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In Situ Electron Microscopy Investigation of Sodiation of Titanium Disulfide Nanoflakes

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Supporting Information

ABSTRACT: Two-dimensional (2D) metal sulfides show great promise for their potential applications as electrode materials of sodium ion-batteries because of the weak interlayer van der Waals interactions, which allow the reversible accommodation and extraction of sodium ions. The sodiation of metal sulfides can undergo a distinct process compared to that of lithiation, which is determined by their metal and structural types. However, the structural and morphological evolution during their electrochemical sodiation is still unclear. Here, we studied the sodiation reaction dynamics of TiS₂ by employing *in situ* transmission electron microscopy and first-principles calculations. During the sodium-ion intercalation process, we



observed multiple intermediate phases (phase II, phase Ib, and phase Ia), different from its lithiation counterpart, with varied sodium occupation sites and interlayer stacking sequences. Further insertion of Na ions prompted a multistep extrusion reaction, which led to the phase separation of Ti metal from the Na₂S matrix, with its 2D morphology expanded to a 3D morphology. In contrast to regular conversion electrodes, TiS_2 still maintained a compact structure after a full sodiation. First-principles calculations reveal that the as-identified phases are thermodynamically preferred at corresponding intercalation/extrusion stages compared to other possible phases. The present work provides the fundamental mechanistic understanding of the sodiation process of 2D transition metal sulfides.

KEYWORDS: *titanium disulfide, sodium-ion batteries, in situ transmission electron microscopy, multistep sodiation, density functional theory*

n recent years, the Li-ion battery (LIB) industry has been continuously expanding due to the steadily increasing demands of a growing market for portable electronic devices.¹⁻³ Nevertheless, the rising cost and unbalanced

Received: May 30, 2019 Accepted: August 6, 2019 Published: August 6, 2019

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Figure 1. (a) XRD pattern of pristine TiS_2 nanoflakes. (b) HAADF-STEM image and (c) HR-STEM image of TiS_2 nanoplates seen along the [001] zone axis. The atomic model overlapping with the enlarged image is shown in the inset. Blue and yellow dots indicate Ti and S, respectively. (d) Galvanostatic discharge curve of the TiS_2 coin cell between 3.0 and 0.1 V. SAED patterns of (e) pristine single nanoflakes and (f) after discharging to 0.1 V.

geometric distribution of lithium resources make it cogent to exploit alternative energy storage systems, such as sodium-ion batteries, which are based on the earth-abundant element sodium.^{4–6} Both Li and Na are alkali metal elements with similar chemical properties, which allows that the development of sodium-ion batteries (NIBs) can be benefitted greatly from the knowledge developed for LIBs.⁷ However, the larger atomic radius and different electronegativity of Na ions directly affect the ion transport and storage in the electrochemical process, making some two-dimensional layered LIB electrode materials, such as graphite, unsuitable for NIBs.^{8–10} Promising electrode materials for NIBs are clearly needed for further improvements.

Two-dimensional transition metal dichalcogenides (TMDs) adopt layered structures, where metal atoms are sandwiched between chalcogen atoms in a hexagonal arrangement, with neighboring layers interacting through weak van der Waals forces.¹¹⁻¹ This layered structure makes TMDs insertion hosts to accommodate foreign atoms.^{14,15} For example, MoS₂, SnS₂, CuS, ReS₂, SnSe₂, etc., recently have been extensively explored for the applications of LIBs or NIBs. $^{16-20}$ Among the TMDs, titanium disulfide (TiS_2) has a high electronic conductivity $(2 \times 10^2 \text{ S/cm at } 25 \text{ °C})^{21}$ and a wide interlayer spacing between Ti-S layers, capable of accommodating large guest cations such as Na and K ions.²² Originally, TiS₂ was explored as a cathode material for LIBs in the 1970s, and recently it started to draw attention from the NIB field.^{23,24} The Na/TiS₂ cell displayed a modest specific capacity of 188 mAh g⁻¹ at 0.2 C rate and retained a reversible capacity of 170 mAh g^{-1} after 100 cycles.²⁵ Great efforts have been made in order to improve its rate capability and cyclability.^{26,27} Despite the chemical similarity of Li and Na, reaction pathways in TiS₂ may be different because of (i) differences in ionic radius (Li⁺:

0.76 Å, Na⁺: 1.02 Å) and standard reduction potential (Li⁺/Li: -3.04 V, Na⁺/Na: -2.71 V vs standard hydrogen electrode);⁷ (ii) distinct structures of stoichiometric Na-TiS₂ compounds: NaTiS₂ has $R\overline{3}m$ structure, while LiTiS₂ has $P\overline{3}m1$ structure;²⁸ (iii) possible trigonal prismatic coordination only possible with Na.²⁹ Further improvement of the performance of the TiS₂ electrode demands a comprehensive understanding of the sodiation mechanism. This challenge has motivated researchers to investigate the sodiation process using various experimental characterizations^{27,30,31} and numerical simulation methods.^{29,32,33}

As revealed in previous X-ray diffraction (XRD) results, 21,25,30 the sodiation of TiS₂ undergoes an intercalation process:

$$x \operatorname{Na} + \operatorname{TiS}_2 \to \operatorname{Na}_x \operatorname{TiS}_2 \left(0 < x < 1 \right) \tag{1}$$

The phase transitions of the Na_xTiS₂ system were investigated via electrochemical and X-ray techniques in samples intercalated with the liquid ammonia technique, and several intermediate phases during the sodiation process were reported that are different from the lithiation process: 0.17 < x< 0.33 (II), 0.38 < x < 0.72 (Ib), and 0.79 < \hat{x} < 1 (Ia).^{31,32,34} The difference in reaction mechanism is assumed to be related to the larger ionic radius of the Na ion, which affects the bonding nature between guest ions and titanium sulfide layers. The density functional theory (DFT) calculations also showed the existence of phase Ib and phase Ia with different Na ordering in the P3 and O3 host (using the notation of Delmas) and predicted the phase transition of $O1-P3 \rightarrow P3 \rightarrow O3$ as the Na ion concentration increases, whereas previous transmission electron microscopy (TEM) studies only showed the existence of an ordered $Na_{0.25}TiS_2$ superstructure.^{29,33,35–37} Indepth real-time investigations are demanded to elucidate the



Figure 2. (a) In situ electron diffraction intensity profile as a function of reaction time during sodiation of TiS_2 . (b) Sodium-ion-insertioninduced lattice changes measured from the TiS_2 diffraction spot during intercalation. Each symbol represents each plane. The different background color means different dominant phase: purple (pristine), blue (II), dark green (Ib), and light green (Ia). The orange background color shows the extrusion phases: Na_2S (Fm3m), TiS (R3m), Ti_2S (Pnnm), and Ti (P6/mmm). (c) Atomic models representing intermediate phase evolution during intercalation with different anion stacking sequences and Na configurations.

exact phase transformation and associated Na-insertion geometries of the TiS_2 host. Up to now, the dynamics of phase transitions along with the morphological and mechanical changes during sodiation are still not well understood.

In this study, we have employed an in situ TEM technique to investigate the structural evolution of TiS2 nanoflakes during sodiation in real time. With in situ selected area electron diffraction (SAED) complemented with DFT calculations, we have identified three intermediate phases, phase II (Na_{0.33}TiS₂), phase Ib (Na_{0.55}TiS₂), and phase Ia (NaTiS₂), in which the sodium-occupied sites and the anion stacking sequence evolution have been elucidated with the insertion of Na ions along Ti-S layers. Combined with in situ scanning TEM (STEM) imaging, we observed the propagation of the phase boundary of the intermediate phases in a single flake. Our results elucidate three sequential reaction steps in the intercalation process. These intercalation reactions occur along the in-plane TiS₂ layer and do not destroy the Ti-S layered structure. Moreover, we find that further Na ions will prompt an extrusion reaction through multiple steps to produce Ti and Na₂S sequentially, as revealed by in situ SAED and ex situ highresolution TEM. In an extrusion reaction, the morphological structure changes from two dimensions to three dimensions. Our work provides a mechanistic understanding of the

structural evolution and electrochemistry of the sodiation process of TMDs.

