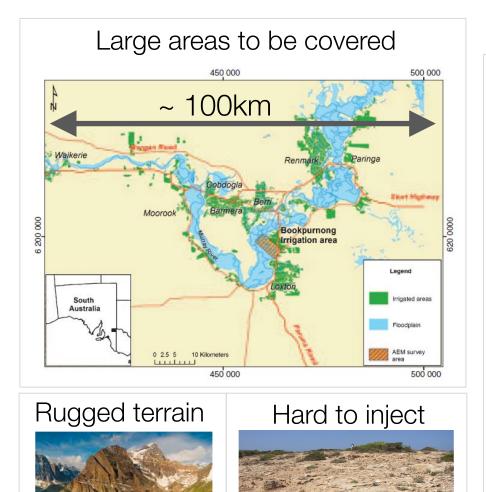
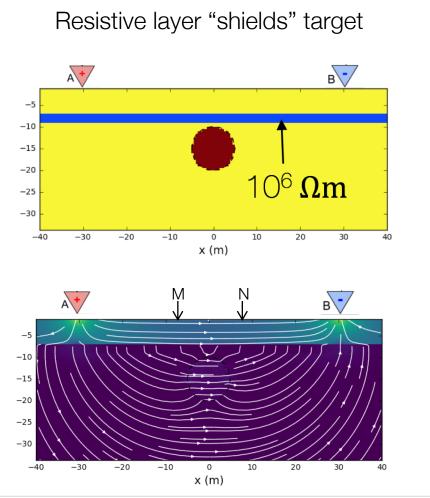
EM Fundamentals





Motivation: applications difficult for DC



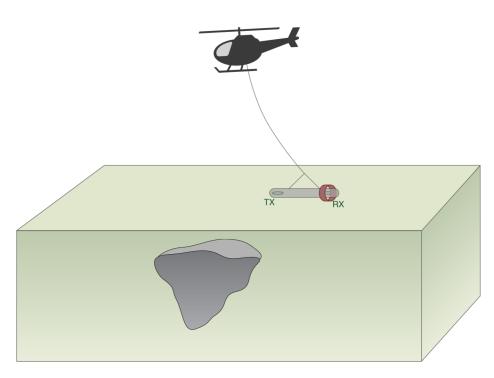


Outline

- Basic Survey
- Ampere's and Faraday's Laws (2-coil App)
- Circuit model for EM induction
- Frequency and time domain data
- Sphere in homogeneous earth
- Cyl code
- Energy losses in the ground

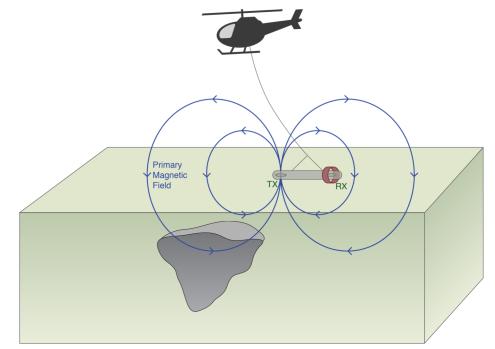
• Setup:

 transmitter and receiver are in a towed bird



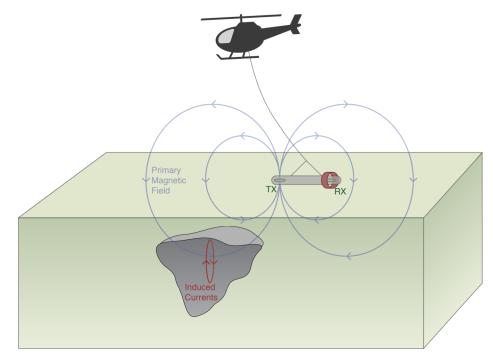
• Setup:

- transmitter and receiver are in a towed bird
- Primary:
 - Transmitter produces a primary magnetic field

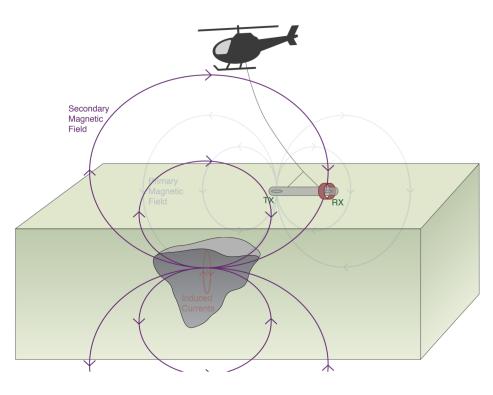


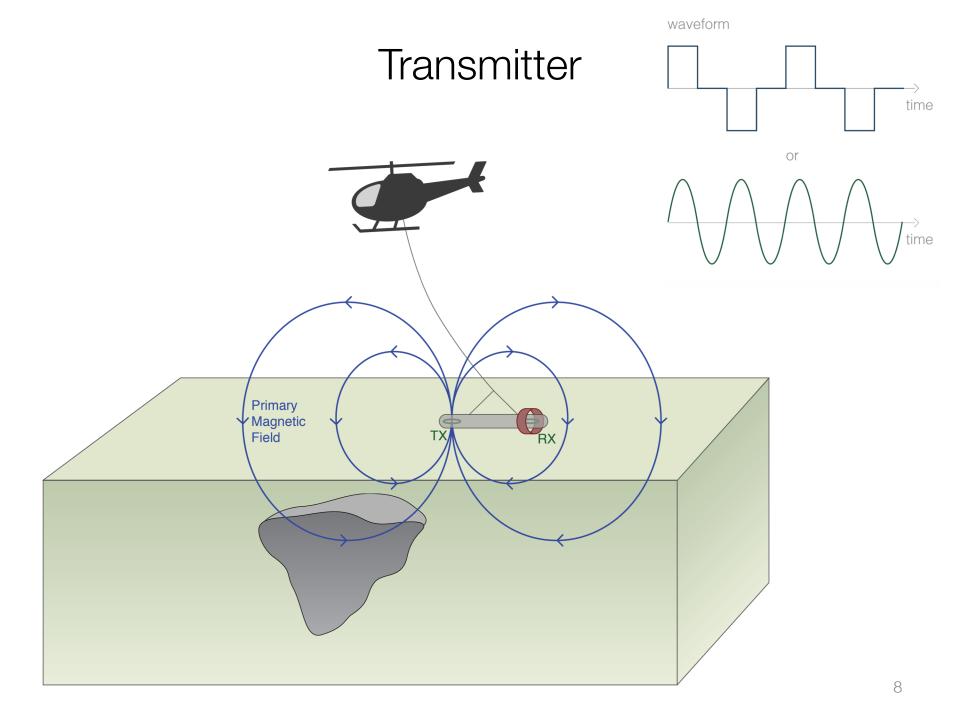
• Setup:

- transmitter and receiver are in a towed bird
- Primary:
 - Transmitter produces a primary magnetic field
- Induced Currents:
 - Time varying magnetic fields generate electric fields everywhere and currents in conductors



- Setup:
 - transmitter and receiver are in a towed bird
- Primary:
 - Transmitter produces a primary magnetic field
- Induced Currents:
 - Time varying magnetic fields generate electric fields everywhere and currents in conductors
- Secondary Fields:
 - The induced currents produce a secondary magnetic field.



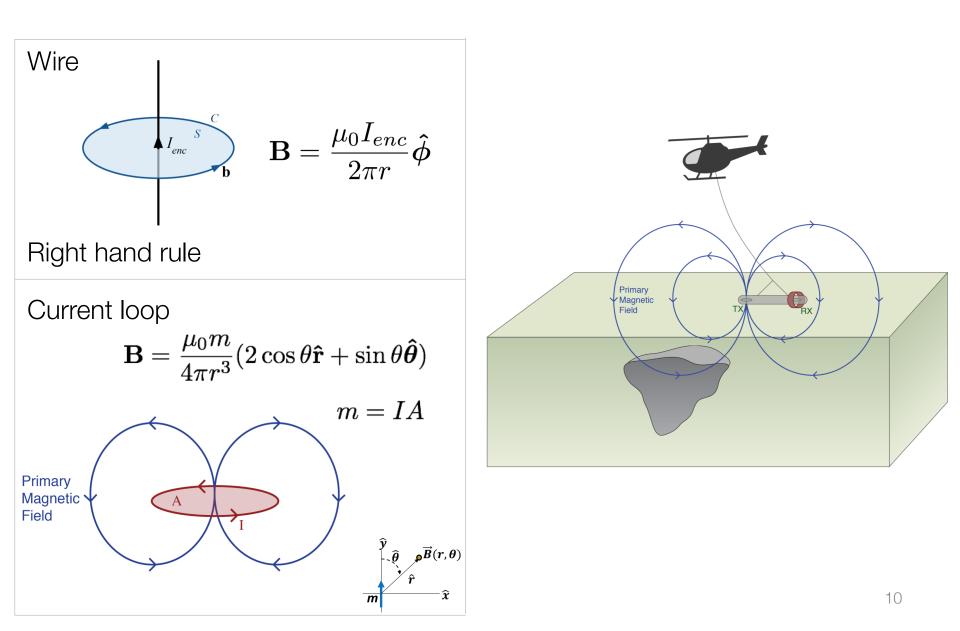


Basic Equations: Quasi-static

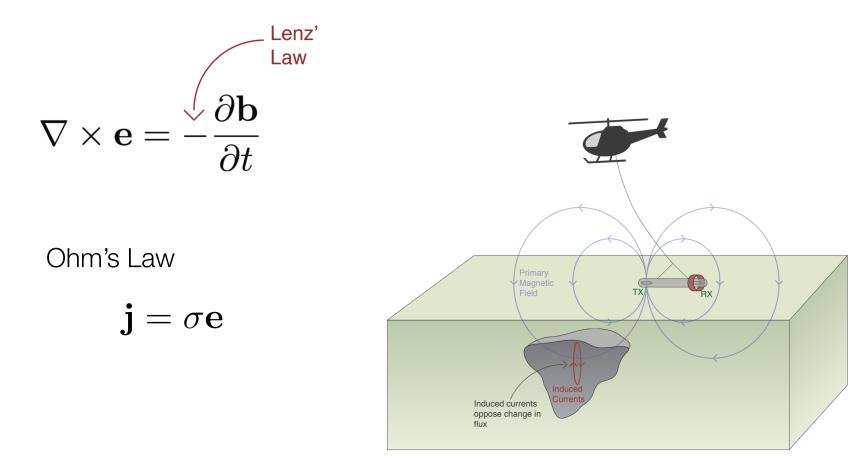
	Time	Frequency
Faraday's Law	$\nabla \times \mathbf{e} = -\frac{\partial \mathbf{b}}{\partial t}$	$ abla imes {f E} = -i\omega {f B}$
Ampere's Law	$ abla imes \mathbf{h} = \mathbf{j} + rac{\partial \mathbf{d}}{\partial t}$	$ abla imes \mathbf{H} = \mathbf{J} + i\omega \mathbf{D}$
No Magnetic Monopoles	$\nabla \cdot \mathbf{b} = 0$	$\nabla \cdot \mathbf{B} = 0$
Constitutive Relationships (non-dispersive)	$\mathbf{j} = \sigma \mathbf{e}$ $\mathbf{b} = \mu \mathbf{h}$ $\mathbf{d} = \varepsilon \mathbf{e}$	$egin{array}{llllllllllllllllllllllllllllllllllll$

* Solve with sources and boundary conditions

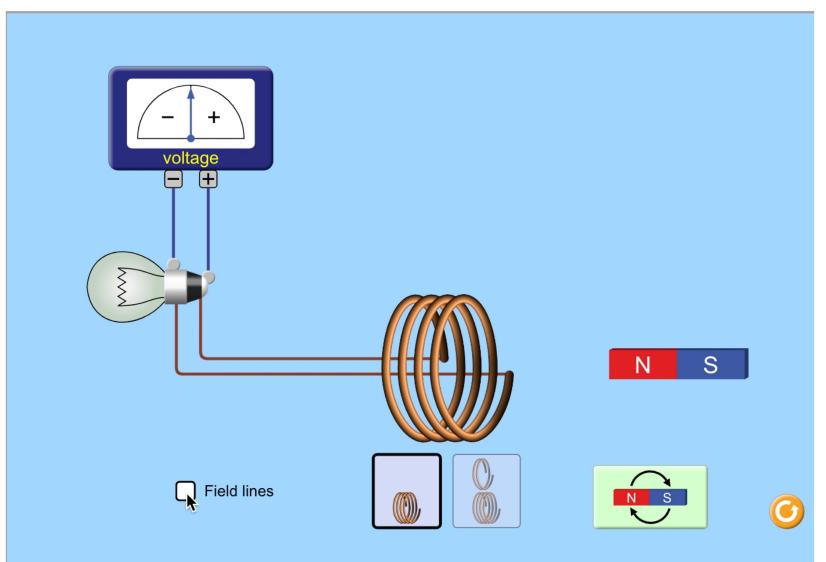
Ampere's Law $\nabla \times \mathbf{H} = \mathbf{J}$



