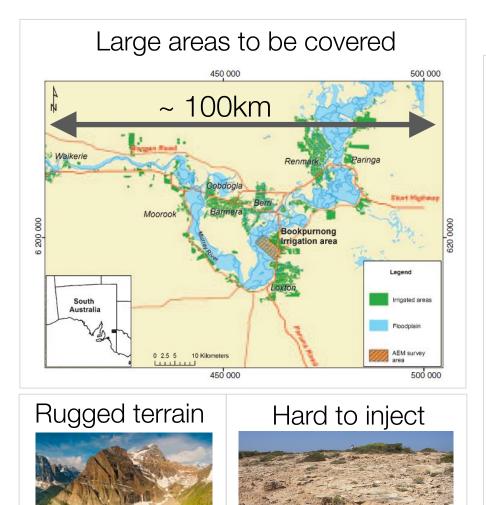
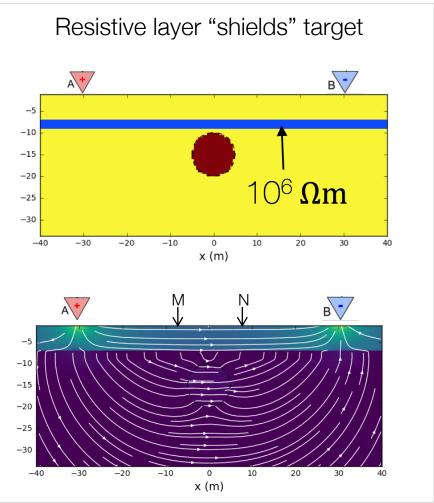
EM Fundamentals





Motivation: applications difficult for DC



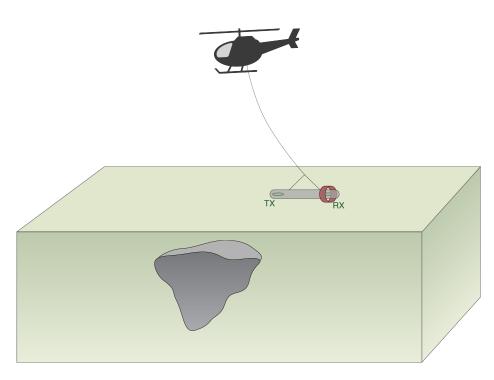


Outline

- Basic Survey
- Ampere's and Faraday's Laws (2-coil App)
- Circuit model for EM induction
- Frequency and time domain data
- Sphere in homogeneous earth
- Cyl code
- Energy losses in the ground

• Setup:

 transmitter and receiver are in a towed bird

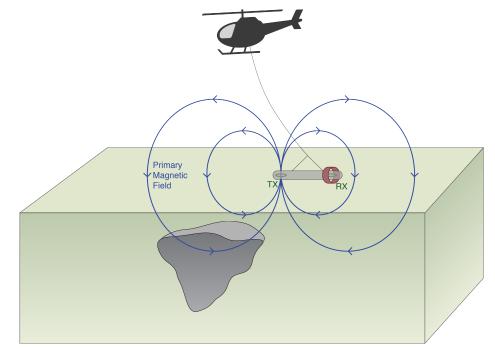


• Setup:

 transmitter and receiver are in a towed bird

• Primary:

 Transmitter produces a primary magnetic field

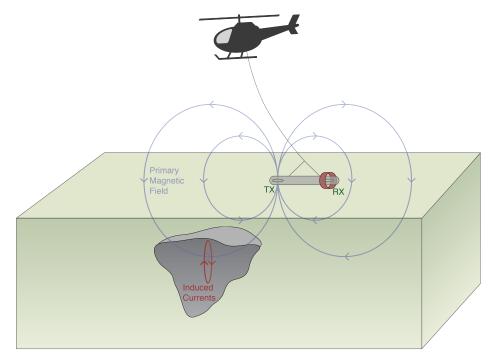


• Setup:

- transmitter and receiver are in a towed bird
- Primary:
 - Transmitter produces a primary magnetic field

Induced Currents:

 Time varying magnetic fields generate electric fields everywhere and currents in conductors



• Setup:

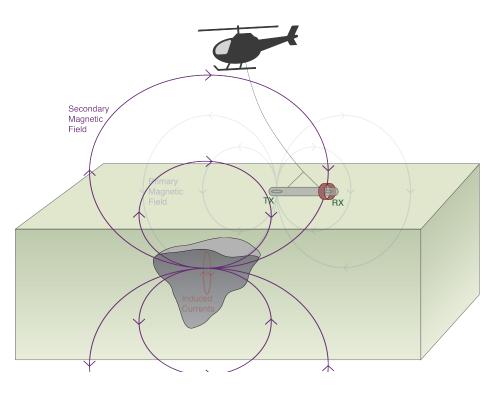
- transmitter and receiver are in a towed bird
- Primary:
 - Transmitter produces a primary magnetic field

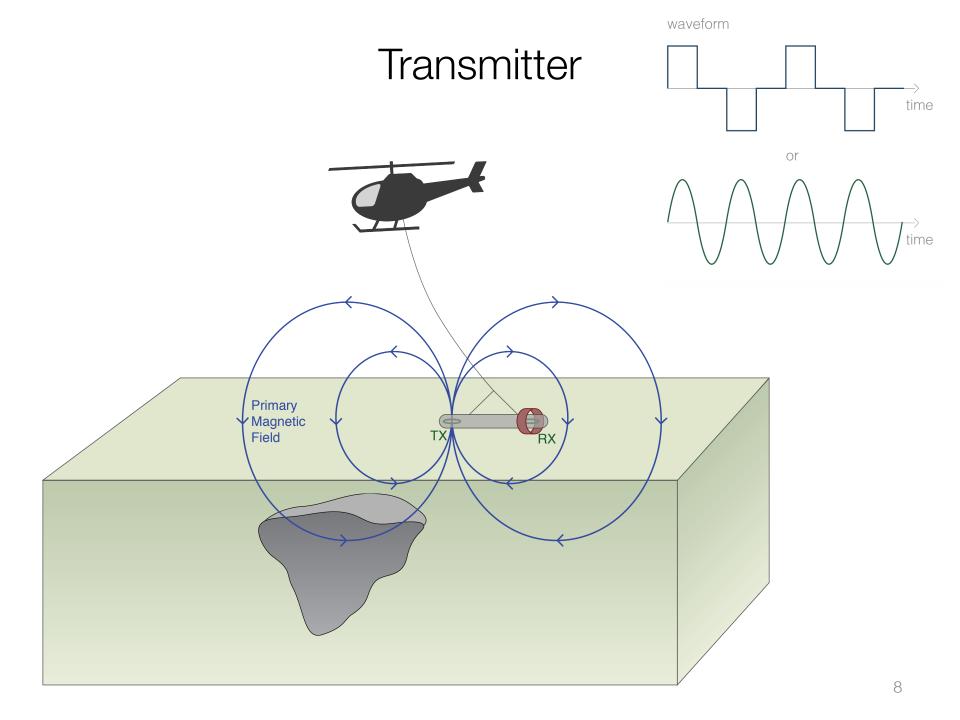
Induced Currents:

 Time varying magnetic fields generate electric fields everywhere and currents in conductors

Secondary Fields:

 The induced currents produce a secondary magnetic field.



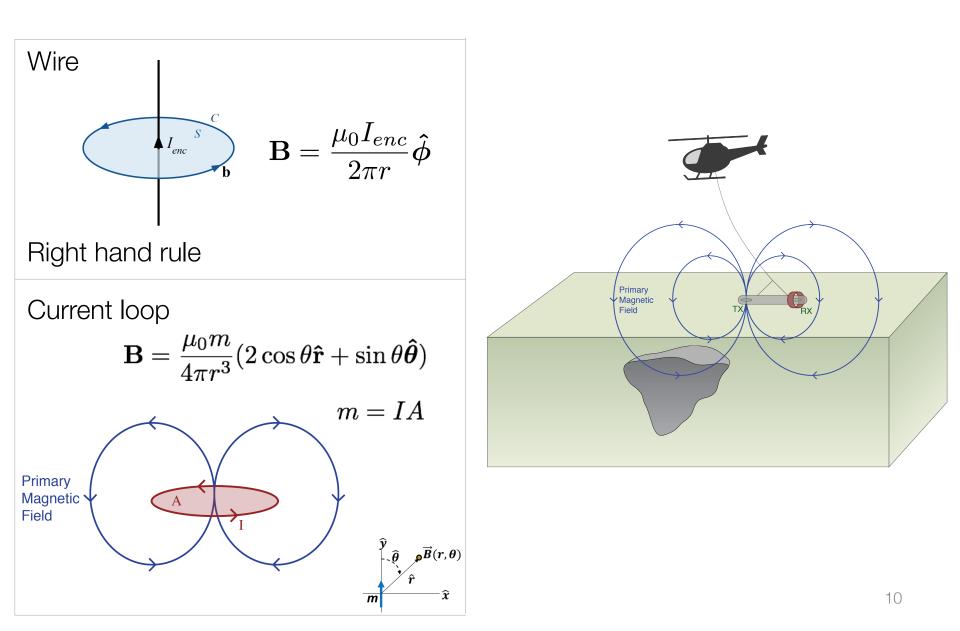


Basic Equations: Quasi-static

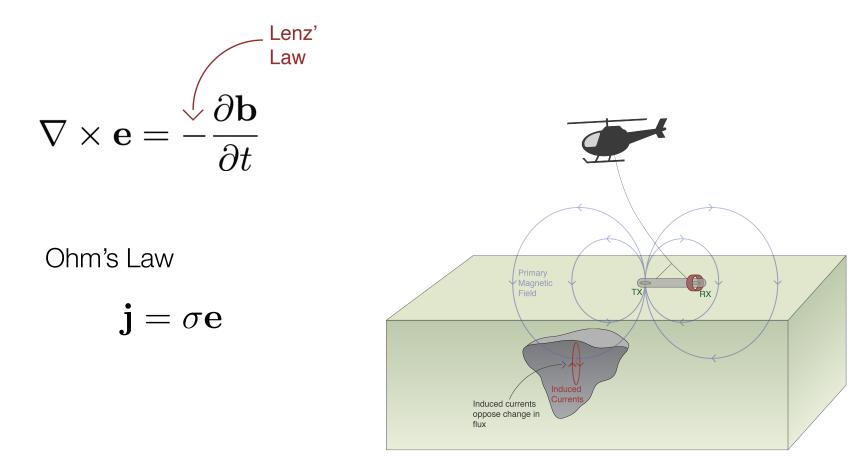
	Time	Frequency
Faraday's Law	$\nabla \times \mathbf{e} = -\frac{\partial \mathbf{b}}{\partial t}$	$ abla imes {f E} = -i\omega {f B}$
Ampere's Law	$ abla imes \mathbf{h} = \mathbf{j} + rac{\partial \mathbf{d}}{\partial t}$	$ abla imes \mathbf{H} = \mathbf{J} + i\omega \mathbf{D}$
No Magnetic Monopoles	$\nabla \cdot \mathbf{b} = 0$	$\nabla \cdot \mathbf{B} = 0$
Constitutive Relationships (non-dispersive)	$\mathbf{j} = \sigma \mathbf{e}$ $\mathbf{b} = \mu \mathbf{h}$ $\mathbf{d} = \varepsilon \mathbf{e}$	$egin{array}{llllllllllllllllllllllllllllllllllll$

