



# Experimental Investigation of turbulent swirling jets

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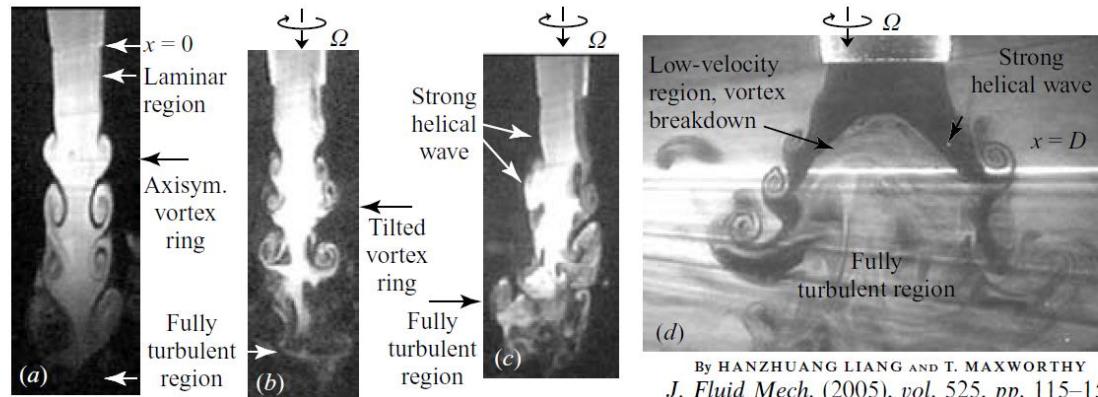
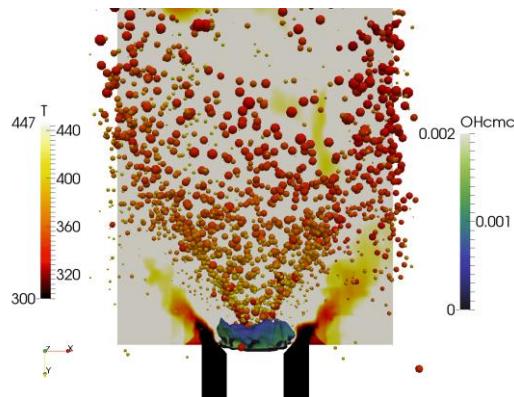


Barcelona, 2-5 July 2023

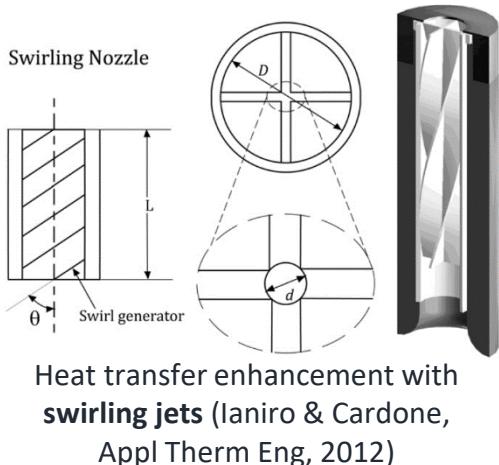


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# INTRODUCTION



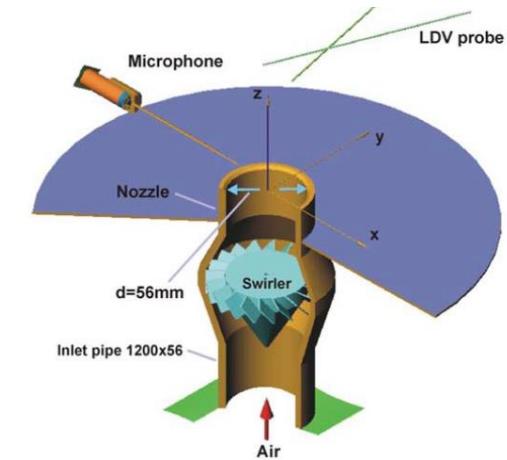
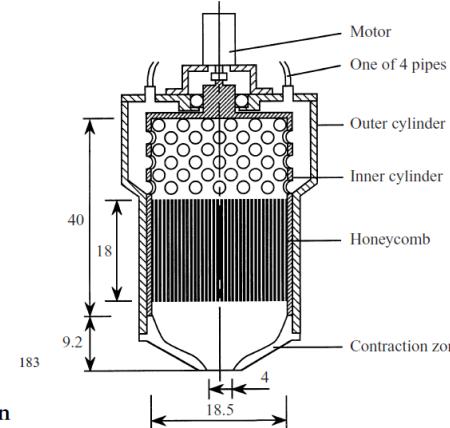
By HANZHUANG LIANG AND T. MAXWORTHY  
*J. Fluid Mech.* (2005), vol. 525, pp. 115–159.



*J. Fluid Mech.* (1998), vol. 376, pp. 183–219. Printed in the United Kingdom  
© 1998 Cambridge University Press

