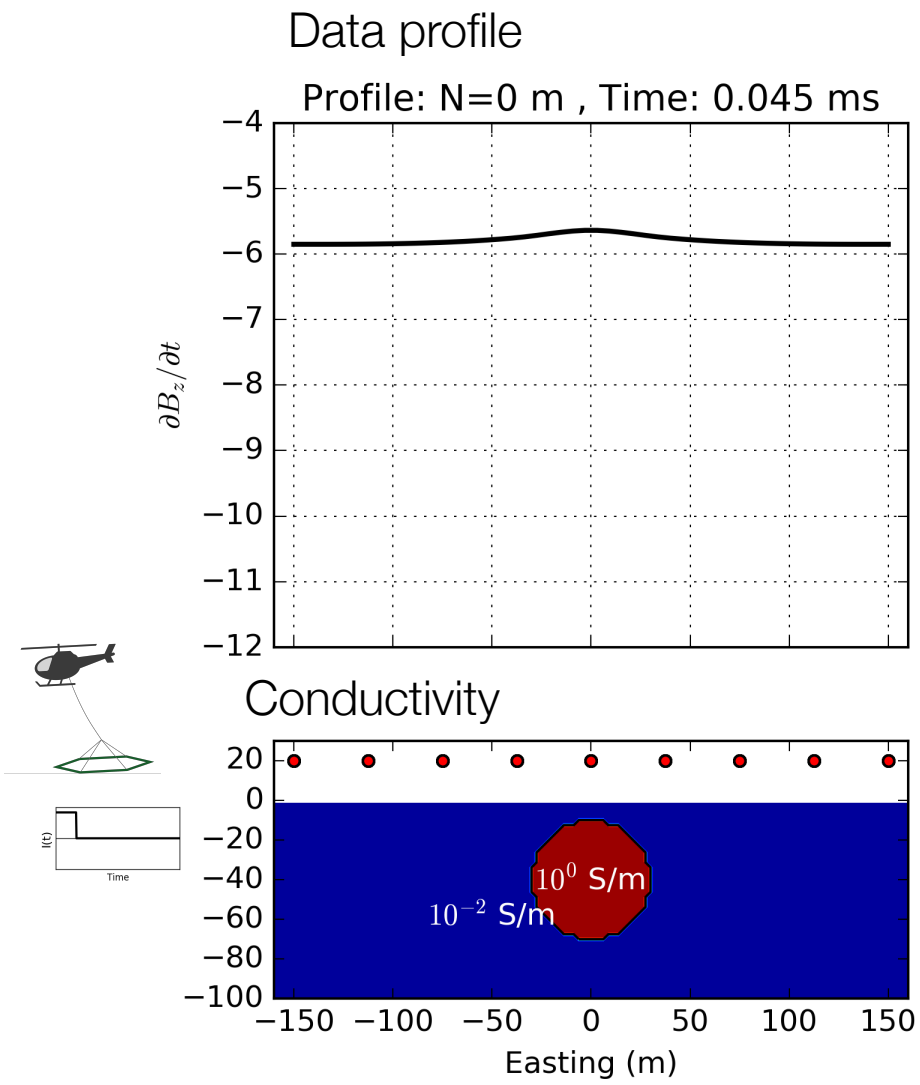
Conductivity

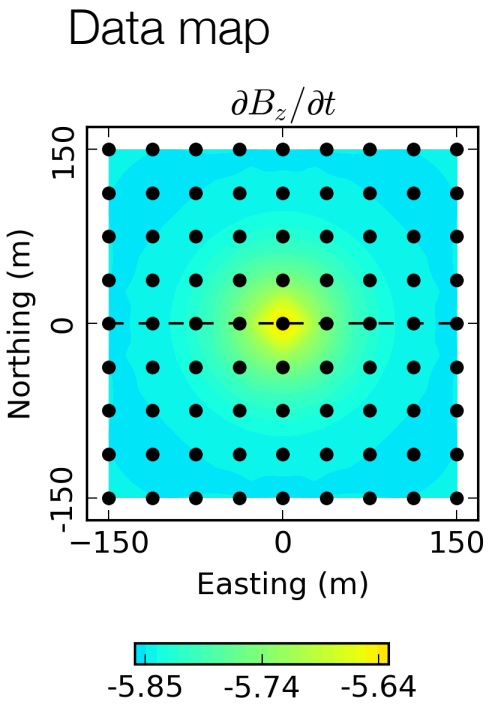


Data map



Airborne example: conductive sphere





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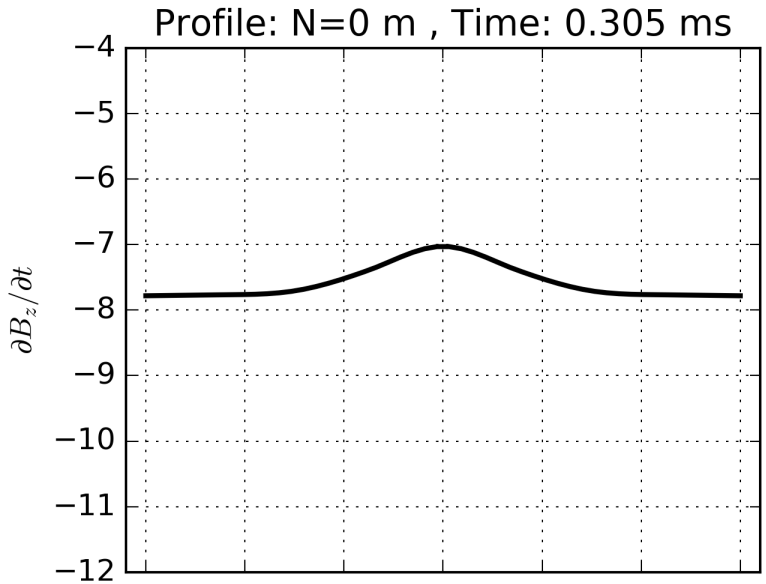
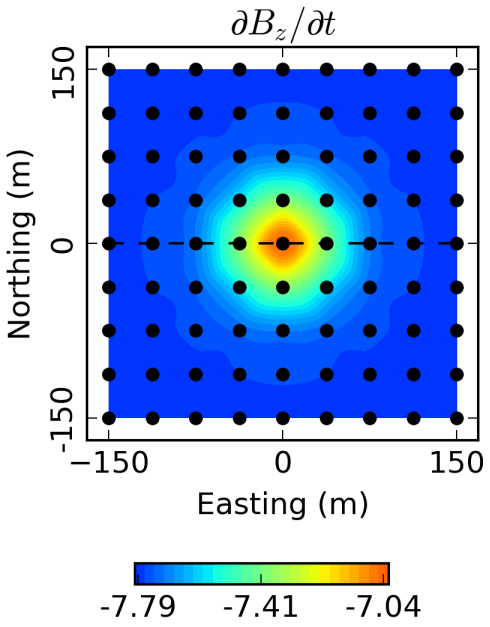
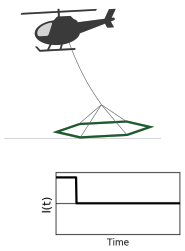
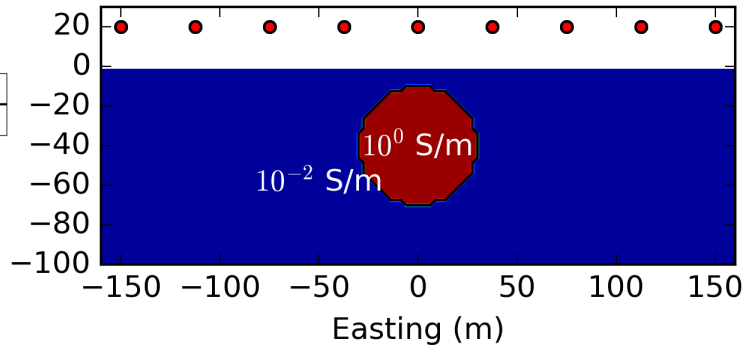