* Solve with sources and boundary conditions

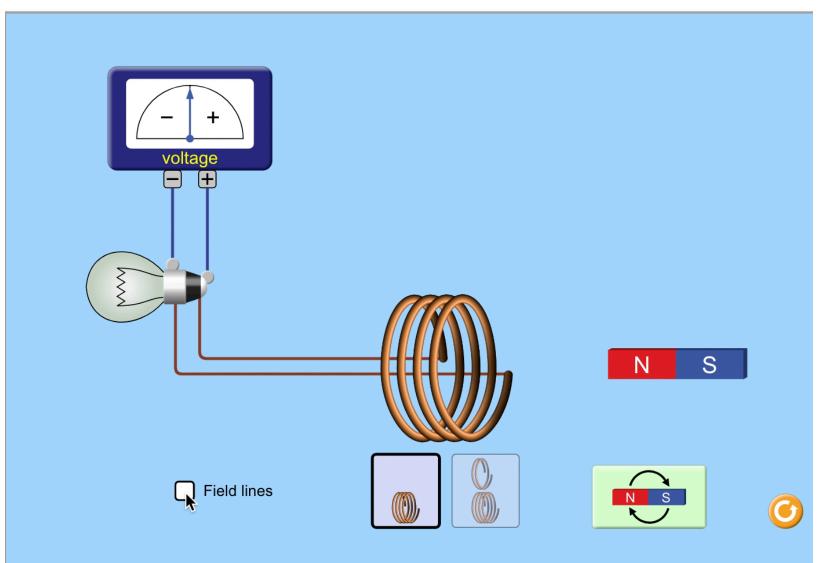
Ampere's Law $\nabla \times \mathbf{H} = \mathbf{J}$



Faraday's Law



Faraday's Law



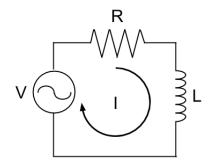


Magnetic Flux

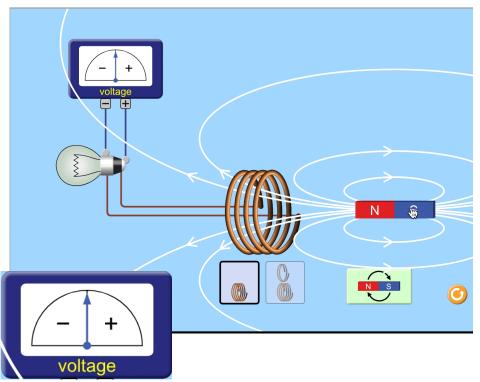
$$\phi_{\mathbf{b}} = \int_{A} \mathbf{b} \cdot \hat{\mathbf{n}} \, da$$

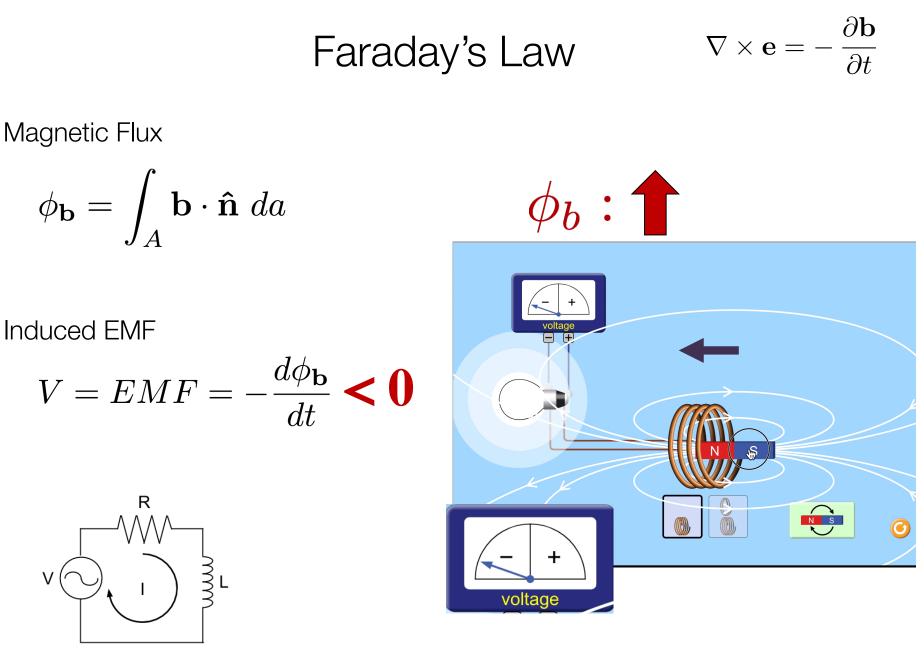
Induced EMF

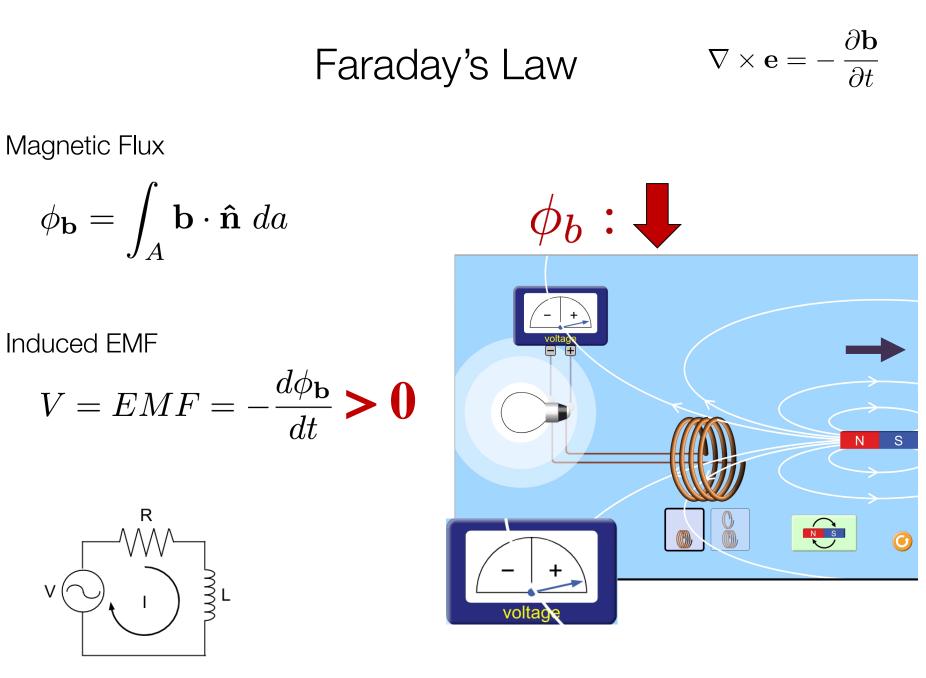
$$V = EMF = -\frac{d\phi_{\mathbf{b}}}{dt} = \mathbf{0}$$



