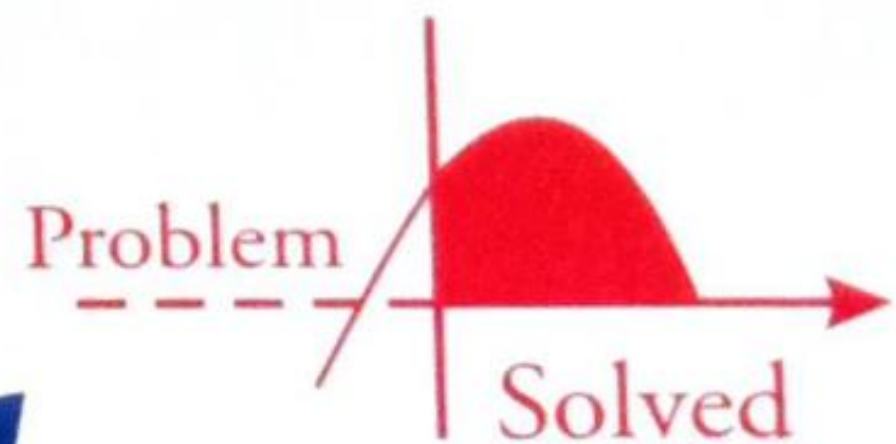


$\alpha\delta - \beta\gamma \neq 0$
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