Data map



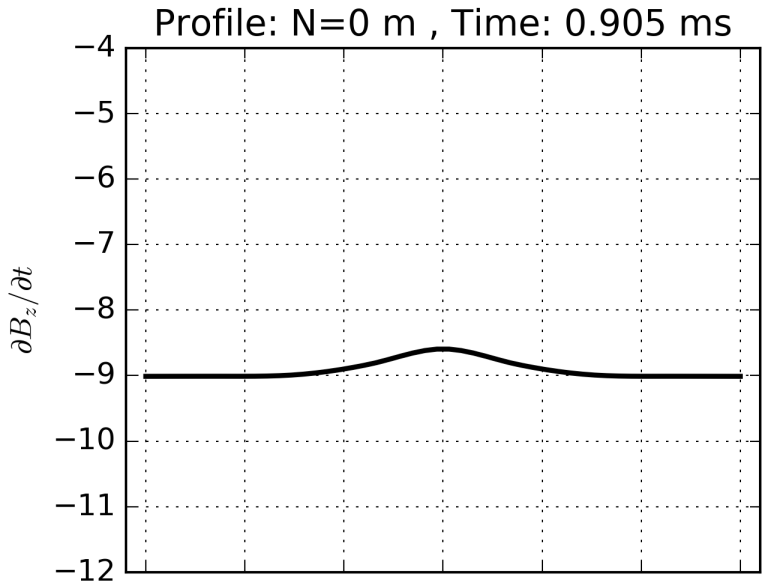


Conductivity

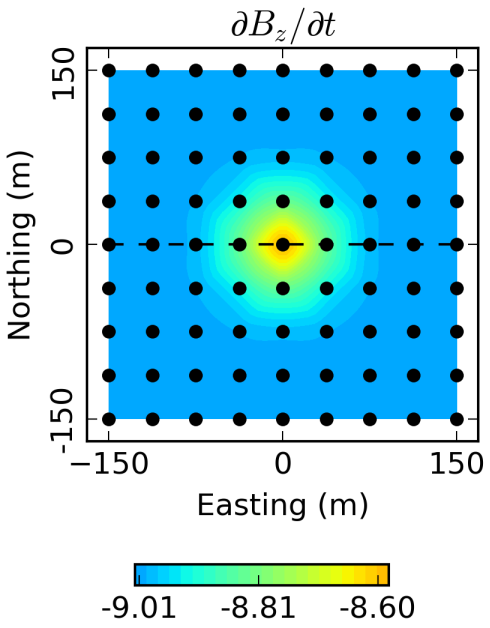


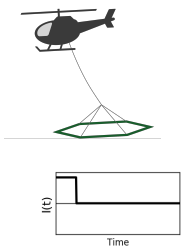
Airborne example: conductive sphere

Data profile

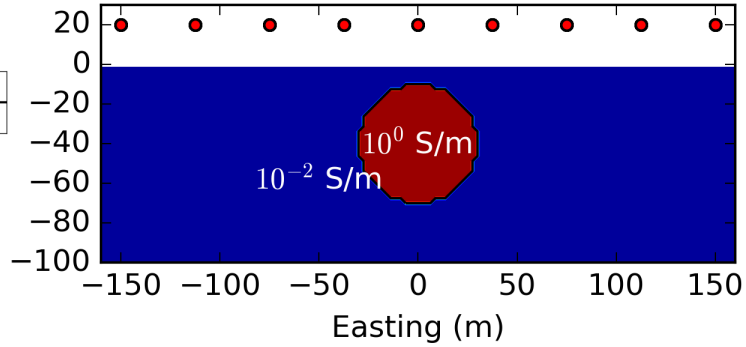


Data map

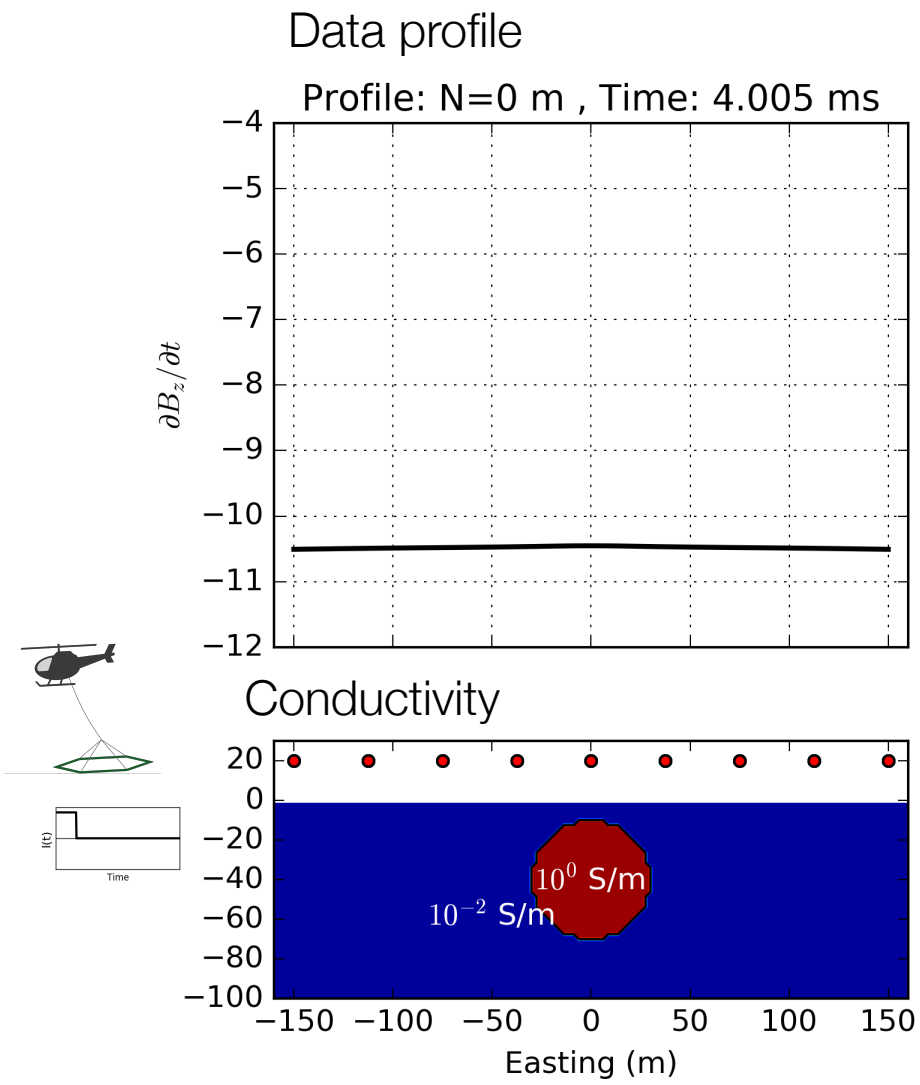


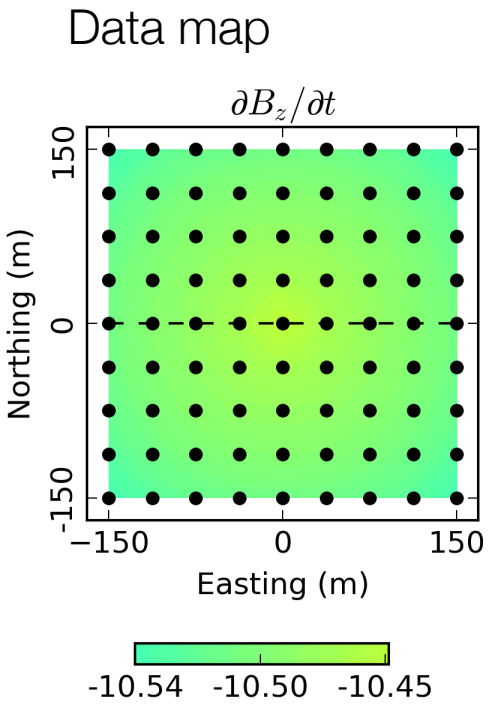


Conductivity



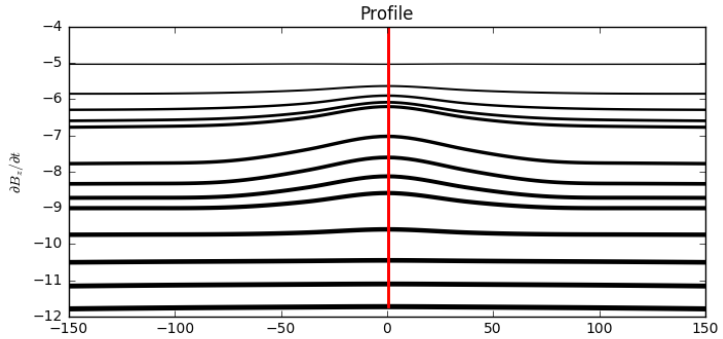
Airborne example: conductive sphere

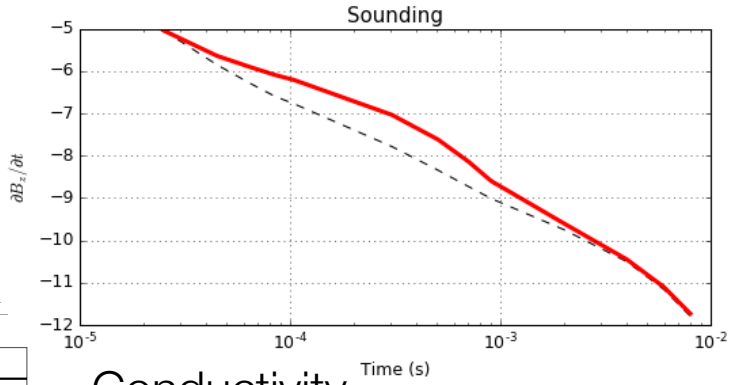


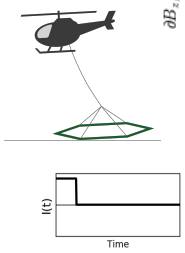


Summary: airborne example

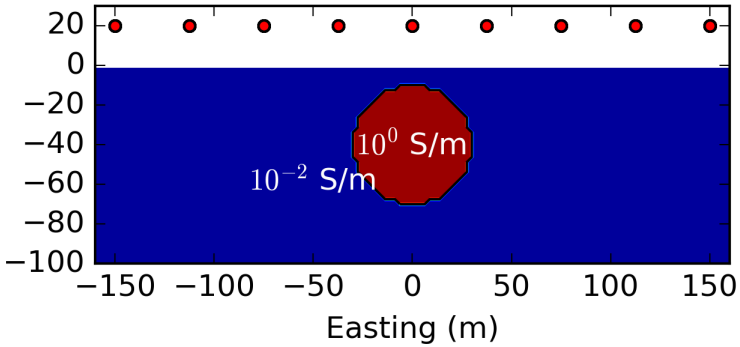
Data profile



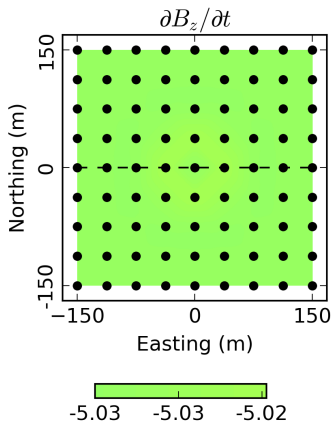




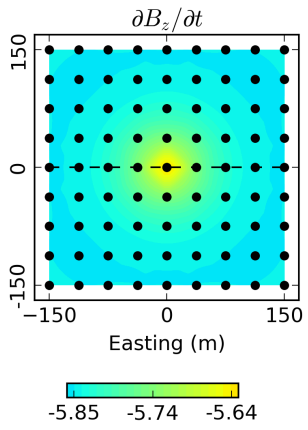
Conductivity



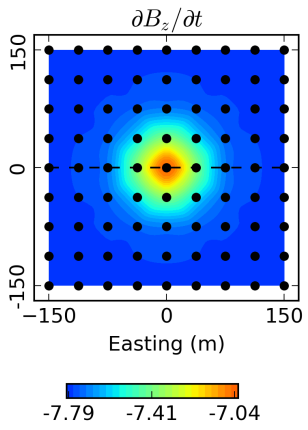