RESULTS AND DISCUSSION

The structure of the pristine TiS2 nanoflakes was revealed as the hexagonal structure of 1T-TiS₂ matching JCPDS card no. 88-1967 (with a space group of $P\overline{3}m1$) by XRD (Figure 1a), without any noticeable impurity phases.³⁸ Figure 1b,c show a low-magnification high-angle annular dark field scanning TEM (HAADF-STEM) image and an atomic-resolution HAADF-STEM image along the [001] zone axis, respectively. The nanoflake exhibits a good crystallinity, and an atomic model with sulfur and titanium atoms is shown in the inset of Figure 1c. Figure 1d shows a galvanostatic discharge curve of TiS₂ under a constant current density of 12 mA g^{-1} in a coin cell. The initial discharge capacity reaches 450 mAh g^{-1} . Since the theoretical capacity of TiS_2 is 239 mAh g⁻¹ (corresponding to 1 Na ion uptake) from the intercalation reaction process, enhanced capacity indicates more than one Na ion inserted into one chemical unit of TiS₂. The voltage profile shows two plateaus at 2.2 and 1.6 V and one slope between them, which are associated with the Na-ion intercalation into Ti-S layers.^{25,26} At the end of these intercalation reactions, TiS₂ is supposed to transfer to NaTiS2. Further discharge to 0.4 V



Figure 3. (a) In situ time-sequential dark field STEM images directly showing the movement of the phase boundary during a multistep intercalation reaction. (b) Evolution of the projected area of each intermediate phase as a function of sodiation reaction time. (c) Diffusivity of sodium ions in TiS_2 calculated from (a).

triggers further insertion of Na-ions, resembling an extrusion reaction resulting in the formation of metallic Ti.

This is evidenced by the comparison of SAED patterns at the pristine state (Figure 1e) and discharged state (Figure 1f), respectively. After discharging to 0.1 V, Ti and Na₂S phases, as well as the possible Ti₂S, are observed, indicating the equations

 $4Na + 2NaTiS_2 \rightarrow 3Na_2S + Ti_2S \tag{2}$

$$2Na + Ti_2S \rightarrow Na_2S + 2Ti$$
(3)

Since the theoretical capacity after the reaction (corresponding to uptake of 4 Na ions) indicated in eq 3 should be 957 mAh g^{-1} , the reaction here is not complete, as indicated from the discharge curve. The Ti₂S phase is supposed to be an intermediate phase. Additionally, *ex situ* high-resolution TEM (HRTEM) images and STEM-electron energy-loss spectroscopy (EELS) mapping of the discharged TiS₂ electrode in Figure S1 confirmed the existence of Ti and Na₂S phases, and the extrusion reaction occurred during full discharge to 0.1 V in the first cycle. The reversibility of electrochemical performance and the structure of the electrode after 1 cycle were characterized, as shown in Figure S2. The reversible capacity is about 250 mAh g^{-1} , and the electrode shows a TiS₂ phase with a uniform distribution of Ti and S elements (Figure S2c). Real-time structural evolution of TiS_2 during the sodiation is integral to understand the mechanism of reaction.

To study the structural evolution of TiS₂ in real time, we employed the *in situ* dry-cell TEM technique,³⁹ which has been applied to study the phase evolution of electrode materials for batteries at atomic resolution.⁴⁰⁻⁴² Figure 2a presents the radial intensity profiles as a function of reaction time retrieved from an in situ SAED experiment. Raw video and SAED patterns can be found in the Supporting Information, Movie S1 and Figure S3, respectively. The intensity profiles were retrieved by integrating the intensity of a series of SAED patterns across the full 2π range along the *r* direction. The final intensity profile was acquired after background subtraction using a power-law model in Figure 2a. It can be seen that the intensity of Bragg reflections formed changed or disappeared in cases, indicating the phase evolution with the proceeding of sodiation. From the pristine phase to the intercalated phase, the three intermediate phases are attributed to a C2/m phase (phase II, Na_xTiS_2 , 0.17 < x < 0.33), a P1 phase (phase Ib, Na_xTiS_2 , 0.38 < x < 0.72), and an $R\overline{3}m$ phase (phase Ia, Na_xTiS_2 , 0.79 < x < 1), respectively. The *in situ* SAED here cannot quantify the amount of Na ion inserted into the system but only reflects the structural information. These phases were proposed in previous studies on TiS₂'s sodiation^{32,43} and confirmed later in the DFT calculations of this work. Our