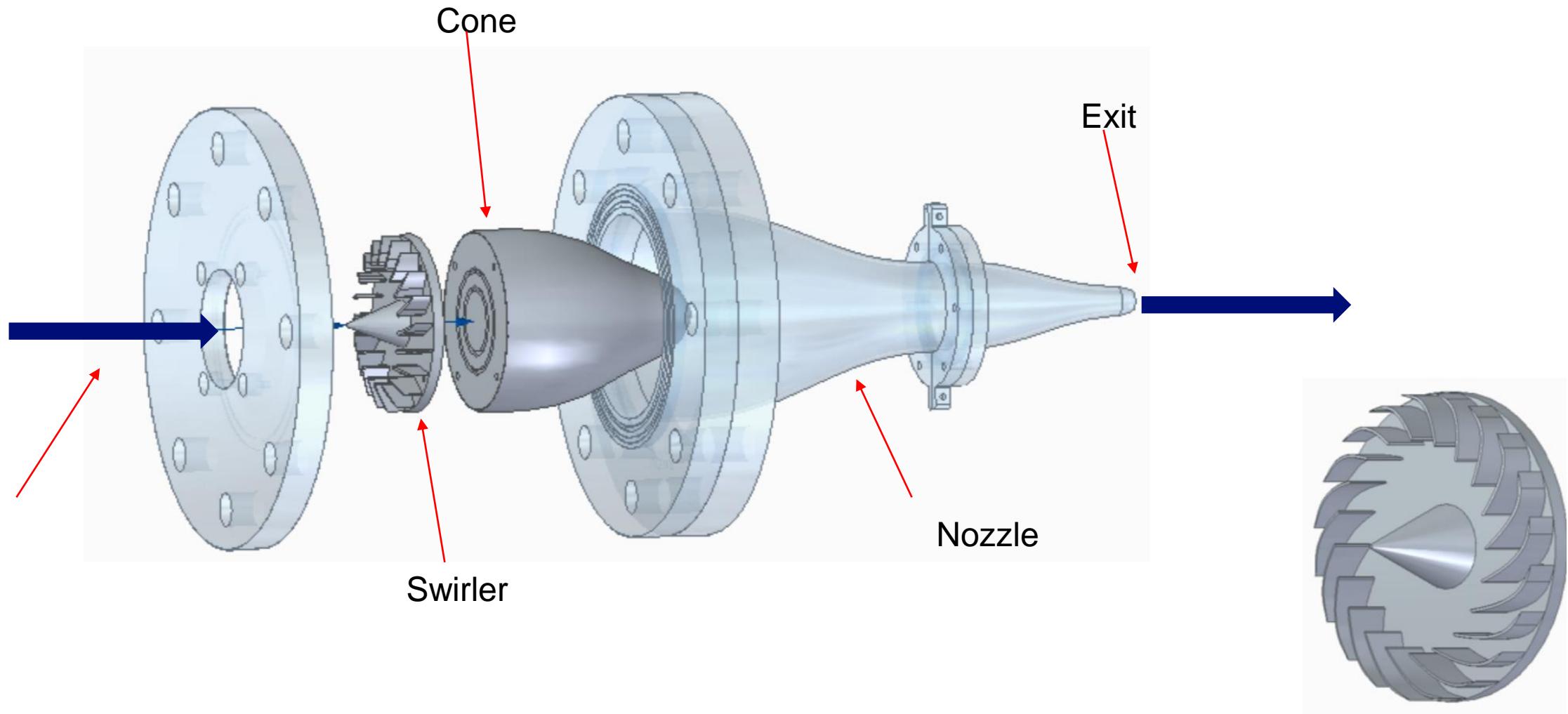
Experimental study of vortex breakdown in swirling jets

By PAUL BILLANT<sup>1,2</sup>, JEAN-MARC CHOMAZ<sup>1</sup>  
AND PATRICK HUERRE<sup>1</sup>