Faraday's Law



Faraday's Law



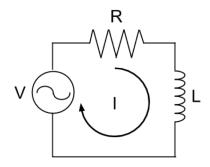


Magnetic Flux

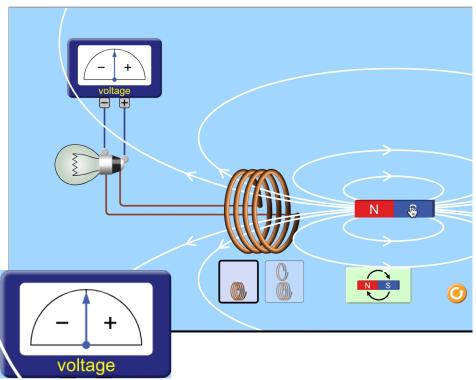
$$\phi_{\mathbf{b}} = \int_{A} \mathbf{b} \cdot \mathbf{\hat{n}} \, da$$

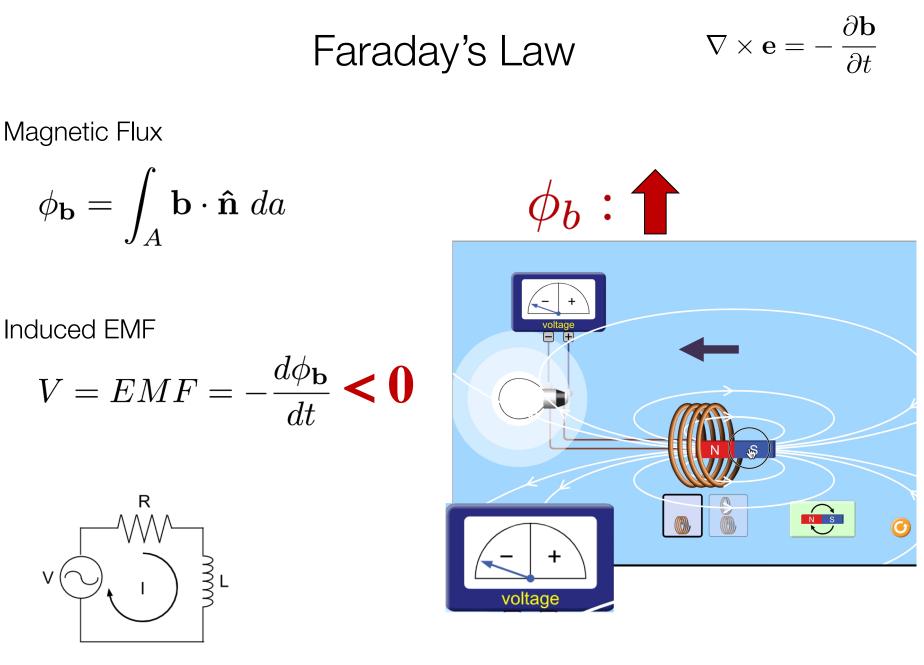
Induced EMF

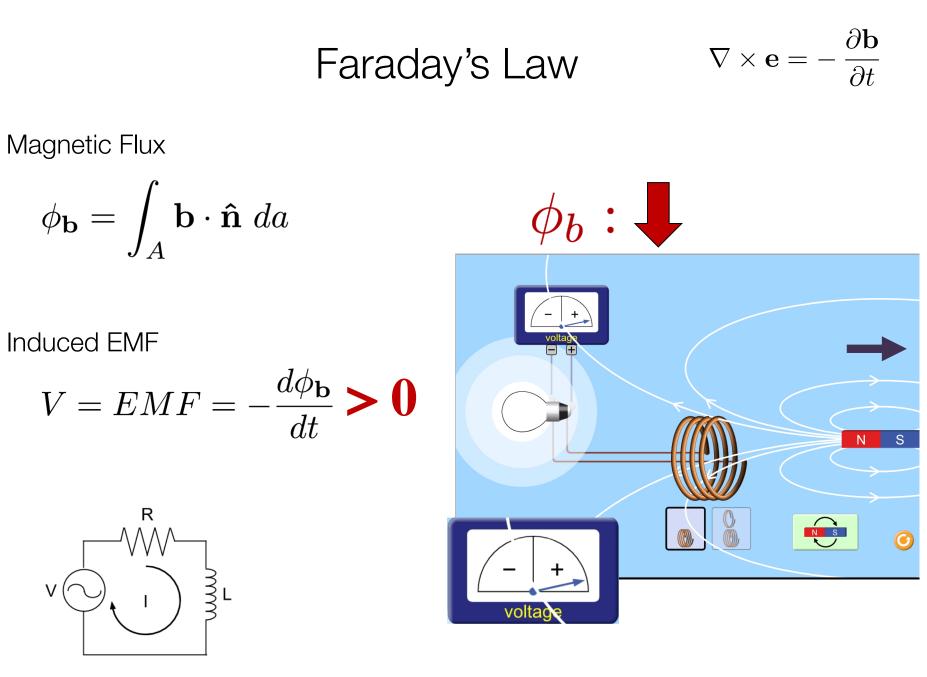
$$V = EMF = -\frac{d\phi_{\mathbf{b}}}{dt} = \mathbf{0}$$



ϕ_b : constant



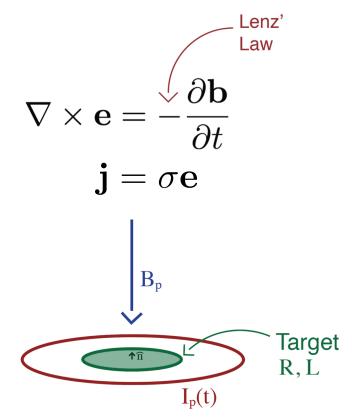


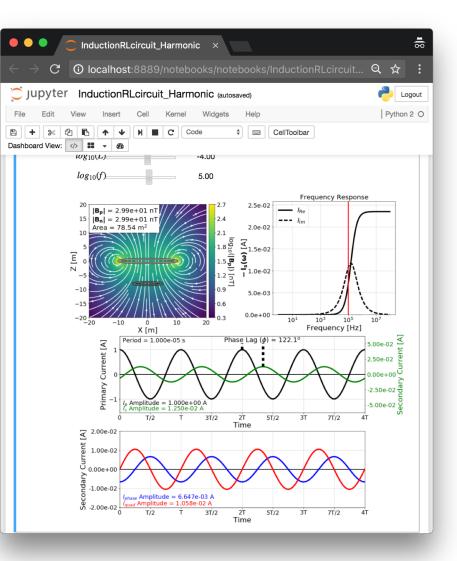


App for Faraday's Law

2 Apps:

- Harmonic
- Transient

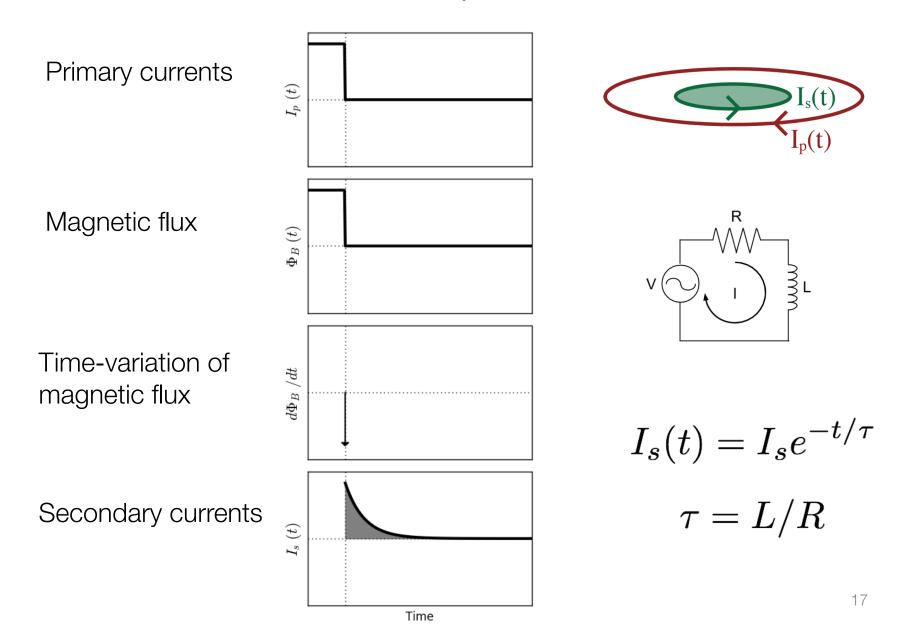




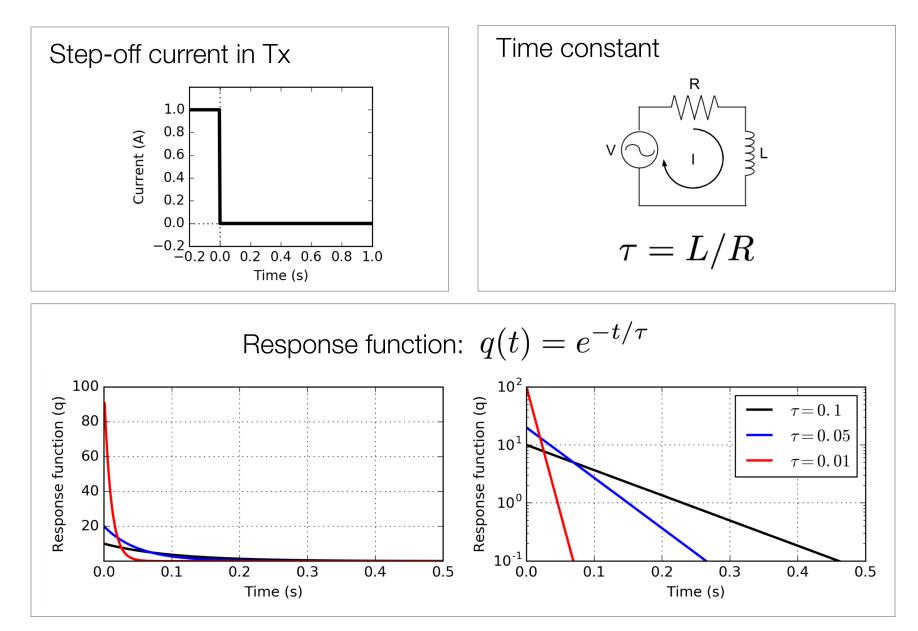
http://em.geosci.xyz/apps.html

Two Coil Example: Transient

TDEM



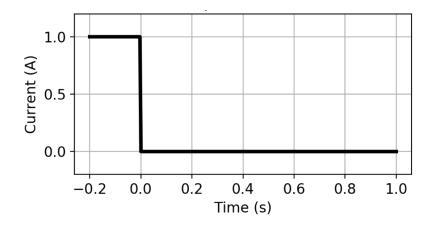
Response Function: Transient

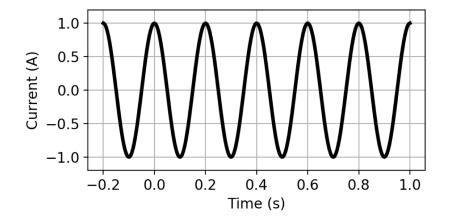


Transient and Harmonic Signals

We have seen a transient pulse...