ϕ_b : constant



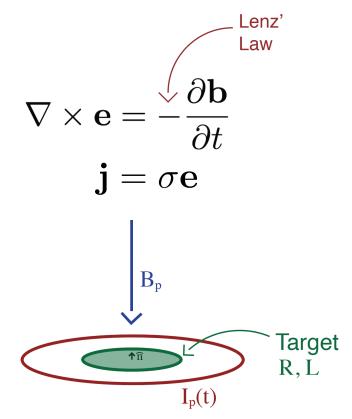


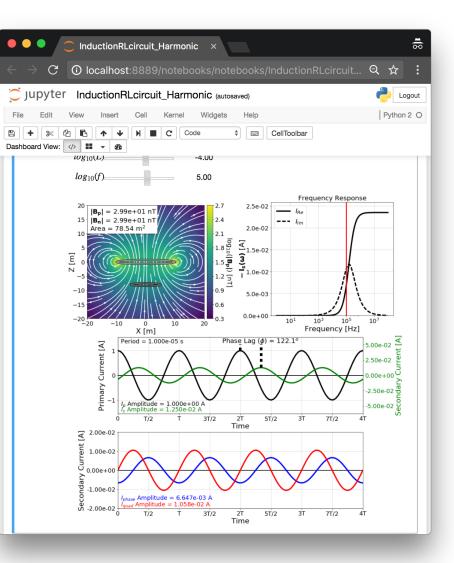


App for Faraday's Law

2 Apps:

- Harmonic
- Transient

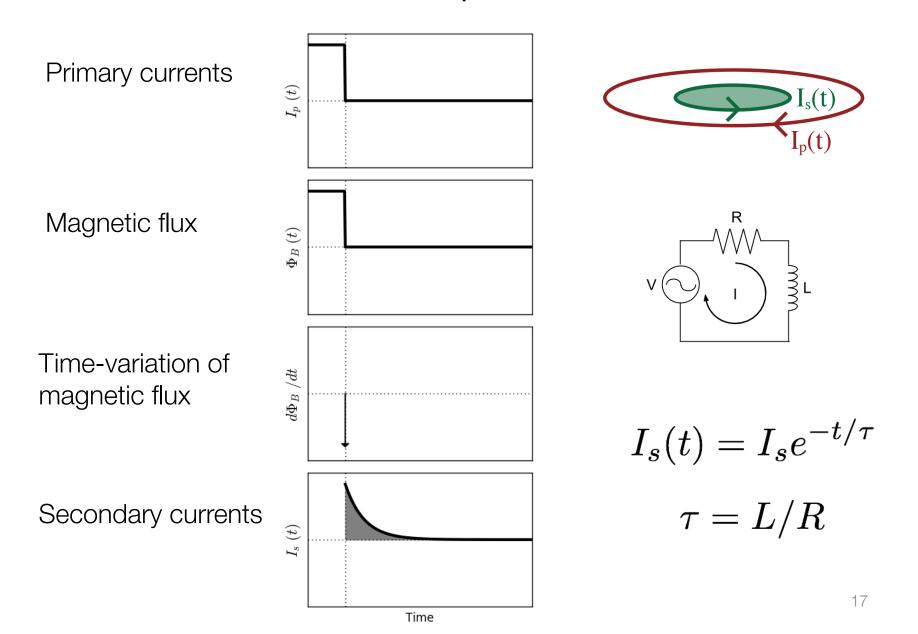




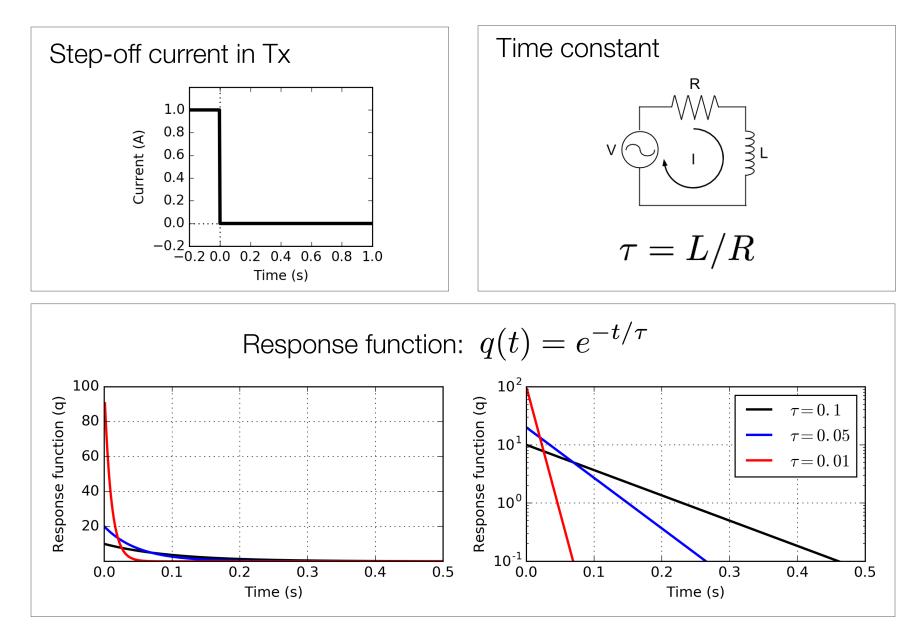
http://em.geosci.xyz/apps.html

Two Coil Example: Transient

TDEM



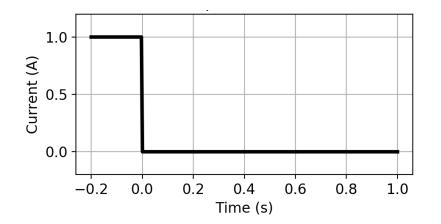
Response Function: Transient

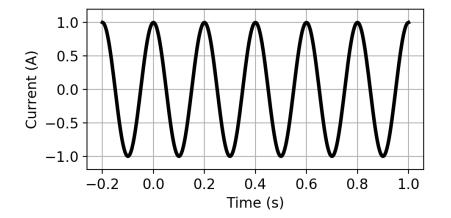


Transient and Harmonic Signals

We have seen a transient pulse...

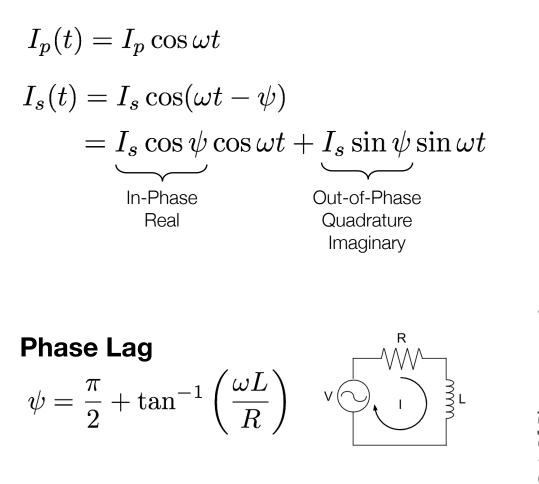
What happens when he have a harmonic?

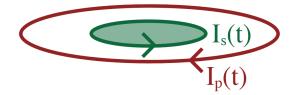


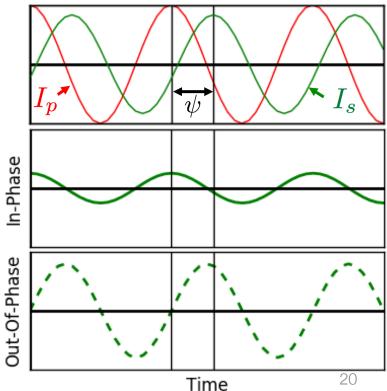


Two Coil Example: Harmonic

Induced Currents

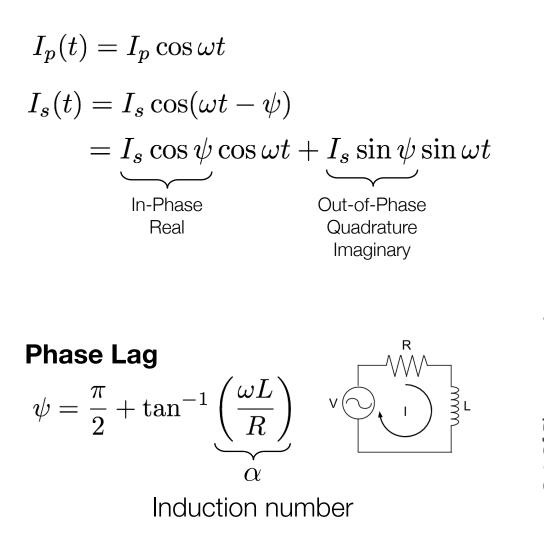


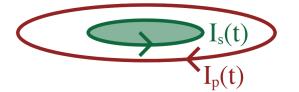


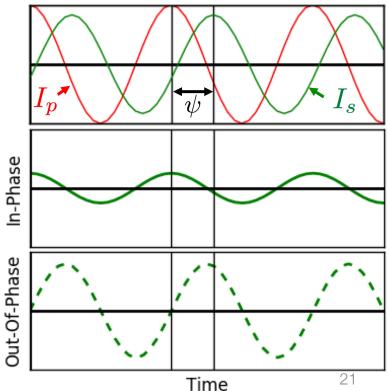


Two Coil Example: Harmonic

Induced Currents

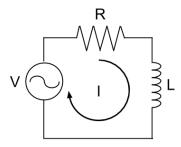


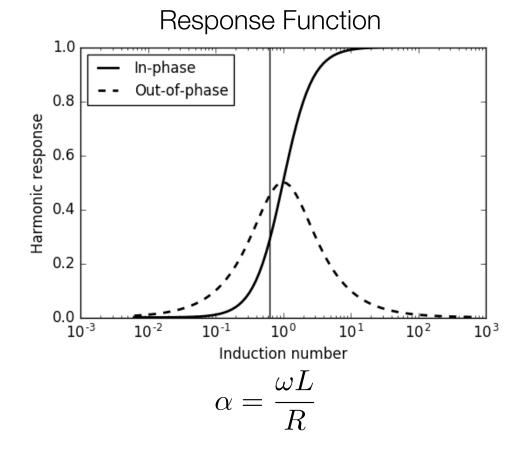


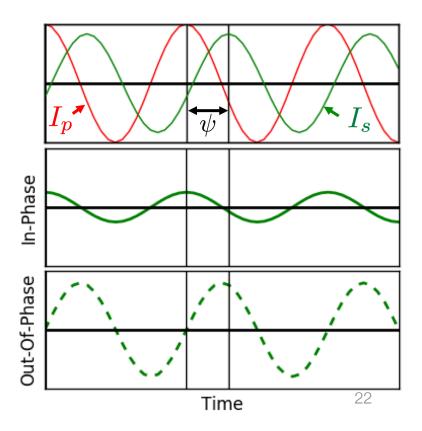


Response Function

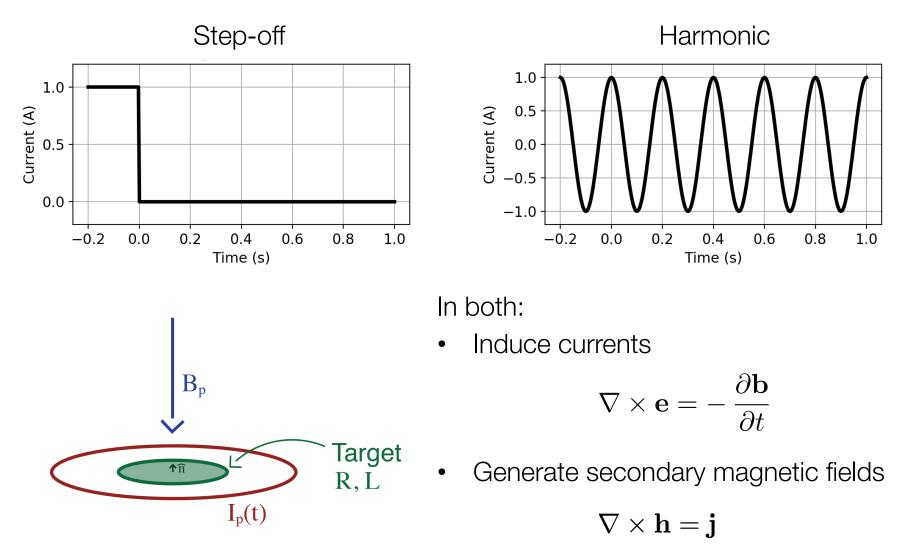
- Quantifies how a target responds to a time varying magnetic field
- Partitions real and imaginary parts