Figure 4. (a) BF-STEM images showing the whole process of phase evolution. The overlaid false colors indicate three different phases: pristine TiS_2 (purple), $NaTiS_2$ (light green), and $Ti+Na_2S$ (orange). (b) Changes in length along two directions as a function of reaction time. (c) Model of the morphology changes from a 2D plate to 3D bulk.

results indicate that these phases can coexist while proceeding within the field of view, indicating the sodiation inhomogeneity in one nanoflake. We plotted the changes of lattice parameters as a function of reaction time based on the in situ SAED (Figure 2b and Figure S3). During the whole Na-ion intercalation processes, the in-plane lattice parameters changed marginally, which was consistent with a typical 2D material intercalation process. Our in situ SAED result of the intercalation process can be repeatedly observed from another single nanoflake as shown in Figure S4 and Movie 2. The three-step phase transition in the intercalation process was observed from the real-time investigation. Atomic models of these intermediate phases are shown in Figure 2c. The initial Na-ion intercalation prompted the phase transition from the $P\overline{3}m1$ (pristine, O1 host) phase to the C2/m (phase II, O1–P3 host) phase until a nominal composition of x = 0.17, in which Na ions filled every two channels between Ti-S layers (stage 2), which may induce the formation of superlattice reflections.³⁷ Phase II (O1-P3 host) is a hybrid stacking that combines octahedral sites and trigonal prismatic sites, in which the trigonal prismatic sites are partly filled with Na ions (A or C sites), while the octahedral sites are empty. Prismatic Na-ion sites (α and β shown in Figure S5) share one face with a Ti-S octahedron directly above or directly below it, which

makes the two prismatic sites symmetrically equivalent.³³ The insertion of Na ions triggered a sliding of every other S-Ti-S layer in the host structure, and the S anion layer stacking followed a distinct AB-AB-BC-BC-CA-CA stacking mode.³ Na-ion ordering in one layer is shown in a top-view depiction of Figure 2c, and the interlayer distance is not the same due to the Na-ion nonuniform insertion. The distance of the adjacent Ti-Ti layer with Na ions filling sites enlarged about 21%, while the Ti layer distance without Na ions expanded less than 2%. With further Na-ion insertion, the C2/m phase transferred to the P1 (phase Ib, P3 host) phase. The phase Ib exhibits an AB-BC-CA stacking sequence of S with Na ions occupying only trigonal prismatic sites. Lithium ions in LixTiS2 do not occupy trigonal prismatic sites due to their relatively smaller ionic size,²⁹ while Na ions with large size can stabilize the trigonal prismatic structure by reducing electrostatic repulsion between anions. With the further intercalation of Na ions, the final $R\overline{3}m$ (phase Ia, O3 host) phase is found with an AB-CA-BC anion stacking, where all the prismatic sites of Na ions are transferred to octahedral sites with the shifting of Ti-S layers, which leads to the shorter interlayer spacing along the c direction and longer spacing along the a direction. For the whole intercalation process, the cell volume was expanded about 20.5%, and each of these host structures can transform



Figure 5. HAADF-STEM images of TiS_2 nanoplates showing the morphology (a) before and (b) after *in situ* sodiation and SAED patterns (c) before and (d) after, respectively. (e) HRTEM image after sodiation and (f) an enlarged image from the selected area in (e), showing the lattice patterns of Ti and Na₂S. Insets are the FFT patterns from the selected areas in (f).

into the other phase sequentially through a simple gliding of the Ti-S layers without the breaking of Ti-S bonds, as shown in Figure 2c.

After intercalation reaction processes, we found that excessive Na ions can trigger an extrusion reaction. After about 1000 s, additional reflections appeared in the electron diffraction intensity profile (Figure 2a and Figure S3), which can be attributed to the phases of Na₂S ($Fm\overline{3}m$), TiS ($R\overline{3}m$), Ti_2S (*Pnnm*), and Ti (*P6/mmm*), respectively. The coexistence of TiS, Ti₂S, and Ti implies an extrusion reaction process and an inhomogeneous degree of sodiation among the same nanoflakes. The extrusion reaction was not completed even after 2000 s, where reflections from TiS and Ti2S were identified in the frame of 2062 s (Figure S3). This suggests that Ti separating from NaTiS₂ nanoflakes underwent an extrusion reaction mechanism rather than a conversion reaction. The mechanistic understanding of the morphological evolution and sodiation dynamics is a significant consideration in the design of high-performance nanostructured electrodes.