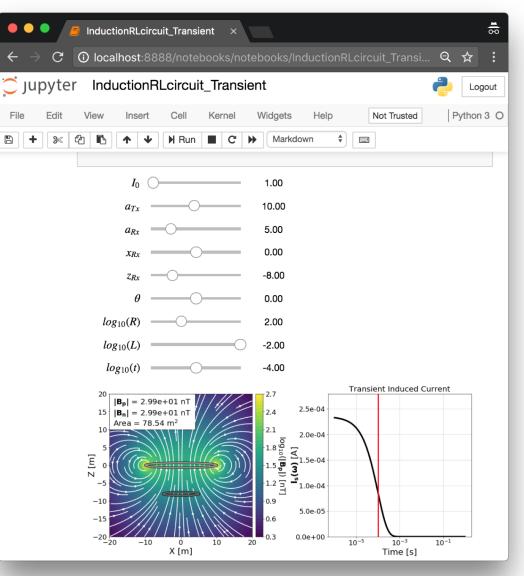
What happens when he have a harmonic?





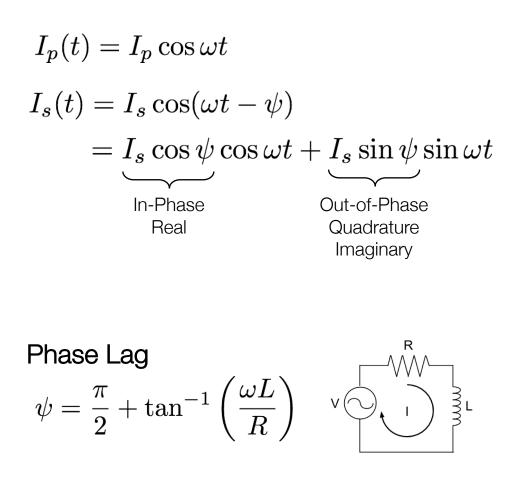
2 Coil Transient app (demo)

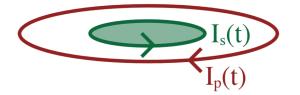
- InductionRLcurcuit_Transient
- Parameters:
 - Current
 - Radius, position of Tx, target loop
 - Resistivity, inductance of target loop
- View:
 - Model
 - Magnetic flux
 - Response through time

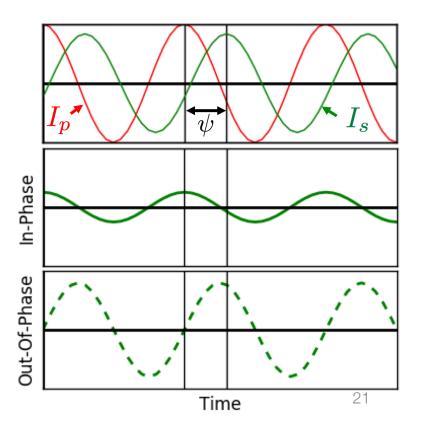


Two Coil Example: Harmonic

Induced Currents

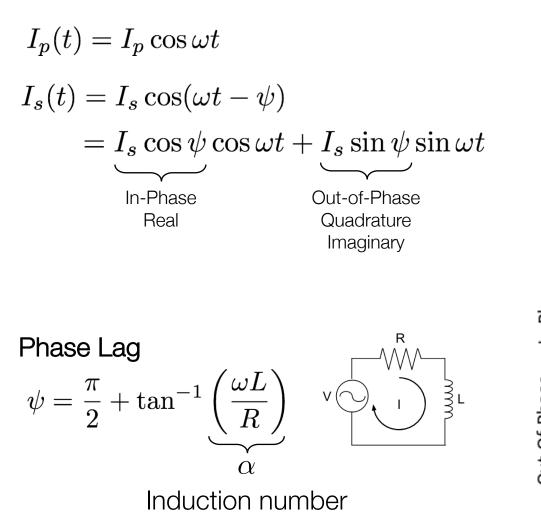


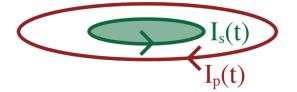


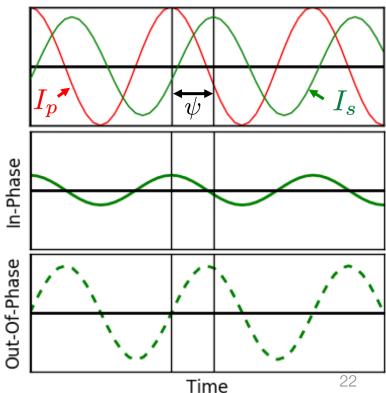


Two Coil Example: Harmonic

Induced Currents

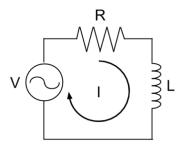


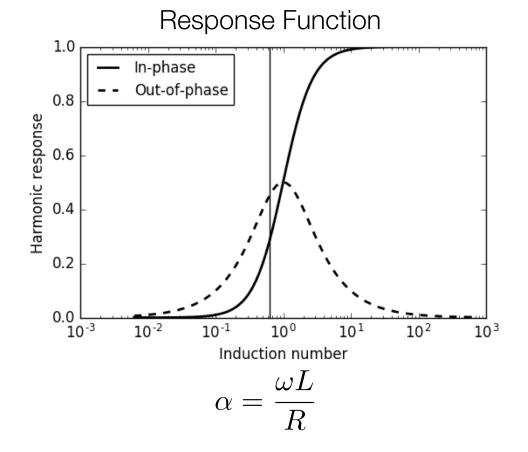


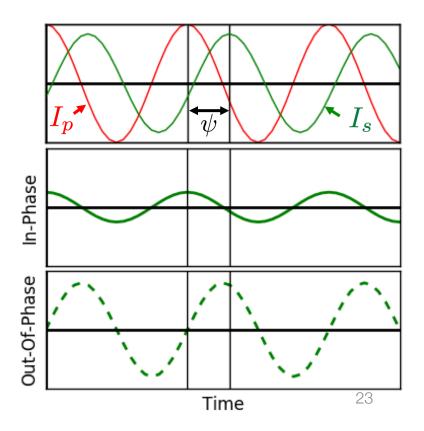


Response Function

- Quantifies how a target responds to a time varying magnetic field
- Partitions real and imaginary parts

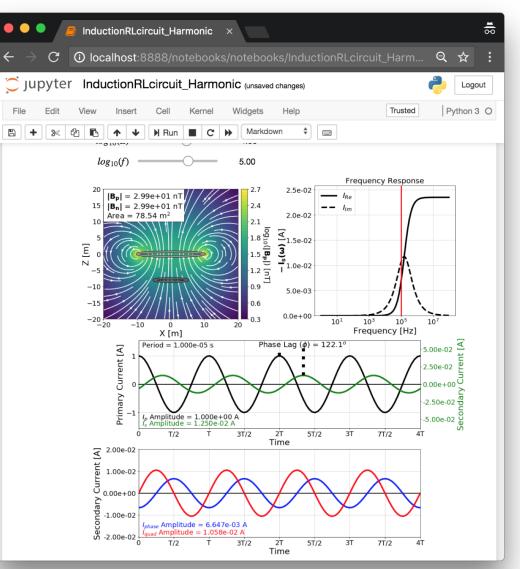




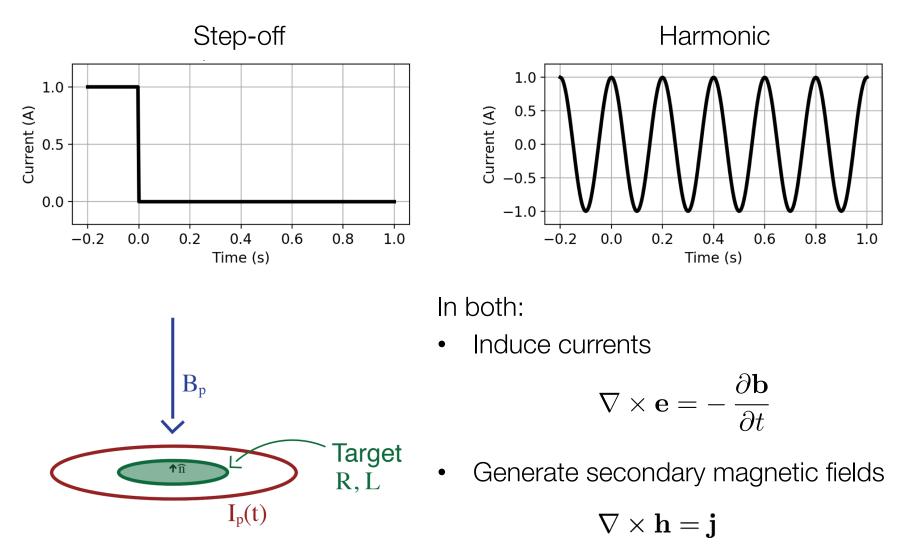


2 Coil Harmonic app (demo)

- InductionRLcurcuit_Harmonic
- Parameters:
 - Current, frequency
 - Radius, position of Tx, target loop
 - Resistivity, inductance of target loop
- View:
 - Model
 - Magnetic flux
 - Response curve
 - Partition of signal into real and imaginary components

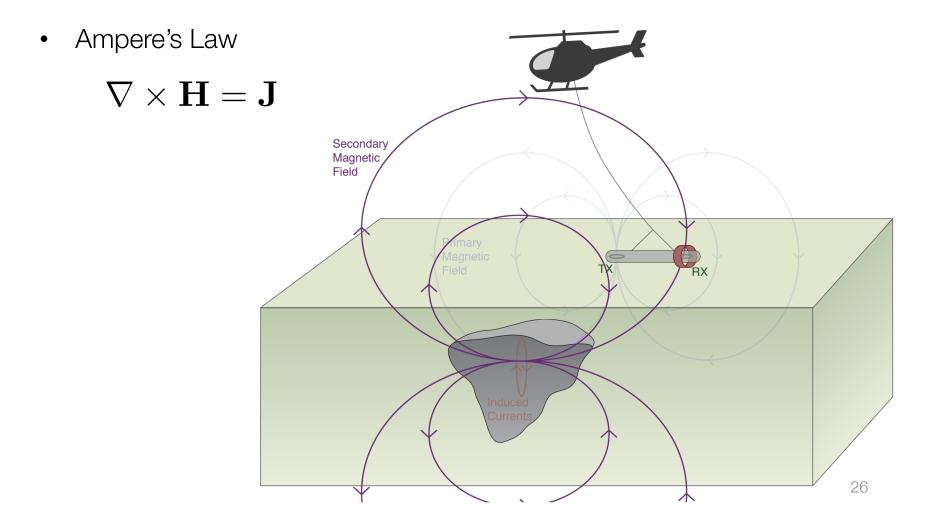


Response Functions: Summary

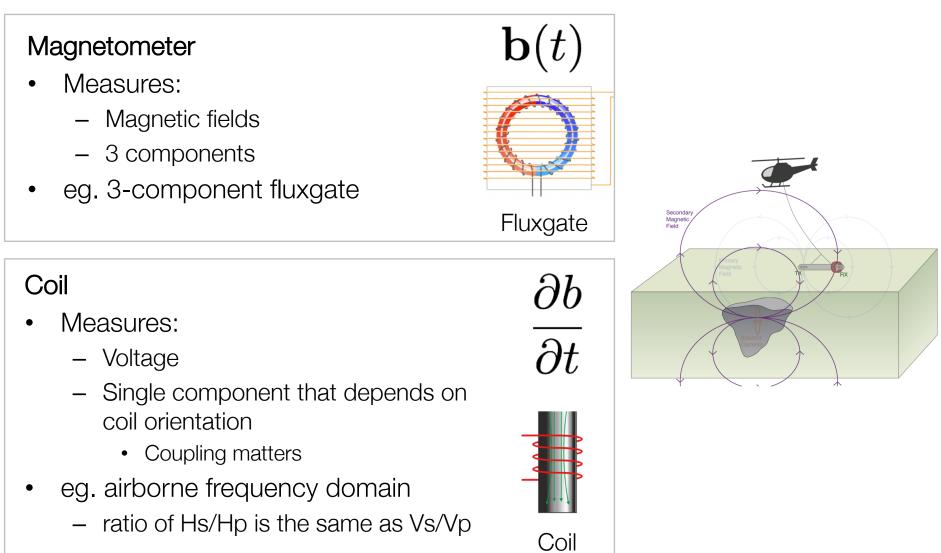


Secondary magnetic fields

Induced currents generate magnetic fields



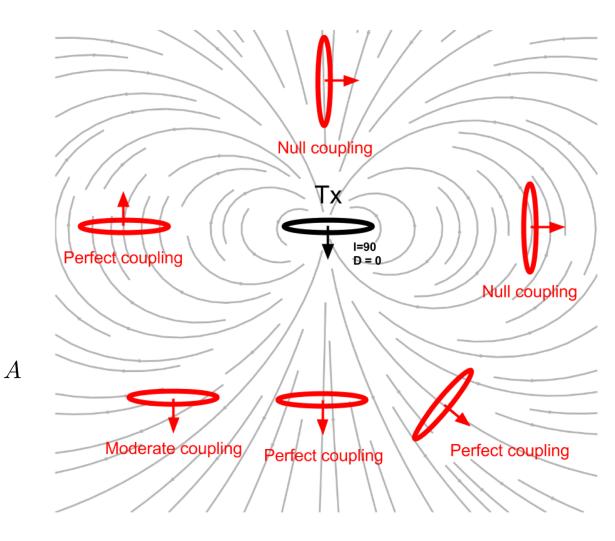
Receiver and Data



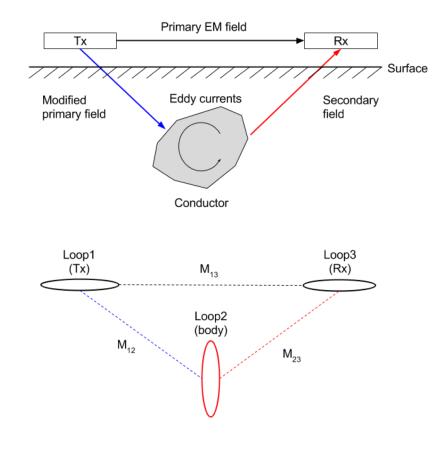
Coupling

- Transmitter: Primary $I_p(t) = I_p \cos(\omega t)$ $\mathbf{B}_p(t) \sim I_p \cos(\omega t)$
- Target: Secondary