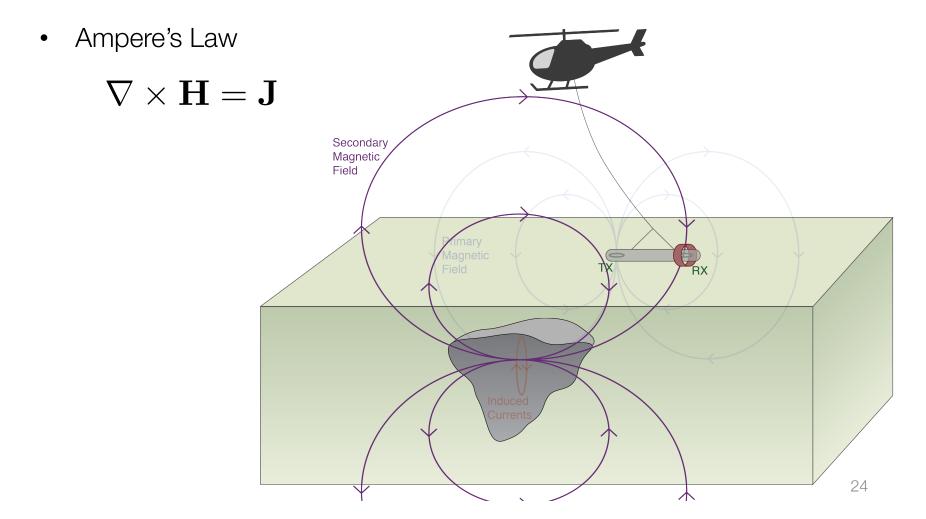


Response Functions: Summary

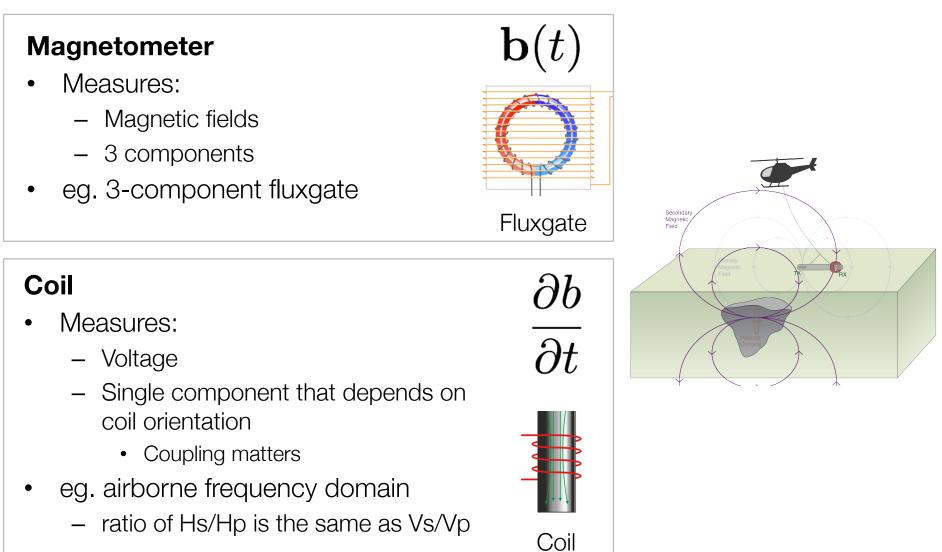


Secondary magnetic fields

Induced currents generate magnetic fields



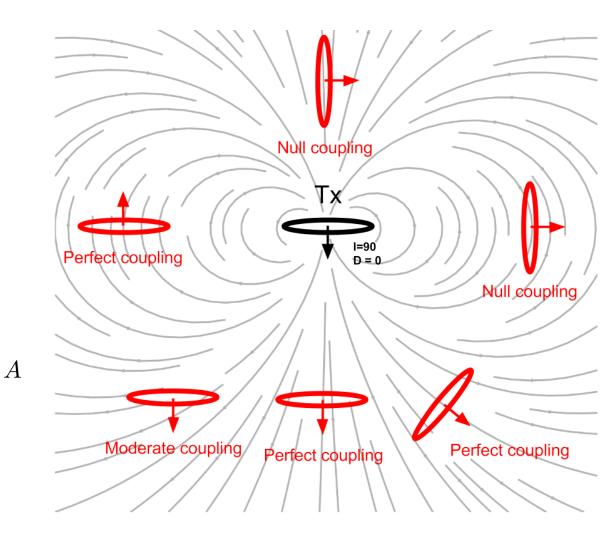
Receiver and Data



Coupling

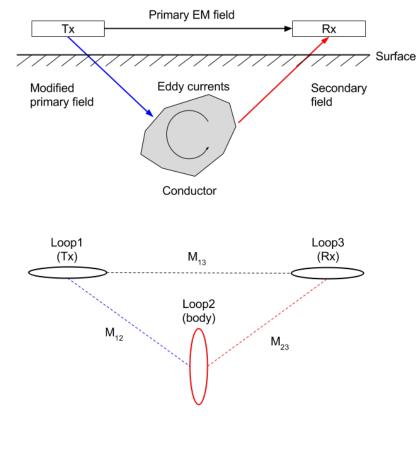
- Transmitter: Primary $I_p(t) = I_p \cos(\omega t)$ $\mathbf{B}_p(t) \sim I_p \cos(\omega t)$
- Target: Secondary

$$EMF = -\frac{\partial \phi_{\mathbf{B}}}{\partial t}$$
$$= -\frac{\partial}{\partial t} \left(\mathbf{B}_{p} \cdot \hat{\mathbf{n}} \right)$$





Circuit model of EM induction



Coupling coefficient

Depends on geometry

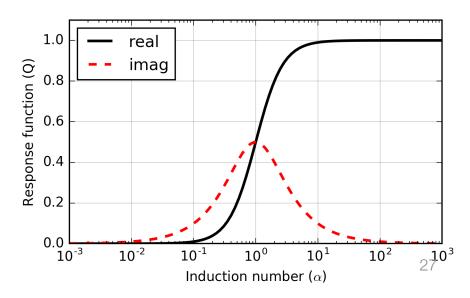
$$M_{12} = \frac{\mu_0}{4\pi} \oint \oint \frac{dl_1 \cdot dl_2}{|\mathbf{r} - \mathbf{r}'|^2}.$$

Magnetic field at the receiver

$$\frac{H^s}{H^p} = -\frac{M_{12}M_{23}}{M_{13}L} \underbrace{\left[\frac{\alpha^2 + i\alpha}{1 + \alpha^2}\right]}_Q$$