0.025 ms



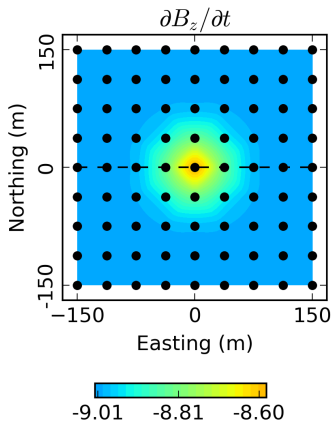
0.045 ms



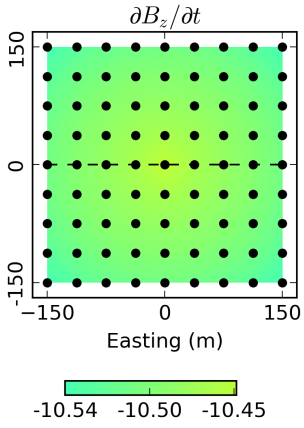
0.305 ms



0.905 ms



4.005 ms

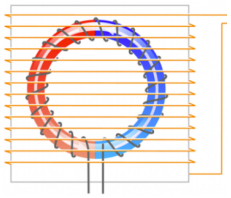


TDEM Receiver

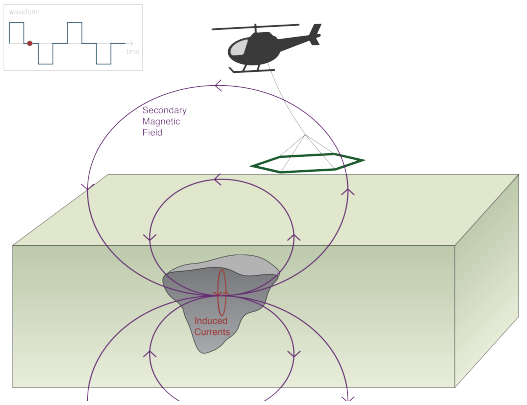
Magnetometer

- Measures:
  - Magnetic field
  - 3 components
- eg. 3-component fluxgate

$$\mathbf{b}(t)$$



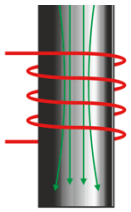
Fluxgate Squid



Coil

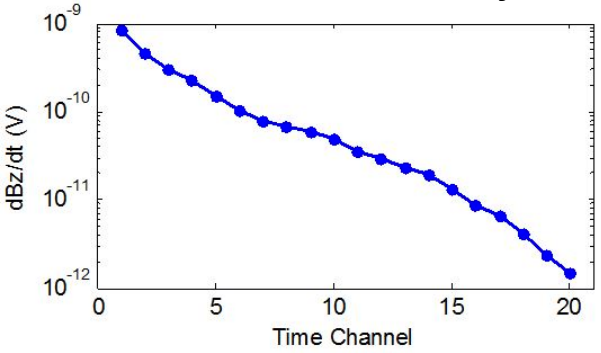
- Measures:
  - Voltage
  - Single component that depends on coil orientation
    - Coupling matters
- Airborne TDEM: measure db/dt

$$\frac{\partial b}{\partial t}$$



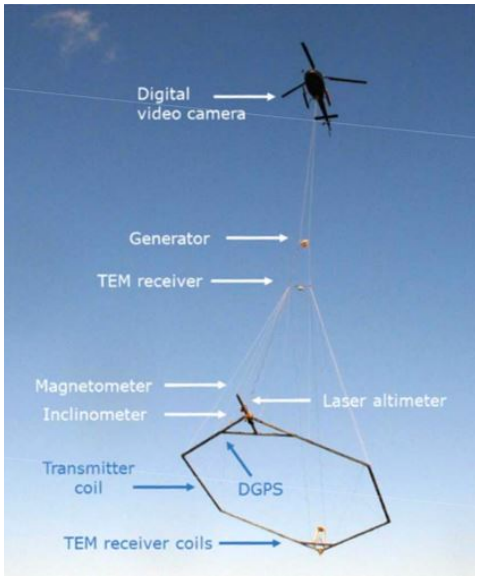
Coil

Measured decay



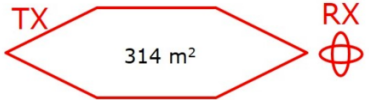
Some Airborne TDEM Systems