$$EMF = -\frac{\partial \phi_{\mathbf{B}}}{\partial t}$$
$$= -\frac{\partial}{\partial t} \left(\mathbf{B}_{p} \cdot \hat{\mathbf{n}} \right)$$







Coupling coefficient

Depends on geometry

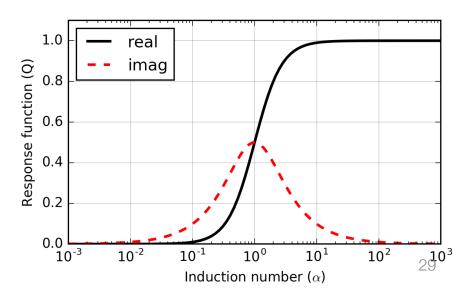
$$M_{12} = \frac{\mu_0}{4\pi} \oint \oint \frac{dl_1 \cdot dl_2}{|\mathbf{r} - \mathbf{r}'|^2}.$$

Magnetic field at the receiver

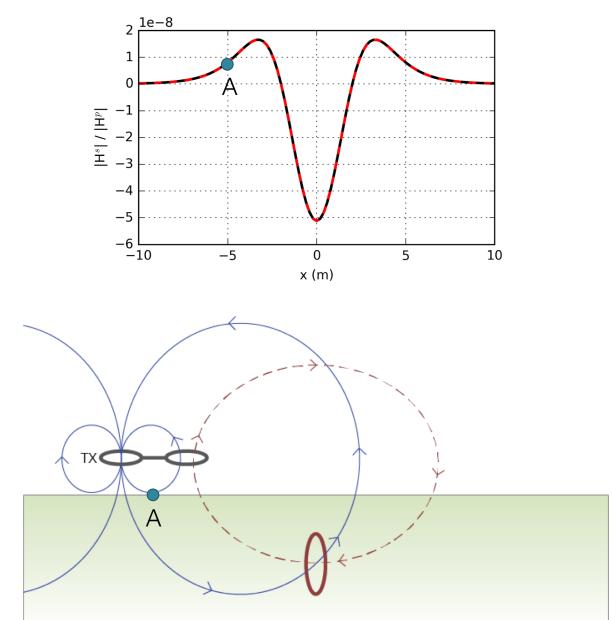
$$\frac{H^s}{H^p} = -\frac{M_{12}M_{23}}{M_{13}L} \underbrace{\left[\frac{\alpha^2 + i\alpha}{1 + \alpha^2}\right]}_Q$$

Induction Number

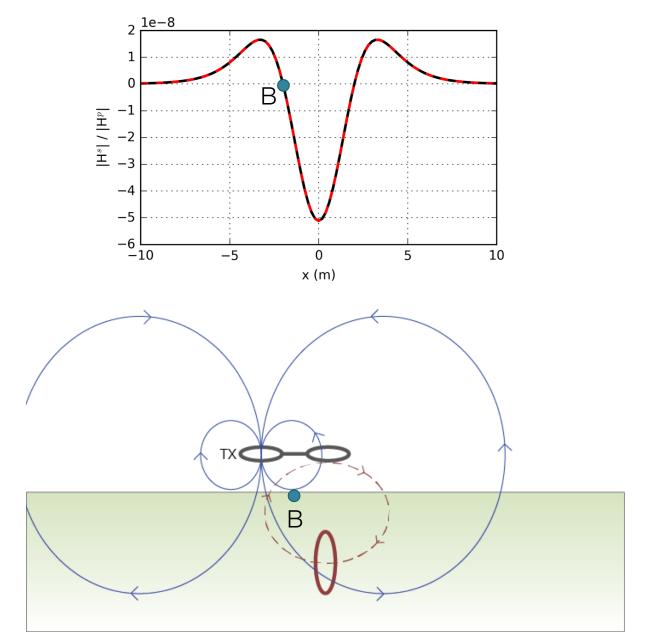
• Depends on properties $\alpha = \frac{\omega L}{R}$ of target