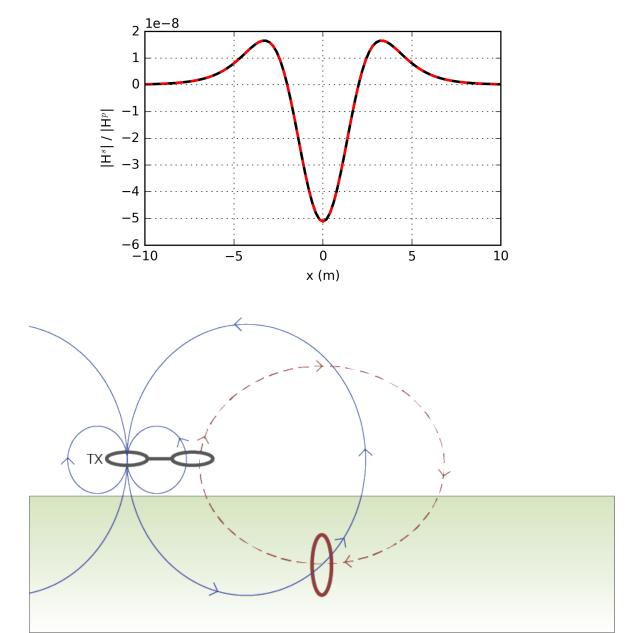
Induction Number

• Depends on properties $\alpha = \frac{\omega L}{R}$ of target

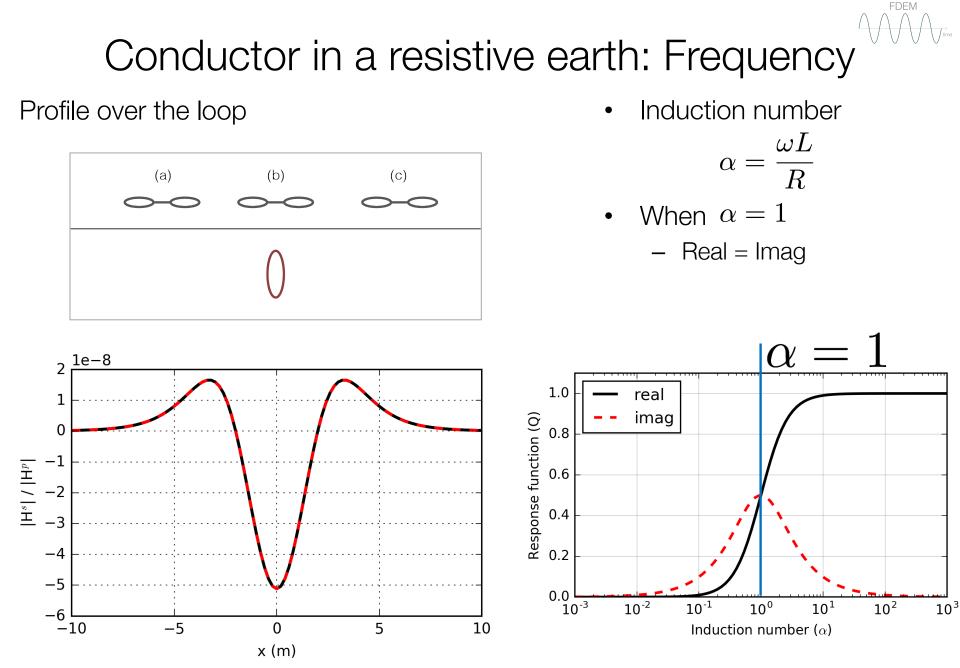


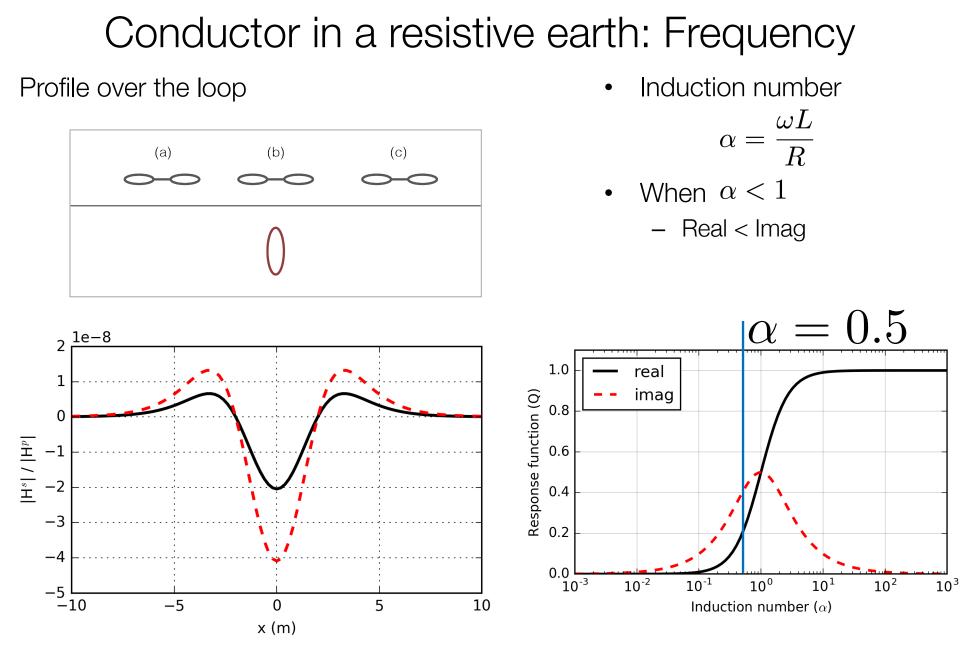


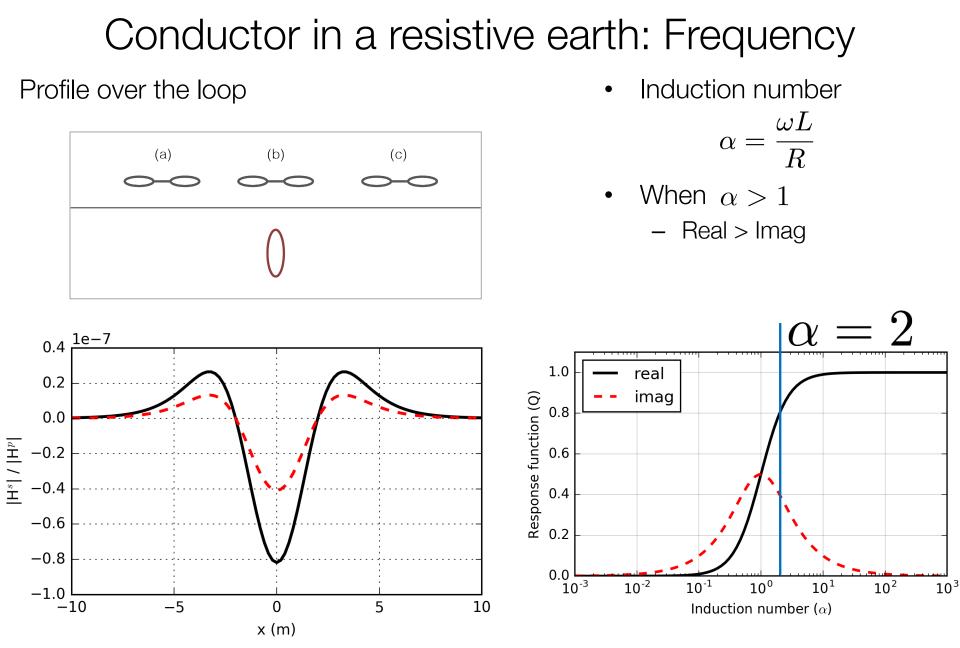
Circuit model of EM induction



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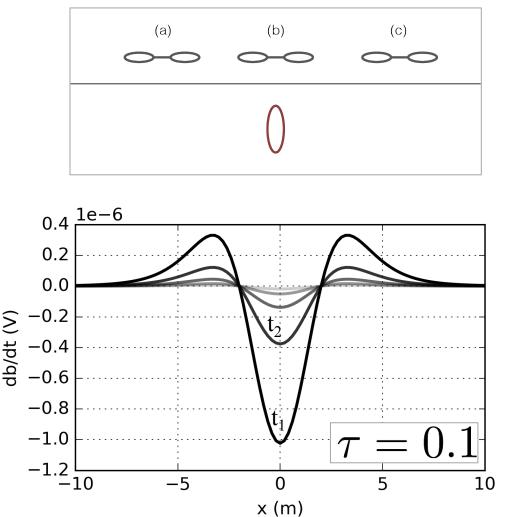






Conductor in a resistive earth: Transient

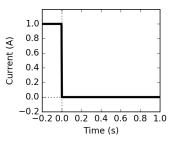
Profile over the loop



• Time constant

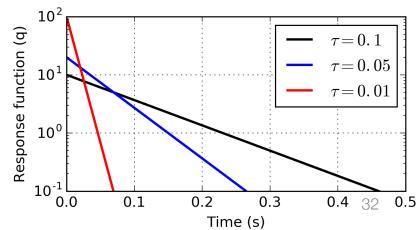
 $\tau = L/R$

• Step-off current in Tx



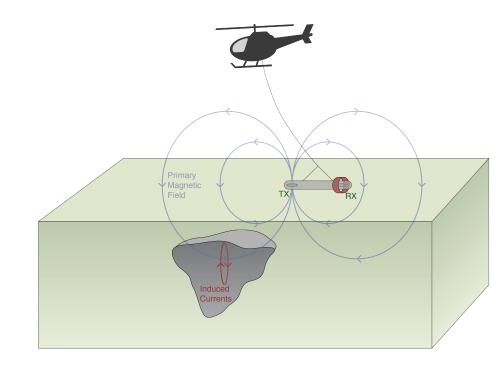
- Response function depends on time, au

$$q(t) = e^{-t/\tau}$$



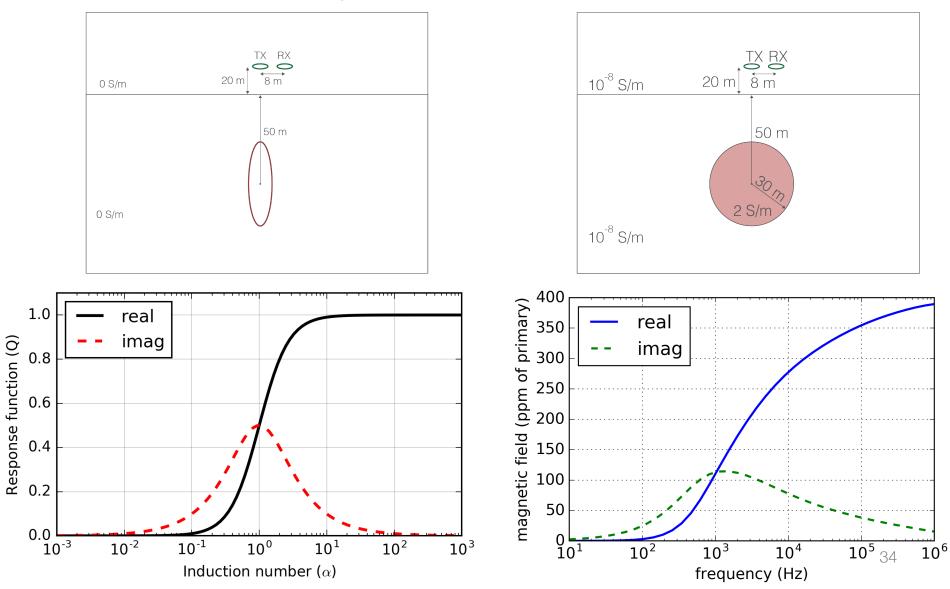
Recap: what have we learned?

- Basics of EM induction
- Response functions
- Mutual coupling
- Data for frequency or time
 domain systems
- Circuit model provides
 representative results
 - Applicable to geologic targets?



Sphere in a resistive background

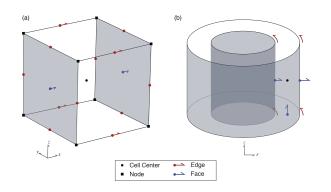
How representative is a circuit model?



Cyl Code

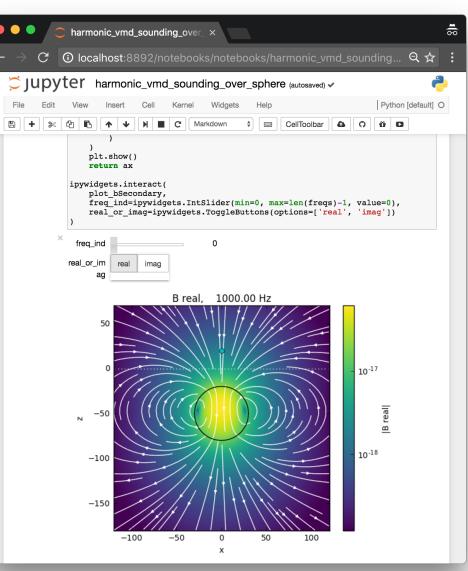


- Finite Volume EM
 - Frequency and Time



- Built on SimPEG
- Open source, available at: <u>http://em.geosci.xyz/apps.html</u>
- Papers

<u>Cockett et al, 2015</u> <u>Heagy et al, 2017</u>

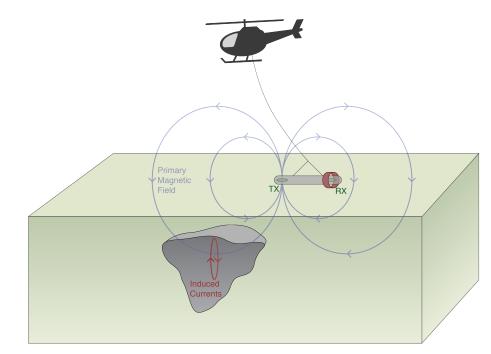


Recap: what have we learned?