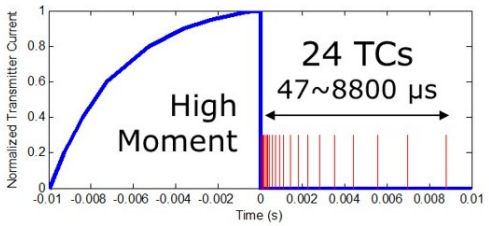
SkyTEM (2006)



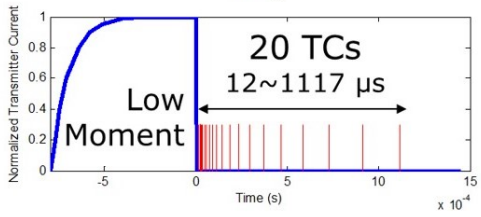
Area = 314 m^2

Peak dipole moment:
- HM: 113040 NIA
- LM: 12560 NIA



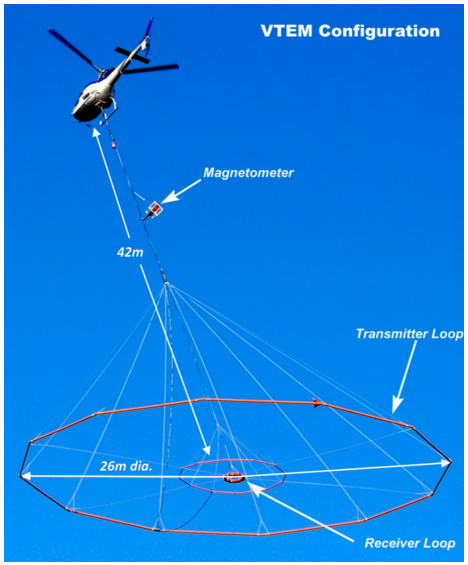


Peak current: 90 A
Turns: 4
On-time: 10 ms
Off-time: 10 ms



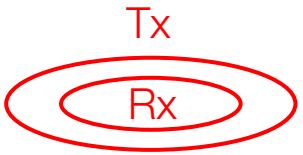
Peak current: 40 A
Turns: 1
On-time: 0.8 ms
Off-time: 1.45 ms

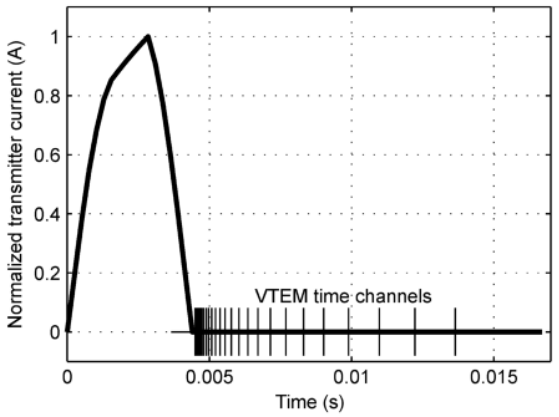
VTEM (2007)



Area = 535 m^2

Peak dipole moment:
- 503,100 NIA





Peak current: 235 A
Turns: 4
On-time: 4.5 ms
Off-time: 9.1 ms

Outline

Setup

Frequency Domain EM

Time Domain EM

- Vertical Magnetic Dipole
- Propagation with Time
- Effects of Background Conductivity
- Transmitters and receivers
- Decay Curves