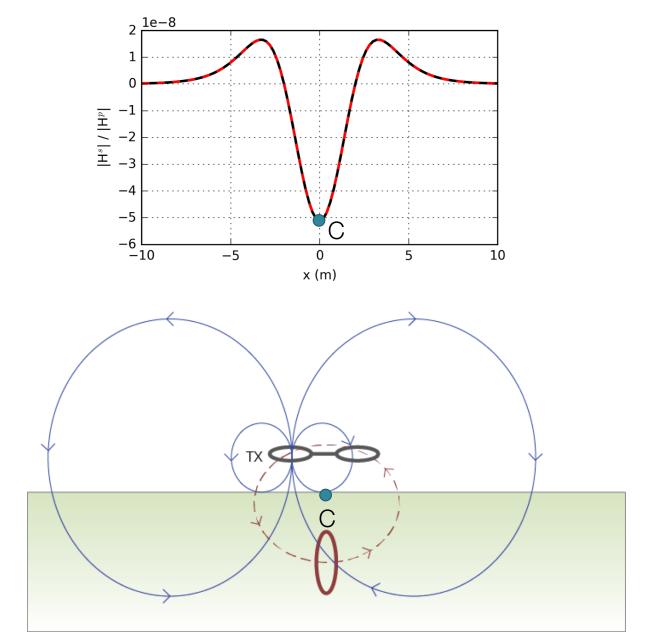




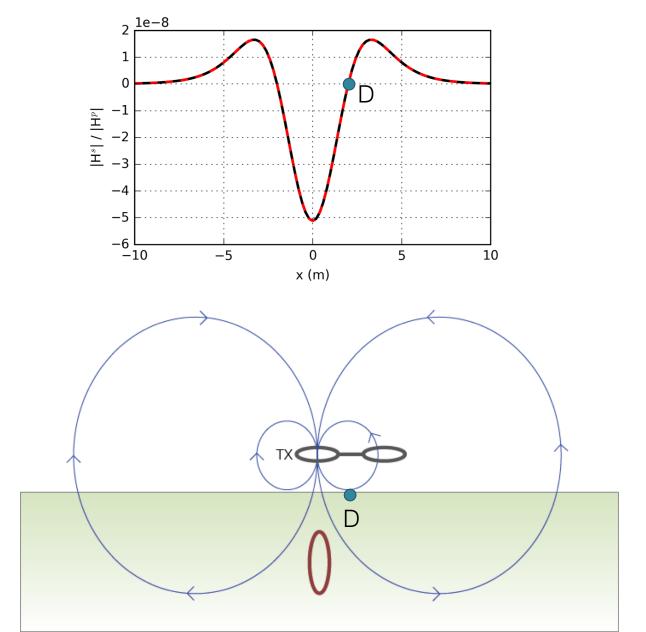




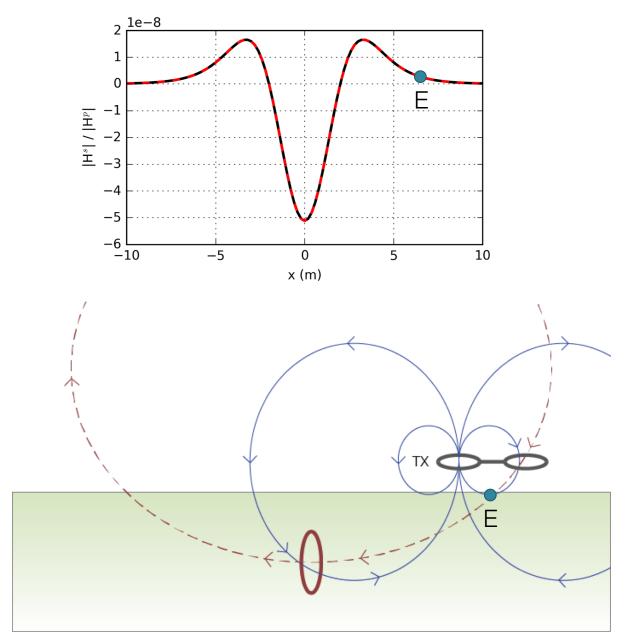


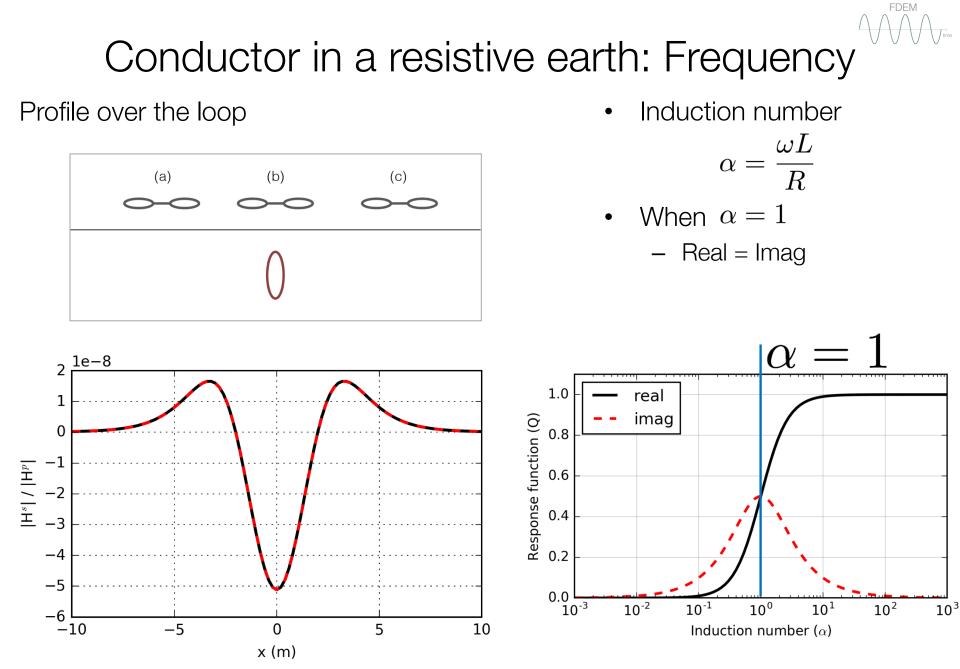


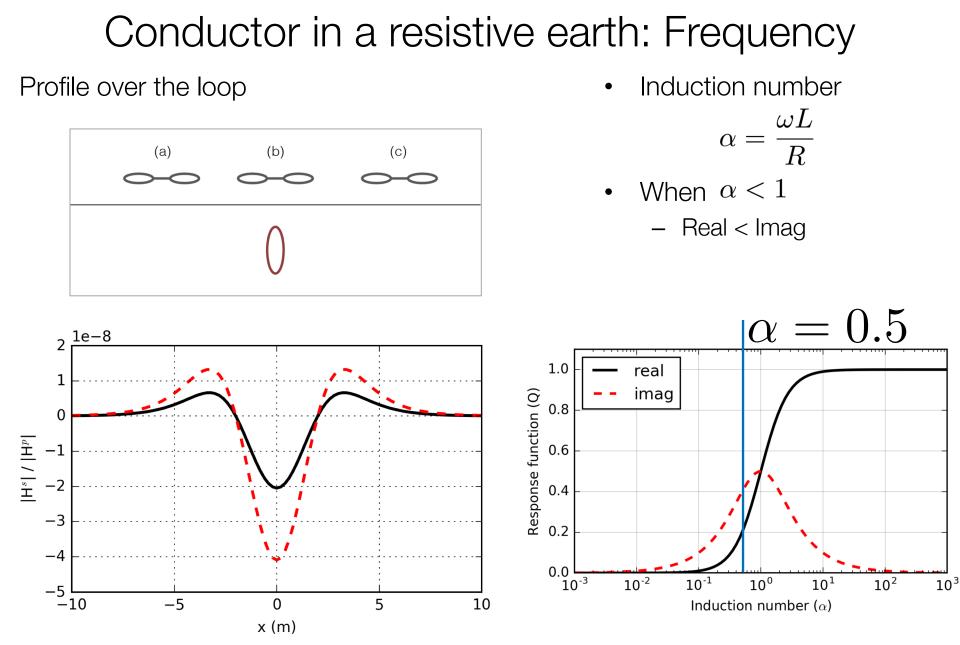


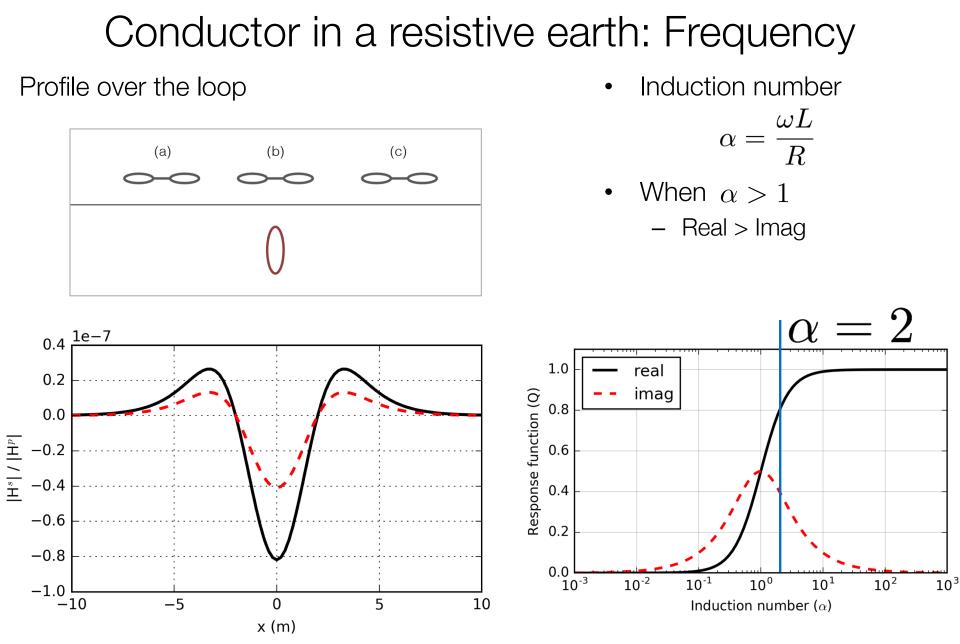






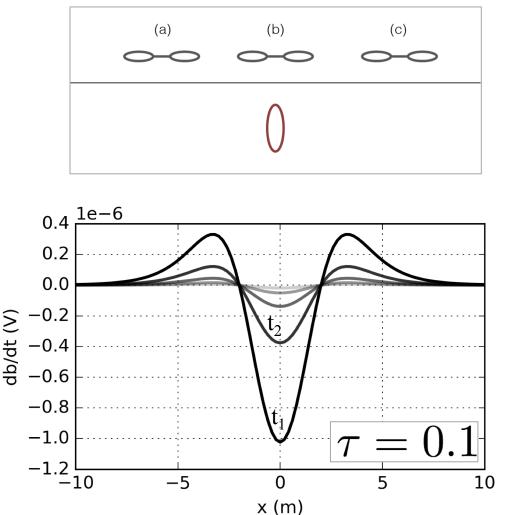






Conductor in a resistive earth: Transient

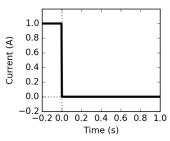
Profile over the loop



• Time constant

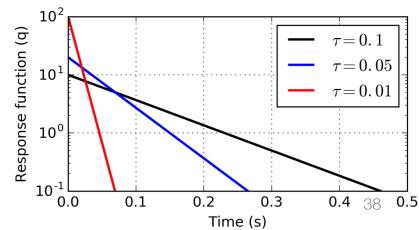
$$\tau = L/R$$

• Step-off current in Tx



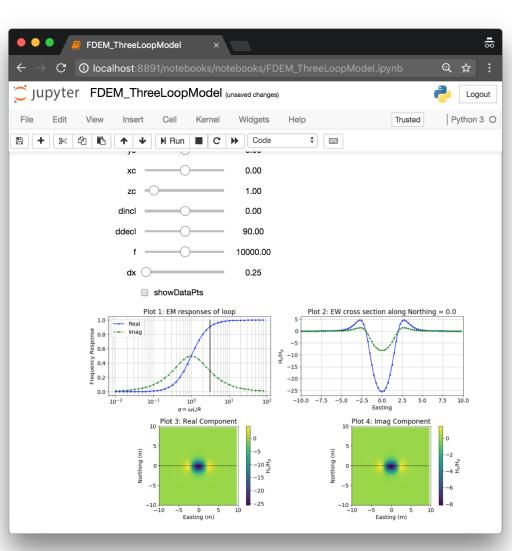
• Response function depends on time, au

$$q(t) = e^{-t/\tau}$$



App: Three Loop Model

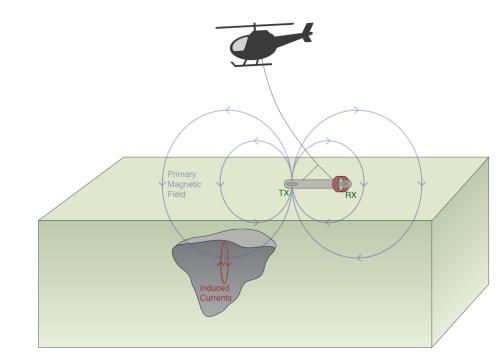
- FDEM_ThreeLoopModel
- Parameters:
 - Location, separation of transmitter and receiver
 - Number of sounding locations
 - Orientation of target loop
 - Resistance, inductance of target loop
- View:
 - Response function
 - Real and imaginary components (plan view and a profile line)



http://em.geosci.xyz/apps.html

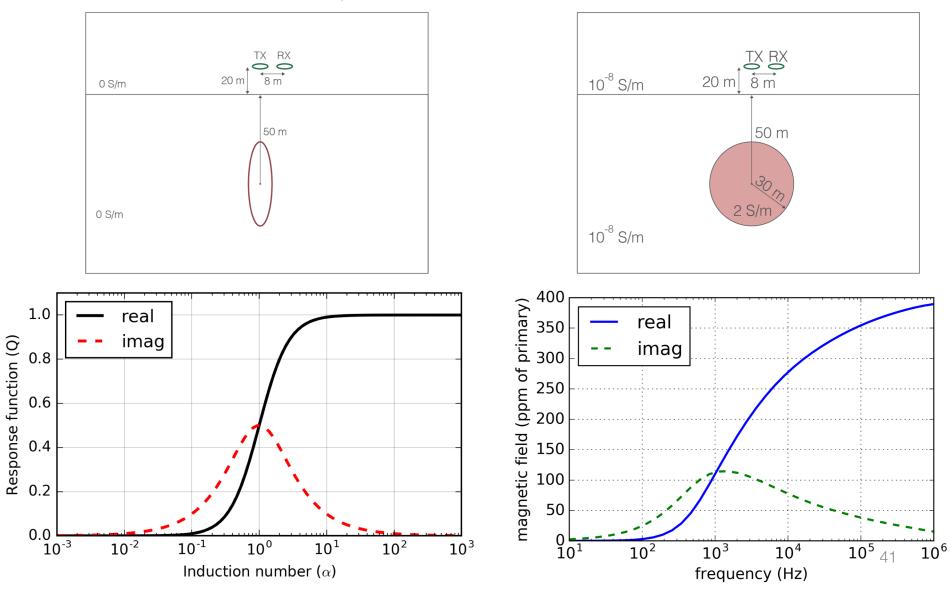
Recap: what have we learned?

- Basics of EM induction
- Response functions
- Mutual coupling
- Data for frequency or time
 domain systems
- Circuit model provides
 representative results
 - Applicable to geologic targets?



Sphere in a resistive background

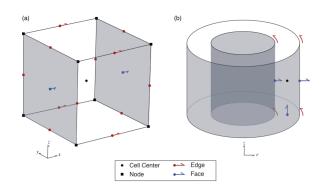
How representative is a circuit model?



Cyl Code

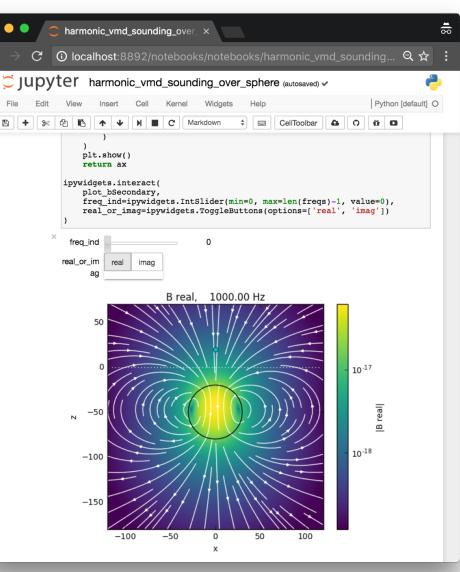


- Finite Volume EM
 - Frequency and Time



- Built on SimPEG
- Open source, available at: <u>http://em.geosci.xyz/apps.html</u>
- Papers

Cockett et al, 2015 Heagy et al, 2017



Recap: what have we learned?

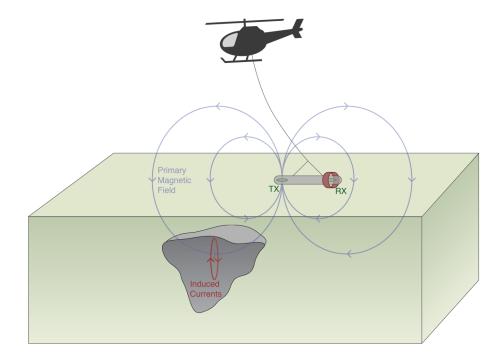
- Basics of EM induction
- Response functions
- Mutual coupling
- Data for frequency or time domain systems
- Circuit model is a good proxy

2-Coil Apps

- Frequency domain
- Time domain

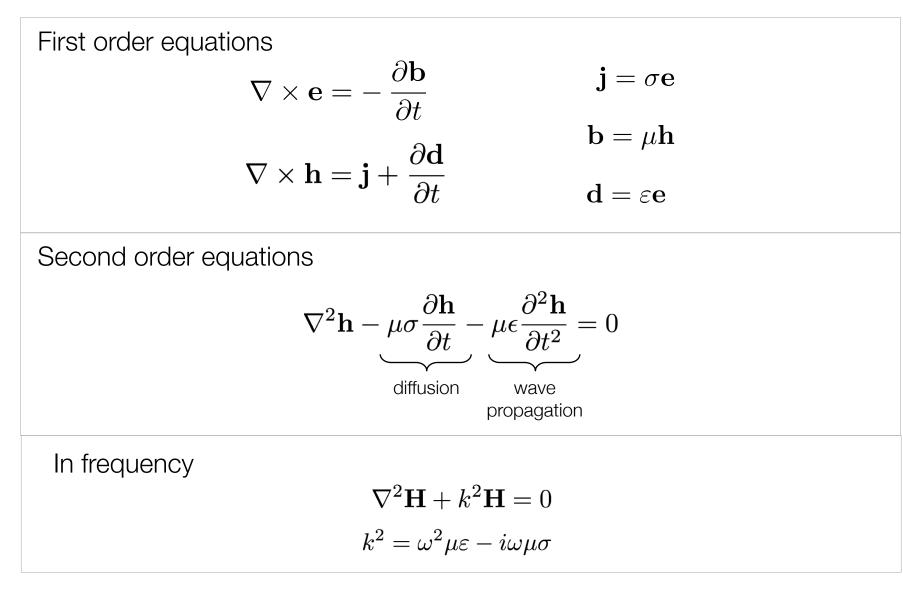
Major item not yet accounted for...