- Basics of EM induction
- Response functions
- Mutual coupling
- Data for frequency or time domain systems
- Circuit model is a good proxy
- 2-Coil Apps
- Frequency domain
- Time domain

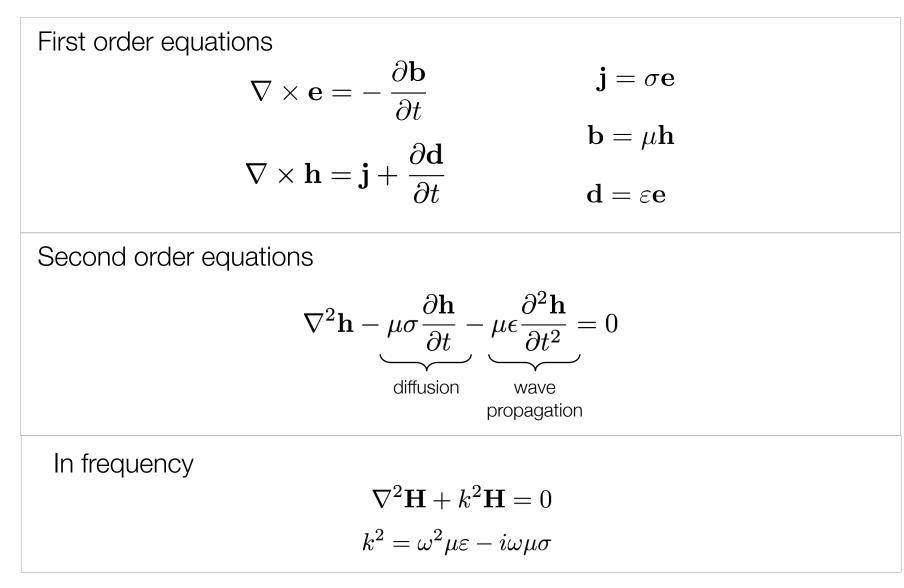
Major item not yet accounted for...

- Propagation of energy from
 - Transmitter to target
 - Target to receiver

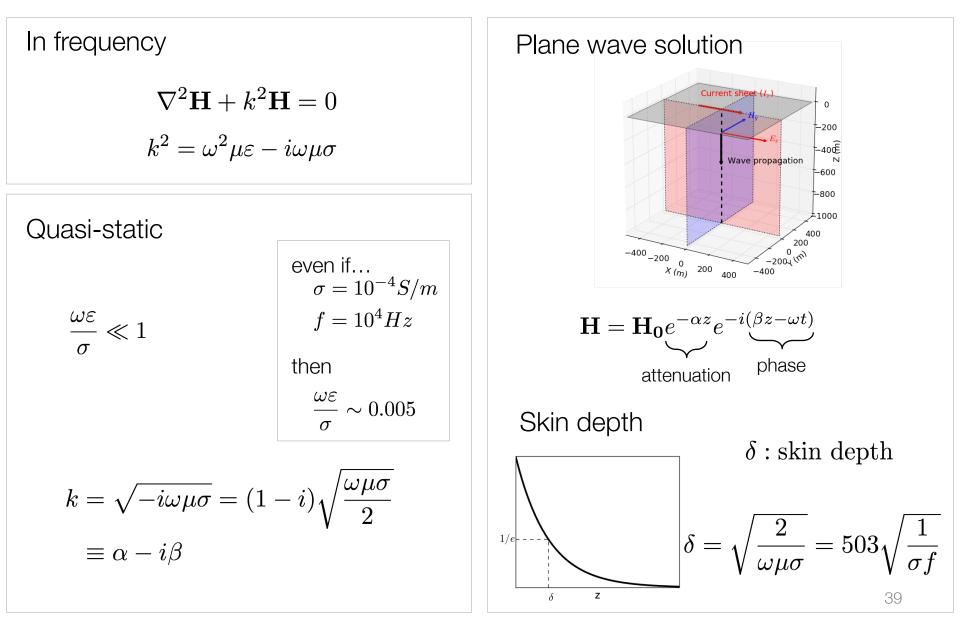


How do EM fields and fluxes behave in a conductive background?