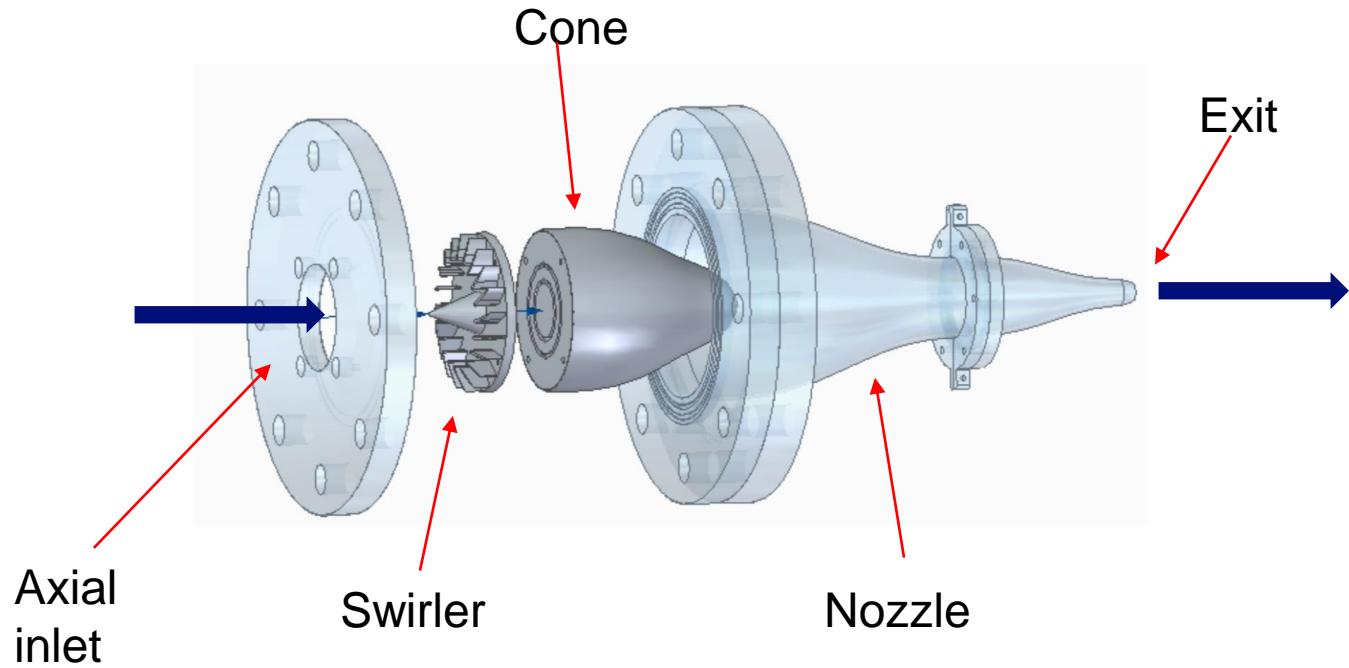


Cala et al. EiF 2006

# GEOMETRICAL DESIGN: CONCEPT



# GEOMETRICAL DESIGN



## Advantage:

- Simplicity

## Disadvantage:

- Less control on effective swirl number

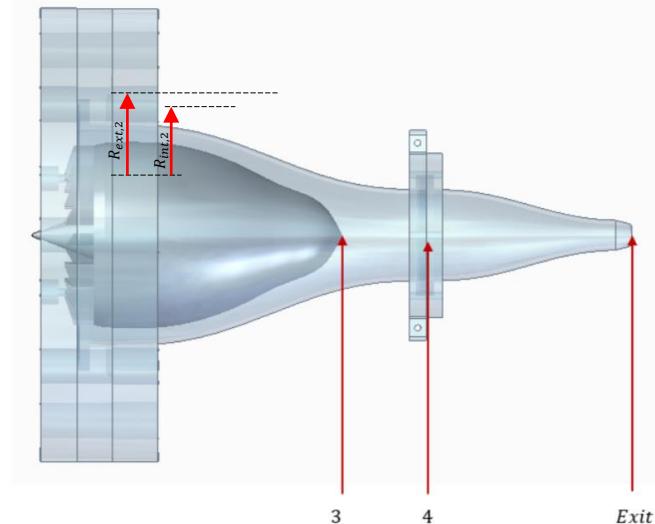
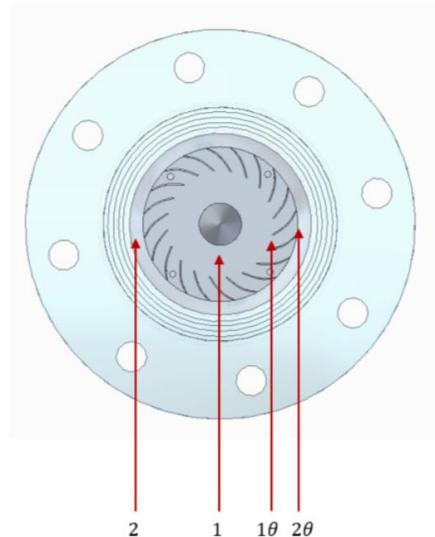
$$S = \frac{G_\theta}{D/2 G_x}$$

# GEOMETRICAL DESIGN

Assumption:

- **Conservation of momentum**

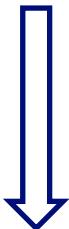
$$G_\theta = 2\pi\rho \int_0^R U_x U_\theta r^2 dr$$
$$G_x = 2\pi\rho \int_0^R U_x^2 r dr$$



$$G_\theta \rightarrow U_{x,2} U_{\theta,2} \frac{R_{ext,2}^3 - R_{int,2}^3}{3}$$
$$G_x \rightarrow U_{x,exit}^2 \frac{R_{exit}^2}{2}$$

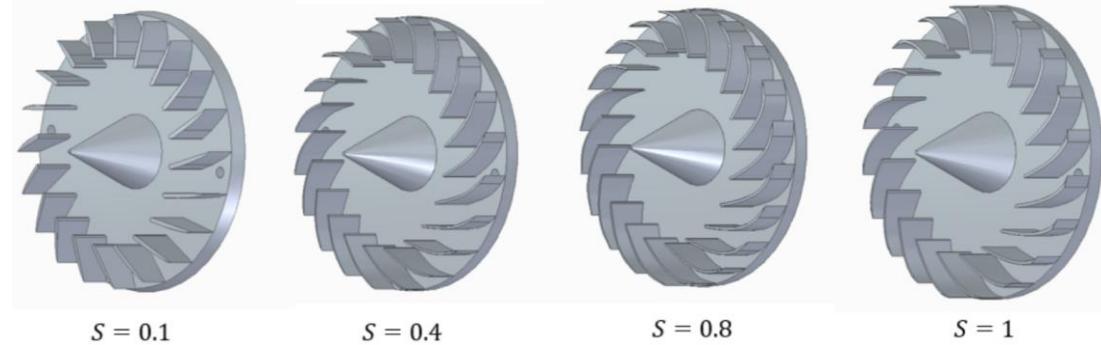
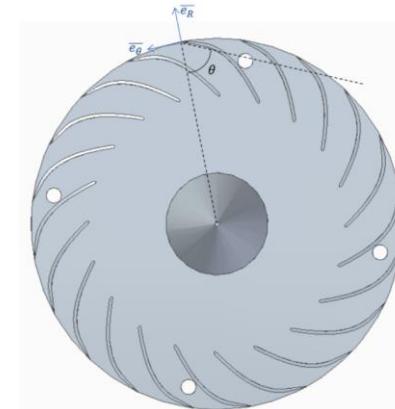
# GEOMETRICAL DESIGN

$$S = \frac{G_\theta}{D/2 G_x} = \frac{2}{3} \frac{U_{x,2} U_{\theta,2}}{U_{x,exit}^2} \frac{{R_{ext,2}}^3 - {R_{int,2}}^3}{{R_{exit}}^3}$$

