

**Fourth Edition**

# **Numerical Methods**

**for**

**Scientific**

**and**

**Engineering**

**Computation**

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