- Questions

- Case History – Near surface geology

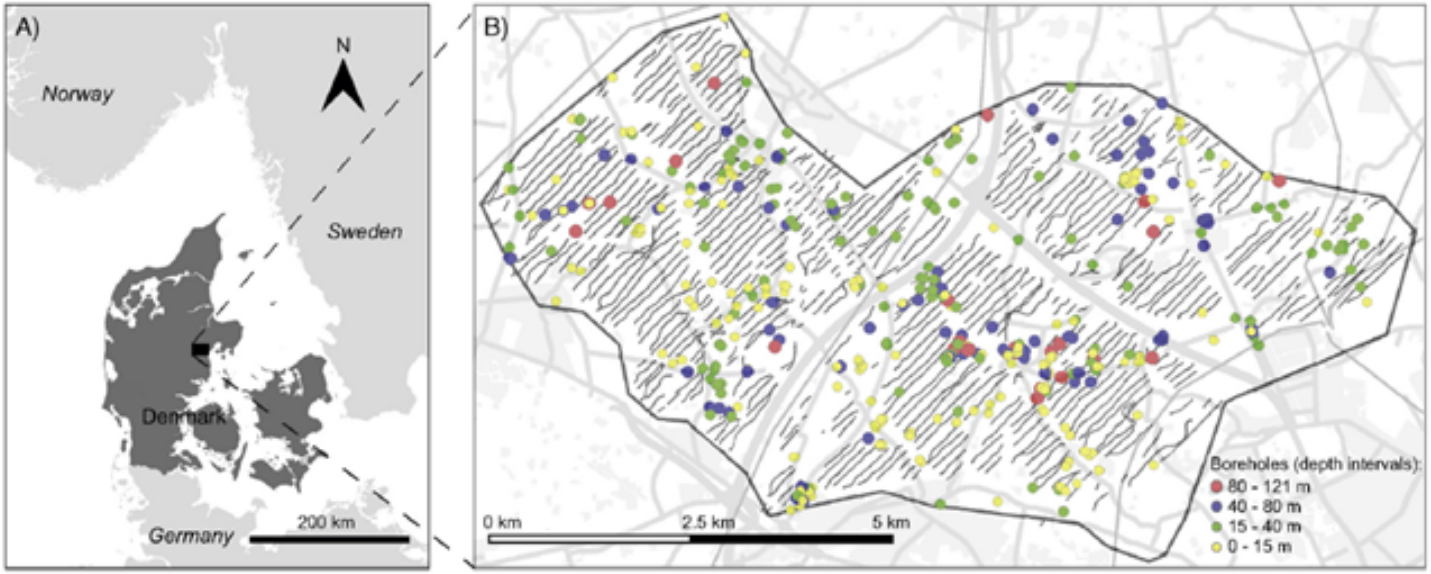
Case History: Kasted

Vilhelmsen et al. (2016)