To understand the sodiation dynamics of TiS₂ in real space, an in situ STEM technique was applied to monitor the microstructural evolution of a single TiS₂ nanoflake upon Naion insertion shown in the time-lapsed images of Figure 3a. The raw annular dark-field (ADF)-STEM images and video are shown in the Supporting Information (Figure S6 and Movie 3). At 266 s, the reaction front was observed to propagate from left to right upon sodiation under a bias voltage of -4.0 V, attributed to the phase transition (TiS₂ \rightarrow phase II). The second phase change was observed at 587 s along the same direction, corresponding to the transition from phase II to phase Ib. With further insertion of Na ions, the third reaction front was also observed at 1226 s, showing the abrupt change in morphology at the boundary of phases Ib and Ia. The difference in the first two steps is the serious deformation of the reaction interface (Figure S6) due primarily to the huge slippage between Ti-S-Ti layers and the expansion of Ti-Ti layers along the a and b directions. After the intercalation reaction, the pristine-layered structure shape was well maintained. The projected area changes as a function of time were measured from time-sequential STEM images during

three-step intercalation reactions (Figure 3b). As shown in Figure 3c, we can quantify the projection speed from the results of Figure 3b. The projection speed of the three phases is estimated to be 50-500 nm² s⁻¹ by calculating the projected reaction area change versus reaction time, based on the equation $D = \Delta S / \Delta t$, where D is the projected prolongation speed, ΔS is the change of projected reaction area, and Δt is the diffusion time. For a 2D structure, Na-ion intercalation occurs preferentially along the in-plane direction and between Ti-S slabs. Our analyses can give an estimation of the reaction kinetics, even though it varies with experimental factors, such as rate, loading, strain, and Na concentration. The lowmagnification HAADF-STEM images before and after the reaction are shown in Figure S7. Sodiation reaction occurred at whole nanoflakes as volume expansion proceeds along all inplane directions from the touch point, which further proved the reaction was not caused by electron beam radiation. In another in situ experiment, we observed not only the intercalation process but also the extrusion process under a higher bias voltage of -8.0 V that prompts the sodium ions to diffuse into the sample, as shown in Figure 4, Figure S8, and Movie 4. After the intercalation process, the extrusion reaction has started at 600 s and the volume expanded up to 17% at 1206 s (Figure 4b), leading to a large volume expansion. The surface became swollen, indicating the extrusion reaction front propagated forward (lateral traverse) and inward (shell-tocore). With further Na-ion diffusion, the projected area shrank and the surface bulged, indicating the two-dimensional (2D) nanoflake expanded to a three-dimensional (3D) bulk shape (Figure 4c). During the early stages of sodiation, the surface of the sample expands, and the inner sample undergoes a compressive stress. With further sodiation, the inner volume of the stressed particle expands and then induces the observed surface deformation. During the extrusion reaction process, more Na-ion insertion breaks the TiS₂ layered structure and surface swell deformation releases stress. The HAADF-STEM and SAED images before and after the in situ sodiation experiment are presented in Figure 5a-d. By comparing the before and after images, we can clearly see the changes. The pristine two-dimensional layered structure expanded to a three-



Figure 6. DFT simulation of the sodiation process in TiS₂ crystals. (a) Na–Ti–S phase diagram. (b) TiS_2 -NaTiS₂ convex hull with sodiated TiS₂ intermediate phases. (c) Discharge voltage profiles as a function of Na content in Na_xTiS₂ calculated from first-principles calculation. (d) Structure evolution during the sodiation process of TiS₂.

dimensional bulk structure. Many small particles were formed on the surface, and their phase structure was confirmed by SAED and HRTEM. The SAED results showed the existences of Ti₂S, Na₂S, and Ti. The separation of Ti and Na₂S should contribute to the volume expansion and morphological structure changes. HRTEM images after sodiation are also shown in Figure 5e and f. The existence of Na₂S and Ti is further confirmed. The morphology and phase structure after the entire sodiation reaction are understood. We investigated here the reaction mechanism of commercial TiS₂ nanoflakes. There might be some kinetic differences if nanoflakes have different sizes, but the reaction mechanism revealed in this work should be applicable in most cases. All in all, the in situ electron diffraction and STEM imaging in this work provides us information about phase evolution and the morphological changes during the full sodiation reaction. This information is important for the mechanical modeling of a practical battery.

