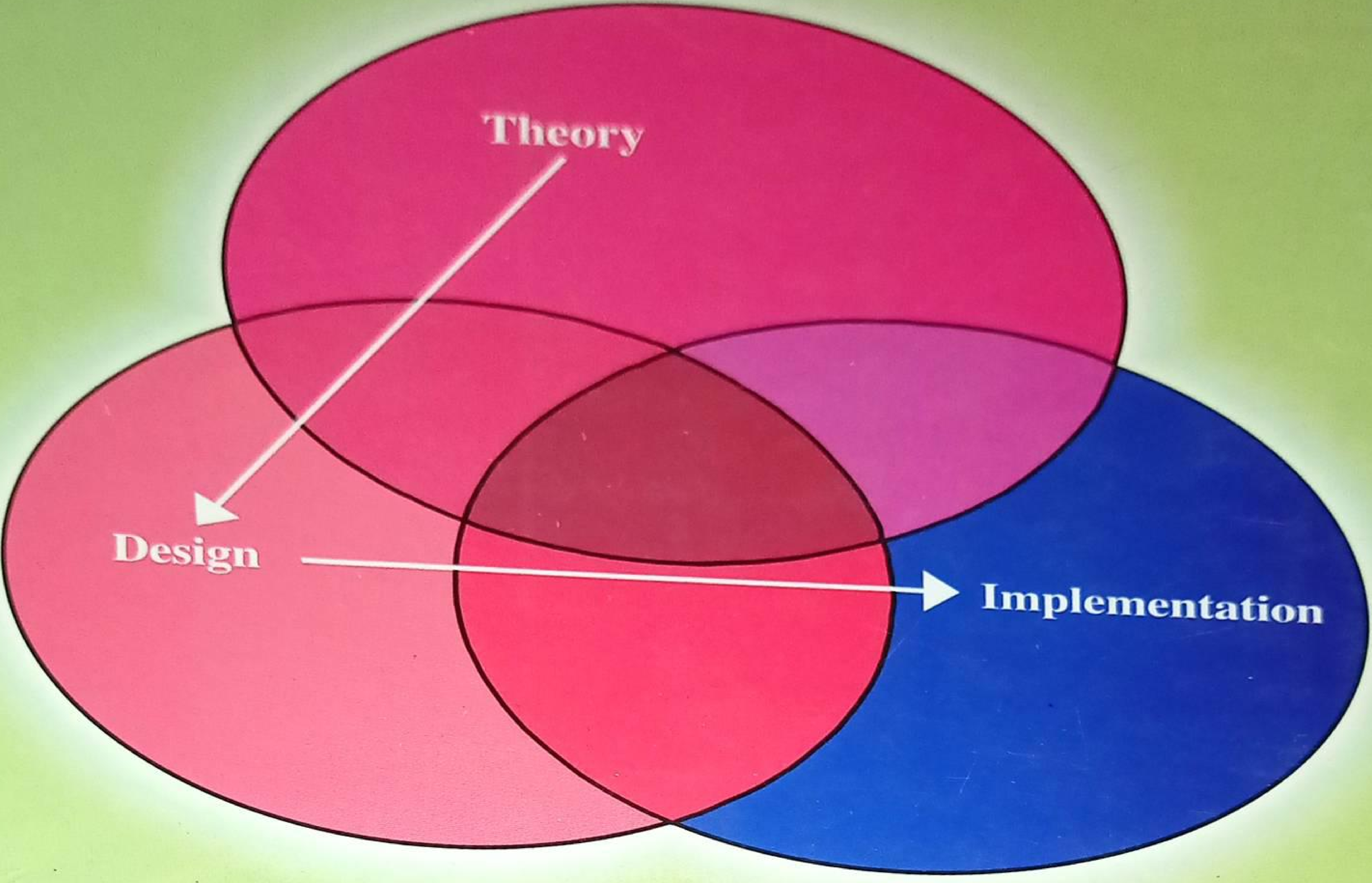
A Simplified Text-cum-Workbook on

Data Structures & Algorithms

Theory, Design and Implementation Using C



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