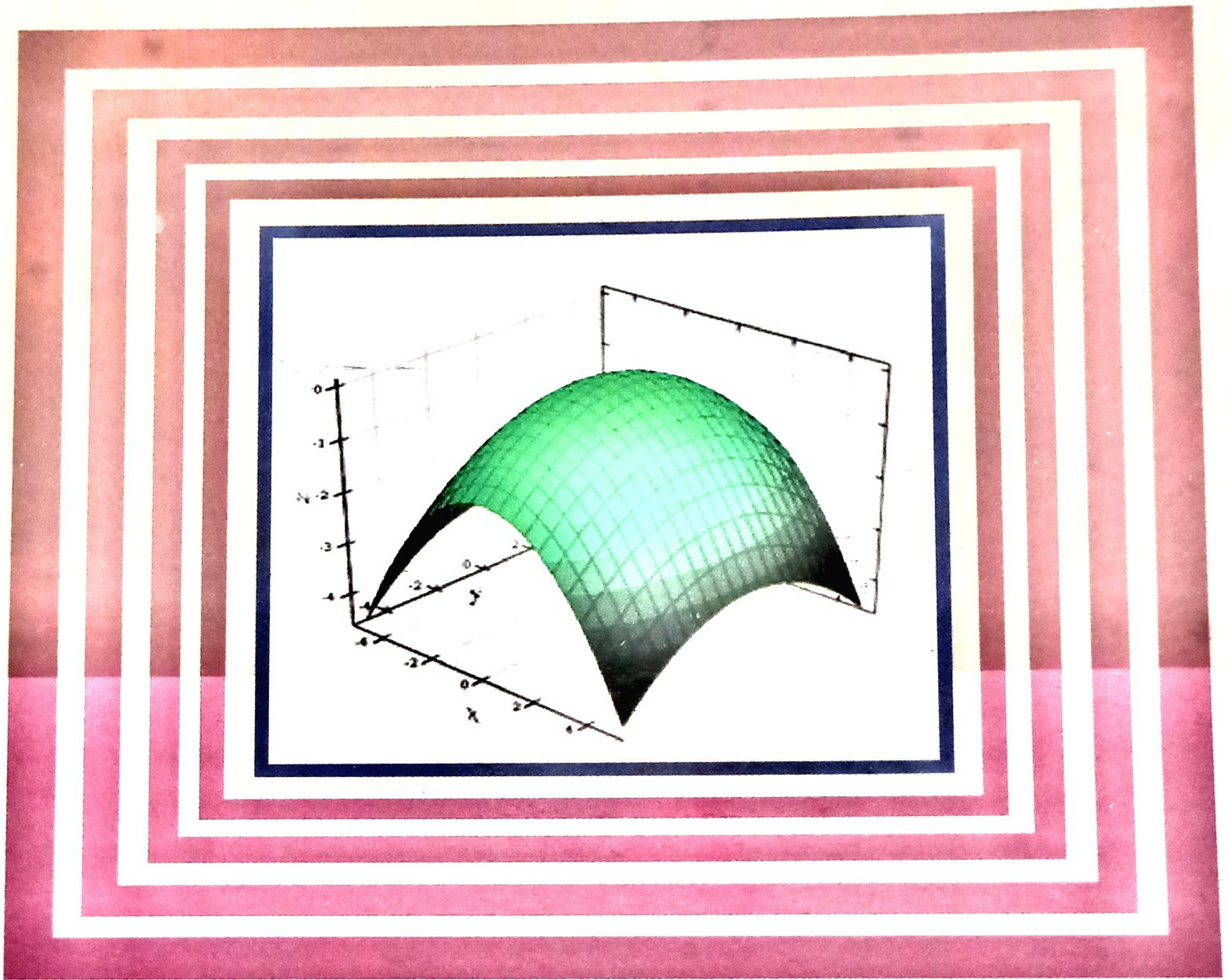


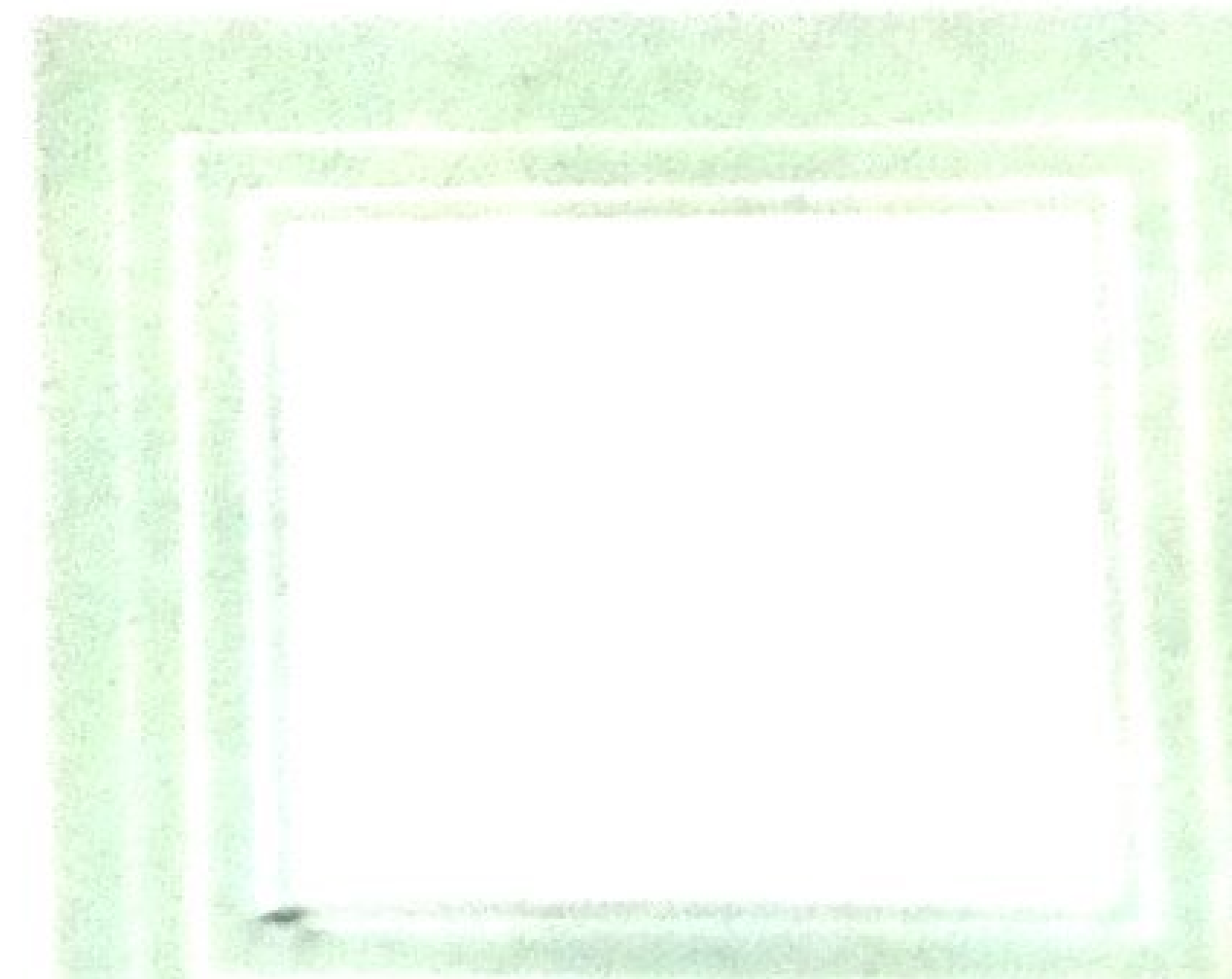


# CALCULUS OF VARIATIONS

PUNDIR  
PUNDIR



*A Pragati Edition*



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