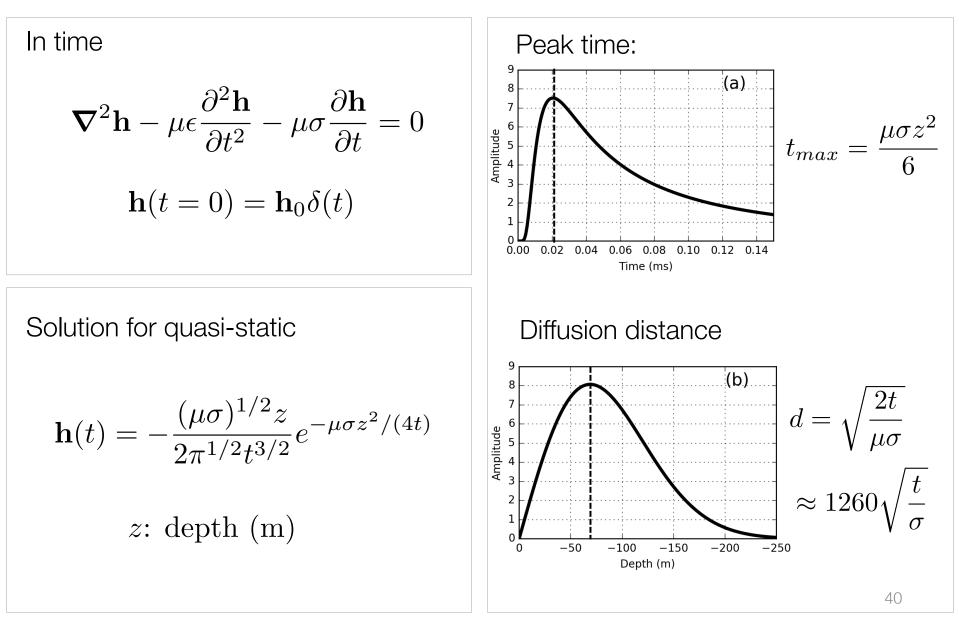
Revisit Maxwell's equations



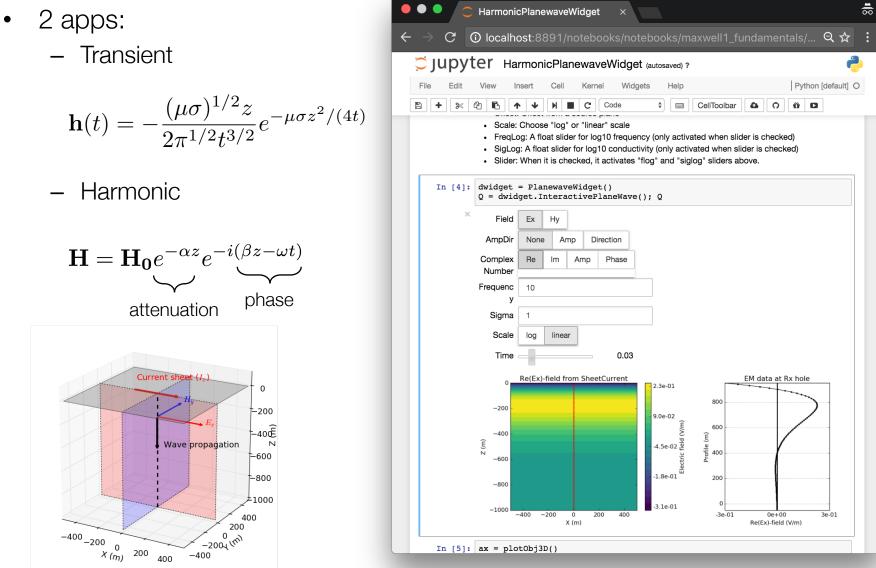
Plane waves in a homogeneous media



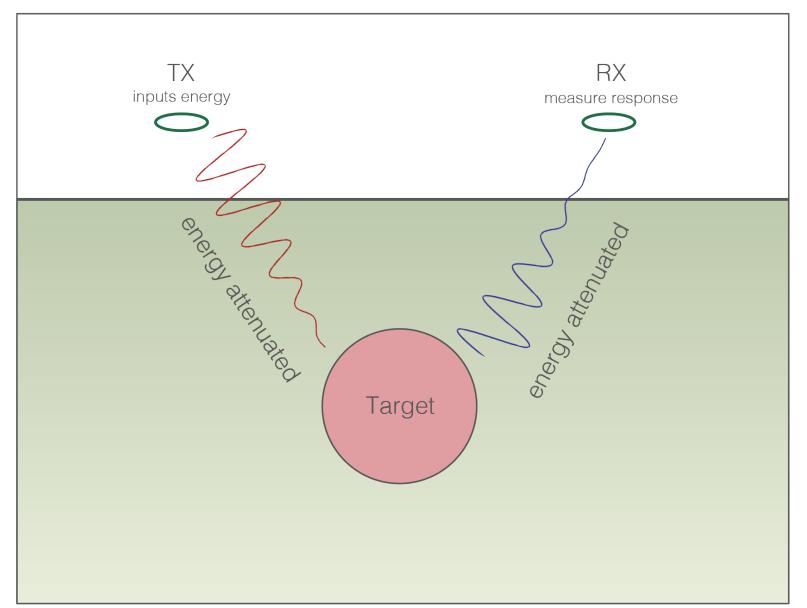
Plane waves in a homogeneous media



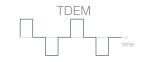
Plane Wave apps

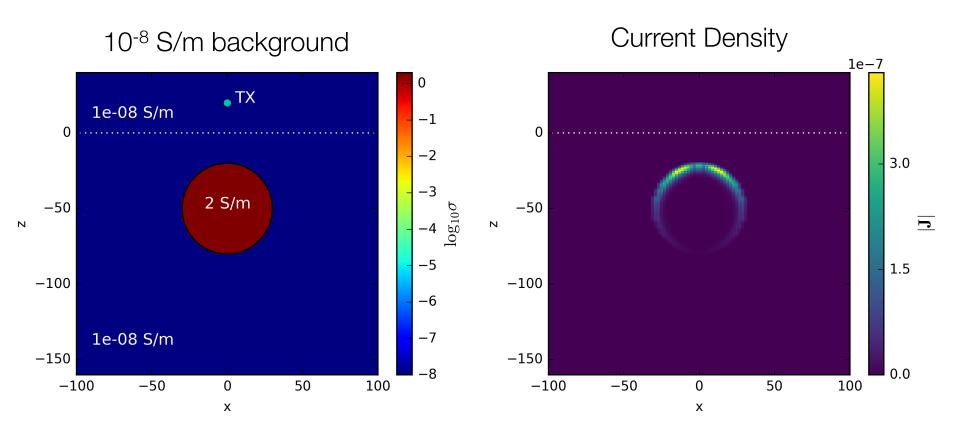


http://em.geosci.xyz/apps.html

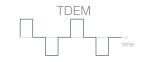


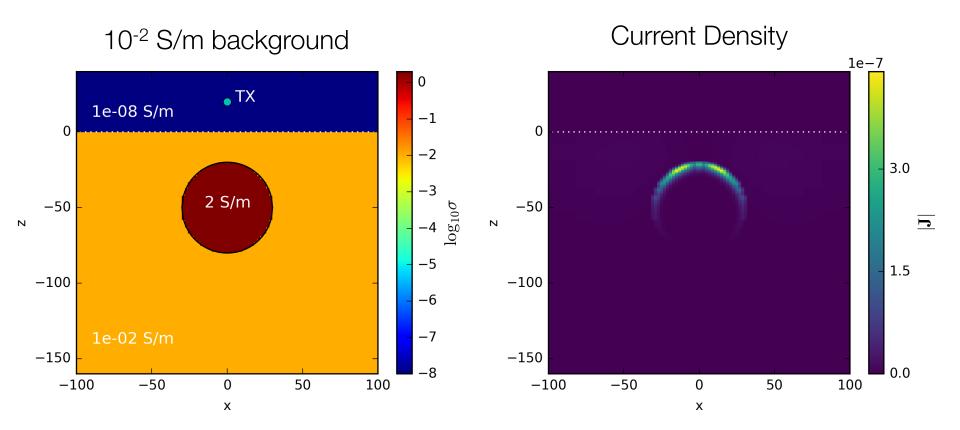
- Buried, conductive sphere
- Vary background conductivity
- Time: 10⁻⁵ s



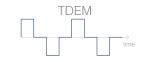


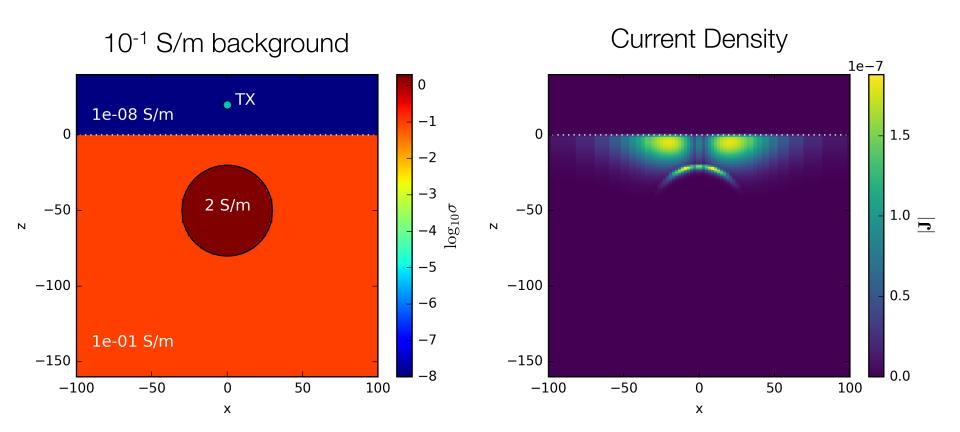
- Buried, conductive sphere
- Vary background conductivity
- Time: 10⁻⁵ s



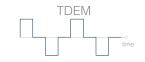


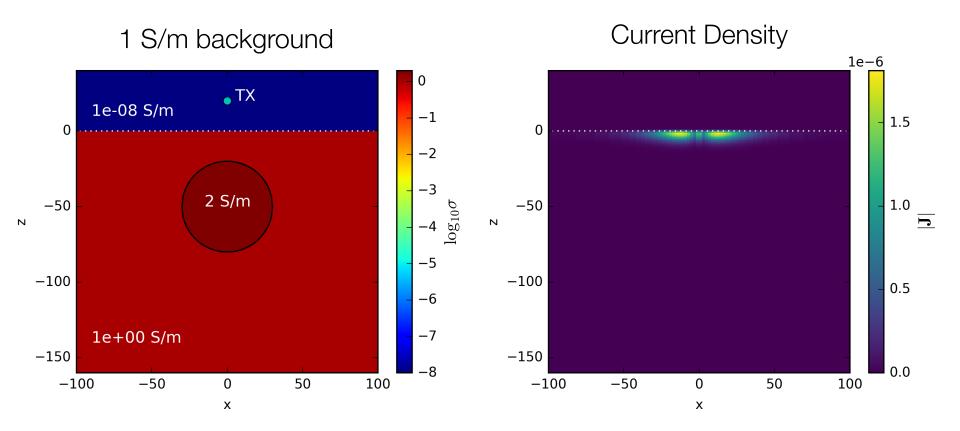
- Buried, conductive sphere
- Vary background conductivity
- Time: 10⁻⁵ s

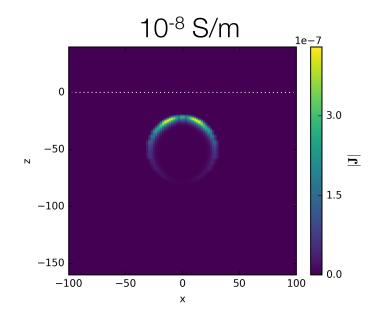




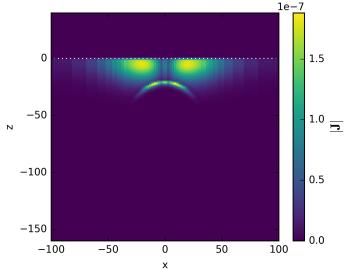
- Buried, conductive sphere
- Vary background conductivity
- Time: 10⁻⁵ s

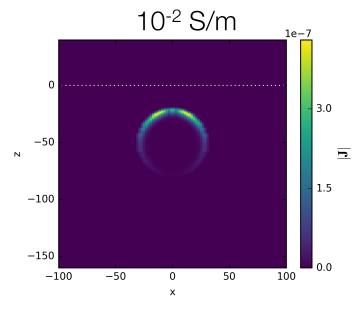




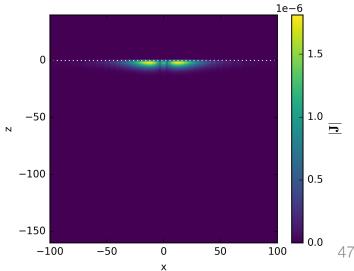


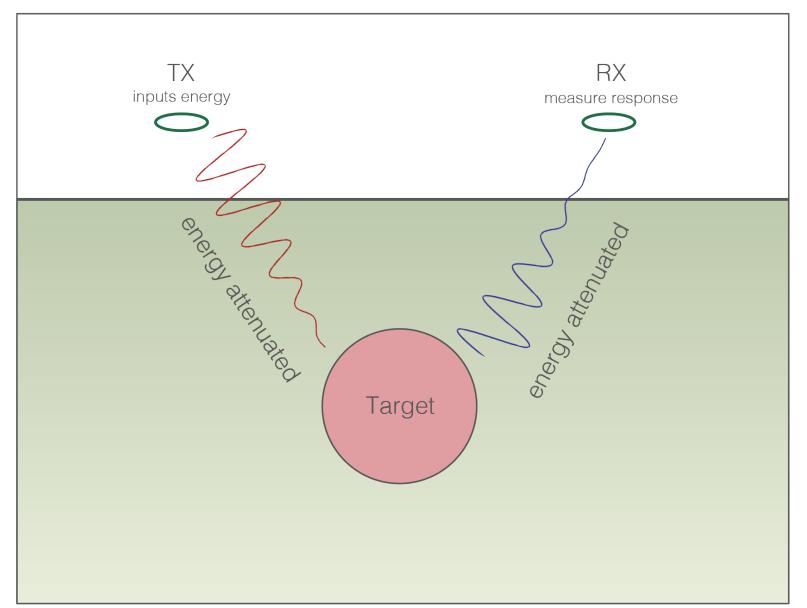




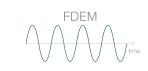


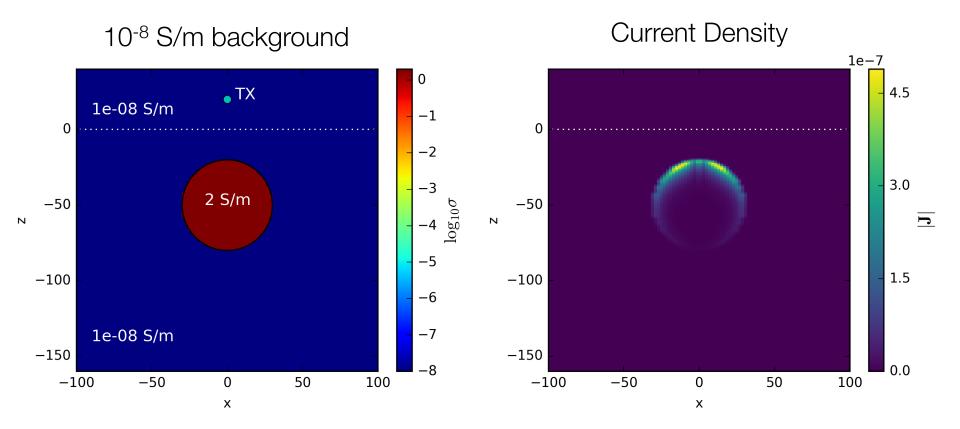






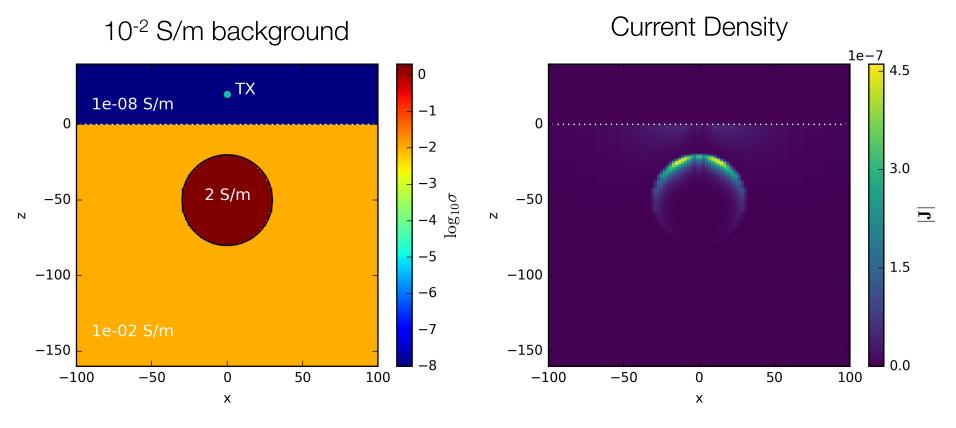
- Buried, conductive sphere
- Vary background conductivity
- Frequency: 10⁴ Hz