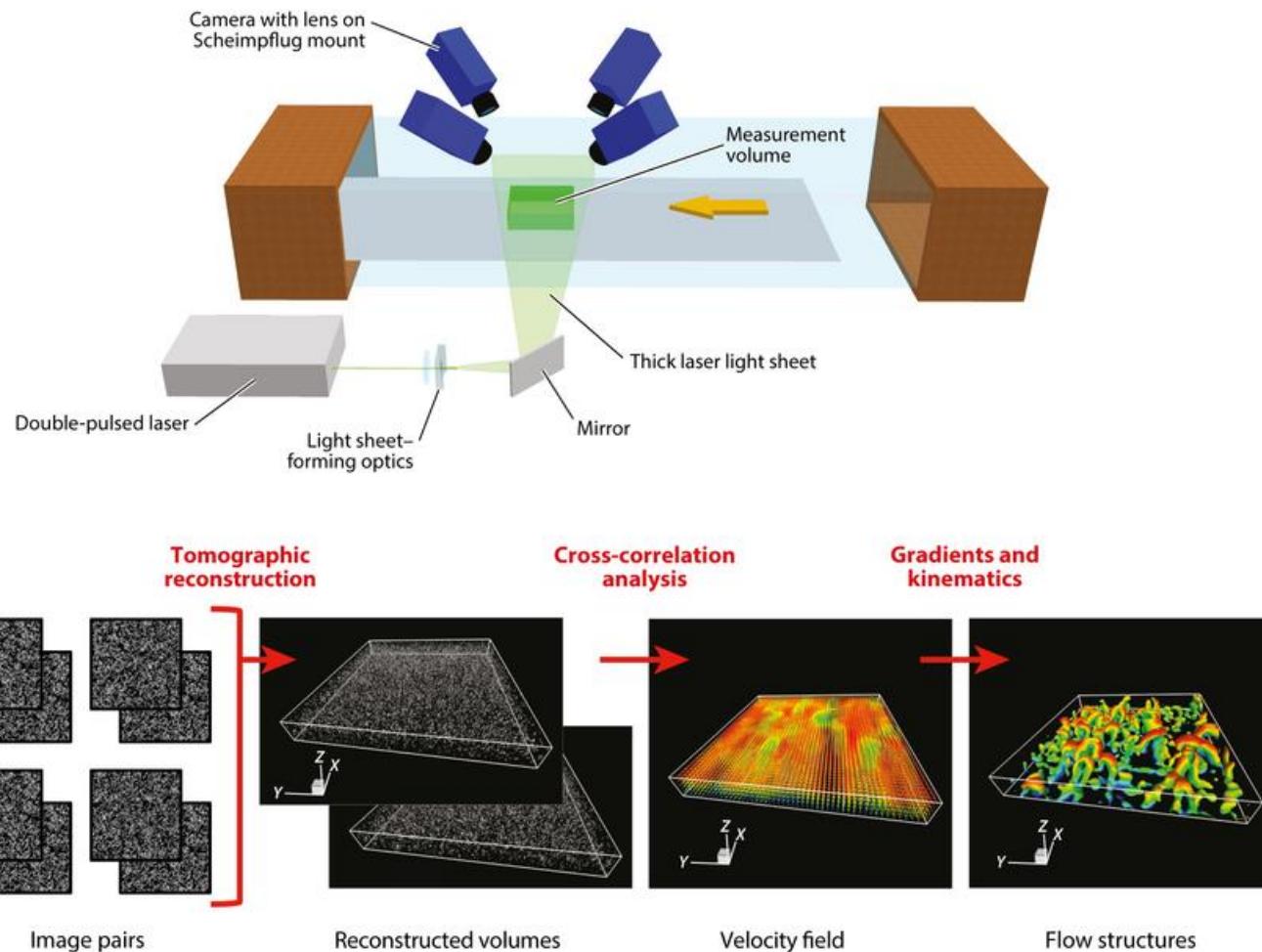


**MASS CONSERVATION**

$$S = \frac{{A_{exit}}^2}{A_2 A_{2,\theta}} \frac{{R_{ext,2}}^3 - {R_{int,2}}^3}{{R_{exit}}^3} \frac{2 \tan \theta}{3}$$