- Propagation of energy from
 - Transmitter to target
 - Target to receiver

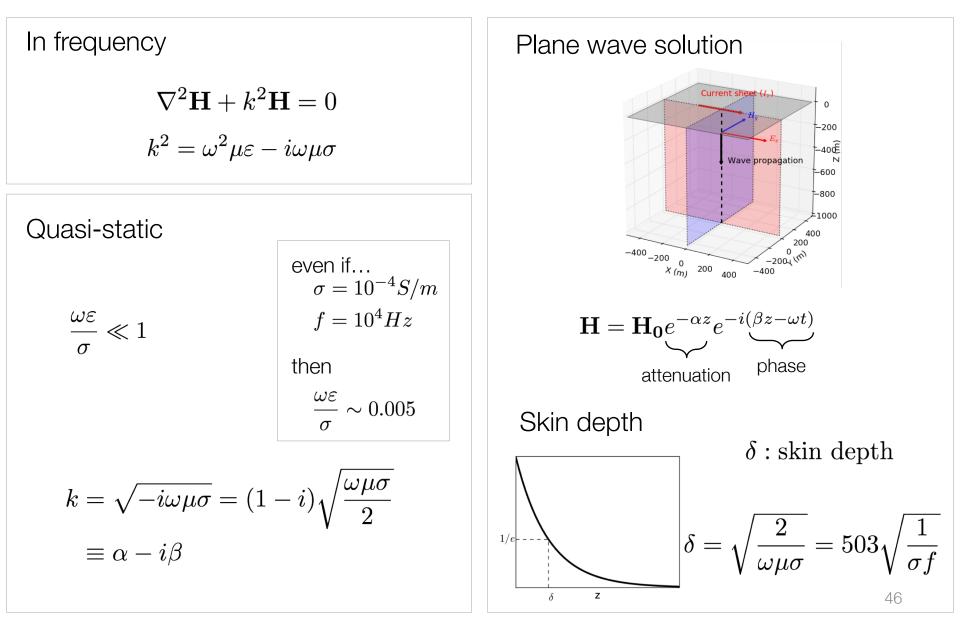


How do EM fields and fluxes behave in a conductive background?

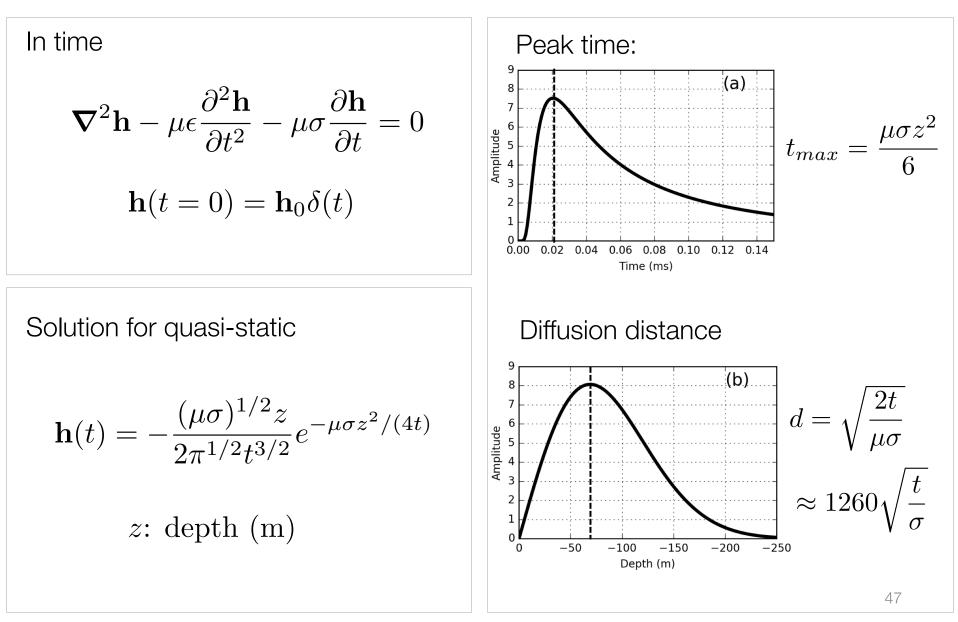
Revisit Maxwell's equations



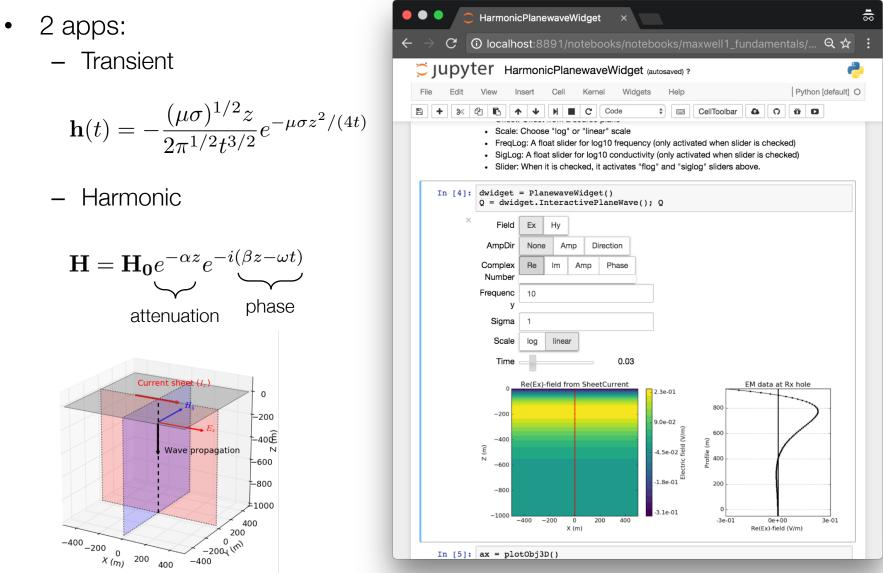
Plane waves in a homogeneous media



Plane waves in a homogeneous media



Plane Wave apps

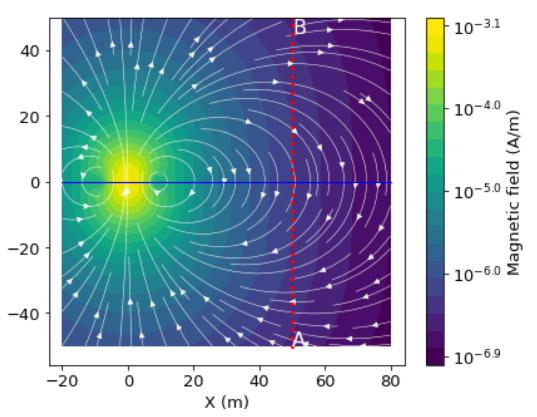


http://em.geosci.xyz/apps.html

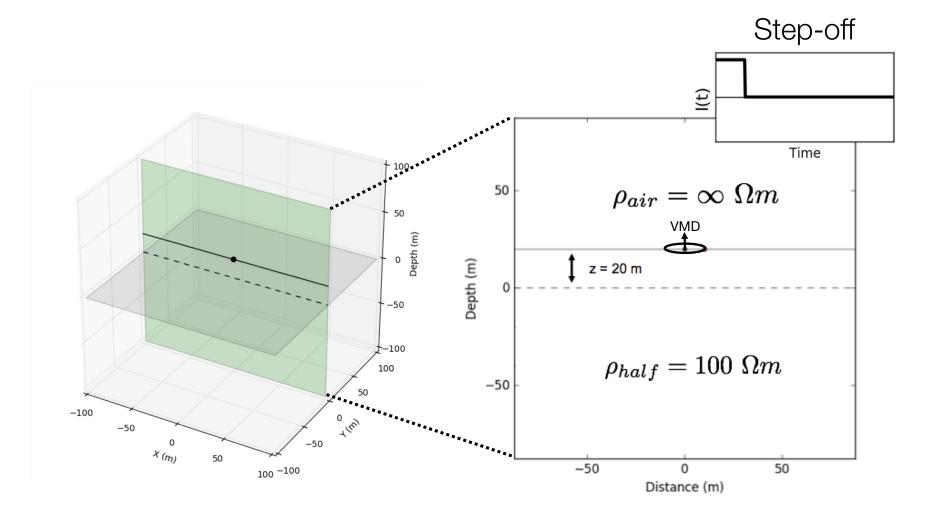
Dipole sources

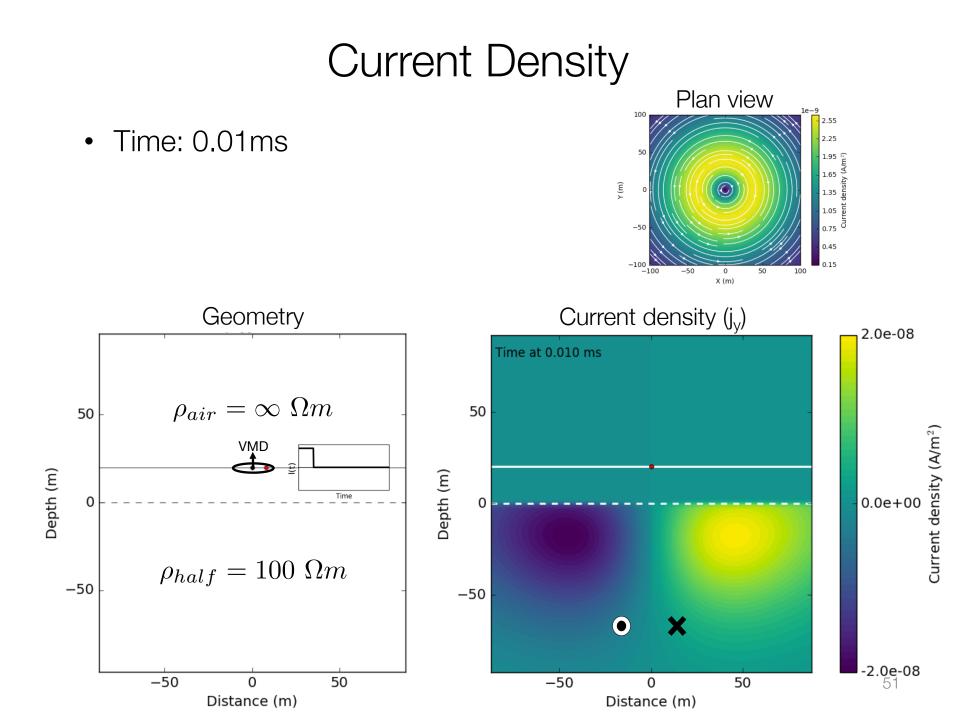
- Primary field has a geometric decay away from the transmitter
 - very different from a plane wave source
- Two principal sources (for small transmitters
 characteristic of airborne surveys):
 - VMD: vertical magnetic dipole
 - HMD: horizontal magnetic dipole

Magnetic field from a vertical magnetic dipole in a wholespace

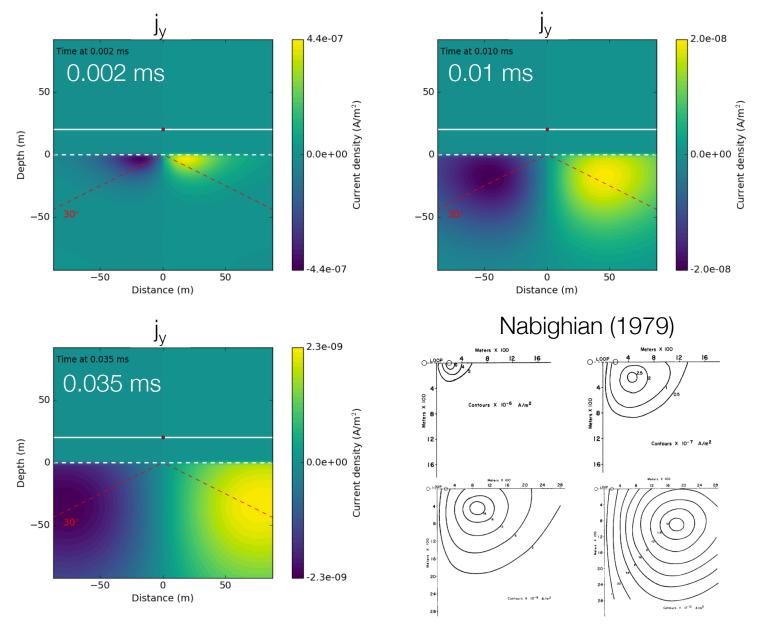


Vertical Magnetic Dipole over a halfspace (TDEM)