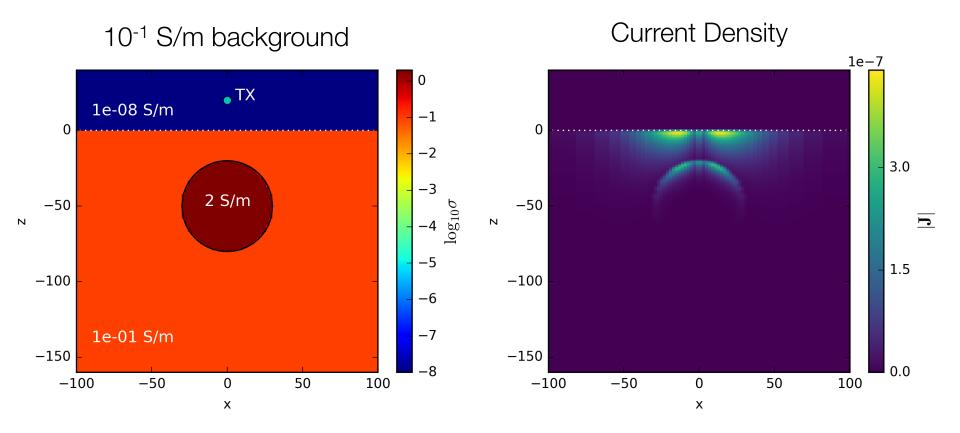
- Buried, conductive sphere
- Vary background conductivity
- Frequency: 10⁴ Hz





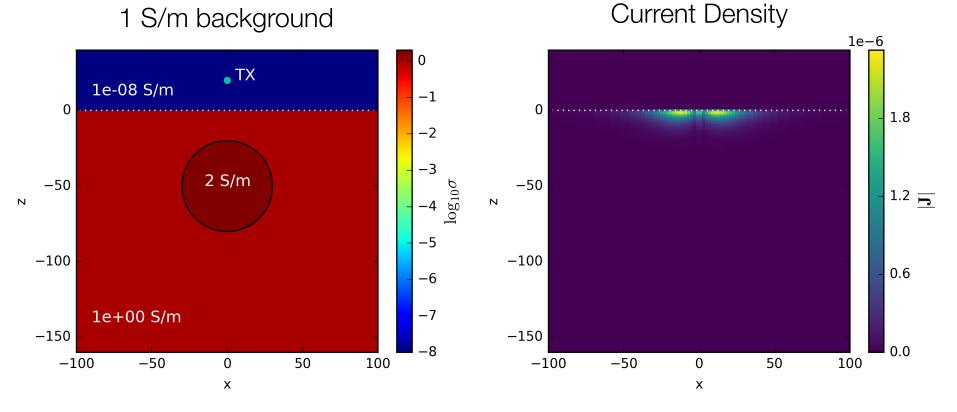
- Buried, conductive sphere
- Vary background conductivity
- Frequency: 10⁴ Hz



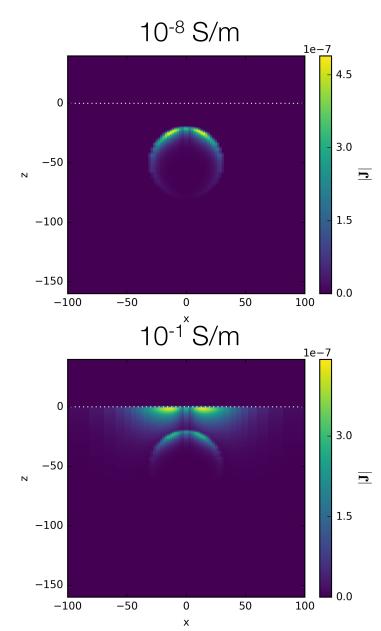


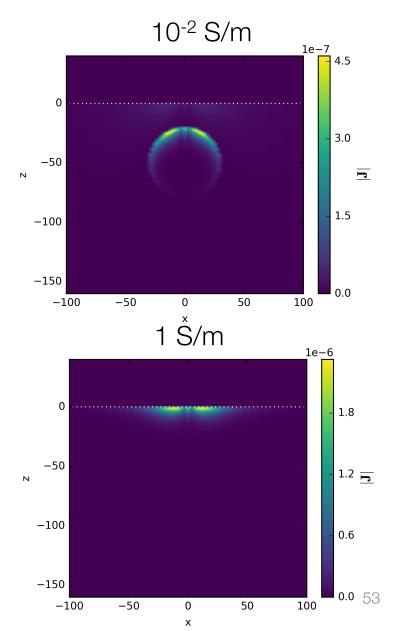
- Buried, conductive sphere
- Vary background conductivity
- Frequency: 10⁴ Hz





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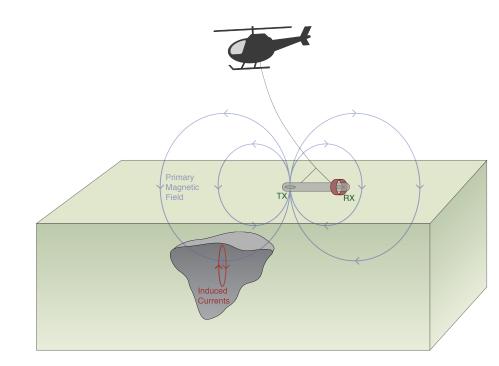




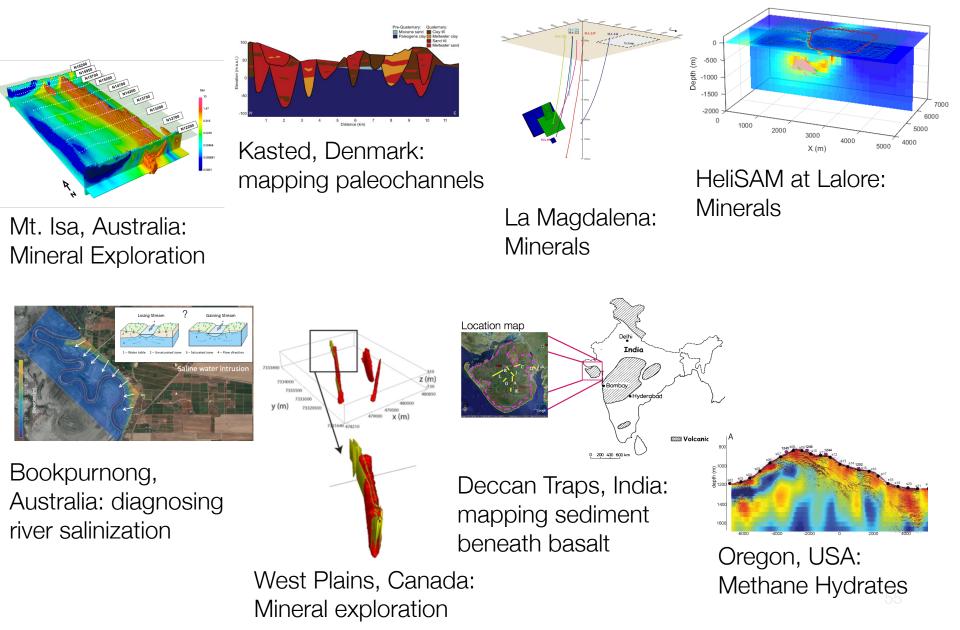
10⁴ Hz

Recap: what have we learned?

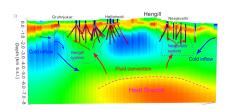
- Basics of EM induction
- Response functions
- Mutual coupling
- Data for frequency or time
 domain systems
- Circuit model is a good proxy
- Need to account for energy losses
- Ready to look at some field examples

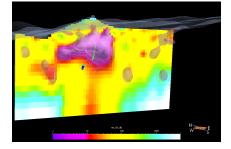


Today's Case Histories

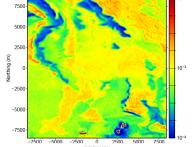


Today's Case Histories

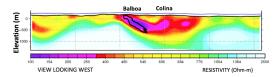




Santa Cecilia, Chile: Mineral Exploration

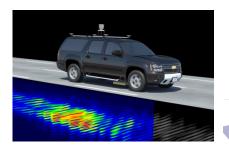


Noranda, Canada: Geologic Mapping

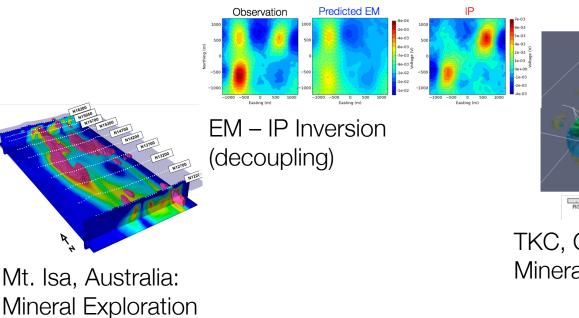


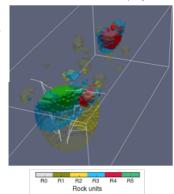
Balboa, Panama: Mineral Exploration

Iceland: characterizing geothermal systems



USA: Self-driving vehicles





TKC, Canada: Mineral Exploration

End of EM Fundamentals