# EXPERIMENTAL SETUP



 Westerweel J, et al. 2013.  
Annu. Rev. Fluid Mech. 45:409–36

# EXPERIMENTAL SETUP

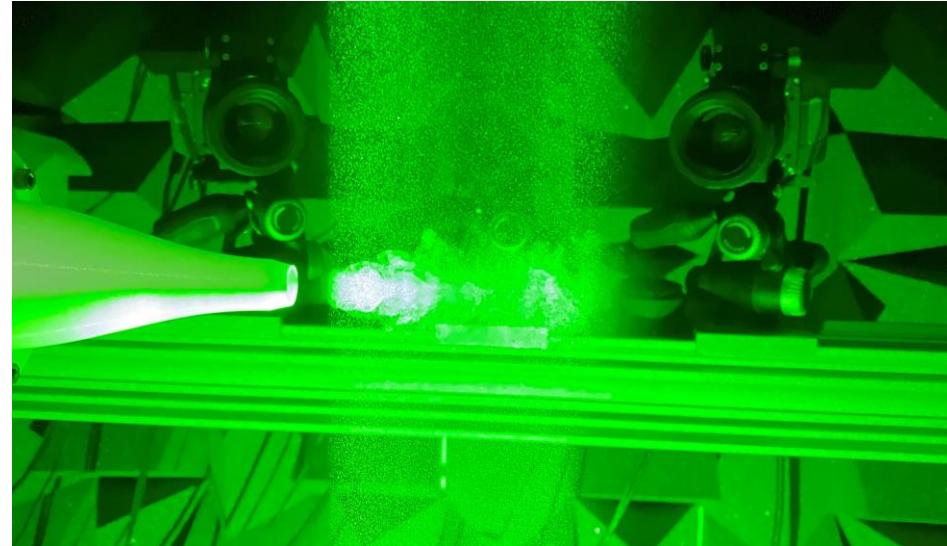
LASER &  
OPTICS



CAMERAS



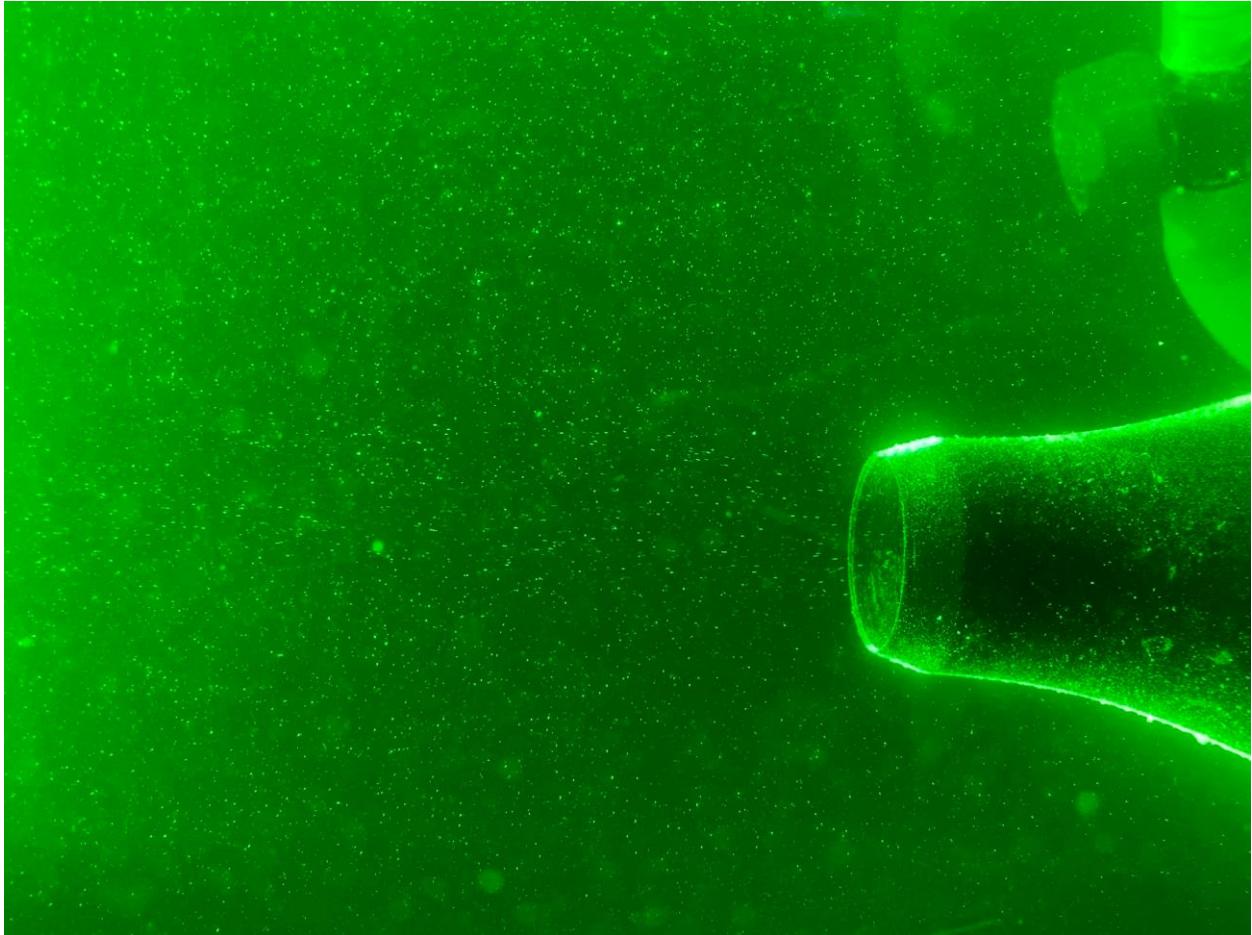
$$D = 1\text{cm}$$
$$Re = 35000$$
$$\dot{m} = 5 \frac{\text{g}}{\text{s}}$$
$$V = 6.40 \times 5.75 \times 0.50 D$$