Summary: propagation through time



52

Important points

- Currents flow in same plane as transmitter currents
- Currents diffuse outward downward
- Each transmitter has a "footprint"
- Max resolution controlled by earliest time
- Depth of investigation controlled by latest time

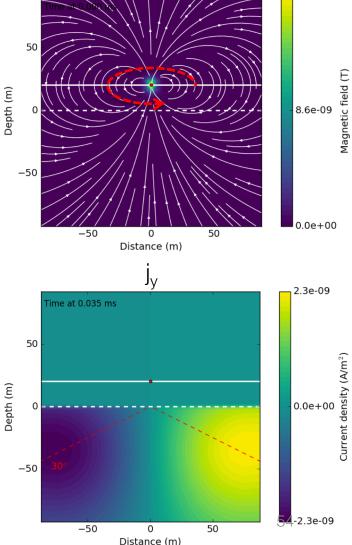
magnetic field (on-time) 1.7e-08 50 Magnetic field (T) Depth (m) 8.6e-09 -50 50 -50 Distance (m) 4.4e-07 me at 0.002 ms 50 Current density (A/m²) Depth (m) 0.0e+00 -50 4.4e-07 -500 50

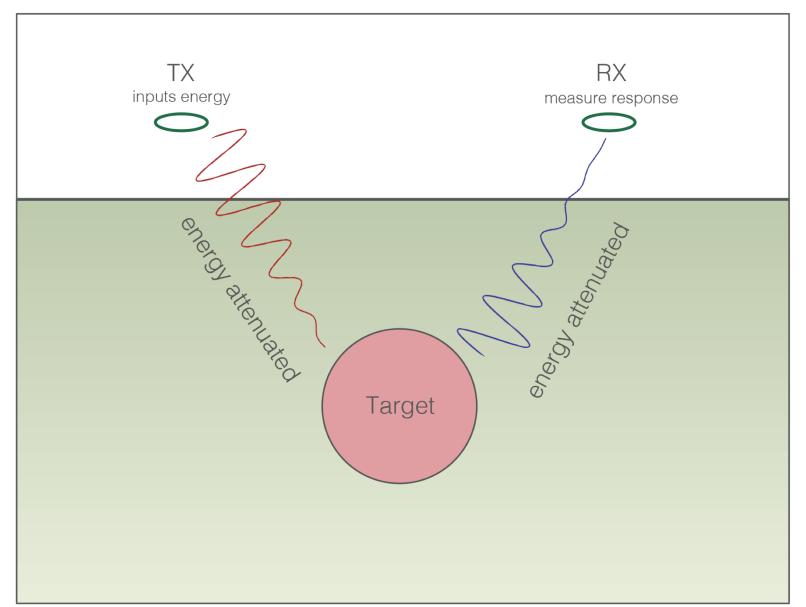
Distance (m)

Important points

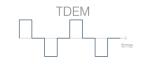
- Currents flow in same plane as • transmitter currents
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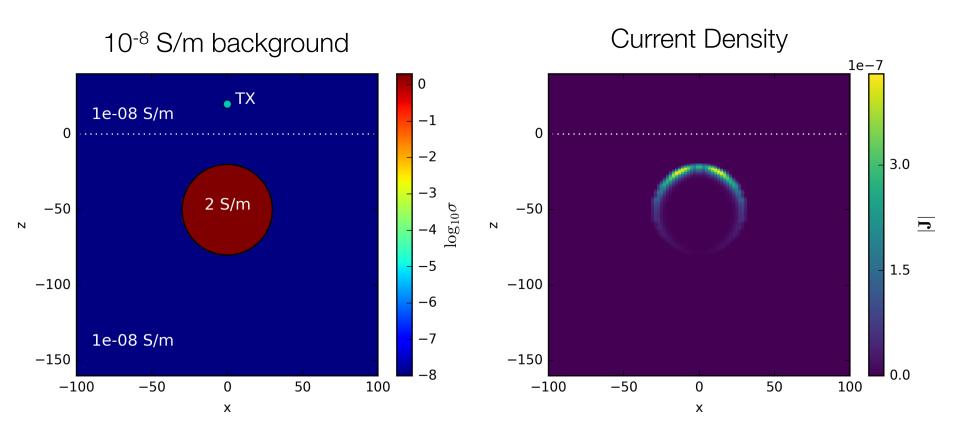
magnetic field (on-time) 1.7e-08



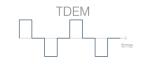


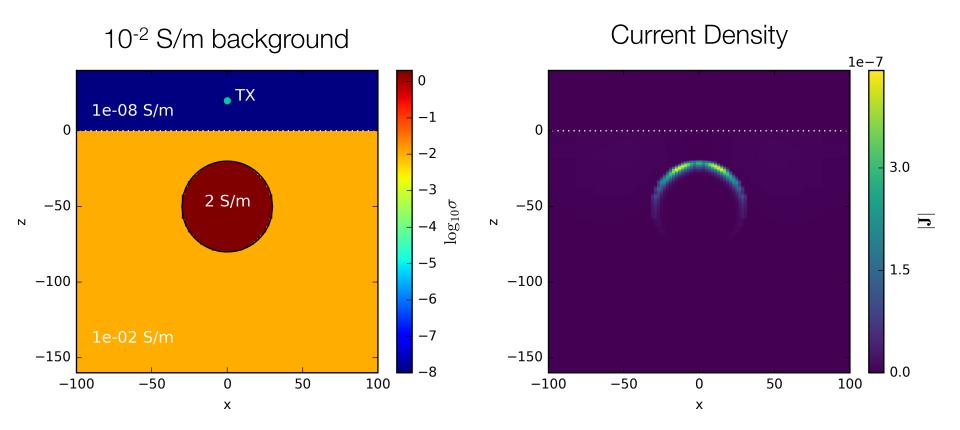
- Buried, conductive sphere
- Vary background conductivity
- Time: 10⁻⁵ s





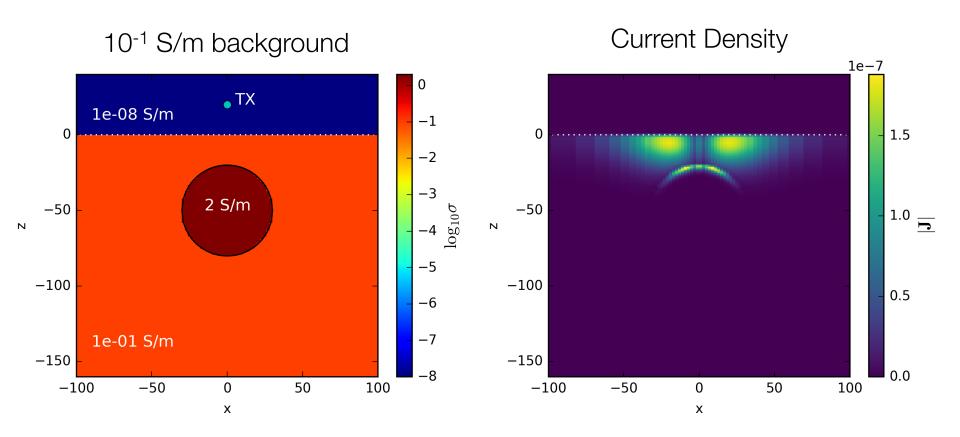
- Buried, conductive sphere
- Vary background conductivity
- Time: 10⁻⁵ s



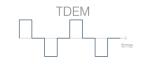


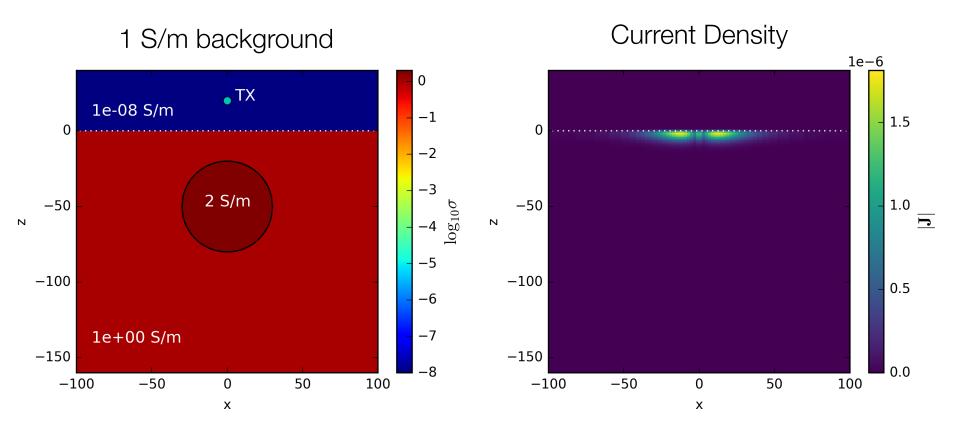
- Buried, conductive sphere
- Vary background conductivity
- Time: 10⁻⁵ s

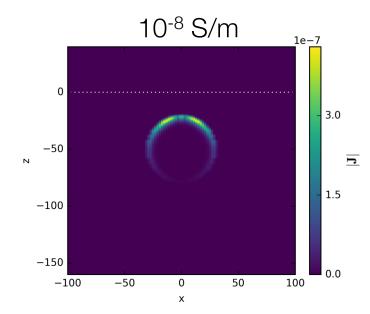




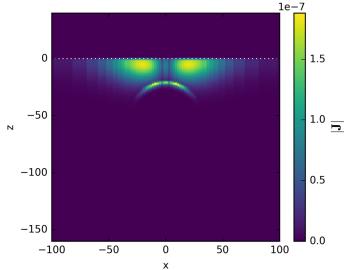
- Buried, conductive sphere
- Vary background conductivity
- Time: 10⁻⁵ s