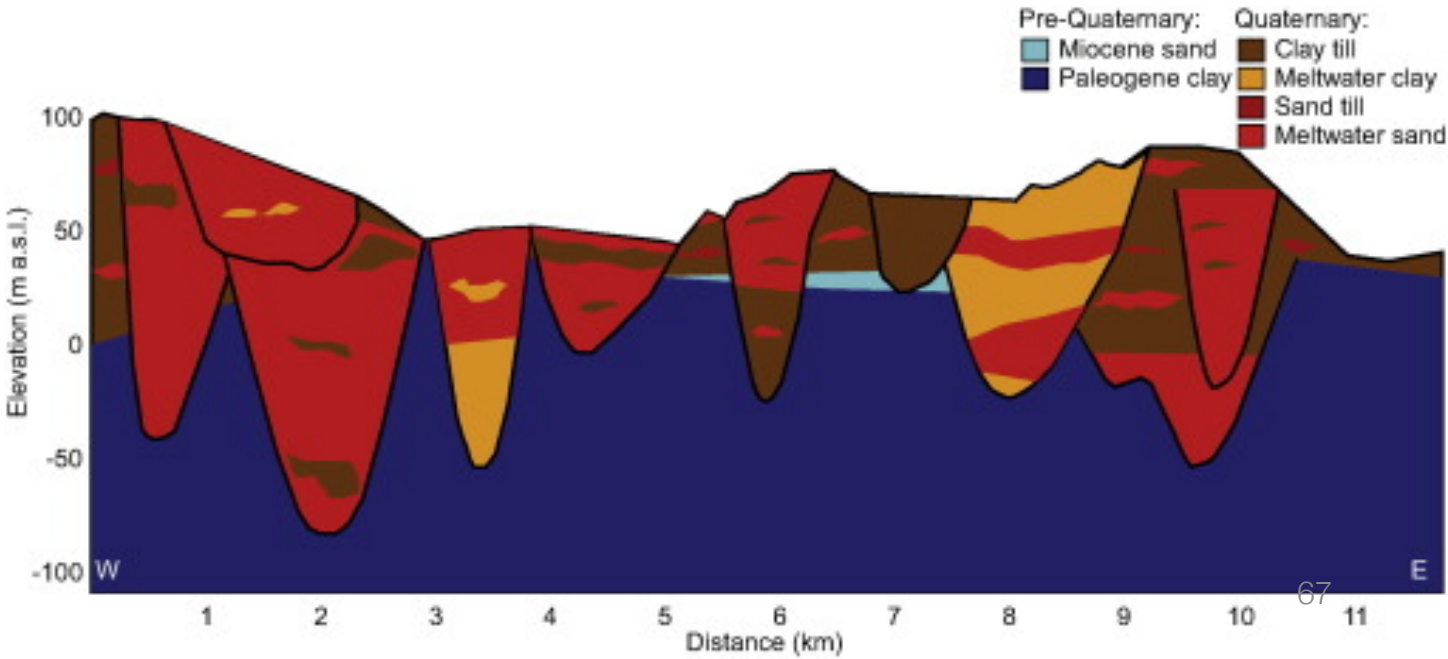
Setup

A) Survey Area: Kasted, Demark

B) Borehole locations

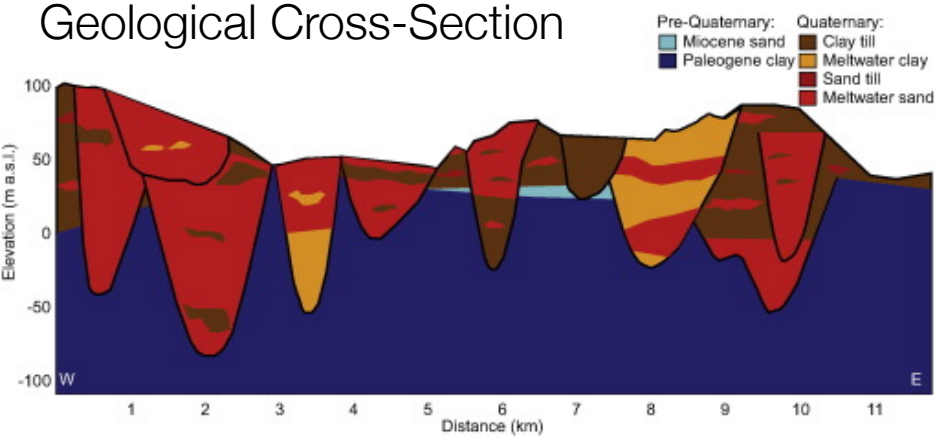


Local Geology: W-E cross-section



Properties

Geological Cross-Section

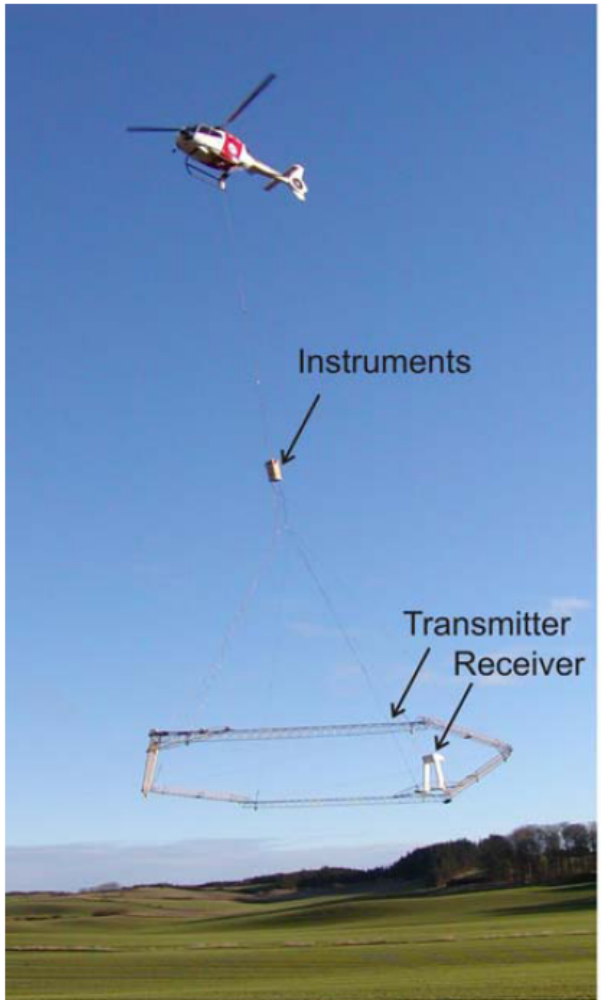


Geological Units	Resistivity (Ωm)
Palaeogene Clay	1-10
Clay Till	25-60
Sand Till	>50
Meltwater Sand and Gravel	>60
Glaciolacustrine Clay	10-40
Miocene Silt and Sand	>40
Miocene Clay	10-40
Sand	>40
Clay	1-60

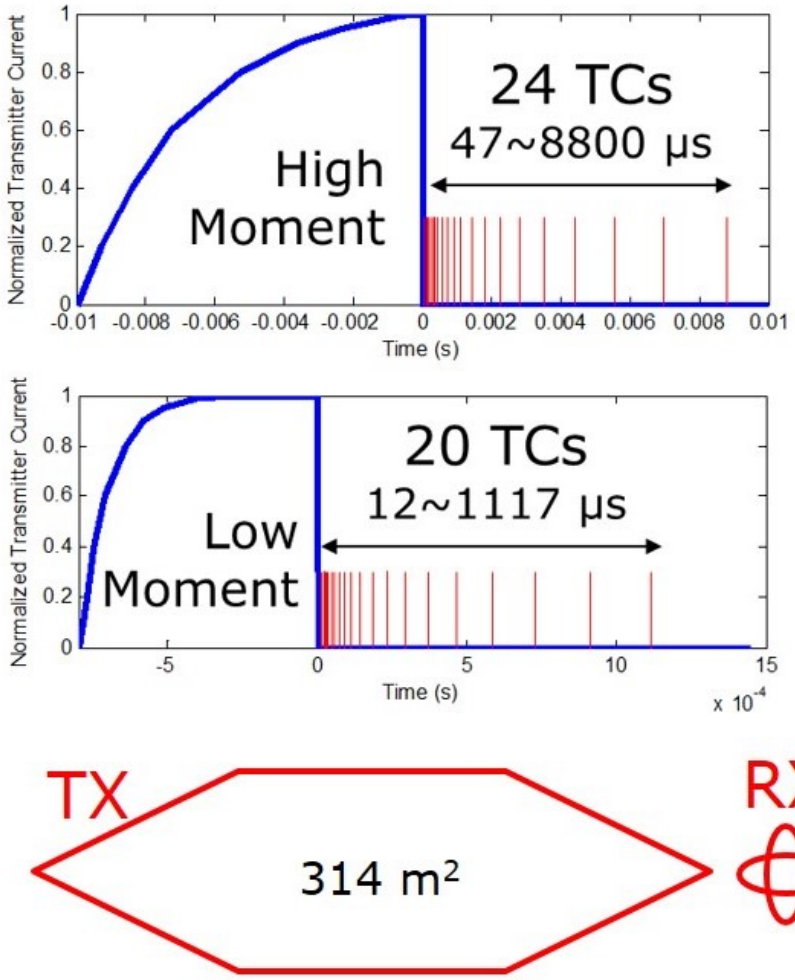
- Buried valleys with clays beneath
- Infill (water-bearing): coarse sand and gravel
- Clays are conductive (1-40 Ωm)
- Water-bearing sands and gravels are more resistive (>40 Ωm)