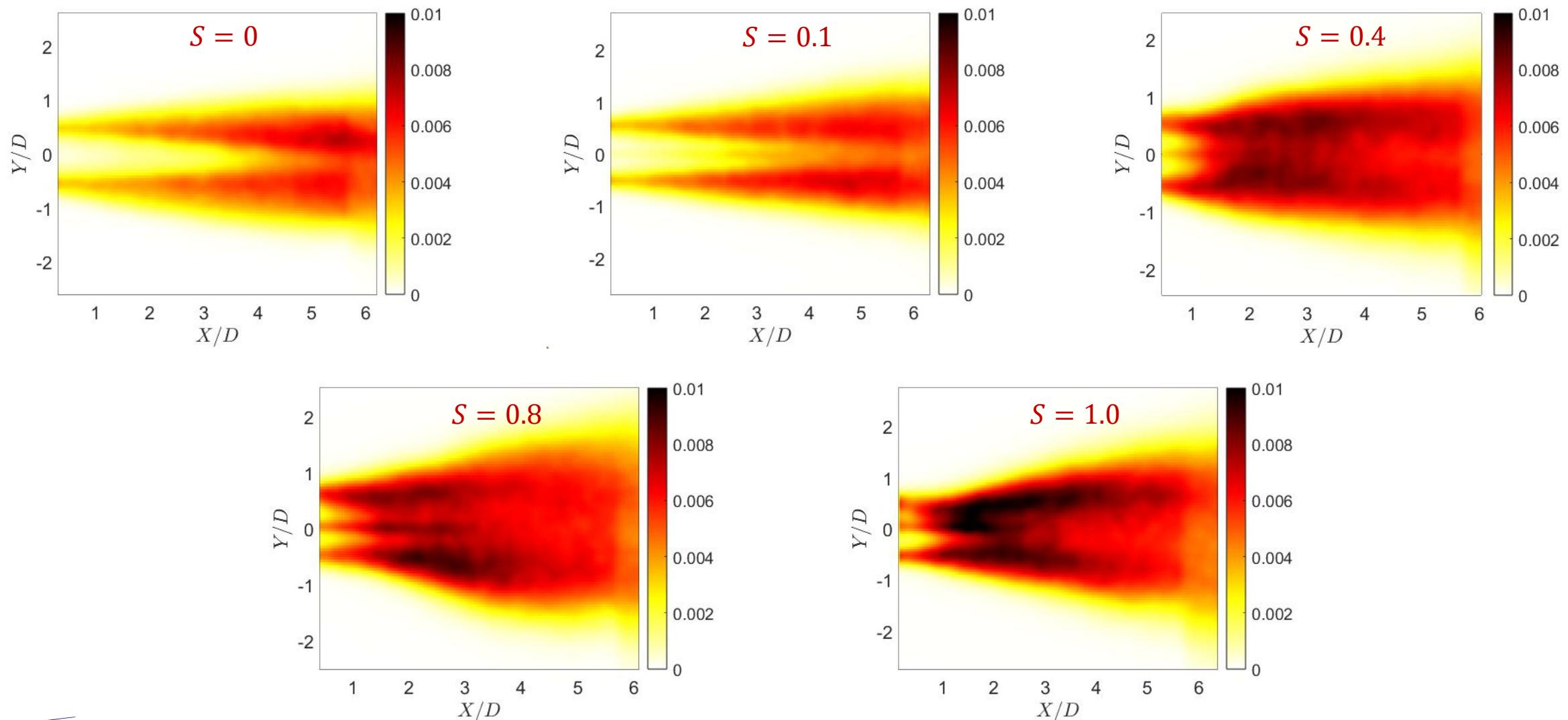
THIN TOMO  
PIV

# SWIRLING JETS IN WATER

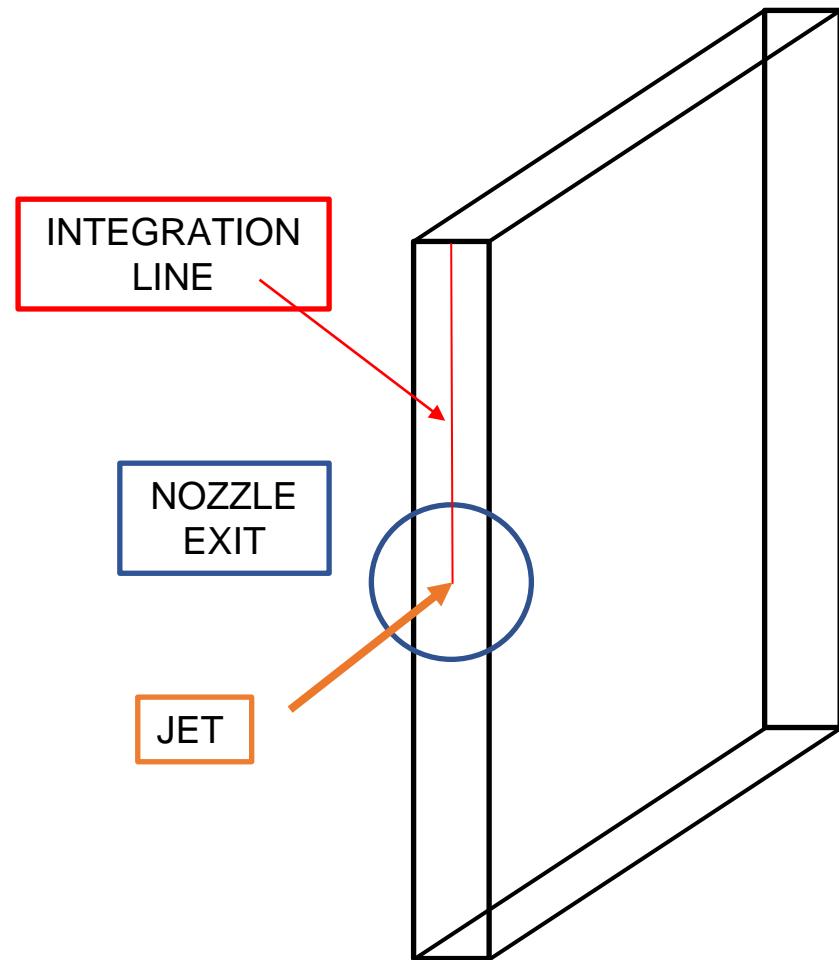
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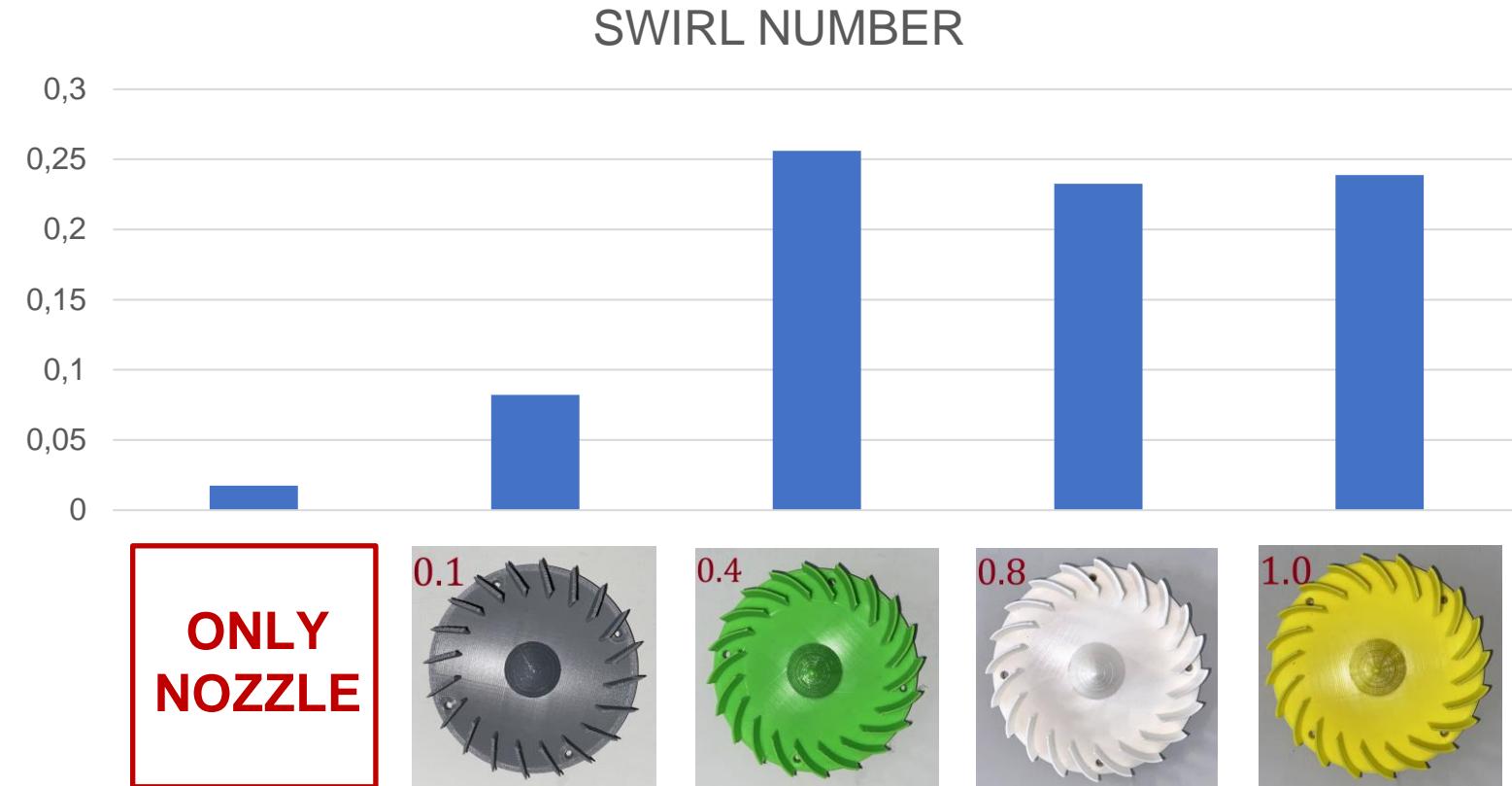
# PIV RESULTS: TURBULENT KINETIC ENERGY



# PIV RESULTS



$$S = \frac{2}{D} \frac{\int_0^{\infty} U_x U_{\theta} r^2 dr}{\int_0^{\infty} (U_x^2 - U_{\theta}^2 / 2) r dr}$$

