

Name:

Class quiz 2

Feb 2, 2018

I) Evaluate the following integral:

$$\text{a- } \int_0^{\frac{\pi}{2}} \cos \theta \cdot \cos(\pi \sin \theta) d\theta$$

$$u = \pi \sin \theta \\ du = \pi \cos \theta d\theta$$

$$\begin{array}{ll} \theta=0 & u=0 \\ \theta=\frac{\pi}{2} & u=\pi \end{array}$$

$$\begin{aligned} &= \frac{1}{\pi} \int_0^{\pi} \cos(u) du \\ &= \left. \frac{\sin(u)}{\pi} \right|_0^{\pi} = 0 \end{aligned}$$

$$\text{b- } \int_1^2 (x+1)(x^2+2x)^3 dx$$

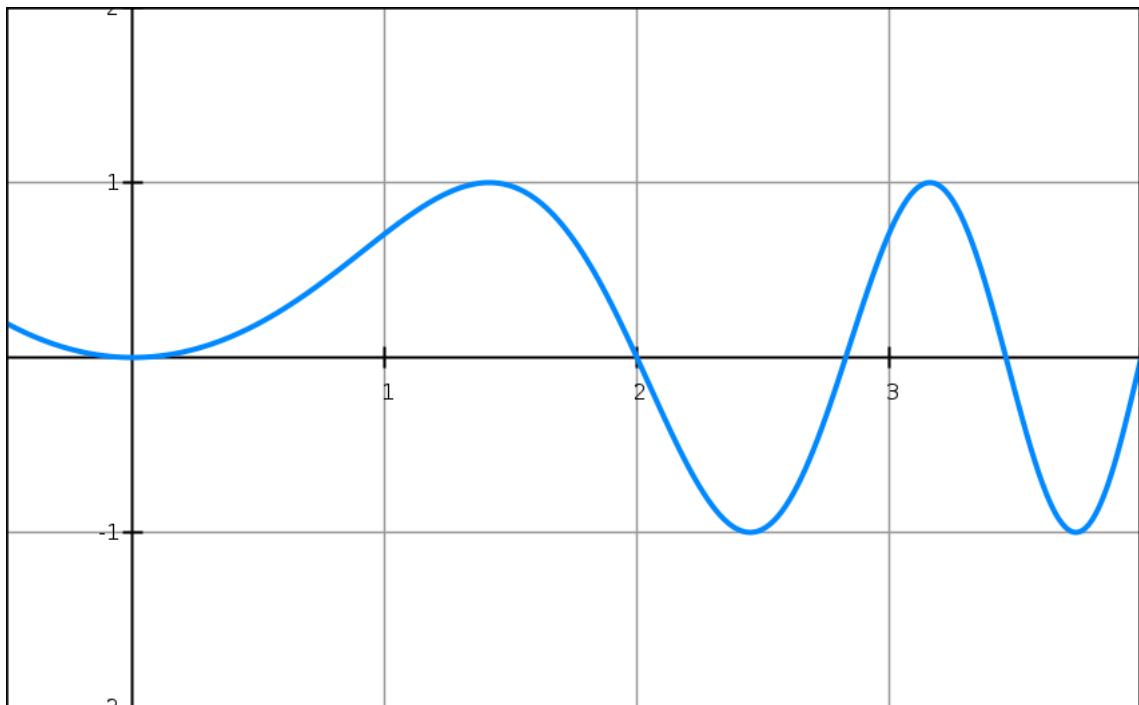
$$\begin{aligned} u &= x^2 + 2x \\ du &= (2x+2)dx \\ &= 2(x+1)dx \end{aligned}$$

$$\begin{array}{ll} x=1 & u=3 \\ x=2 & u=8 \end{array}$$

$$= \frac{1}{2} \int_3^8 u^3 du$$

$$= \left. \frac{u^4}{8} \right|_3^8 = \frac{8^4}{8} - \frac{3^4}{8}$$

II) Given the following graph of a function $f(x)$.



Define $g(x) = \int_0^x f(t)dt$ on the interval $[0,4]$.

a- At what value x does g have an absolute maximum on $[0,4]$.

at $x=2$

b- At what value x does g have an absolute minimum on $[0,4]$.

at $x=0$

c- On what interval is g increasing.

on $(0,2)$ and $(2.8, 3.5)$