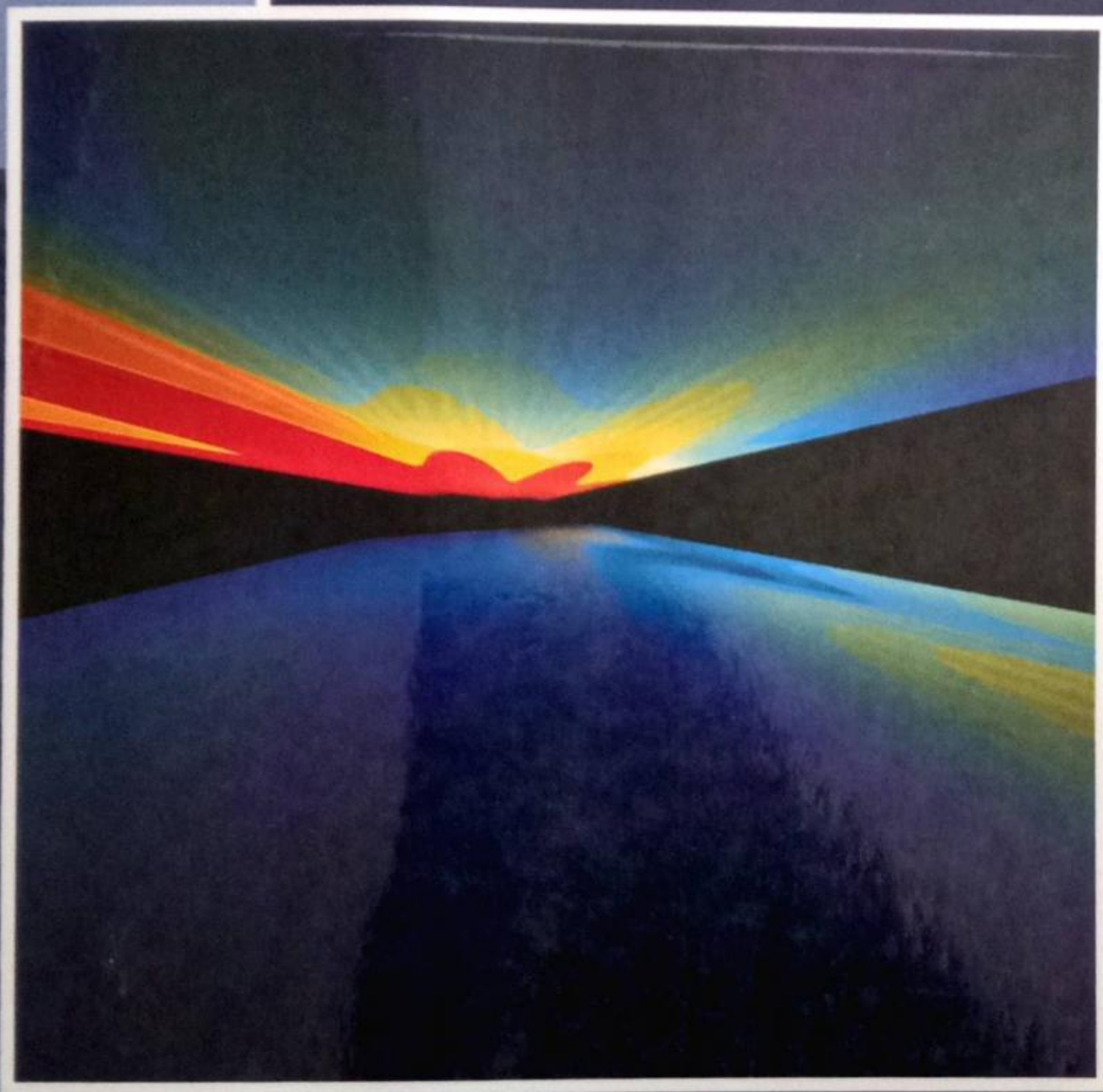


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# Quantum Mechanics



SECOND EDITION

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ALWAYS LEARNING

**PEARSON**



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