Survey

SkyTEM System



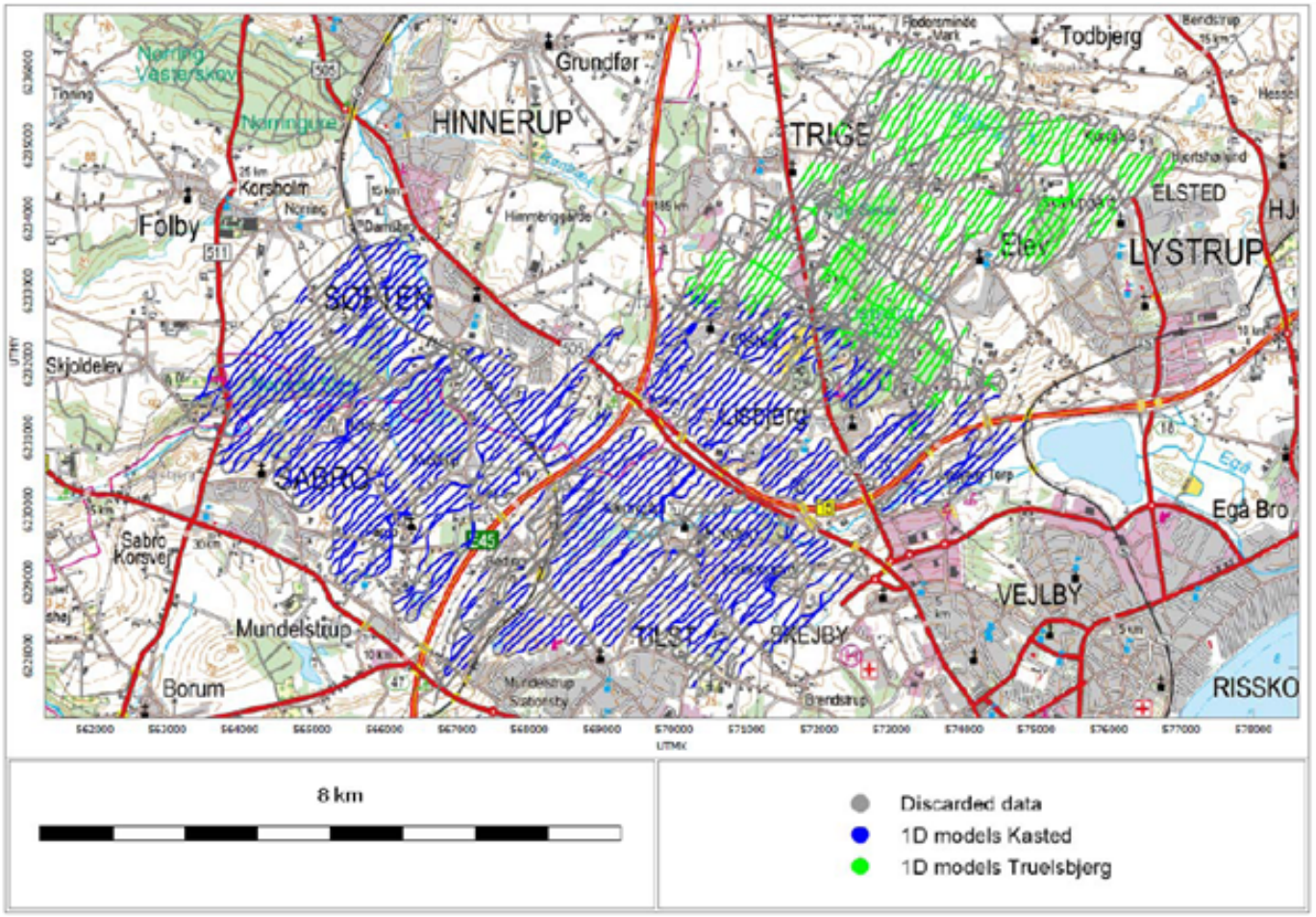
System Configuration



- Low moment (LM) used to image near surface structures
- High moment (HM) used to image deeper structures

Data

Blue: data used for Kasted study

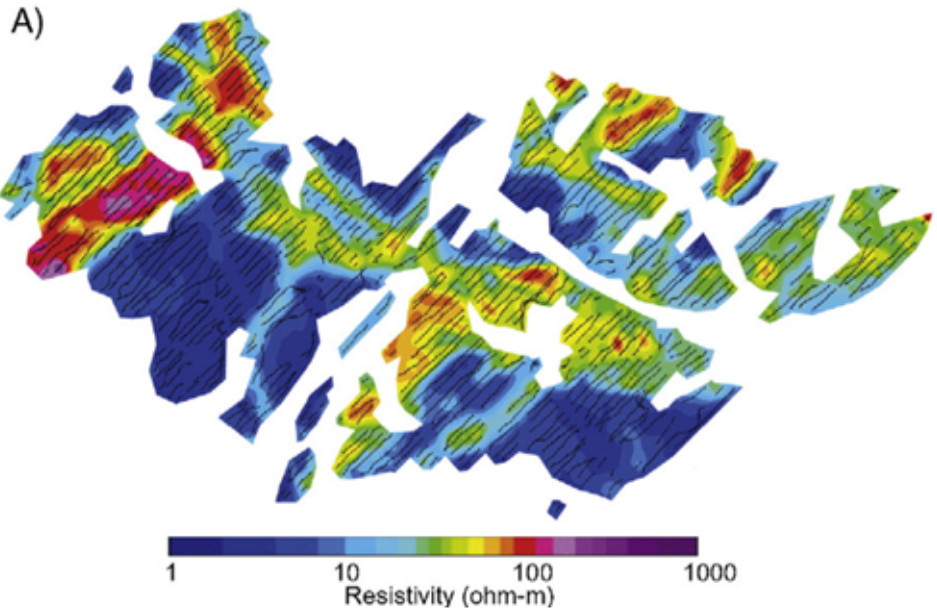


- 333 line km of data, 100 m line-spacing
- Data points with strong coupling to cultural noise were removed (~30%)

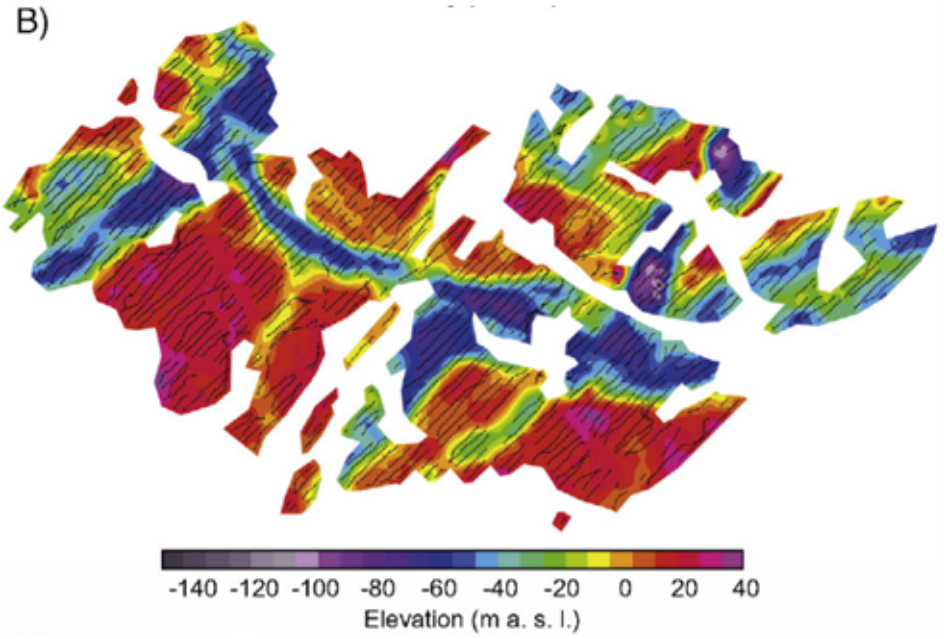
Processing (inversion)

- Spatially constrained 1D inversion → quasi-3D approach
- 9,500 soundings were inverted using 25 layers