Phase diagrams constructed using first-principles calculations-computed energies have been broadly used to demonstrate the thermodynamic phase equilibrium of multicomponent systems and predict chemical reactions between phases.⁴⁴ Here in this study, we built the ternary Na–Ti–S phase diagram using the structures that have the lowest energy for all compositions obtained from the Inorganic Crystal Structure Database (ICSD).⁴⁵ We determined the elemental reference states (Na, Ti, S) *via* fitting⁴⁶ to experimental formation energies, which were obtained from the SGTE substance database (SSUB) and a database constructed by P. Nash *et al.*^{46–50} All the calculations needed to build the Na–Ti–S phase diagram were conducted within the Open Quantum Materials Database (OQMD) framework.⁵¹ For the compounds with partial occupancy on the Na sites (Na_{0.33}TiS₂, Na_{0.55}TiS₂), ground state structures were identified using the NEPS method (Figures S9 and S10 in Section SI).⁵² Both of these phases are predicted to be stable, validating the experimental observations (phase II and phase Ib) as shown in Figure 6a and b. The Na–Ti–S phase diagram (T = 0 K) is shown in Figure 6a, while all thermodynamically stable compounds are marked by circles. The sodiation reaction pathway of TiS₂ is shown as the tie-line between TiS₂ and Na, which goes through several intermediate phases and multiple-phase zones as shown in the ternary phase diagrams. These regions correspond to multiple sodiation reaction steps as listed in Table 1, where the capacities and average voltages of

Table 1. Thermodynamic Equilibrium Multistep Route during the Sodiation of TiS₂ Predicted by DFT Calculations

	reaction	capacity (mAh/g)	voltage (V)
i	$\mathrm{TiS}_2 + 0.33~\mathrm{Na} \rightarrow \mathrm{Na}_{0.33}\mathrm{TiS}_2$	80	2.20
ii	+ 0.55 Na \rightarrow Na _{0.55} TiS ₂	133	1.93
iii	+ 1 Na \rightarrow NaTiS ₂	239	1.35
iv	+ 2 Na \rightarrow Na ₂ S + TiS	479	0.90
v	+ 3 Na \rightarrow 3/2Na ₂ S + 1/2Ti ₂ S	718	0.45
vi	+ 4 Na \rightarrow 2Na ₂ S + Ti	957	0.03

these reaction steps are also evaluated. The full sodiation process can be divided into two periods (Figure 6c): (1) 0 < x < 1, intercalation, and (2) 1 < x < 4, extrusion, validating the experimental observations. In Figure 6c, we compare the equilibrium reaction voltage profiles calculated with DFT with the experimentally measured voltage curve. We note that the calculated equilibrium voltage profile of TiS₂ during the intercalation period exhibits good agreement with the

experimental sodiation curves. Meanwhile, the overall height of the computed equilibrium voltage profile of the extrusion period reasonably agrees with the experimental sodiation curve. Considering the sodiation inhomogeneity as observed in the TEM characterization, the calculated voltage profile shifts toward the low-Na content (Figure 6c). The observed early emergence of Ti2S, Ti, and their coexistence of TiS brings forward the later reaction steps of v and vi as shown in Table 1. Predicted phase structural evolution during the sodiation process of TiS_2 (O1) is shown in Figure 6d, which is initiated (x = 0.33) with Na ion occupying the trigonal prismatic structure of every two layers. Meanwhile, the accommodation of Na ions triggers the TiS2 layer gliding, compared to the empty layers. Further intercalations will occur between all layers (x = 0.55, 1) with the TiS₂ layers continuing to glide to realize the ordering transformation from the P3 sequence to the O3 sequence. The insertion of Na ions is supposed to be necessary for this gliding. The further sodiation process will proceed *via* extrusion reactions with the formation of TiS, Ti₂S, metallic Ti phases, and the Na₂S phase. Even a 2D to 3D morphology change was observed from the in situ STEM experiment, and the nanoplates still kept their structural integrity and did not decompose into the composited structure that was commonly observed in the sodiation of conversiontype oxides. A recent report indicates that the structural integrity may play an essential role in improving the cycling stability.⁵³ The resulting structural integrity can lead to alleviated morphological pulverization and contact failure between the active material and the binder/current collector after discharge. Enhancing the morphological integrity and therefore the electronic conductivity of electrode particles will help in improving the battery cycling stability.