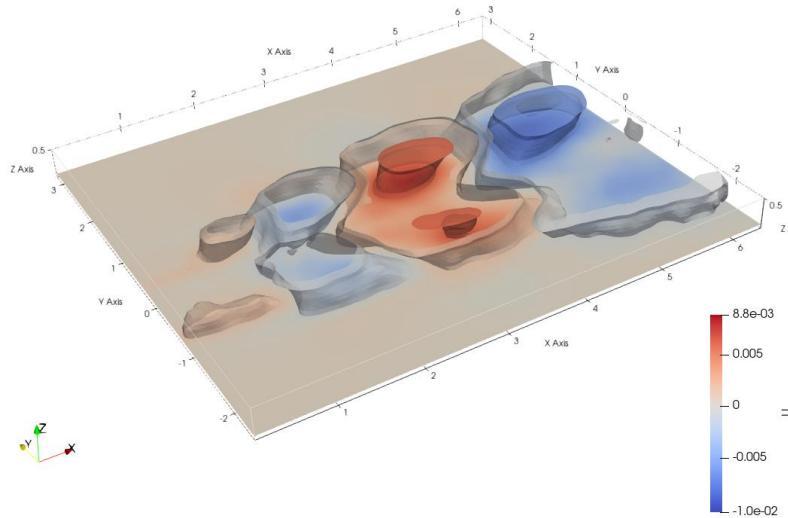


# PIV RESULTS: POD MODES – $S = 0.4$

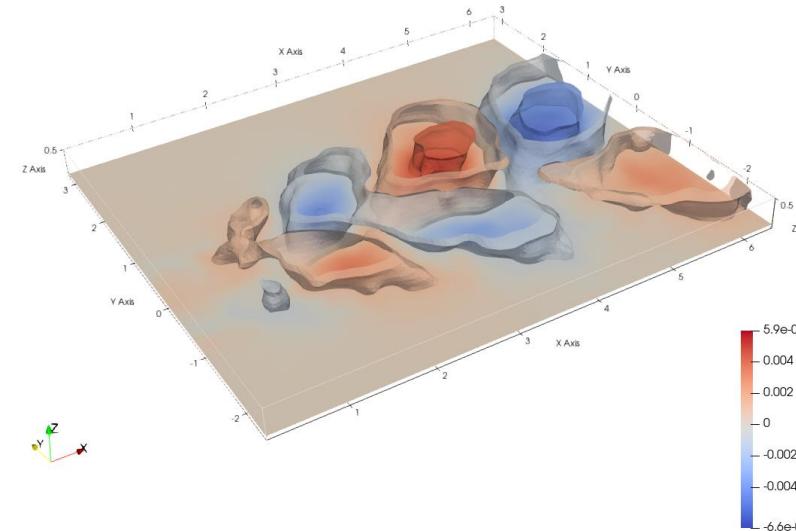
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$$[u', v', w'] = \Psi \Sigma \Phi$$

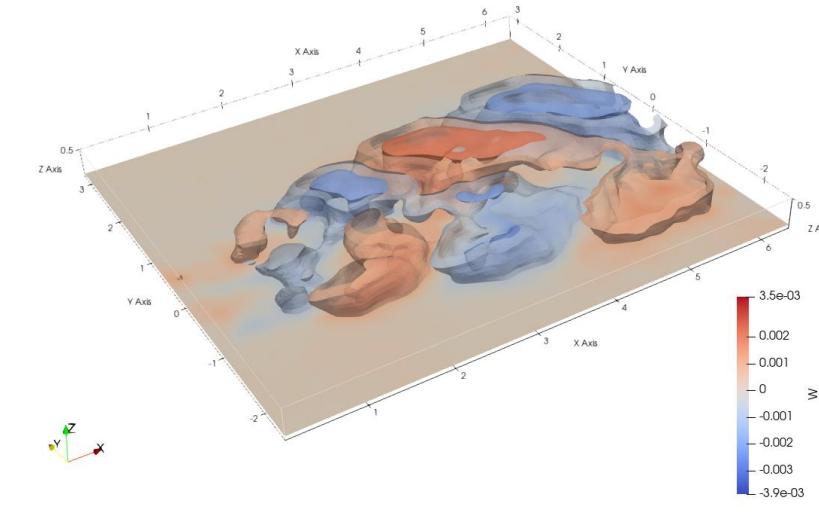
$\Phi_u$



$\Phi_v$



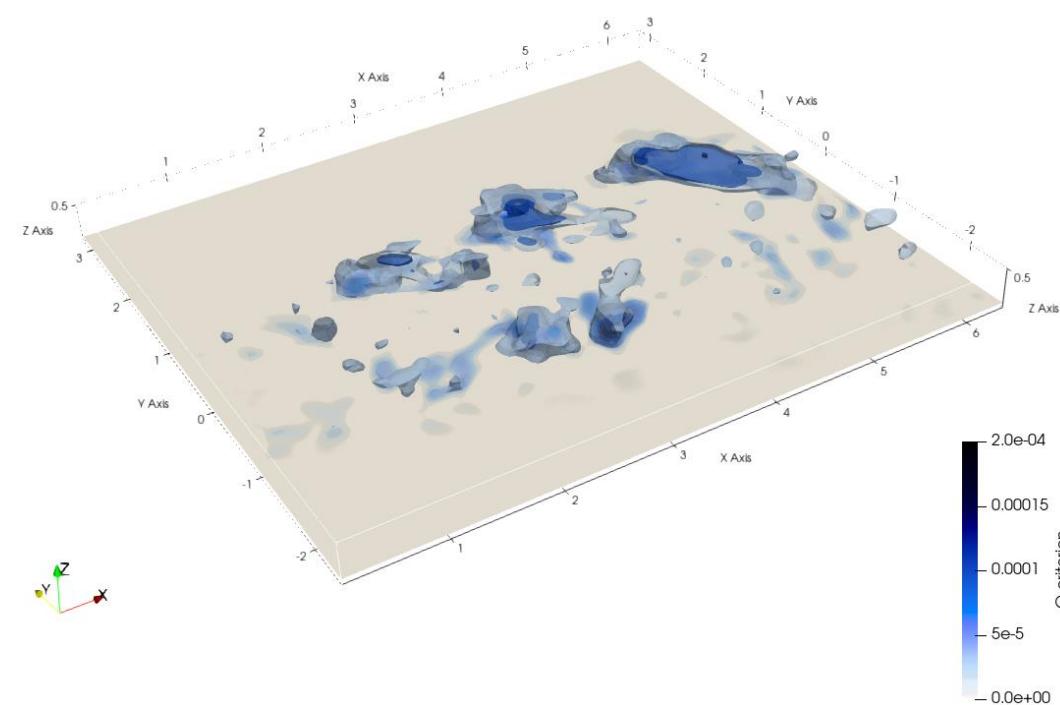
$\Phi_w$



# PIV RESULTS: POD MODES – $Q$ – criterion

$$S = 0.4$$

1<sup>st</sup> POD mode



# SUMMARY

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- Preliminary assessment of a concept of “geometrical swirl nozzle”
- The method is accurate for low swirl ( $S = 0.4$ )
- Larger swirl numbers are more difficult to reproduce

## FUTURE DEVELOPMENT

- Address Reynolds number effect and nozzle geometry on exit swirl
- Identify empirical scalings for the design of the geometrical swirl nozzle



# Experimental Investigation of turbulent swirling jets

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