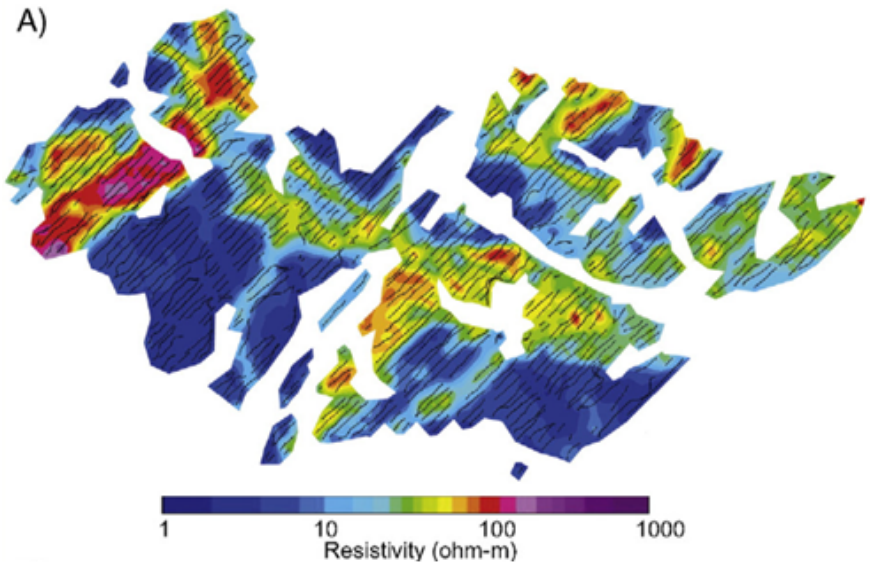
Depth slice 5 m above sea-level

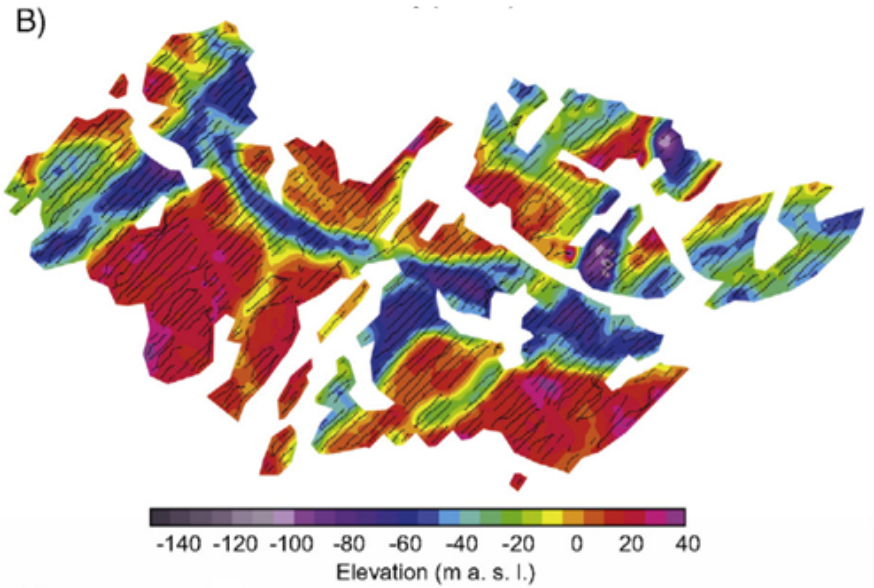


Approximate depth to the top of Paleogene clay layer

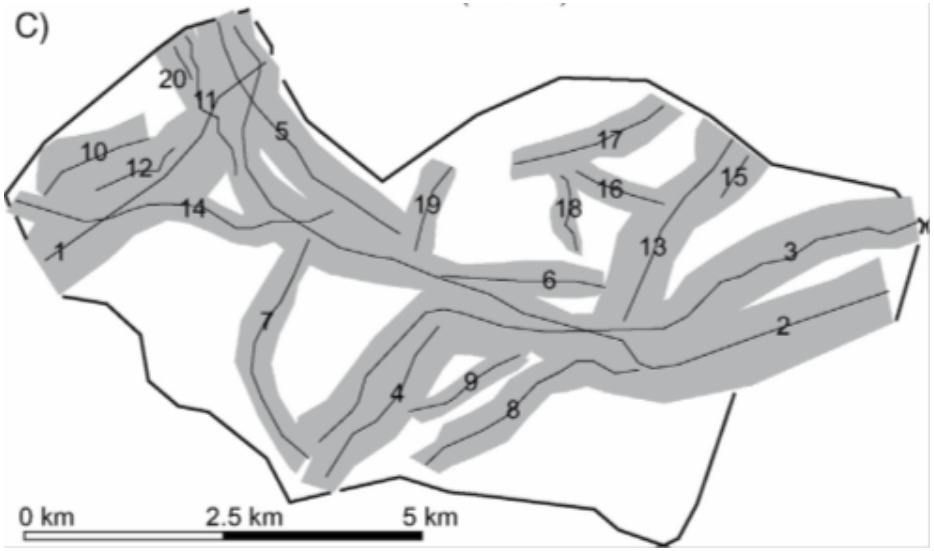


Interpretation



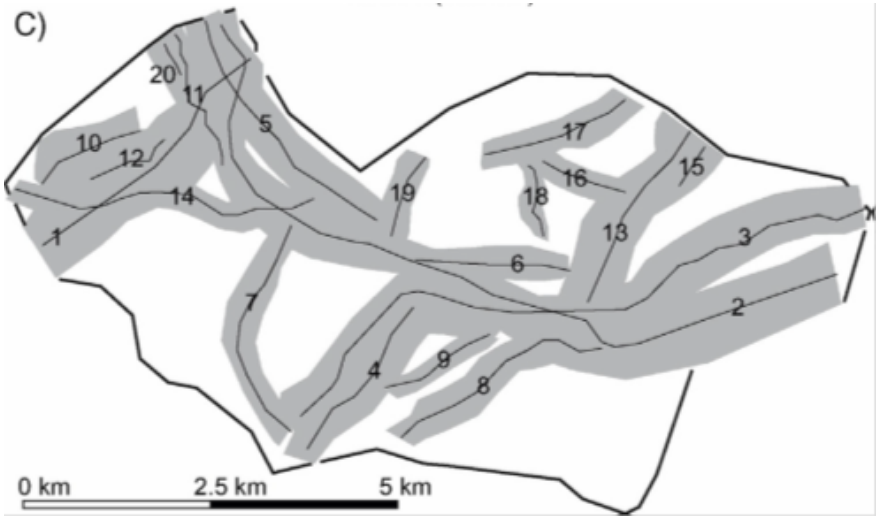


Delineation of valley structures

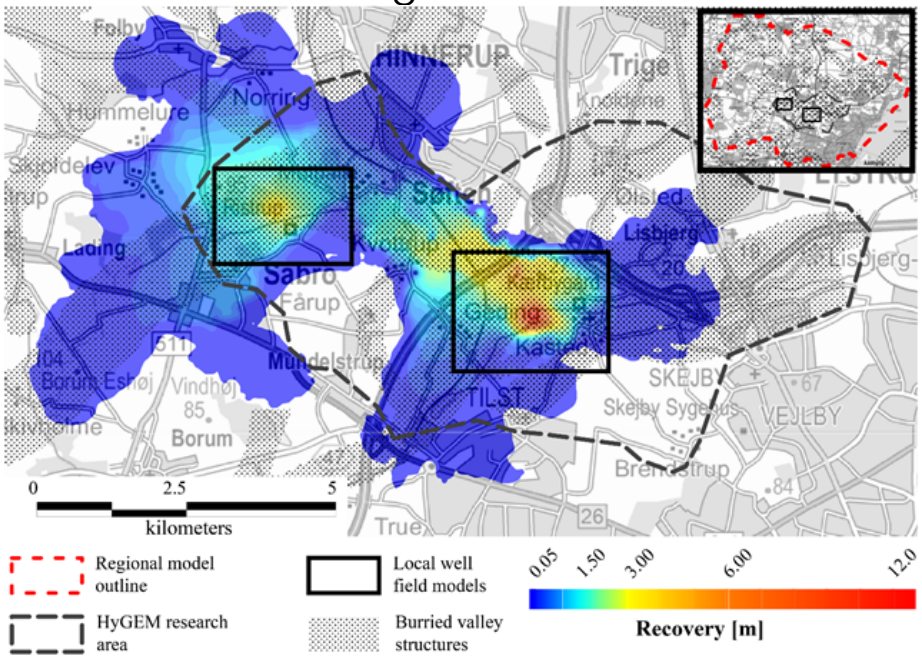


- Inversion results used to construct geological model.
- Delineated 20 buried and cross-cutting valley structures.

Synthesis



MODFLOW-USG groundwater model



- 3D geologic model incorporated into MODFLOW-USG groundwater modeling tool
- Extracted water from 2 wells.
- Downdraw between the two wells correlated with the resistive valley structures

End of Inductive Sources