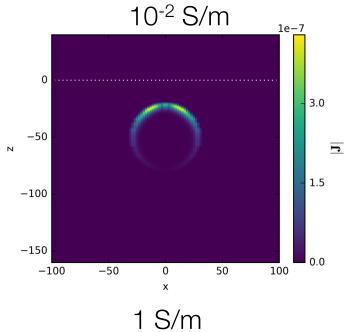


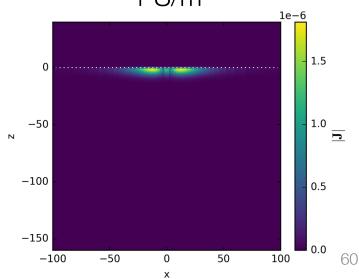


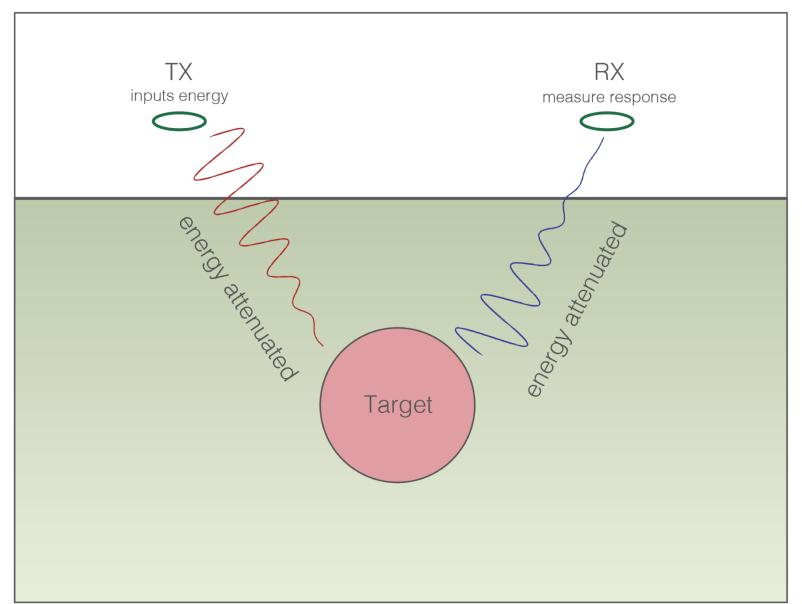




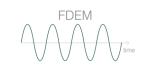


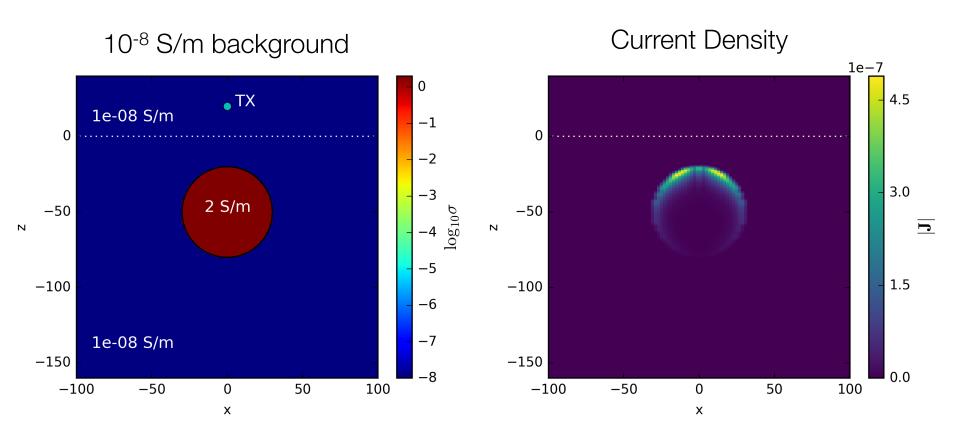




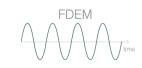


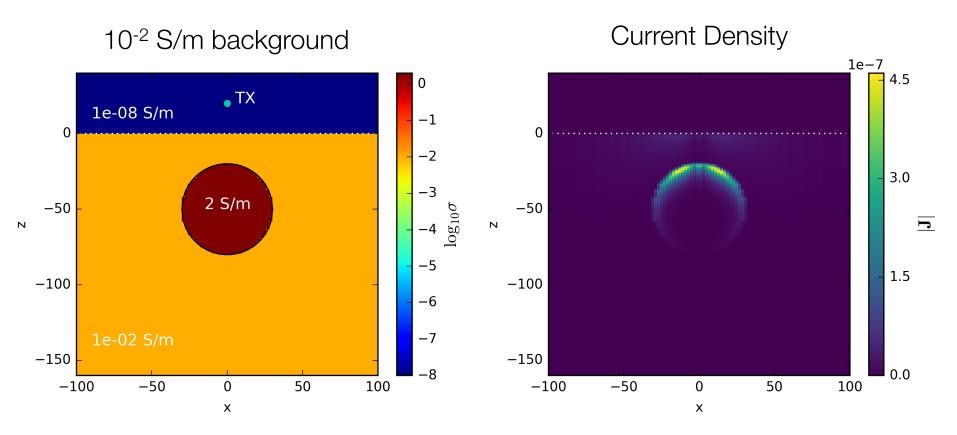
- Buried, conductive sphere
- Vary background conductivity
- Frequency: 10⁴ Hz



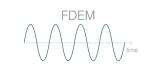


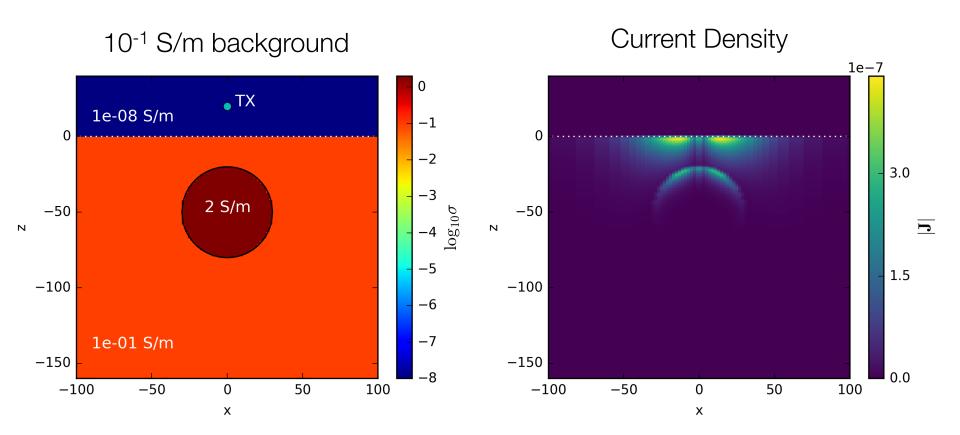
- Buried, conductive sphere
- Vary background conductivity
- Frequency: 10⁴ Hz





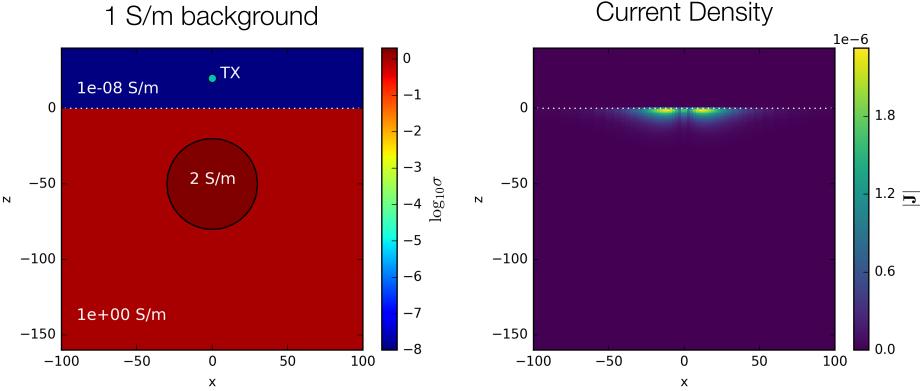
- Buried, conductive sphere
- Vary background conductivity
- Frequency: 10⁴ Hz

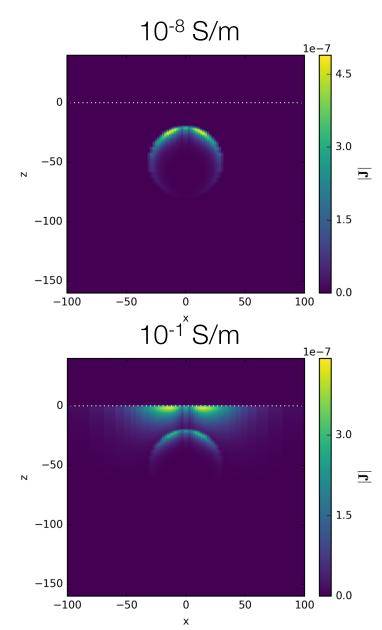


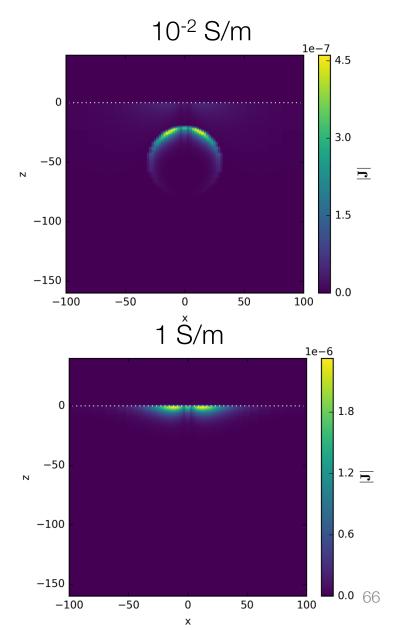


- Buried, conductive sphere
- Vary background conductivity
- Frequency: 10⁴ Hz





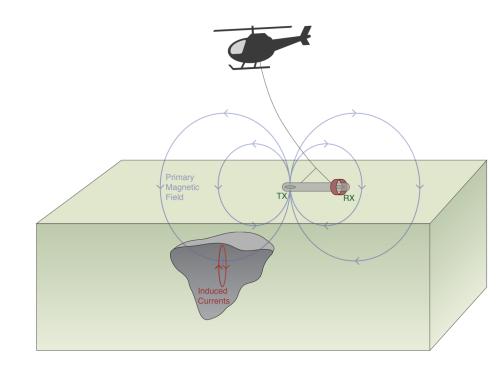




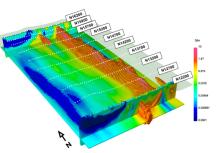
10⁴ Hz

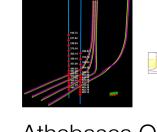
Recap: what have we learned?

- Basics of EM induction
- Response functions
- Mutual coupling
- Data for frequency or time
 domain systems
- Circuit model is a good proxy
- Need to account for energy losses
- Ready to look at some field examples

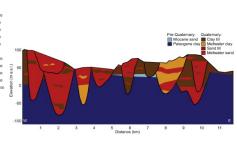


Case Histories

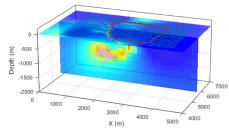




Athabasca Oil Sands, Canada: Monitoring

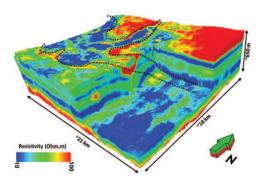


Kasted, Denmark: mapping paleochannels



HeliSAM at Lalore: Minerals



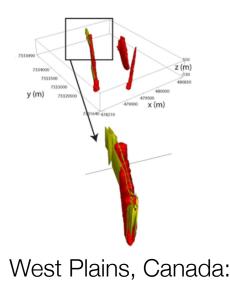


Wadi Sahba, Saudi Arabia: static corrections for seismic

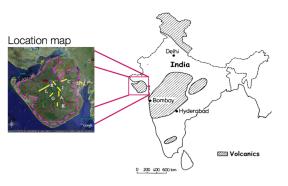


Bookpurnong, Australia: diagnosing river salinization

T R Dom João, Brazil: water flood monitoring

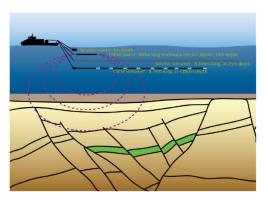


Mineral exploration

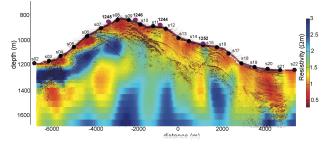


Deccan Traps, India: mapping sediment beneath basalt

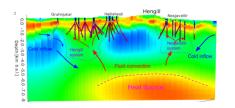
Case Histories



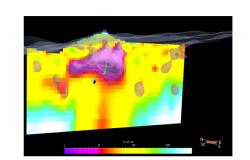
Barents Sea, Norway Hydrocarbon de-risking



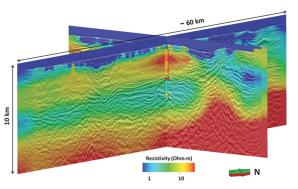
Hydrate Ridge, USA: Marine CSEM



Iceland: characterizing geothermal systems

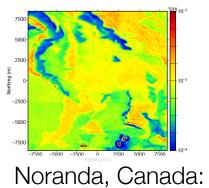


Santa Cecilia, Chile: Mineral Exploration



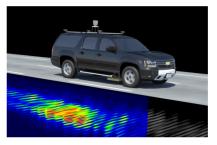
Red Sea: Mapping complex marine geology

Case Histories

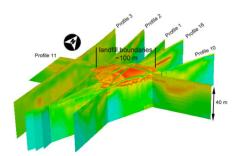


Geologic Mapping

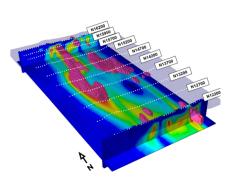
Balboa, Panama: Mineral Exploration



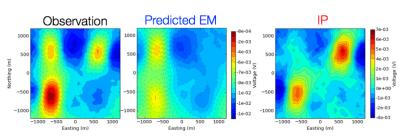
USA: Self-driving vehicles



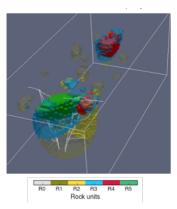
Denmark: IP for landfills



Mt. Isa, Australia: Mineral Exploration



EM – IP Inversion (decoupling)



TKC, Canada: Mineral Exploration

End of EM Fundamentals