CONCLUSIONS

In summary, we have investigated the sodiation mechanism of TiS2 nanoflakes using in situ SAED and STEM imaging techniques, complemented with DFT calculations. The results elucidated three sequential reaction steps in the intercalation process: II, Ib, and Ia. The stacking sequences of S-Ti-S layers change with the insertion of Na⁺: from the initial phase of Na_xTiS₂ (II) with O1–P3 structure when 0.17 < x < 0.33 to the Na_xTiS₂ (Ib) phase with P3 structure when 0.38 < x <0.72, and then to the Na_xTiS_2 phase (Ia) with O3 structure when 0.79 < x < 1. The extrusion reaction was also observed following the intercalation with a slower reaction speed compared to the intercalation counterpart. Morphological evolution during the whole reaction process has been thoroughly studied by in situ STEM images: These intercalation reactions are in-plane and will not destroy the Ti-S layered structure, whereas the morphological structure expands from two dimensions to three dimensions during the extrusion reaction. With Na ions' insertion, the inner volume of the particle continues to expand, then induces a morphology deformation. However, the electrode materials are still kept compact, which is very different from the sodiation of the conversion-type metal oxide and may help to avoid the issue of inner passivation.⁵⁴ The reaction process thoroughly studied in this work provides microscopic insights into reaction dynamics during sodiation and offers mechanistic insights for designing high-performance electrode materials for NIBs.

METHODS

Materials. We have used commercial high-purity TiS_2 (>99%) nanopowders purchased from US Research Nanomaterials.

In Situ TEM Characterization. The in situ TEM experimental setup was incorporated into a Nanofactory TEM-STM specimen holder, in which TiS2 nanoflakes dispersed onto a half lacey carbon gold. TEM half-grids were analogous to the TiS₂/C electrode, Na metal was attached to a piezo-driven W probe as the counter electrode, and a thin laver of Na₂O and NaOH formed on the Na metal as the electrolyte instead of the liquid organic electrolyte. The Na was loaded onto the holder in an Ar-filled glovebox and then transferred to a TEM column using a sealed Ar bag to avoid air exposure. During the in situ electrochemical tests, a negative potential of 4 V or higher was applied to the TiS₂ electrode against the Na source during the sodiation process. All the in situ and ex situ TEM measurements were performed on a JEOL 2100F TEM operated at 200 kV, and supplementary ex situ characterization was conducted on a Hitachi HD2700C scanning transmission electron microscope operated at 200 kV and equipped with a probe aberration corrector (spatial resolution <1 Å, energy resolution 0.35 eV) and a secondary electron microscopy detector. In this work, we performed in situ STEM imaging at a low current intensity (0.2 pA/cm^2). The beam effect on the sample and sodium ions can be disregarded in this case, which have been tested in our previous in situ sodiation work.55,50

Battery Assembly and Testing. The composite electrodes were prepared by casting the slurry containing 80 wt % TiS₂, 10 wt % acetylene black, and 10 wt % polyvinylidene fluoride dispersed into Nmethyl-2-pyrrolidone on a copper foil current collector. The electrodes were dried at 60 °C under vacuum for 12 h. The electrolyte is 1 M NaClO₄ in ethylene carbonate/dimethyl carbonate (EC:DMC = 1:1 in volume). The CR2032-type coin cells were assembled in an argon-filled glovebox with a TiS₂ electrode as the working electrode, pure Na foil as the counter electrode, a glass fiber as the separator, and 1 M NaClO₄ in ethylene carbonate/dimethyl carbonate (EC:DMC = 1:1 in volume) as the electrolyte. The galvanostatic charge/discharge tests were performed on a Land BT2000 battery test system at a current density of 12 mA g^{-1} in a voltage range of 3.0-0.1 V. After the electrochemical tests, the coin cells were disassembled in the Ar-filled glovebox. The cycled electrode materials were washed in DMC to eliminate the electrolyte residue and then dispersed onto a Cu grid for ex situ TEM characterization.

First-Principles Calculations. All the first-principles DFT calculations were conducted using the Vienna *ab Initio* Simulation Package (VASP)^{44–47} within the projector augmented wave (PAW) formalism,⁴⁸ and the Perdew–Becke–Ernzerhof (PBE) approximation⁴⁹ was employed to deal with the exchange–correlation potential. A plane wave basis with a cut-off energy of 520 eV and Γ -centered *k*-meshes with a density of 8000 *k*-points per reciprocal atom were used.

The average sodiation voltage (relative to Na/Na^+) can be computed using the negative of the reaction free energy per Na added/removed, as shown in eq 4:⁵⁰

$$V = \frac{\Delta G_{\rm f}}{F \Delta N_{\rm Na}} \tag{4}$$

where *F* is the Faraday constant, ΔN_{Na} is the amount of Na added/ removed, and ΔG_{f} is the (molar) change in free energy of the reaction. Considering a two-phase reaction between Na_xMS and Na_yMS, Na_xMS + (y - x)Na \rightarrow Na_yMS, ΔG_{f} can be approximated by the total internal energies from DFT calculations neglecting the entropic contributions (0 K),

$$\Delta E = E(\mathrm{Na}_{y}\mathrm{MS}) - E(\mathrm{Na}_{x}\mathrm{MS}) - (y - x)E(\mathrm{Na}_{\mathrm{metal}})$$
(5)

where $E(Na_xMS)$ and $E(Na_yMS)$ are the DFT energies at the respective compositions. The neglect of entropic contributions means that the sodiation voltage profiles will follow the T = 0 K ground state convex hull and consist of a series of constant voltage steps along the two-phase regions of the convex hull, separated by discontinuities that indicate the single phase compounds on the hull. It is worth mentioning here that, in practice, sodiation/desodiation do not

necessarily proceed through two-phase reactions. Thus, the calculated T = 0 K voltage profiles should be viewed as an approximation to the actual voltage profiles.⁵¹ At finite temperatures (*e.g.*, room temperature), the voltage drops in the profile become more rounded, due to entropic effects.⁵²

ASSOCIATED CONTENT

S Supporting Information

The Supporting Information is available free of charge on the ACS Publications website at DOI: 10.1021/acsnano.9b04222.

Additional details of *ex situ* S/TEM, raw diffraction patterns and images, data analysis, and theoretical calculations (PDF)

Movie S1: *In situ* electron diffraction during a whole sodiation process (AVI)

Movie S2: *In situ* electron diffraction during the intercalation process (AVI)

Movie S3: *In situ* STEM showing the intercalation reaction process (AVI)

Movie S4: *In situ* STEM showing the extrusion reaction process (AVI)

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Notes

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ACKNOWLEDGMENTS

This work is supported by the National Natural Science Foundation of China (51771053, 51471085), the National Key Research and Development Program of China (2016YFA0300803), the Fundamental Research Funds for the Central Universities, and the open research fund of Key Laboratory of MEMS of Ministry of Education, Southeast University. Electron microscopy work was performed at the Center for Functional Nanomaterials, Brookhaven National Laboratory, which is supported by the U.S. Department of Energy (DOE), Office of Basic Energy Science, under contract number DE-SC0012704. Z.Y. and A.A.G. (DFT calculations) were supported as part of the Nanoporous Materials Genome Center by the U.S. Department of Energy, Office of Science, Office of Basic Energy Sciences, under award number DE-FG02-17ER16362. We thank Dr. Qingping Meng for helpful discussions. H.D. and Y.Y. acknowledge funding support from the U.S. Department of Energy's Office of Energy Efficiency and Renewable Energy (DE-EE0008234), UH Technical Gap Fund, and UH High Priority Area Large Equipment Grant.

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